



## **Deliverable 8.3: SFC Training materials.**

Work Package 8

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**The SFC Training materials document consists of two volumes. This document corresponds to the first volume.**

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## Executive Summary

This report collects the main training materials (documents used in all kind of training actions, such as courses, for new members or grant holders training, etc.) produced by WP8 team in tasks 2-4.

Forty documents are grouped into six different categories, depending on the type of event for which the material was developed:

EURAD annual event	6 documents
External training course	6 documents
Internal meeting	2 documents
Participation to a Conference	6 documents
Participation to a Workshop	9 documents
Participation to an Event other than a Conference or a Workshop	6 documents

Each section lists the documents embedded its pdf version.

These training materials contain the state-of-the-art of nuclear fuel modelling, characterisation and evolution of nuclear fuel until disposal.

If any parts of this training material is used, it is free, but must be acknowledged to EURAD

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## Glossary

ARIANE	Actinide Research In A Nuclear Element
ATF	Accident Tolerant Fuels
BDBA	Beyond Design Base Accident
BU	Burnup
BUC	Burnup Credit
BWR	Boiling Water Reactor
CIRFT	Cyclic Integrated Reversible-bending Fatigue Tester
CRAM	Chebyshev Rational Approximation Method
DA	Destructive Analysis
DBA	Basis Accidents
DBTT	Ductile-to-Brittle Transition Temperature
DDEP	Decay Data Evaluation Project
DHC	Delayed Hydride Cracking
DBRC	Doppler-Broadening Rejection Correction
EGADSNF	Expert Group on Assay Data of Spent Nuclear Fuel

EGBCC	Expert Group on Burnup Credit Criticality
ENDF	Evaluated Nuclear Data Files
EOL	End Of Life
ESARDA	European Safeguards Research and Development Association
FA	Fuel Assembly
FCCI	Fuel/Cladding Chemical Interaction
FDC	Final Disposal Canister
FEA/FEM	Finite Element Analysis/Finite Element Modelling
FIP	Fuel Integrity Project
FP	Fission Product
IAEA	International Atomic Energy Agency
ICP-SF-MS	Inductively Coupled Plasma – Sector Field – Mass Spectrometer
ICPS	Inductively Coupled Plasma Spectrometer
IE	Initial Enrichment
INL	Idaho National Laboratory



JRC	Joint Research Center
LWR	Light Water Reactor
MCNP	Monte Carlo N-Particle Transport Code
NDA	Non-Destructive Analysis
NEA	Nuclear Energy Agency
NPP	Nuclear Power Plants
ORNL	Oak Ridge National Laboratory
PGET	Passive Gamma Emission Tomography
PCI	Pellet-Cladding Interaction
PCMI	Pellet-Cladding Mechanical Interaction
PIE	Post-Irradiation Examination
PNNL	Pacific Northwest National Laboratory
PWR	Pressurised Water Reactor
RCT	Ring Compression Test
RHCF	Radial Hydride Continuity Factor
SCC	Stress Corrosion Cracking

SCIP	Studsvik Cladding Integrity Project
SNF	Spent Nuclear Fuel
SPAR	Spent fuel Performance Assessment and Research
TIMS	Thermal Ionisation Mass Spectrometer
TSC	Transport Storage Cask
UFDC	Used Fuel Disposition Campaign

## **EURAD Spent Fuel characterisation and evolution until disposal (SFC) training materials.**

## 1. EURAD annual event

- Thermal power produced by spent nuclear fuel; P. Schillebeeckx, JRC Geel; EURAD Annual event 2021; 16 - 18/03/2021
- Neutrons as a signature for the characterisation of spent nuclear fuel; P. Schillebeeckx, JRC Geel; EURAD Annual event 2021; 16 - 18/03/2021
- Validation and uncertainty analysis of SNF characterization based on SCALE code system; A. Shama, NAGRA; EURAD Annual event 2021; 16 - 18/03/2021
- Fuel dry storage modelling with INL's BISON code at VTT; A. Arkoma, VTT; WP8 SFC Annual Meeting 2023; 11/1/2023
- Statistical approach for evaluating the safety of spent fuel during transport accidents; C. Aguado, F. Fera, L.E. Herranz, CIEMAT; WP8 SFC Annual Meeting 2023; 11/1/2023
- Mechanical behaviour of pre- hydrided cladding; Miguel Cristóbal-Beneyto, Jesus Ruiz-Hervias, Daniel Pérez-Gallego; WP8 SFC Annual Meeting 2023; 11/01/2023

**1.1 Thermal power produced by spent nuclear fuel; P.  
Schillebeeckx, JRC Geel; EURAD Annual event 2021; 16 -  
18/03/2021**



# THERMAL POWER OF SPENT NUCLEAR FUEL

17 March 2021 • Peter Schillebeeckx (EC – JRC)  
 WP8: Spent Fuel Characterisation



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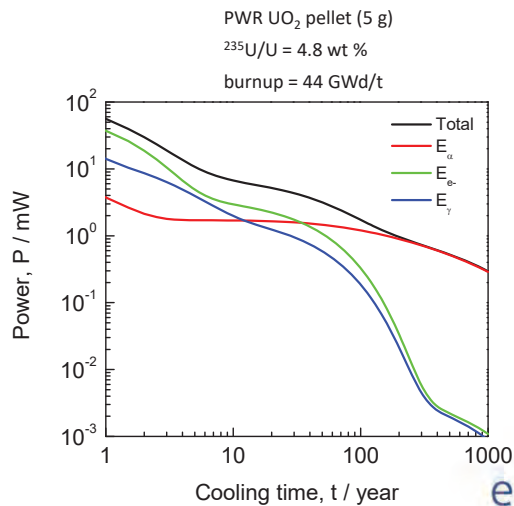
17/03/2021

EURAD Annual Event 2021



## WP8: SPENT FUEL CHARACTERISATION

How accurate can we determine the thermal power of spent nuclear fuel for transport, intermediate storage and final disposal?



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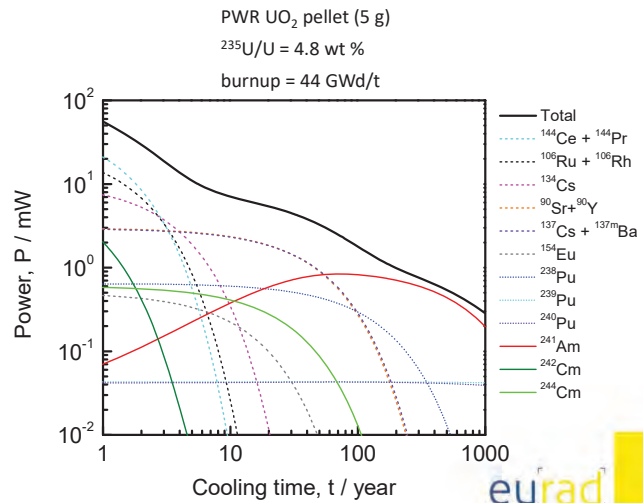




### THERMAL POWER PRODUCED BY SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

17/03/2021



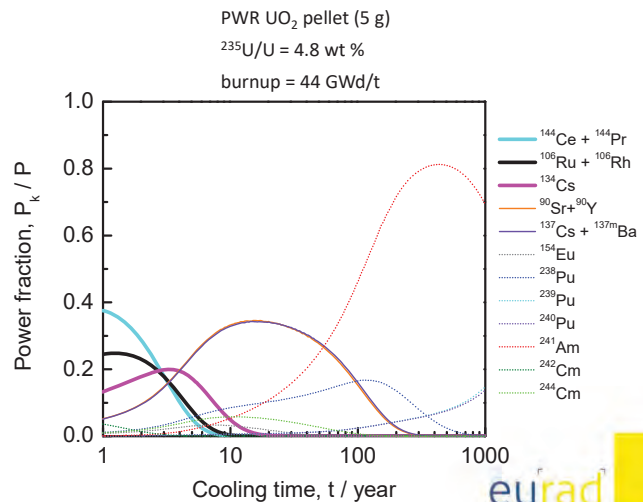
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### THERMAL POWER PRODUCED BY SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
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  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

17/03/2021



EURAD Annual Event 2021

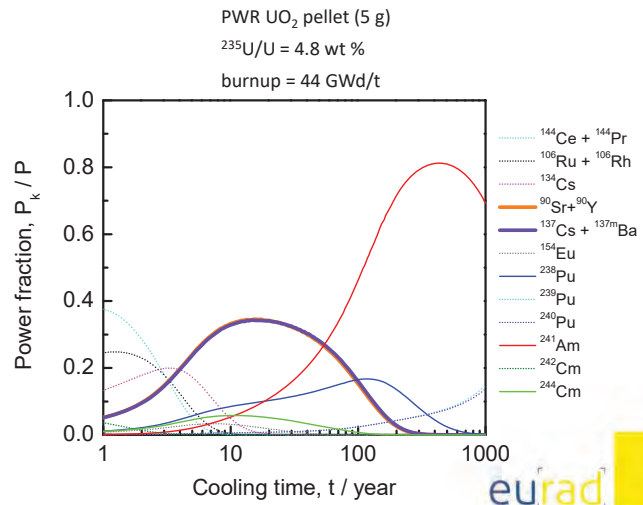




### THERMAL POWER PRODUCED BY SNF

- 1 a ≤ t ≤ 10 a
  - <sup>144</sup>Ce / <sup>144</sup>Pr
  - <sup>106</sup>Ru / <sup>106</sup>Rh
  - <sup>134</sup>Cs
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
- 10 a ≤ t ≤ 100 a
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
  - <sup>238</sup>Pu
  - <sup>241</sup>Am
  - <sup>244</sup>Cm
- 100 a ≤ t
  - <sup>241</sup>Am
  - <sup>238</sup>Pu
  - <sup>239,241</sup>Pu

17/03/2021



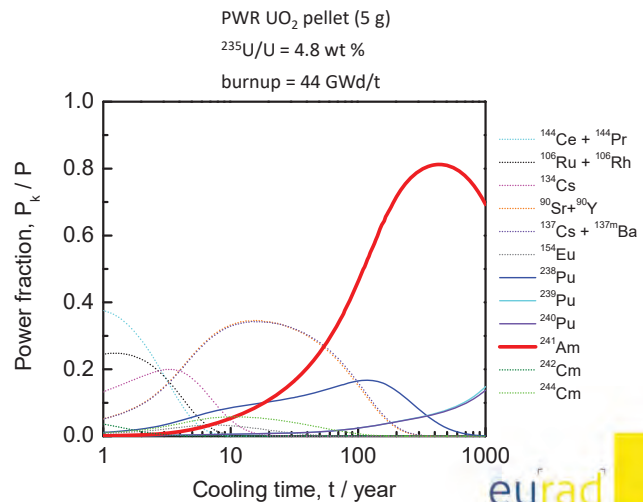
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### THERMAL POWER PRODUCED BY SNF

- 1 a ≤ t ≤ 10 a
  - <sup>144</sup>Ce / <sup>144</sup>Pr
  - <sup>106</sup>Ru / <sup>106</sup>Rh
  - <sup>134</sup>Cs
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
- 10 a ≤ t ≤ 100 a
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
  - <sup>238</sup>Pu
  - <sup>241</sup>Am
  - <sup>244</sup>Cm
- 100 a ≤ t
  - <sup>241</sup>Am
  - <sup>238</sup>Pu
  - <sup>239,241</sup>Pu

17/03/2021



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### THERMAL POWER PRODUCED BY SNF

$$P(t) = \sum_k p_k N_k(t) \quad t: \text{cooling time or time after end of irradiation}$$

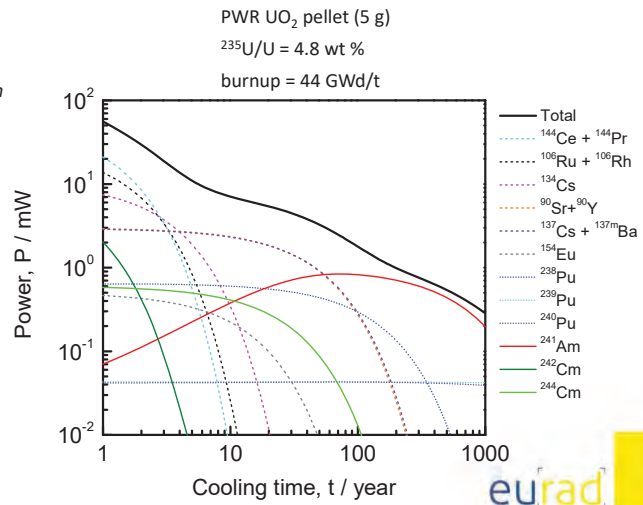
$P(t_2 > t_1)$  cannot be extrapolated from  $P(t_1)$

$N_k(t)$  : nuclide inventory at time  $t$

- $N_k(t_0)$  : nuclide inventory at time  $t_0$  with  $t > t_0$
- Nuclide inventory at  $t > t_0$

$$\frac{dN_k}{dt} = \sum_i \lambda_i N_i - \lambda_k N_k$$

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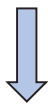
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### THEORETICAL CALCULATIONS OF NUCLIDE INVENTORY

Burnup code: coupled neutron transport – nuclide depletion/creation calculations

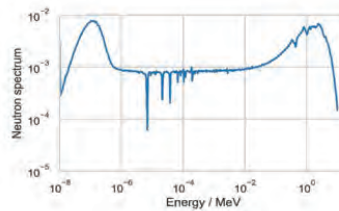
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

Update nuclide vector



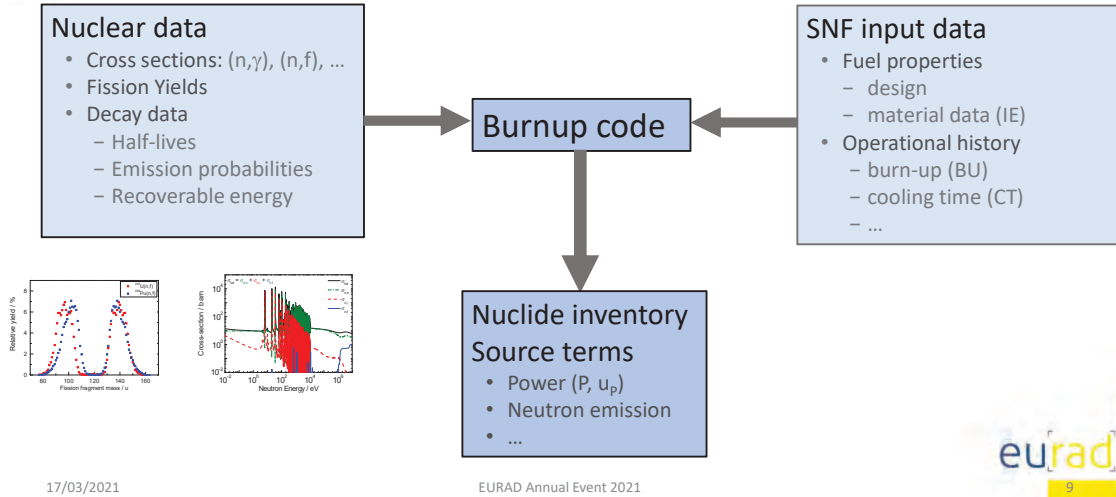
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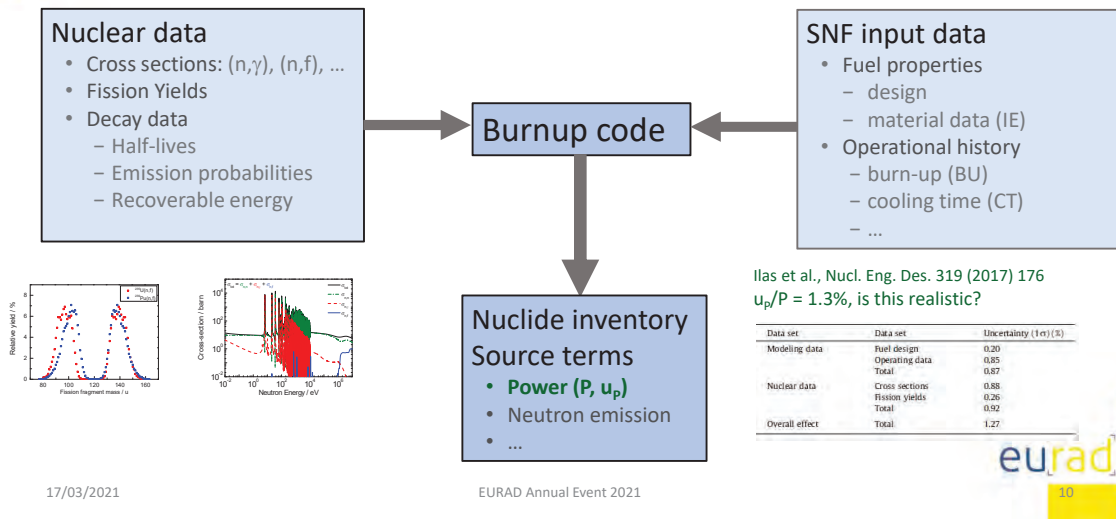




### BURNUP CALCULATIONS



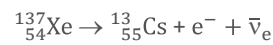
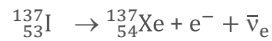
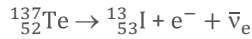
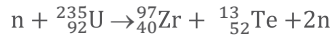
### BURNUP CALCULATIONS



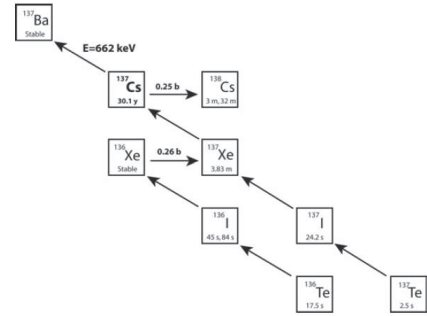


### PRODUCTION OF <sup>137</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$



<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)



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### PRODUCTION OF <sup>137</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

$$N_k(t') \approx \frac{Y_c \sigma_f N_f \phi}{\lambda_k + \sigma_{k,\gamma} \phi} [1 - e^{-(\lambda_k + \sigma_{k,\gamma} \phi) t'}]$$

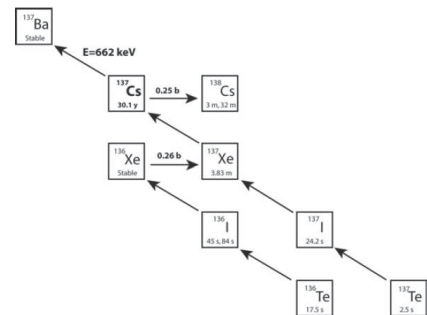
$(\lambda_k + \sigma_{k,\gamma} \phi) \ll 1$

$$N_k(t') \approx Y_c \sigma_f N_f \phi t'$$

$t'$  : irradiation time

- $Y_c$  : cumulative fission yield (nuclear data)
- $\sigma_f$  : fission cross section (nuclear data)
- $N_f$  : number of fissile nuclei, i.e. <sup>235</sup>U (fuel properties)
- $\phi t'$  : total neutron fluence (operation history)

<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)



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### PRODUCTION OF <sup>137</sup>Cs DURING REACTOR OPERATION

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)

$$N_k(t') \approx \frac{Y_c \sigma_f N_f \phi}{\lambda_k + \sigma_{k,\gamma} \phi} [1 - e^{-(\lambda_k + \sigma_{k,\gamma} \phi) t'}]$$

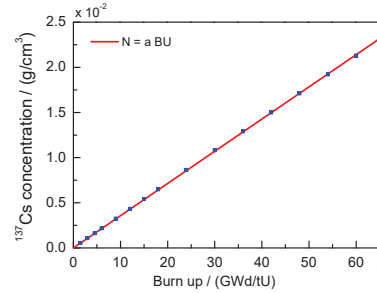
$(\lambda_k + \sigma_{k,\gamma} \phi) \ll 1$

$$N_k(t') \approx Y_c \sigma_f N_f \phi t'$$

$(\sigma_f N_f \phi t')$  : total number of fissions  
 $(\sigma_f N_f \phi t') \times E_f$  : time integrated reactor power  
 $E_f =$  recoverable energy per fission

$$N_k(t_0) \propto Y_c BU$$

$$\Rightarrow N_k(t_0) \propto BU$$



17/03/2021

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### PRODUCTION OF THERMAL POWER BY <sup>137</sup>Cs

Thermal power by <sup>137</sup>Cs at t (cooling time):

$$P_k(t) = p_k N_k(t_0) e^{-\lambda_k (t-t_0)} \quad t_0 : \text{end of irradiation}$$

- Production: <sup>137</sup>Cs inventory at end of irradiation

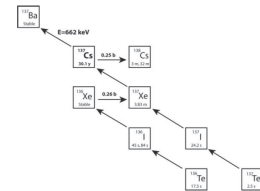
$$N_k(t_0) \propto Y_c BU$$

- $Y_c$  : cumulative fission yield for <sup>137</sup>Cs
- BU : burnup

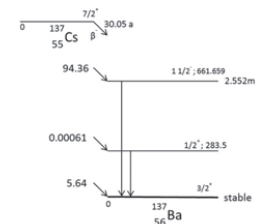
- Decay :  $(\lambda_k, E_{dk}) \quad p_k = E_{dk} \lambda_k$

- $\lambda_k$  : decay constant
- $E_{dk}$  : recoverable energy

Production



Decay



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## NUCLEAR DATA ( $Y_c, E_d$ ): $^{137}\text{Cs}$

$T_{1/2} = 30.05$  (8) a

Library	$E_d$ / keV	Ratio	$^{137}\text{Cs}$		$(Y_c \times E_d)$ / keV	Ratio
			$100 \times Y_c$	Ratio		
DDEP/IAEA	811.8 (18)	1	6.221 (69)	1	50.5 (6)	1
JEF-2.2	812.0 (69)	1.000 (8)	6.244 (54)	1.004 (9)	50.7 (6)	1.004 (12)
JEFF-3.1.1	<b>810.1 (23)</b>	<b>0.998 (3)</b>	<b>6.221 (69)</b>	<b>1.000 (11)</b>	<b>50.4 (6)</b>	<b>0.998 (11)</b>
JEFF-3.3	<b>801.8 (23)</b>	<b>0.988 (3)</b>	<b>6.090 (63)</b>	<b>0.979 (10)</b>	<b>48.8 (5)</b>	<b>0.967 (10)</b>
ENDF/B-VI.8	813.4 (41)	1.002 (5)	6.188 (31)	0.995 (5)	50.3 (4)	0.997 (7)
ENDF/B-VII.0	805.7 (16)	0.992 (2)	6.188 (31)	0.995 (5)	49.9 (3)	0.987 (5)
ENDF/B-VIII.0	<b>805.8 (18)</b>	<b>0.993 (2)</b>	<b>6.188 (31)</b>	<b>0.995 (5)</b>	<b>49.9 (3)</b>	<b>0.987 (5)</b>

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## NUCLEAR DATA ( $Y_c, E_d$ ): $^{90}\text{Sr}$

$T_{1/2} = 28.80$  (7) a

Library	$E_d$ / keV	Ratio	$^{90}\text{Sr}$		$(Y_c \times E_d)$ / keV	Ratio
			$100 \times Y_c$	Ratio		
DDEP/IAEA	1129.4 (14)	1	5.730 (130)	1	64.7 (15)	1
JEF-2.2	1129.6 (7)	1.000 (1)	<b>5.847 (188)</b>	<b>1.020 (33)</b>	<b>66.0 (21)</b>	<b>1.021 (33)</b>
JEFF-3.1.1	1107.8 (13)	0.981 (1)	5.729 (132)	1.000 (23)	63.5 (15)	0.981 (23)
JEFF-3.3	1127.3 (13)	0.998 (1)	<b>5.676 (131)</b>	<b>0.991 (23)</b>	<b>64.0 (15)</b>	<b>0.989 (23)</b>
ENDF/B-VI.8	1129.9 (12)	1.000 (1)	5.782 (58)	1.009 (10)	65.3 (7)	1.010 (10)
ENDF/B-VII.0	1129.4 (13)	1.000 (1)	5.782 (58)	1.009 (10)	65.3 (7)	1.009 (10)
ENDF/B-VIII.0	1128.8 (11)	0.999 (1)	<b>5.782 (58)</b>	<b>1.009 (10)</b>	<b>65.3 (7)</b>	<b>1.009 (10)</b>
<b>Ramthun (Exp. 1976)</b>	<b>1147.0 (90)</b>					

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## NUCLEAR DATA ( $Y_c E_d$ ): $^{90}\text{Sr}$ and $^{137}\text{Cs}$

Library	$^{90}\text{Sr}$		$^{137}\text{Cs}$	
	( $E_d \times Y_c$ ) / keV	Ratio	( $Y_c \times E_d$ ) / keV	Ratio
DDEP/IAEA	64.7 (15)	1	50.5 (6)	1
JEF-2.2	<b>66.0 (21)</b>	<b>1.021 (33)</b>	<b>50.7 (7)</b>	<b>1.004 (12)</b>
JEFF-3.1.1	63.5 (15)	0.981 (23)	50.4 (6)	0.998 (11)
JEFF-3.3	<b>64.0 (15)</b>	<b>0.989 (23)</b>	<b>48.8 (5)</b>	<b>0.967 (10)</b>
ENDF/B-VI.8	65.3 (7)	1.010 (10)	50.3 (4)	0.997 (7)
ENDF/B-VII.0	65.3 (7)	1.009 (10)	49.9 (3)	0.987 (5)
ENDF/B-VIII.0	<b>65.3 (7)</b>	<b>1.009 (10)</b>	<b>49.9 (3)</b>	<b>0.987 (5)</b>

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## CONCLUSIONS

- Prediction of thermal power of SNF strongly depends on
  - Nuclear data
  - Operational history
- $u_p/P = 1.3\%$  : not realistic

⇒ WP8: Spent fuel characterisation until final disposal

“Define best practice procedures to determine thermal power with realistic confidence limits”

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**1.2 Neutrons as a signature for the characterisation of spent nuclear fuel; P. Schillebeeckx, JRC Geel; EURAD Annual event 2021; 16 - 18/03/2021**





## Neutrons as a signature for the characterisation of spent nuclear fuel

18 March 2021 • Peter Schillebeeckx (EC – JRC)  
WP8: Spent Fuel Characterisation



This project has received funding from the European Union's Horizon 2020 research and innovation programme 2014-2018 under grant agreement N°847593

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## SPENT NUCLEAR FUEL (SNF): INTERMEDIATE STORAGE OR FINAL DISPOSAL

A **safe, secure, ecological** and **economical** transport, storage and final disposal requires that **SNF is characterised** for the main source terms of interest:

- Decay Heat
- Neutron emission
- $\gamma$ -ray emission
- Reactivity  
(fissioning nuclides + nuclides with high neutron absorption cross sections for BUC)
- Fissile material (Nuclear Safeguards)
- Specific long-lived radionuclides for long term safety  
(e.g.  $^{14}\text{C}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ )



⇒ Requires a **nuclide inventory** that can only be determined by **theoretical calculations**

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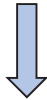




## THEORETICAL CALCULATIONS OF NUCLIDE INVENTORY

**Burnup code:** coupled neutron transport – nuclide depletion/creation calculations

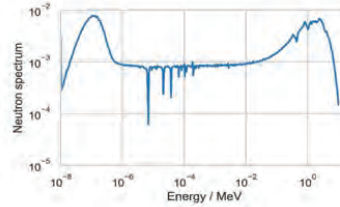
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

Update nuclide vector



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## BURNUP CALCULATIONS

**Verify by NDA experiments:**

- Gamma-ray
- Neutron

**Nuclear data**

- Cross sections: (n,γ), (n,f), ...
- Fission Yields
- Decay data
  - Half-lives
  - Emission probabilities
  - Recoverable energy

Burnup code

**SNF input data**

- Fuel properties
  - design
  - material data (IE)
- Operational history
  - burn-up (BU)
  - irradiation cycles
  - cooling time (CT)
  - ...

**Source terms**

- Power
- Neutron emission
- ...

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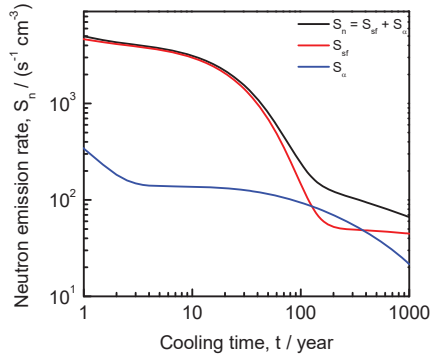
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### NEUTRON EMISSION OF SNF

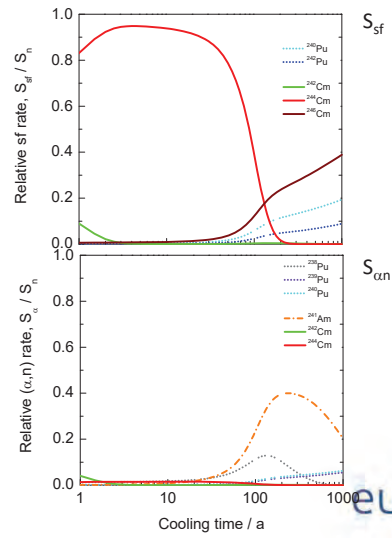
PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt %  
 burnup = 44 GWd/t



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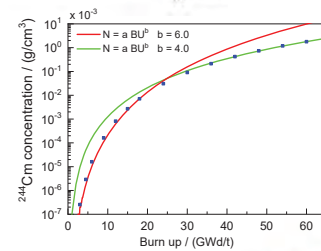
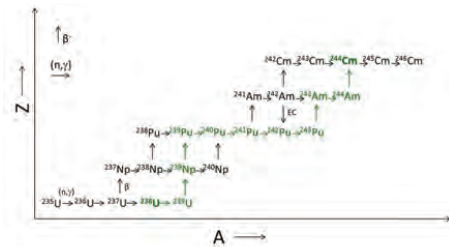
$$S_n(t) = \sum_k (s_{sf,k} + s_{\alpha,n,k}) N_k(t)$$



### NEUTRON EMISSION OF SNF

- Neutron emission rate: main contribution due to <sup>244</sup>Cm(sf)
- <sup>244</sup>Cm inventory depends on operational history

⇒ Neutron measurement provides information about operational history



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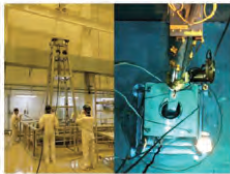
## VERIFICATION OF SNF INPUT DATA BY NEUTRON MEASUREMENTS

### Neutron based NDA measurements of SNF assemblies

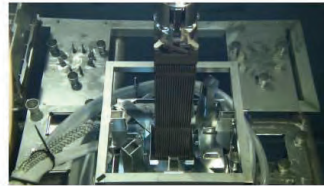
Nuclear safeguards: DOE (NGSI), IAEA, EURATOM

- Total neutron emission rate (Fork) : routine inspections
- Passive Neutron Albedo Reactivity (PNAR) : Finland
- Differential Die Away Self-Interrogation (DDSI) : Sweden

PNAR and DDSI: also sensitive to neutron multiplication



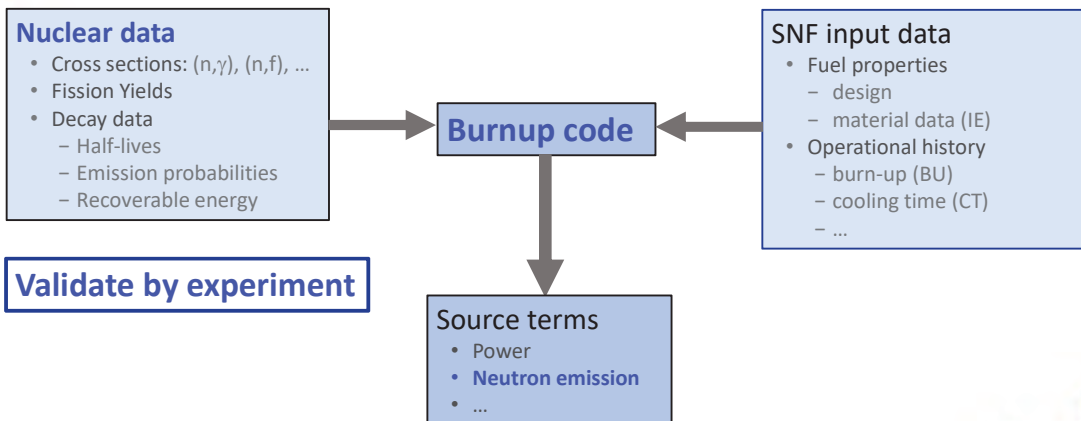
PNAR: Tupasela et al., NIMA 986 (2021) 164707  
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DDSI: Trahan et al., NIMA 955 (2020) 1643329  
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## BURNUP CALCULATIONS



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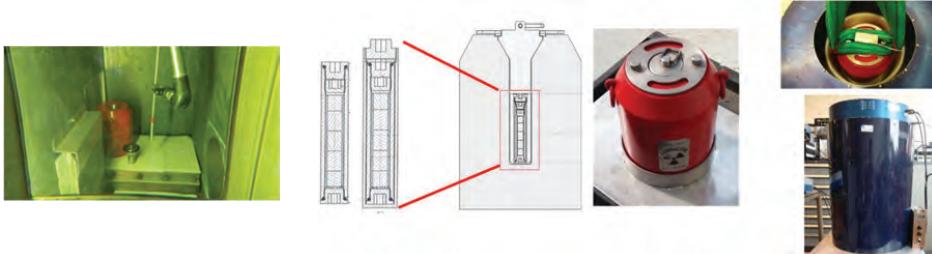
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## ABSOLUTE MEASUREMENT OF NEUTRON EMISSION RATE OF A SNF SAMPLE

- Procedure to **transfer SNF segment sample** from hot cell to **neutron detection system**
  - Based on a multi-layer barrier encapsulation making use of special features of hot cell facilities at SCK•CEN (LHMA)



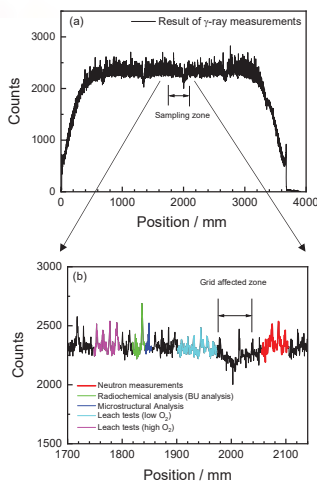
- **Absolute** determination of **neutron emission rate** by **NDA** in **standard controlled area conditions** using **conventional well-counter** for nuclear safeguards applications

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## SELECTION AND CHARACTERISATION OF SNF SEGMENT SAMPLE



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- Irradiation history of the SNF
  - Segment (~50 mm) from rod of a PWR Assembly
  - PWR (15 x 15): 188 UO<sub>2</sub> rod (4.5 wt% <sup>235</sup>U/U) and 16 (U,Gd)O<sub>2</sub> rods
  - Irradiated at Tihange 1 (BE)
  - Rod used for other international project (First-Nuclides, REGAL, WETFUEL & AGAF, SF-ALE)
- SNF segment sample characteristics
  - Part of a set of 4 samples (**REGAL project**)
    - **Radiochemical analysis (BU)**
    - Microstructural analysis
    - Leach tests (low O<sub>2</sub>)
    - Leach tests (high O<sub>2</sub>)

**EURAD – SFC (NDA): neutron measurements**

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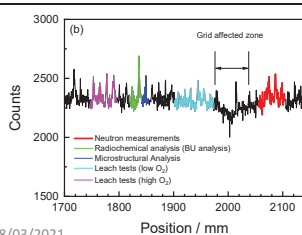


## SELECTION AND CHARACTERISATION OF SNF SEGMENT SAMPLE

- SNF segment sample: nuclide inventory and BU
- SNF segment sample: characteristics

BU indicator	Nuclide inventory mg/g	Burnup GWd/t
<sup>137</sup> Cs	1.288 (30)	52.6 (10)
<sup>143</sup> Nd + <sup>144</sup> Nd	3.029 (32)	53.0 (6)
<sup>143</sup> Nd + <sup>144</sup> Nd	1.962 (21)	53.1 (6)
<sup>148</sup> Nd	0.534 (12)	53.3 (12)
<sup>150</sup> Nd	0.257 (11)	52.2 (23)
<b>Average</b>		<b>52.8 (4)</b>

Parameter	Value
Length	52.01 (4) mm
Segment weight	42.616 (1) g
Cladding weight	6.71 (4) g
Net fuel weight	35.91 (4) g



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## RESULTS AND COMPARISON WITH THEORETICAL CALCULATIONS

- Neutron emission rate determined by absolute neutron measurements

$$S_{sf} = 682 (10) \text{ s}^{-1}\text{g}^{-1} \quad S_{\alpha n} = 25 (10) \text{ s}^{-1}\text{g}^{-1}$$

- Comparison with theoretical calculations

Code	Library	$(\alpha, n)$		$S_{sf} / (\text{g}^{-1}\text{s}^{-1})$	$S_{\alpha} / (\text{g}^{-1}\text{s}^{-1})$	Calculation/Experiment	
		Method	Library			$S_{sf}$	$S_{\alpha n}$
SCALE	ENDF/B-VII.1	$Y(\alpha, n)$		665	11.8	0.974	0.48
SERPENT(1)	ENDF/B-VII.1	$Y(\alpha, n)$		662	14.2	0.971	0.58
SERPENT(2)	ENDF/B-VII.1	$Y(\alpha, n)$		694	14.2	<b>1.017</b>	0.58
	ENDF/B-VIII.0	$Y(\alpha, n)$		692	14.1	<b>1.013</b>	0.57
	JEFF-3.1.2	$Y(\alpha, n)$		629	13.2	0.922	0.56
	JEFF-3.3	$Y(\alpha, n)$		658	13.8	0.964	0.56
	JEFF-4T0	$Y(\alpha, n)$		695	13.7	<b>1.018</b>	0.56
ALEPH28	ENDF/B-VIII.0	$\sigma(\alpha, n)$	TENDL2015	660	26.5	0.968	1.08
		$\sigma(\alpha, n)$	JENDL_AN/500		22.4		0.91
	JEFF-3.3	$\sigma(\alpha, n)$	TENDL2015	641	28.1	0.940	1.14
		$\sigma(\alpha, n)$	JENDL_AN/500		23.9		0.97

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## RESULTS AND COMPARISON WITH THEORETICAL CALCULATIONS

- Neutron emission rate determined by absolute neutron measurements

$$S_{sf} = 682 (10) \text{ s}^{-1}\text{g}^{-1} \quad S_{\alpha n} = 25 (10) \text{ s}^{-1}\text{g}^{-1}$$

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Code	Library	$(\alpha, n)$		$S_{sf} / (\text{g}^{-1}\text{s}^{-1})$	$S_{\alpha} / (\text{g}^{-1}\text{s}^{-1})$	Calculation/Experiment	
		Method	Library			$S_{sf}$	$S_{\alpha n}$
SCALE	ENDF/B-VII.1	$\Upsilon(\alpha, n)$		665	11.8	0.974	0.48
SERPENT(1)	ENDF/B-VII.1	$\Upsilon(\alpha, n)$		<b>662</b>	14.2	<b>0.971</b>	0.58
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## RESULTS AND COMPARISON WITH THEORETICAL CALCULATIONS

- Neutron emission rate determined by absolute neutron measurements

$$S_{sf} = 682 (10) \text{ s}^{-1}\text{g}^{-1} \quad S_{\alpha n} = 25 (10) \text{ s}^{-1}\text{g}^{-1}$$

- Comparison with theoretical calculations

Code	Library	$(\alpha, n)$		$S_{sf} / (\text{g}^{-1}\text{s}^{-1})$	$S_{\alpha} / (\text{g}^{-1}\text{s}^{-1})$	Calculation/Experiment	
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SCALE	ENDF/B-VII.1	$\Upsilon(\alpha, n)$		665	11.8	0.974	<b>0.48</b>
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	JEFF-4T0	$\Upsilon(\alpha, n)$		695	13.7	1.018	<b>0.56</b>
ALEPH28	ENDF/B-VIII.0	$\sigma(\alpha, n)$	TENDL2015	660	26.5	0.968	<b>1.08</b>
		$\sigma(\alpha, n)$	JENDL_AN/500		22.4		<b>0.91</b>
	JEFF-3.3	$\sigma(\alpha, n)$	TENDL2015	641	28.1	0.940	<b>1.14</b>
		$\sigma(\alpha, n)$	JENDL_AN/500		23.9		<b>0.97</b>

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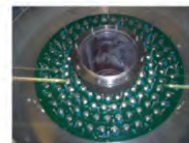
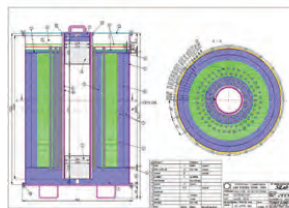
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## SUMMARY AND OUTLOOK

- Absolute **neutron emission rate measurements** of SNF sample with **uncertainty < 2% in standard controlled area conditions**
  - Calculated  $S_{sf}$  with latest libraries (ENDF/B-VIII.0, JEFF-4T0): **within experimental uncertainty**
  - Differences in  $S_{sf}$  only due to methodology can be **about 5 %**
  - Calculated  $S_{\alpha n}$ : best agreement by including  $\alpha$ -transport
- Development of **optimised neutron counter and transfer container**  
Increased detection efficiency and reduced  $\gamma$ -ray sensitivity
  - Reduce uncertainty of both  $S_{sf}$  and  $S_{\alpha n}$
  - **Broader application range:**  
MOX, short cooling times, low burnup, end of rod, ...



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## THANK YOU FOR YOUR ATTENTION

- JRC Geel (BE) and Ispra (IT)  
G. Alaerts, J. Paepen, P. Schillebeeckx, R. Wynants, G. Žerovnik\* (JRC Geel)  
B. Pedersen, G. Varasano (JRC Ispra)
- SCK CEN (BE)  
K. Govers\*\*, N. Messaoudi, Y. Parthoens, P. Romojaro, A. Stankovskiy, M. Verwerft  
  
\*JSI (SI)  
\*\*FANC (BE)

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**1.3 Validation and uncertainty analysis of SNF characterization based on SCALE code system; A. Shama, NAGRA; EURAD Annual event 2021; 16 - 18/03/2021**



## Validation and Uncertainty Analyses of SNF Characterization based on SCALE Code System

EURAD WP8/Subtask 2.1

A. Shama (EPFL / Switzerland), 17.03.2021

1



### **Nagra's activities in WP8/Subtask 2.1**

- Subtask 2.1: Theoretical study of SNF source terms
- Subtask leader: PSI
- Contributors: CIEMAT, JSI, NAGRA, PSI, SCK.CEN, VTT, KIT, JRC-Geel, ENRESA
- **Nagra's activities:**
  - (1) Selection of SNF benchmarks (decay heat / nuclide inventory)
  - (2) Modelling of SNF benchmarks
    - Comparison with existing measurements:
      - Calculations using simplified assumptions and modelling
      - Calculations using advanced method
  - (3) Uncertainty propagation
    - Estimate uncertainties of different origins:
      - Nuclear Data (ND)
      - SNF design and irradiation
  - (4) Identification of parameters contributing to uncertainties

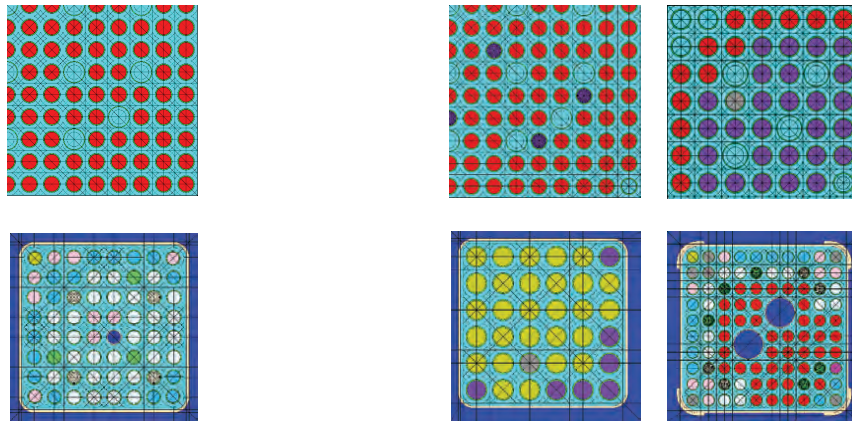
2



## 1. Selection of SNF benchmarks

SNF Decay Heat calorimetric measurements	1. Clab PWR OE2
	2. Clab BWR 6432

SNF Nuclide Inventory PIE samples	1. Takahama SF95-5
	2. KKB BM1
	3. Gundremmingen-7
	4:11. ENRESA 1:8



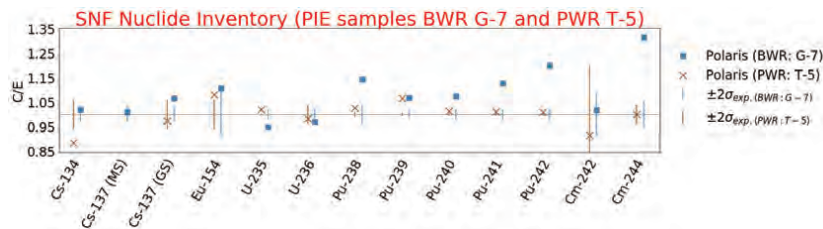
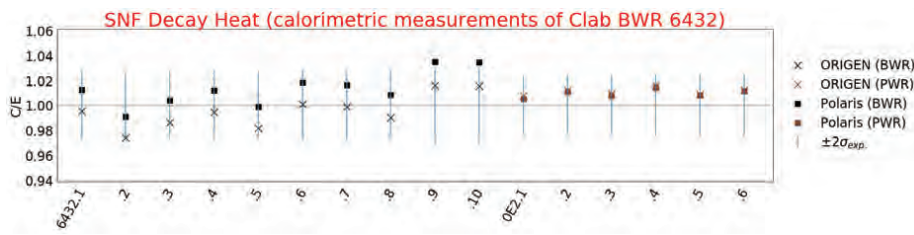
3



## 2. Modelling of SNF benchmarks

Comparison with existing measurements:

- Calculations using simplified assumptions/modelling
  - ORIGEN, prepared one-group XS libraries
- Calculations using advanced method
  - Polaris, 2D lattice code with multi-group XS libraries



4



### 3. Uncertainty Propagation

Estimate uncertainties of different origins:

- Nuclear Data (ND)
  - Cross-sections, Fission-yield, Decay Data: SCALE data based on ENDF/B-VII.1
- SNF design and irradiation
  - Material, geometrical, operational (whenever provided by operators and fuel vendors)
  - NEA/NSC "Evaluation Guide for the Evaluated Spent Nuclear Fuel Assay Database (SFCOMPO)"

Parameter	1 $\sigma$
Clad thickness	16.7 $\mu\text{m}$
Clad diameter	67/100 $\mu\text{m}$ (PWR/BWR)
Pellet density	0.67%
Pellet diameter	6.7 $\mu\text{m}$
U-235 wt.%	0.0167%
SFA powers	1.67%
Water temp. (PWR)	2 K
Water density (PWR)	0.005 g/cm <sup>3</sup>
Void fraction (BWR)	6%
Fuel temp.	50 K
Boron (PWR)	10 ppm

Based on  
[NEA/NSC, 2015]

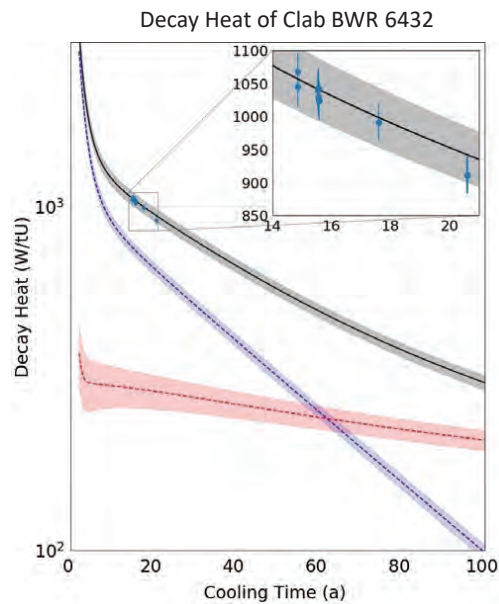
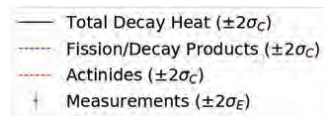
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### 3. Uncertainty Propagation

Estimate uncertainties of different origins:

- Nuclear Data (ND)
- SNF design and irradiation



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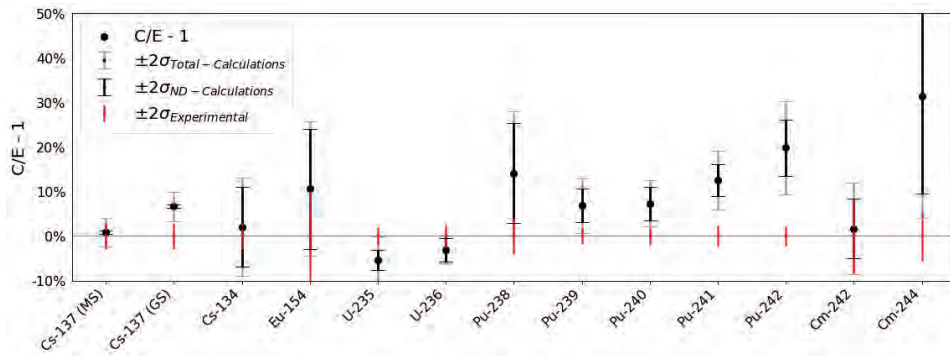


### 3. Uncertainty Propagation

Estimate uncertainties of different origins:

- Nuclear Data (ND)
- SNF design and irradiation

Nuclide conc. in Gundremmingen (BWR) B23 – E3 sample



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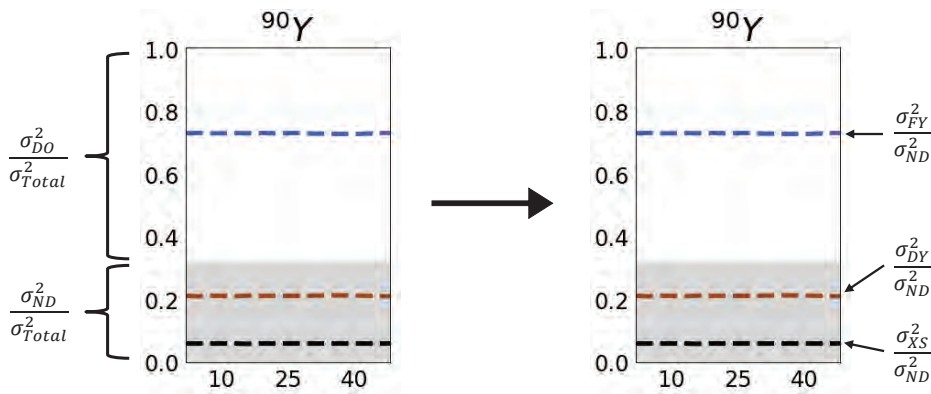
### 4. Identification of relevant parameters contributing to uncertainties

**Nuclear Data:**

by analyzing fractional variances

XS: Cross-sections  
 FY: Fission yield  
 DY: Decay  
 ND: Nuclear Data  
 DO: Design and Operation

$$\sigma_{Total}^2 = \sigma_{ND}^2 + \sigma_{DO}^2 \quad \sigma_{ND}^2 = \sigma_{XS}^2 + \sigma_{FY}^2 + \sigma_{DY}^2$$



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#### 4. Identification of relevant parameters contributing to uncertainties

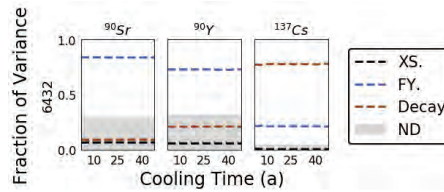
**Nuclear Data:**

by analyzing fractional variances

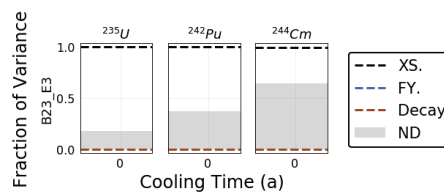
$$\sigma_{total}^2 = \sigma_{ND}^2 + \sigma_{DO}^2 \quad \sigma_{ND}^2 = \sigma_{XS}^2 + \sigma_{FY}^2 + \sigma_{DY}^2$$

XS: Cross-sections  
 FY: Fission yield  
 DY: Decay  
 ND: Nuclear Data  
 DO: Design and Operation

Decay Heat of Clab BWR 6432



Nuclide conc. in Gundremmingen B23 – E3 sample



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#### 4. Identification of parameters contributing to uncertainties

**Model Parameters:**

Correlation Analysis  
 Decay Heat of Clab PWR 0E2 and BWR 6432

	Burnup	U-235 wt. %	Fuel Den.	Clad Rad.	Boron	Water Dens.
0E2	0.97	-0.04	-0.02	0.17	0.01	-0.05
6432	0.96	-0.04	-0.02	0.06	-0.01	-0.24

Correlation Analysis  
 Nuclide conc. in Gundremmingen B23 – E3 sample

	Burnup	U-235 wt. %	Fuel Den.	Clad Rad.	Fuel Rad.	Water Dens.
U-235	-0.73	0.55	0.11	0.09	0.11	-0.41
Pu-239	0.32	0.03	0.2	0.16	0.03	-0.9
Cs-137	1.0	-0.04	-0.03	-0.04	-0.1	0.0

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## Publications

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### (1) Related to SNF decay heats

- **Accepted** in [Nuclear Engineering and Technology](#)  
“Uncertainty Analyses of Spent Nuclear Fuel Decay Heat Calculations using SCALE Modules”
- **Submitted** to [Annals of Nuclear Energy](#)  
“Validation of Spent Nuclear Fuel Decay Heat Calculations Using Polaris, TRITON/ORIGEN-ARP and CASMO5”

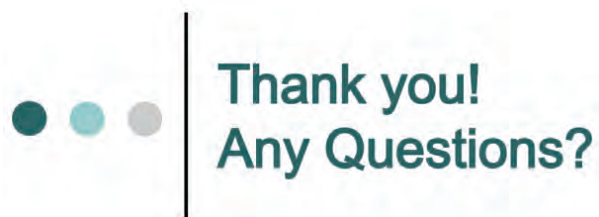
### (2) Related to SNF nuclide concentration

- **Planned**

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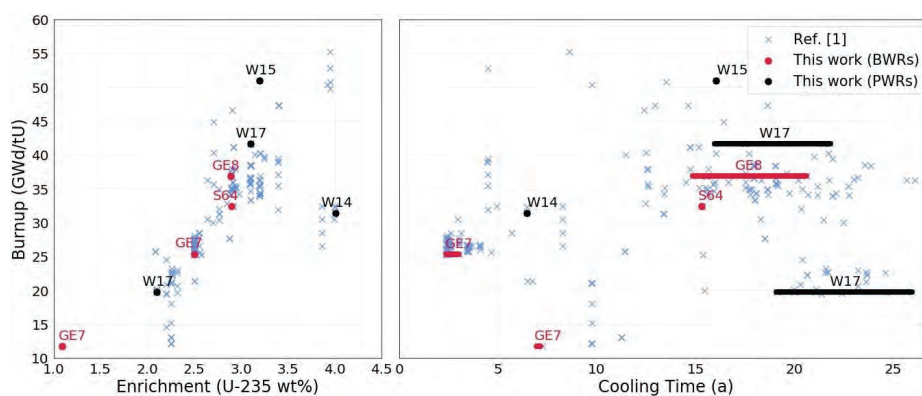
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## Appendix

### (1) Area of Applicability (AOA)



Burnups, enrichments, and cooling times of the selected SFAs

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## Appendix

### (2) Uncertainties of the Measurements

Table 1. Uncertainties ( $2\sigma$ ) in the decay heat measurements at the Clab facility based on [15].

SFA	Power (W)	Uncertainty (W)	Uncertainty (%)
BWR	50	4.2	8.4
	350	6.2	1.8
PWR	250	9.2	3.7
	900	18.8	2.1

Table 2. Uncertainties ( $2\sigma$ ) in the decay heat measurements at the GE-Morris facility based on [5].  
The values correspond to both PWRs and BWRs.

SFA	Power (W)	Uncertainty (W)	Uncertainty (%)
GE	200	16	8
	700	28	4

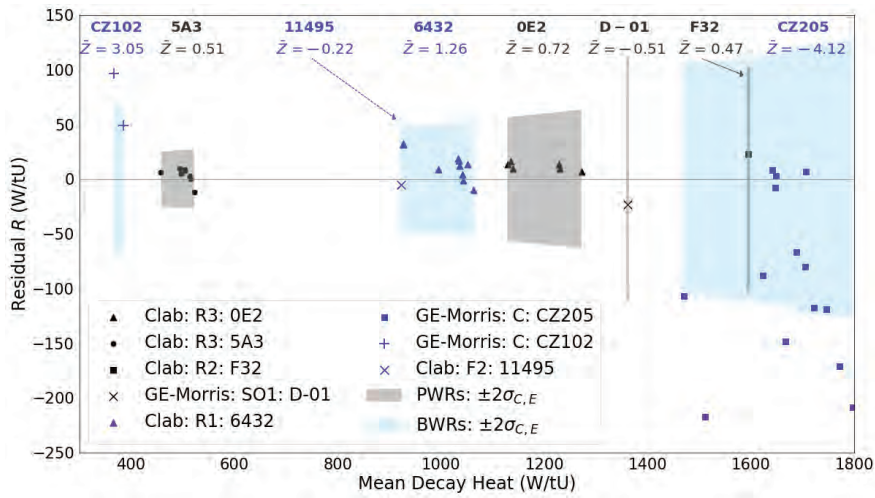
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Appendix

(3) Hypothesis Testing on Calc. and Meas.



Mean-difference plot of calculations and measurements along with shaded total uncertainty band. Combined z-scores are shown for each SFA (top).

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Appendix

(4) Uncertainties Components

	Burnup (GWd/tU)	Cooling time (a)	Decay heat (W/tU)	Meas.	Calc.	Total
				(2σ) %		
PWRs	51.0	16.1	1595	2.3	5.6	6.1
BWRs	36.9	16.6	1015	2.8	4.6	5.4

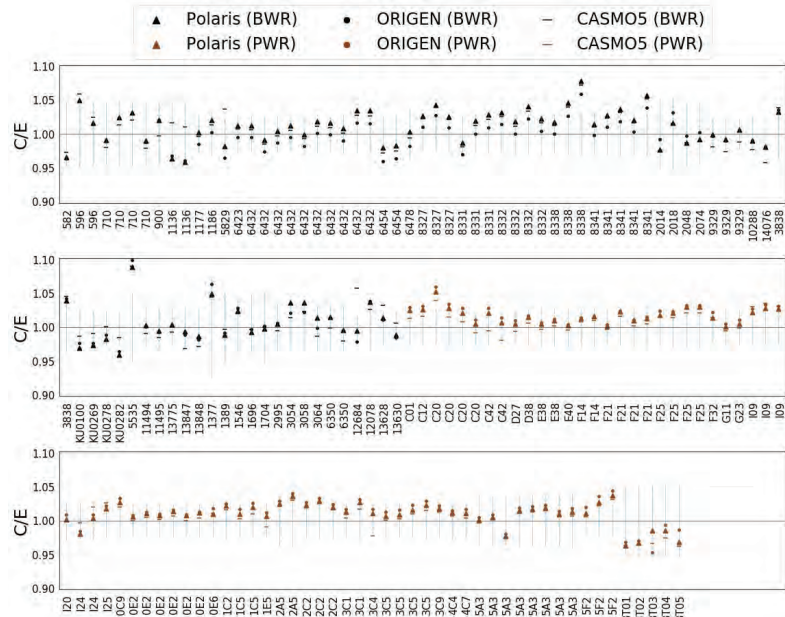
	Burnup (GWd/tU)	Cooling time (a)	Decay heat (W/tU)	Calc.	ND	DO
				(2σ) %		
PWRs	51.0	16.1	1595	5.6	3.1	4.7
BWRs	36.9	16.6	1015	4.6	1.8	4.2

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## Appendix

### (5) Validation (Clab)

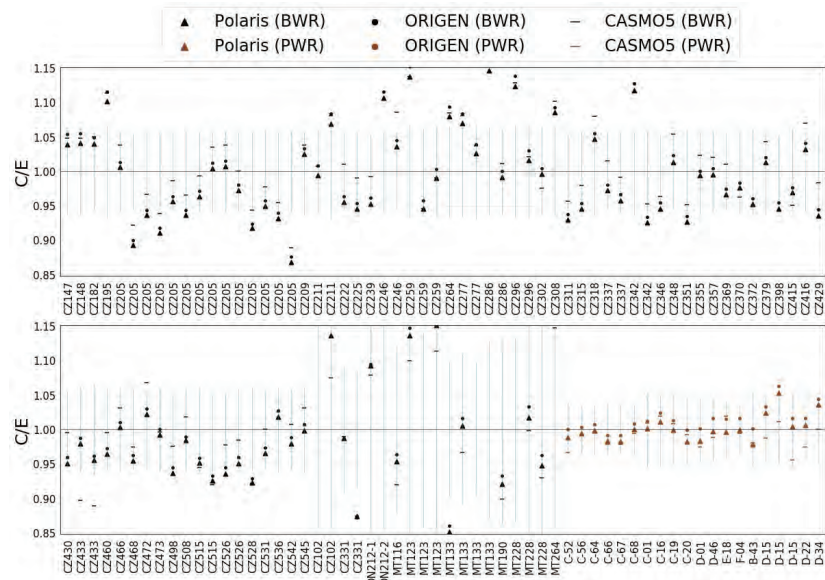


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## Appendix

### (5) Validation (GE and HEDL)



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**1.4 Fuel dry storage modelling with INL's BISON code at VTT; A. Arkoma, VTT; WP8 SFC Annual Meeting 2023; 11/1/2023**



## THERMO-MECHANICAL PROPERTIES OF THE SNF CLADDING: CREEP MODELLING WITH THE BISON CODE

1 November 2023 • Asko Arkoma (VTT)



*This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement N°847593.*

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### Outline

- Background for the investigation
- Applied simulation tool
- Modifications to the code
- Simulation cases
- Results of the verification simulation
- Creep results of the CIP0-1 mother rod
- Summary and conclusions



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VTT

## Background for the study

- Creep rupture is one of the postulated cladding failure mechanism during dry storage, another being embrittlement caused by hydrides
- In this work, CIEMAT's dry storage creep law (Feria and Herranz, 2011; Feria et al., 2015) was implemented into fuel performance code BISON
  - Previously, the model has been implemented (Arkoma et al., 2018) into VTT's version of the ENIGMA code
  - No dry storage creep model was available in BISON

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VTT

## Simulation tool: BISON fuel performance code

- Developed by Idaho National Laboratories (INL) since 2009 (Newman et al., 2009)
- BISON is built within the INL's MOOSE (Multi-physics Object-Oriented Simulation Environment) framework (Gaston et al., 2009)
  - MOOSE is a general solver that uses finite element method (FEM) to solve partial differential equations
- BISON solves the fully coupled thermo-mechanics and species diffusion in 1D-, 2D- (axisymmetric) and 3D-geometries
- Fuel models describe temperature and burnup dependent thermal properties, swelling, densification, thermal and irradiation creep, relocation, fracture, and fission gas production and release
- In order to model cladding mechanical behaviour, plasticity, irradiation growth, and thermal and irradiation creep models are included
- Models are also able to simulate gap heat transfer, mechanical contact, and the evolution of free volume pressure
- The calculation mesh can be generated with an external tool, or a simple mesh created through the input file

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VTT

## Modifications to the code

- The implemented dry storage creep law by CIEMAT (Feria and Herranz, 2011; Feria et al., 2015):

$$\varepsilon_{\theta} = \frac{a\sigma_{\theta}^b e^{-c/T} e^{-d/\phi t}}{\sqrt{t_{dry\_storage}}}$$

- a, b, c and d are fitted constants
- $t_{dry\_storage}$  is the time spent in dry storage,  $\phi t$  is the fast neutron fluence
- The law is based on experimental database of stress-relieved annealed Zircaloy-4 cladding alloy
- The default creep model in BISON by Limbäck and Hoppe is used before entering the dry storage period (INL, 2023)
- The cladding oxidation model in BISON is modified to stop outer surface oxidation during wet and dry storage
  - Without this modification, the default EPRI/KWU/C-E oxidation model in BISON continues to produce significant oxidation during dry storage

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## Simulation cases

### Verification case

- To verify the implementation, the creep model was first tested with a spent fuel example input delivered with BISON
- In this simple case, constant linear heat rate of 25 kW/m and axially flat power profile is used throughout the irradiation
- Rod segment consisted of ten pellets, and the calculation mesh was generated with an external meshing tool (the mesh file was also provided with the code delivery)
- Three radial and 40 axial meshes in the cladding
- Average burnup of 58 GWd/tU

### Application to a full rod irradiated in a commercial reactor (CABRI CIP0-1 mother rod)

- Next, the law was applied to the mother rod of a reactivity-initiated accident (RIA) test made in CABRI test reactor, the CIP0-1 test: 17x17 PWR rod with Zirlo cladding, mother rod average burnup 68 GWd/tU
- 2D axisymmetric mesh with smeared solid fuel pellets (i.e., no dishes and chamfers) was generated within the BISON input file
- For the sake of simplicity, wet storage period was not modelled except that there is a period of one week with 50 °C in between the irradiation and dry storage
- The number of pellet and cladding elements in axial direction was 200 and in radial direction 12 and 4, respectively
- Cladding thermal boundary conditions during steady-state calculated by the built-in coolant channel model of BISON
  - Flat axial temperature profile was imposed during dry storage, the evolution given by Penalva et al., 2021

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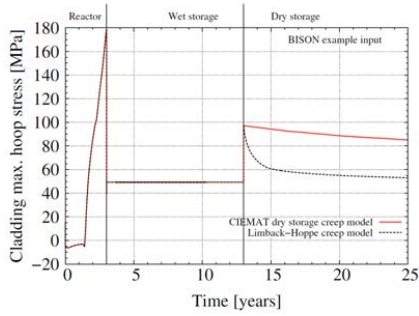
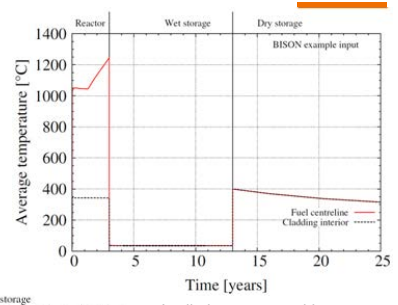
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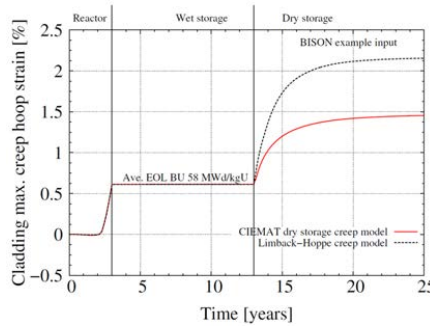
## Verification of the creep model

- The results show high creep at the beginning of dry storage, and after a few years, the creep rate slows down
- The results are qualitatively reasonable
- The behaviour is consistent with the earlier results with the CIEMAT correlation calculated with FRAPCON-xt (Feria et al., 2015)



Axially maximum cladding hoop stress calculated with the CIEMAT model and compared with the default Limbäck-Hoppe creep model

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Axially maximum cladding creep hoop strain calculated with the CIEMAT model and compared with the default Limbäck-Hoppe creep model

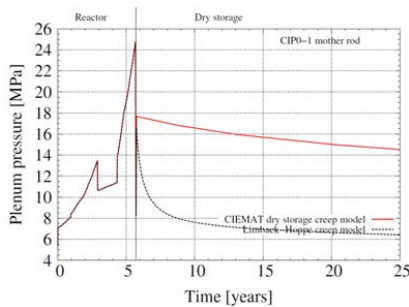
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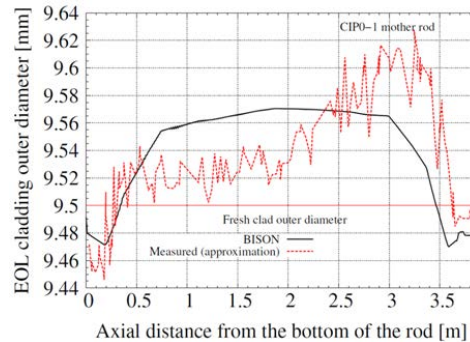
## Simulated state of CIP0-1 mother rod prior to dry storage

VTT

- Calculated FGR is 8.2% and measured is 7.4% (NEA, 2022)
- Calculated end-of-life plenum volume is 10.5 cm<sup>3</sup> at 20 °C; measured free volume 12.26 cm<sup>3</sup>
- Measured plenum pressure 5.85 MPa at 0 °C



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Cladding outer surface diameter axial profile after irradiation at 20 °C. Comparison is made to paper by Georgethuth et al. (2017), where the measurement result is published. In the figure, one of the curves from the paper is digitalized (approximation)

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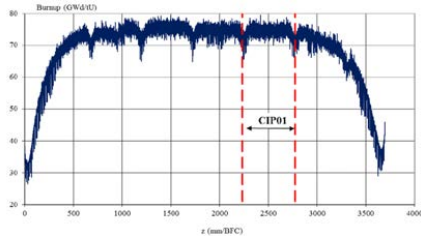




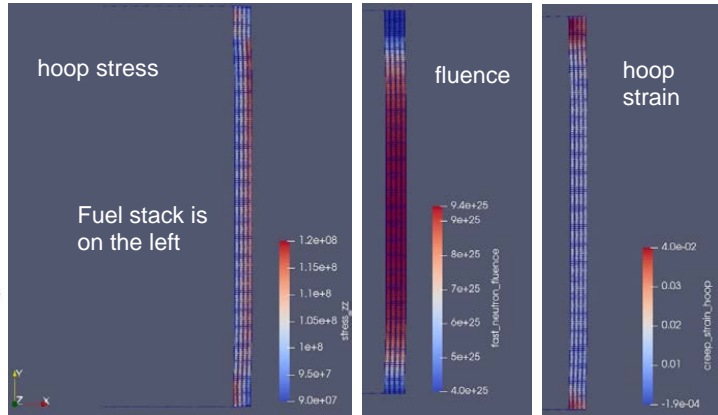
## Creep results of the CIP0-1 mother rod (1/2)



- Creep is highest at both ends of the rod
  - Calculated hoop stress axial distribution is quite uniform, but the fast neutron fluence distribution is non-uniform
  - Fast fluence (thus, burnup) is lower at the end parts of the rod, and according to the CIEMAT creep correlation that results in higher creep
  - The maximum creep strain after 19.2 years of dry storage in is 3.0% (at the ends of the rods) and 0.9% in the axial middle part of the rod

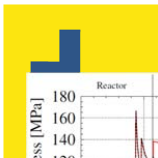


Axial burnup profile in CIP0-1 mother rod (NEA, 2022)



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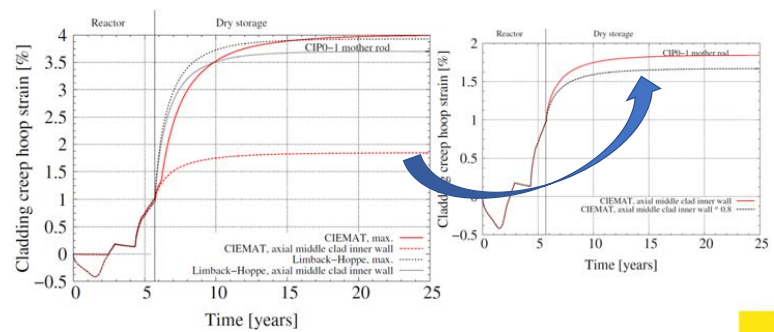
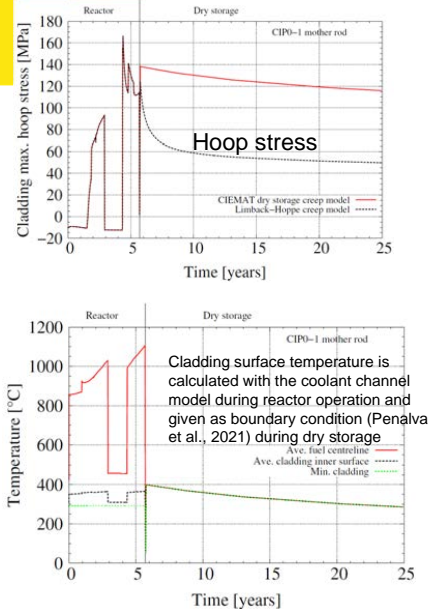
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## Creep results of the CIP0-1 mother rod (2/2)



- The Limbäck-Hoppe steady-state creep model for Zirlo applies a factor of 0.8 to decrease the creep given by the creep law of Zry-4. However, during dry storage, this model is bypassed and replaced by the CIEMAT model in which this reduction was not applied
  - If the 0.8 multiplication factor is applied, the innerwall axial midplane hoop creep strain at the end of dry storage simulation is reduced from 0.9% to 0.7%



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Creep hoop strain







## Summary and conclusions

VTT

- CIEMAT's dry storage creep law was implemented into INL's fuel performance code BISON
- The creep law was tested with a spent fuel example input delivered with BISON, and the results were found to be qualitatively reasonable
- Then the law was applied to the mother rod of a RIA test rodlet tested in CABRI sodium loop, the CIP0-1 test
- In addition to creep, cladding hydrogen radial distribution in the beginning of dry storage was modelled in CIP0-1 mother rod with BISON by making use of the existing models in BISON (results are given in VTT Research Report)
- Compared to FRAPCON-xt results of the CIP0-1 mother rod, creep calculated with BISON is considerable higher
  - According to analysis by CIEMAT, the differences can be explained by the differences in calculated rod internal pressure and fast neutron fluence prior to dry storage, and different calculated stress evolution during the dry storage
- In the CIP0-1 mother rod, dry storage creep was found to be mostly reasonable (i.e., less than 1%) but in the top and bottom parts of the rod, the creep was considerable higher
  - In these parts, the fast neutron fluence (burnup) was lower, and that results in higher creep according to the CIEMAT creep correlation

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## References

VTT

- Arkoma, A., Huhtanen, R., Leppänen, J., Peltola, J., Pättikangas, T., 2018. Calculation chain for the analysis of spent nuclear fuel in long-term interim dry storage. *Annals of Nuclear Energy*, Vol. 119, pp. 129–138
- Feria, F., Herranz, L.E., Penalva, J., 2015. On the way to enabling FRAPCON-3 to model spent fuel under dry storage conditions: the thermal evolution. *Annals of Nuclear Energy* 85, 995–1002.
- Feria, F., Herranz, L.E., 2011. Creep assessment of Zry-4 clad high burnup fuel under dry storage. *Prog. Nucl. Energy* 53, 395–400.
- Gaston, D., Newman, C., Hansen, G., Lebrun-Grandié, D., 2009. MOOSE: A parallel computational framework for coupled systems of nonlinear equations. *Nuclear Engineering and Design*, Vol. 239, pp.1768–1778.
- Georgenthum, V., Folsom, C., Moal, A., Marchand, O., Williamson, R., Ban, H., Wachs, D., 2017. SCANAIR-BISON BENCHMARK ON CIP0-1 RIA TEST. *Water Reactor Fuel Performance Meeting 2017*, September 10-14, Korea
- INL, 2023. Complete BISON input syntax and reference manual. <https://mooseframework.inl.gov/bison/syntax/index.html> (accessed 2 Aug. 2023)
- NEA, 2022. Reactivity Initiated Accident Benchmark Phase III Report. NEA/CSNI/R(2020)10
- Newman, C., Hansen, G., Gaston, D., 2009. Three dimensional coupled simulation of thermomechanics, heat, and oxygen diffusion in UO<sub>2</sub> nuclear fuel rods. *Journal of Nuclear Materials*, Vol. 392, pp. 6–15.
- Penalva, J., Feria, F., Herranz, L.E., 2021. Modeling maximum fuel temperature in dry storage: From the CFD analysis to the engineering approach. *Nuclear Engineering and Design*, Volume 383, 111435.

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**1.5 Statistical approach for evaluating the safety of spent fuel during transport accidents; C. Aguado, F. Feria, L.E. Herranz, CIEMAT; WP8 SFC Annual Meeting 2023; 11/1/2023**



## Subtask 4.1 - CIEMAT

### Statistical approach for evaluating the safety of spent fuel during transport accidents

C. Aguado, F. Feria, L.E. Herranz (CIEMAT)

EURAD WP8 SFC – Spent Fuel Characterization and evolution until disposal

SFC Annual meeting, November 01-02, 2023



*This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement N°847593.*

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## OUTLINE

- INTRODUCTION
- METHODOLOGY
- APPLICATION
- FINAL REMARKS

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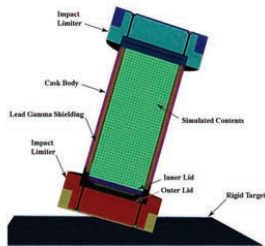
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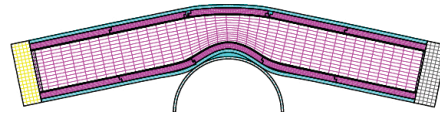


## INTRODUCTION

3D codes based full mechanical evaluation of SNF under handling/transport accidents require high computational cost...

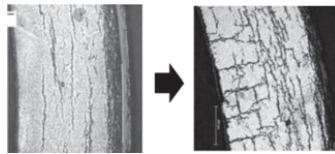


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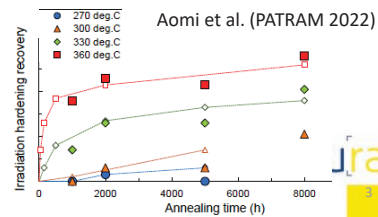
... and further clad characterization after irradiation & storage is needed

### Hydrides embrittlement



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### Irradiation damage annealing



## INTRODUCTION

### Main goal

Development of a methodology for the assessment of SNF performance under handling/transport accident from statistical cladding characterization based on 1D T-M tools

### Main achievements

- Derivation and verification of proof of concept from information available
- Assessment of factors affecting cladding mechanics:
  - Radial hydrides embrittlement
  - Irradiation damage annealing

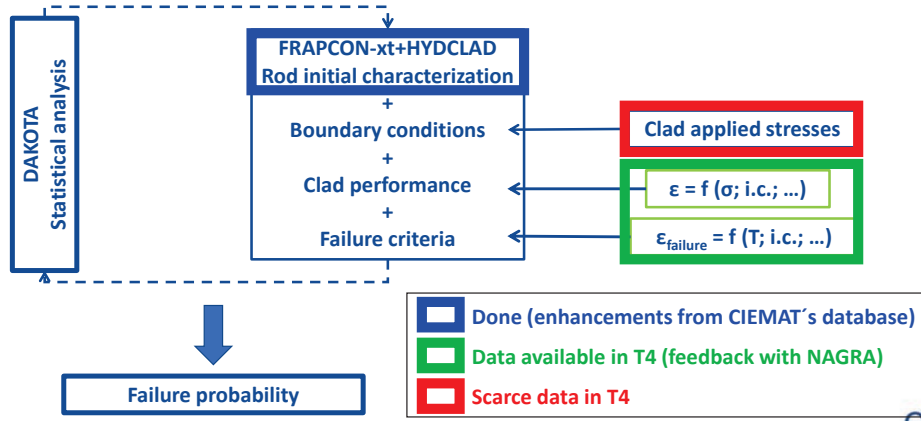
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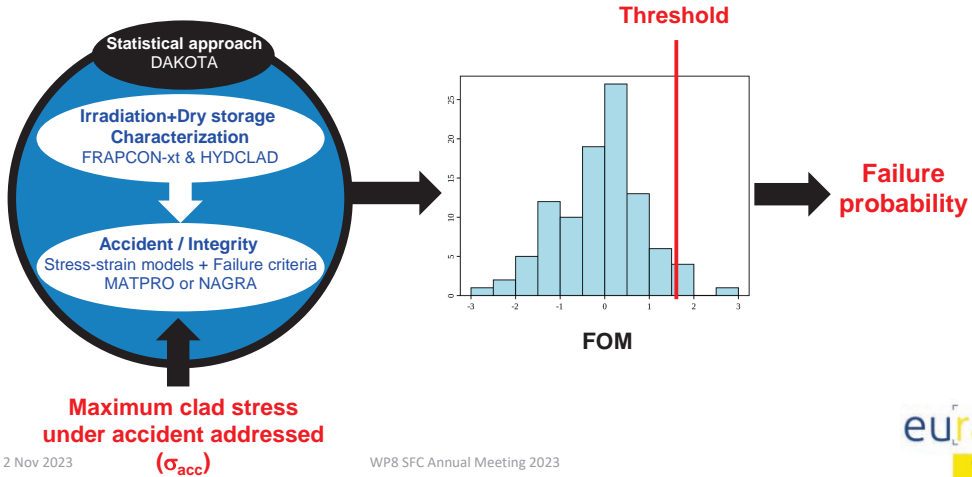


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## METHODOLOGY APPROACH



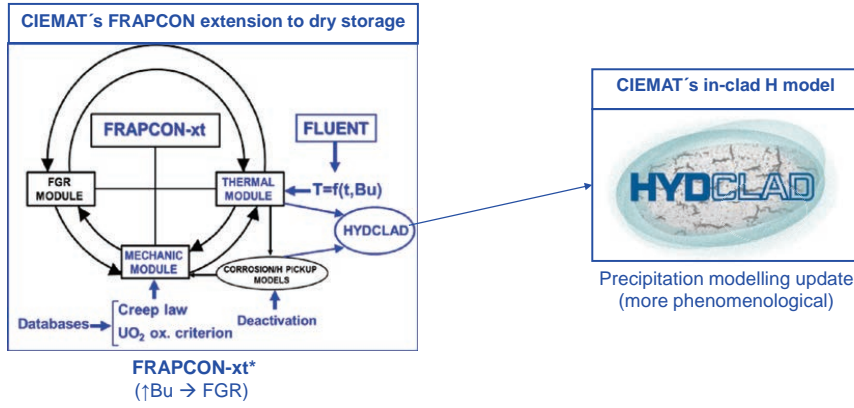
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## METHODOLOGY TOOLS (UPDATE IN T3.1)

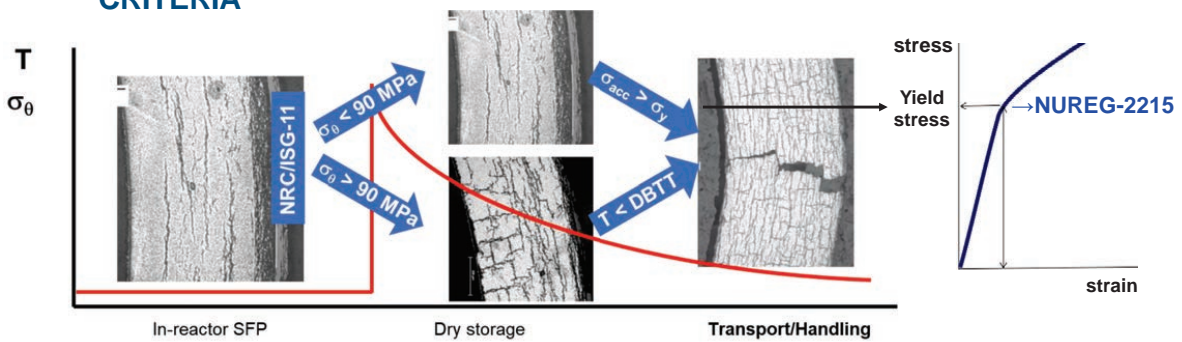


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## METHODOLOGY CRITERIA



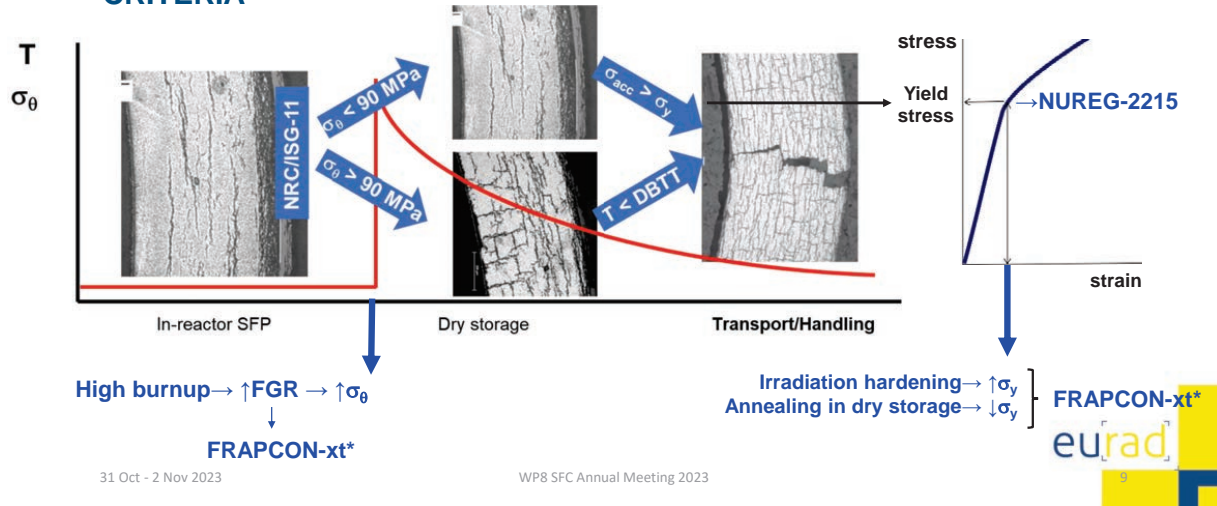
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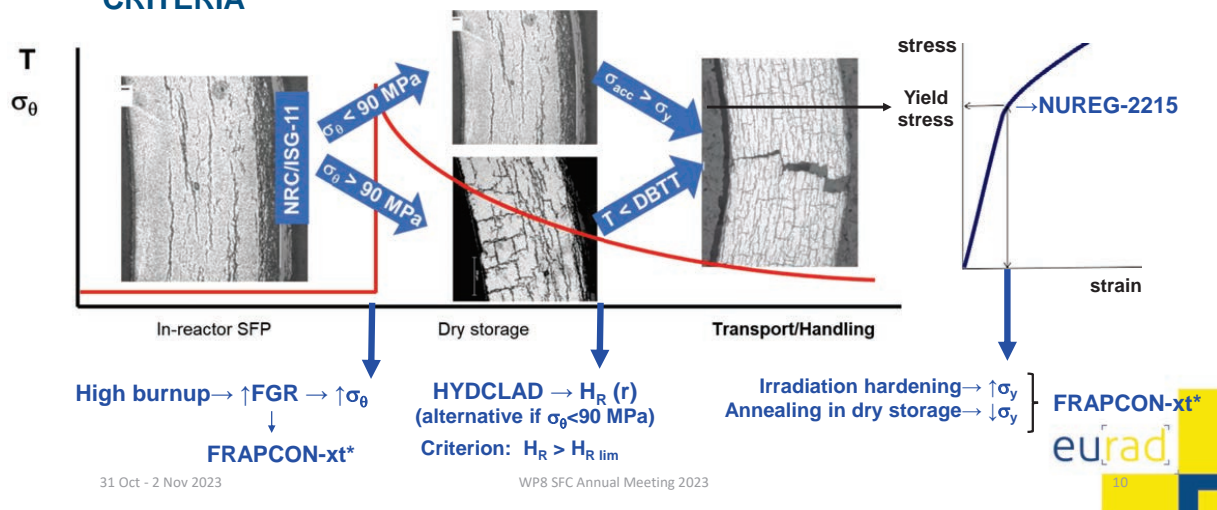


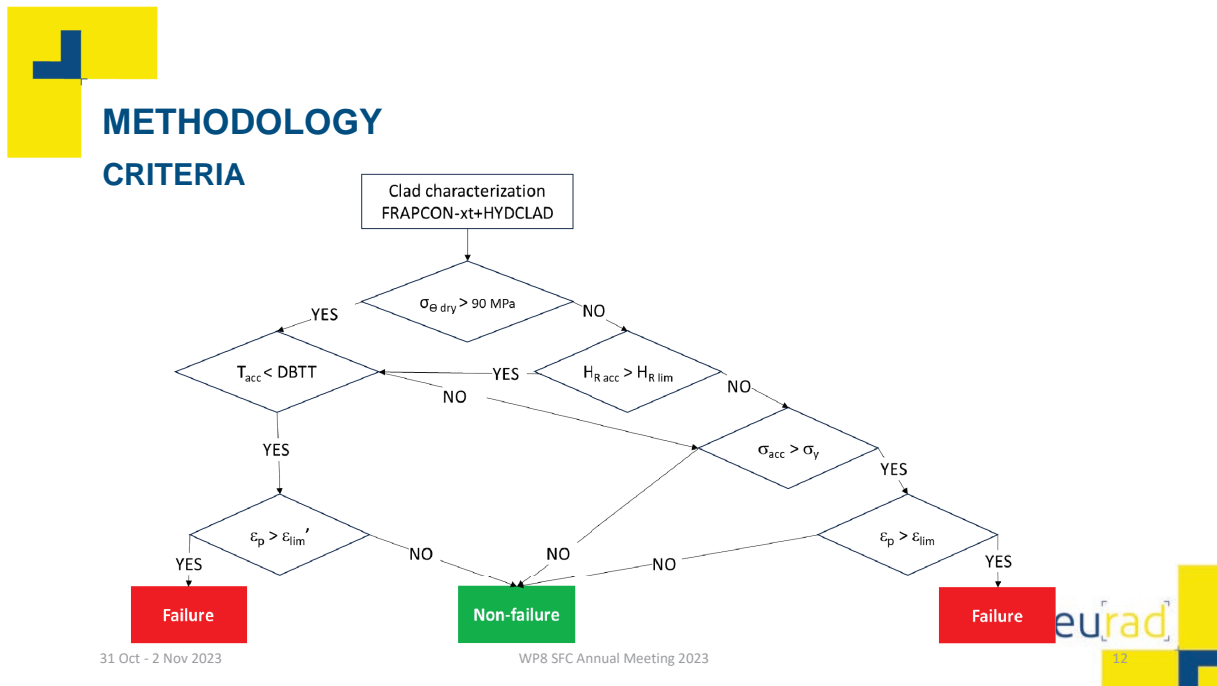
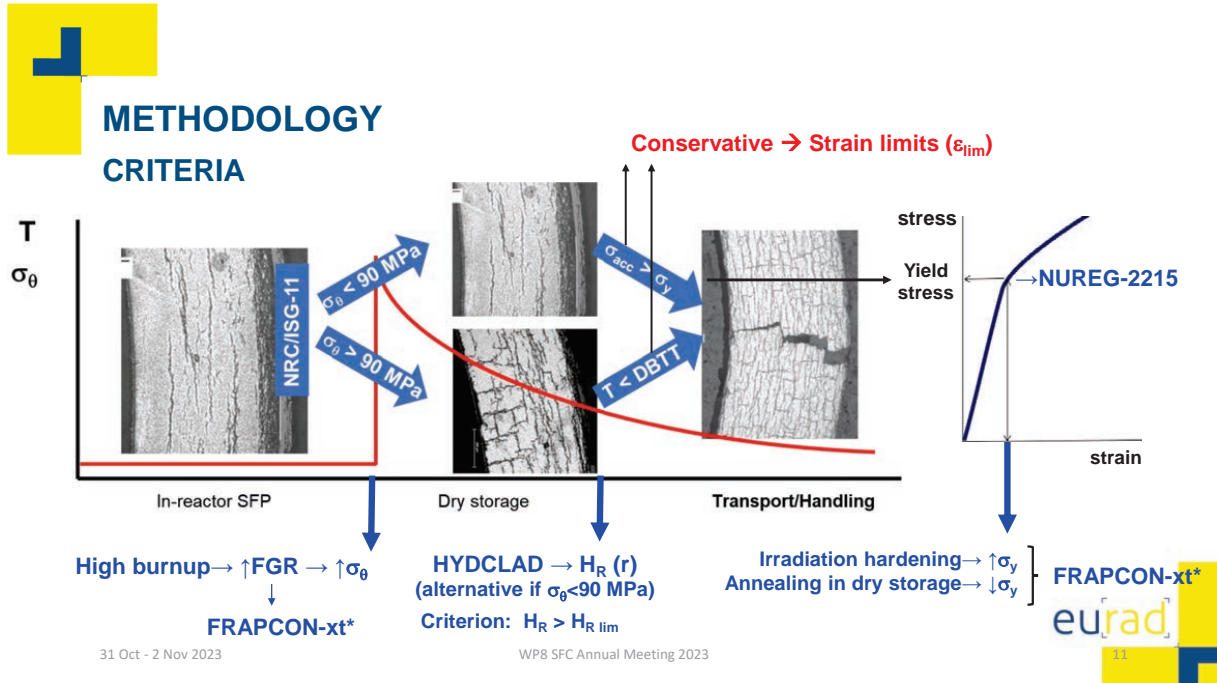


## METHODOLOGY CRITERIA



## METHODOLOGY CRITERIA



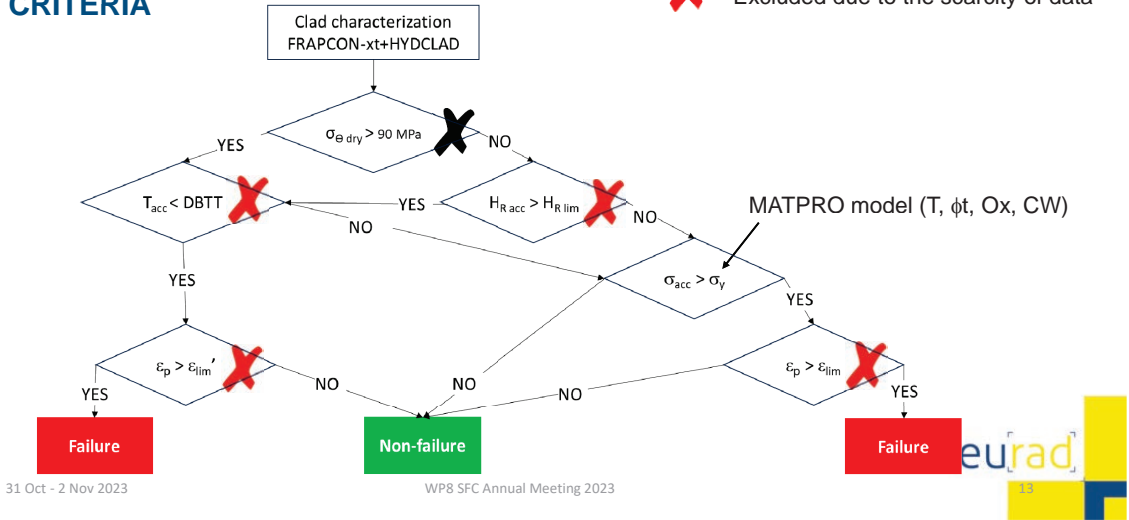






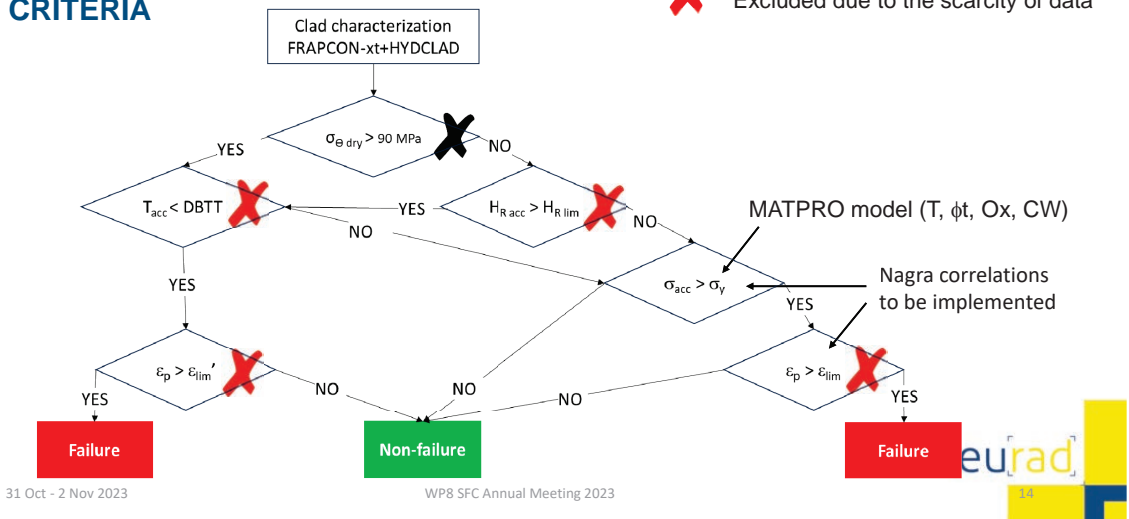
**METHODOLOGY  
CRITERIA**

- Excluded for axial loads
- Excluded due to the scarcity of data



**METHODOLOGY  
CRITERIA**

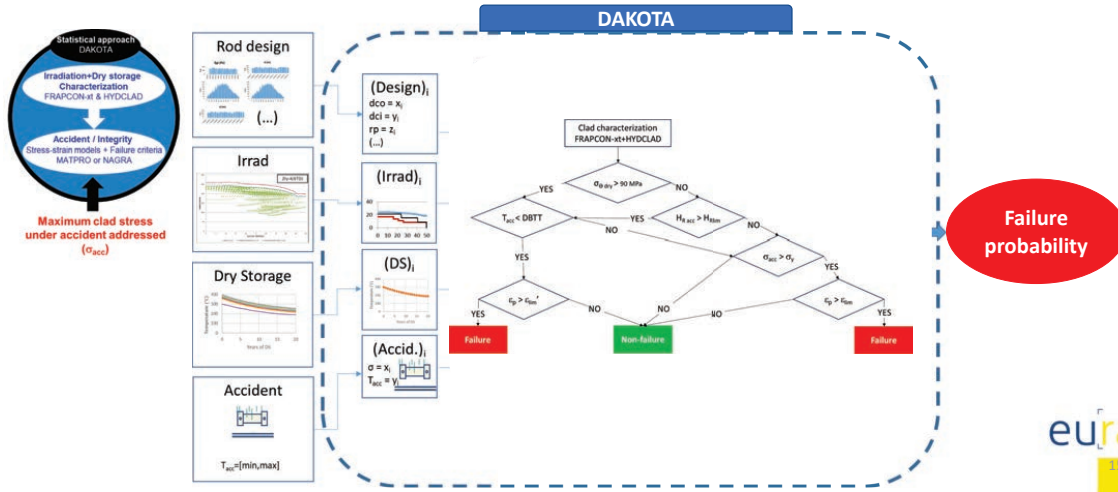
- Excluded for axial loads
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## METHODOLOGY

### STATITICAL ANALYSIS - MONTECARLO BASED



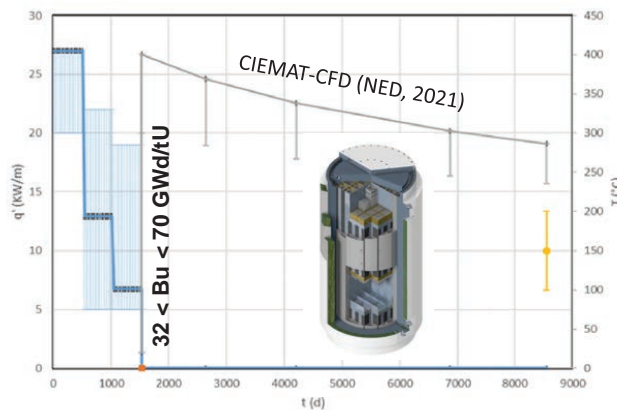
## APPLICATION

### SCENARIO

**PWR 17x17**    **Irradiation**    **Dry storage - Metallic cask**    **Handling accident**

**Variability: Rod design + Power history + Clad temperature (DS&Accident) + Clad maximum stress ( $\sigma_{acc}$ )**

↑  
Open literature



↓  
**405 MPa**  
(IDOM, sT 4.1, 2021)

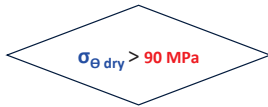
Maximum stress in cladding during a 75 g side drop accident (17x17 fuel assembly)

31 Oct - 2 Nov 2023

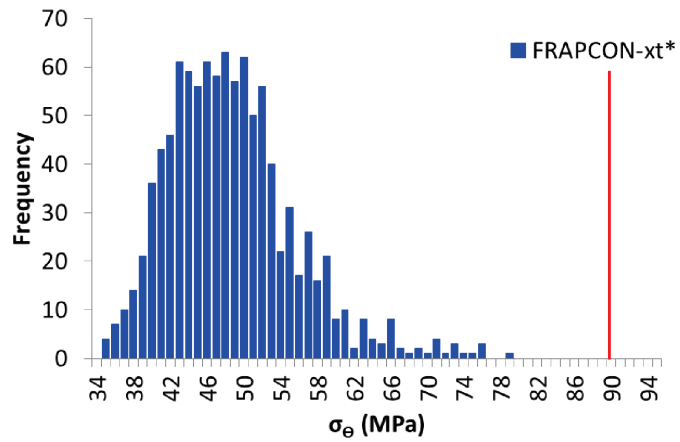




**APPLICATION  
BASE CASE**



31 Oct - 2 Nov 2023

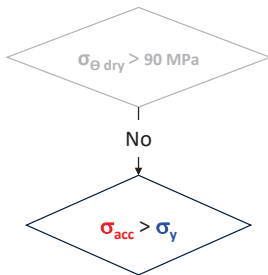


No radial hydrides embrittlement

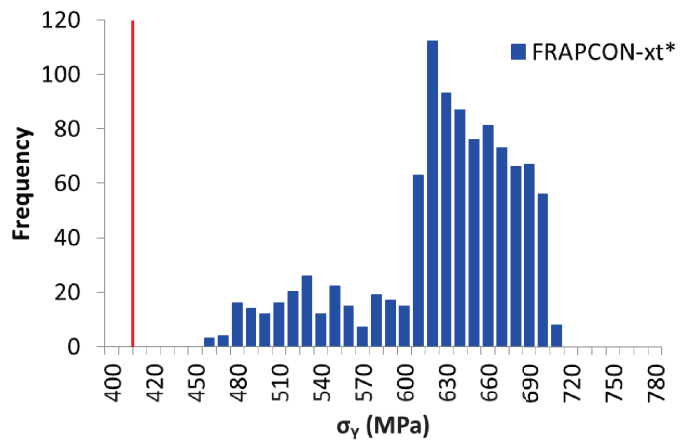
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**APPLICATION  
BASE CASE**



31 Oct - 2 Nov 2023



Failure probability = 0%

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## APPLICATION SCOPING CALCULATIONS

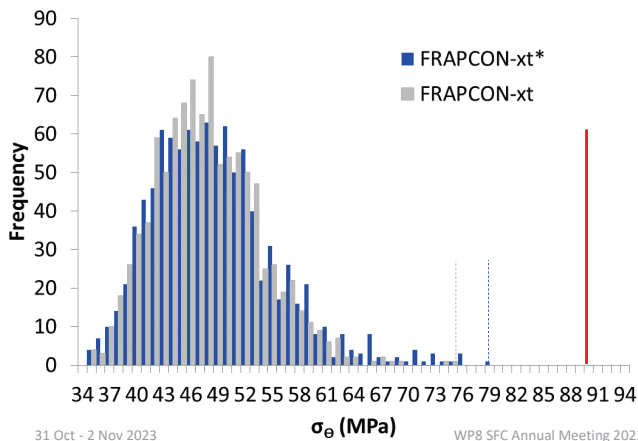
- **Stress at drying for radial hydrides embrittlement** – FRAPCON-xt vs FRAPCON-xt\*
- **Yield stress at accident** – Full annealing vs no annealing

31 Oct - 2 Nov 2023

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## APPLICATION STRESS AT DRYING



No significant impact of the FGR modeling improvement up to 70 GWd/tU

31 Oct - 2 Nov 2023

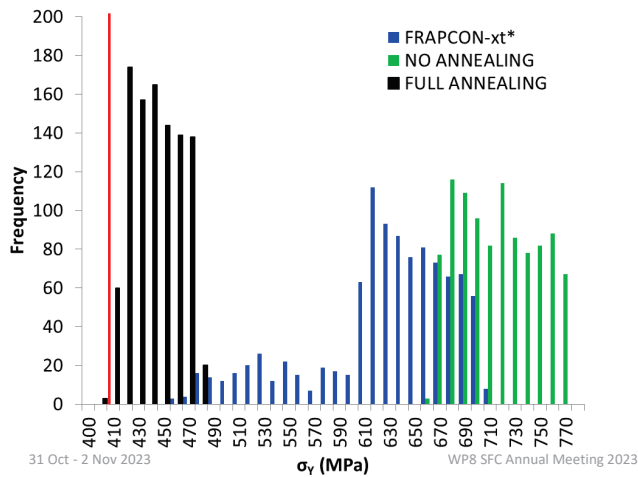
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## APPLICATION

### YIELD STRESS AT ACCIDENT



Significant impact of the IDA model



## APPLICATION

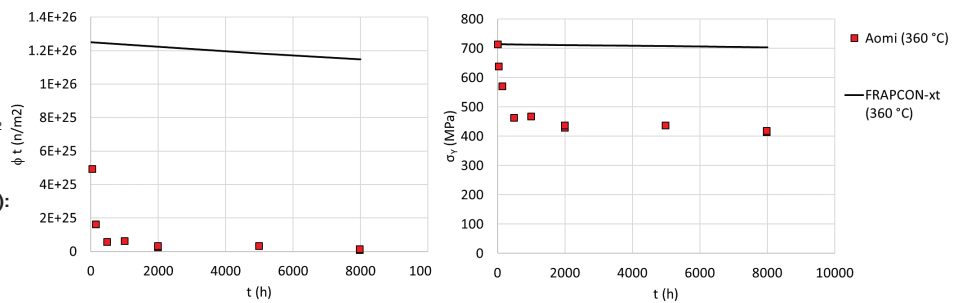
### YIELD STRESS AT ACCIDENT - ANNEALING DATA FROM LITERATURE

**FRAPCON-xt (MATPRO):**

- 220 – 700 °C
- $3.6 \cdot 10^{23} - 4.4 \cdot 10^{25} \text{ n/m}^2$

**New data (Aomi et al., 2023):**

- 270 – 360 °C
- $11.9 - 13.2 \cdot 10^{25} \text{ n/m}^2$



Significant differences between MATPRO and new data





## FINAL REMARKS

- CIEMAT has developed a methodology to evaluate SNF under handling/transport accidents, based on statistical cladding characterization.
- The proof of concept derived has been verified. It allows analyzing the impact of aspects of interest for the cladding characterization.
- Main conclusions:
  - Safety margin of hoop stress at drying for radial hydrides embrittlement (up to 70 GWd/tU).
  - Potential impact of irradiation damage annealing.
- Further work:
  - Continuation of irradiation damage annealing analysis.
  - NAGRA's data implementation. WP8 SFC Annual Meeting 2023



**THANK YOU FOR YOUR ATTENTION!!**



**1.6 Mechanical behaviour of pre- hydrided cladding; Miguel  
Cristóbal-Beneyto, Jesus Ruiz-Hervias, Daniel Pérez-Gallego;  
WP8 SFC Annual Meeting 2023; 11/01/2023**



# Mechanical behaviour of pre-hydrated cladding

*Miguel Cristóbal-Beneyto, Jesus Ruiz-Hervias, Daniel Pérez-Gallego*

Department of Materials Science  
Universidad Politécnica de Madrid (UPM), Spain  
[miguel.cristobal@upm.es](mailto:miguel.cristobal@upm.es)



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## INDEX



Introduction



Experimental



Results



Conclusions



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## INTRODUCTION

- Cladding is the first engineering barrier: let us take advantage of it.
- In-reactor cladding degradation: irradiation, corrosion, creep, **H pickup**
- Effect on cladding safety? (particularly in case of accident)
- Structural integrity cladding/rod: irradiated samples (scarce & expensive)
- Non-irradiated material: alternative to develop testing protocols applicable to irradiated material, increasing test outcome



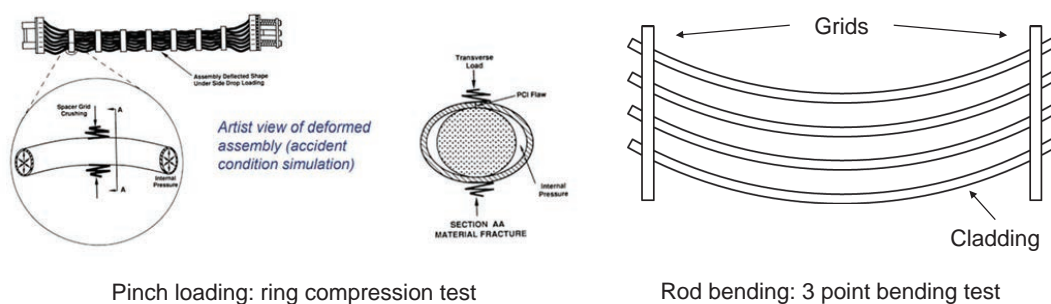
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## INTRODUCTION

### Cask drop accident: rod failure modes



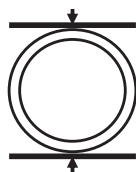
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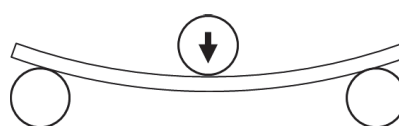
## INTRODUCTION

- **Objective**
  - **Study the mechanical behavior of un-irradiated pre-hydrided cladding in accident conditions**
    - Perform RCT test and TPB in pre-hydrided samples
      - Effect of hydride morphology
      - Effect of surrogate fuel pellet
      - Effect of temperature

Ring compression test



3 point bending test

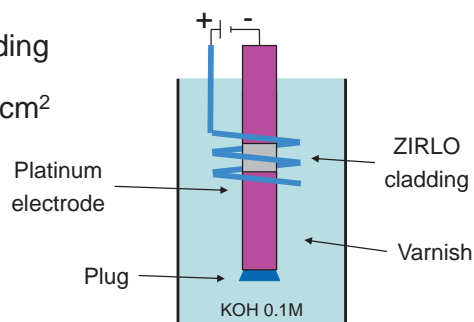


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## EXPERIMENTAL

- **Hydrogen charge**
  - ZIRLO<sup>1</sup> cladding samples
  - Charge through the outer surface of cladding
  - Cathodic charge: 3h, 0.1 M KOH, 0.25 A/cm<sup>2</sup>
  - Precipitation treatment:
    - 7h at 450 °C
    - Cooling at 60 °C/h



<sup>1</sup> ZIRLO® is a registered trademark of Westinghouse Electric Company, LLC, its affiliates and/or its subsidiaries in the United States of America and may be registered in other countries throughout the world. All rights reserved. Unauthorized use is strictly prohibited.

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## EXPERIMENTAL

- Hydride Reorientation treatment (RHT)**
  - Using internal pressure (argon gas)
  - Independent temperature and pressure control
  - T = 400 °C
  - P = 19 MPa →  $\sigma_{\theta} = 140$  MPa

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## EXPERIMENTAL

- Ring compression test**
  - Sample is compressed between two parallel plates

RCT setup

- Three point bending**
  - Sample is placed over two supports, and load is applied in the middle point
  - Similar to JRC-KA

TPB device schematic

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## EXPERIMENTAL

- **Test conditions:**

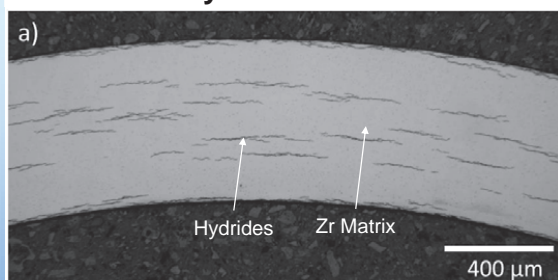
	Filling	Hydrides	Temperature
RCT	Hollow	Circumferential	20, 135 and 300 °C
		Radial	20, 135 and 300 °C
	Inserts	Circumferential	20°C
		Radial	20°C

TPB	Hollow	As Received	20, 135 and 300 °C
		Circumferential	20, 135 and 300 °C
	Inserts	As Received	20, 135 and 300 °C
		Circumferential	20, 135 and 300 °C

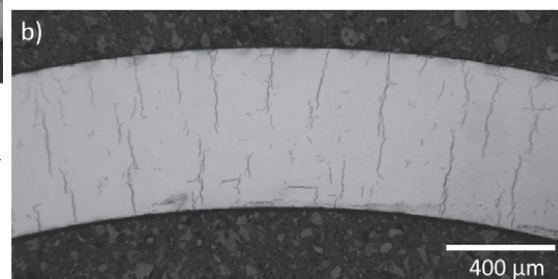


## RESULTS

### Hydride Reorientation treatment: 140 MPa hoop stress



← Before RHT ( $\approx$  75 wppm Hydrogen)



Microstructure of samples:  
(a) before and (b) after  
reorientation treatment

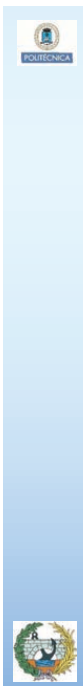
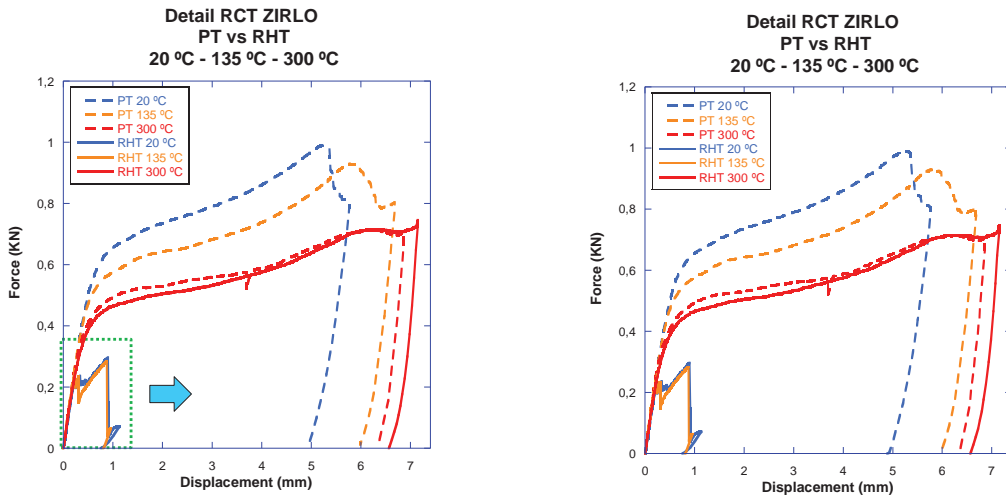
After RHT →





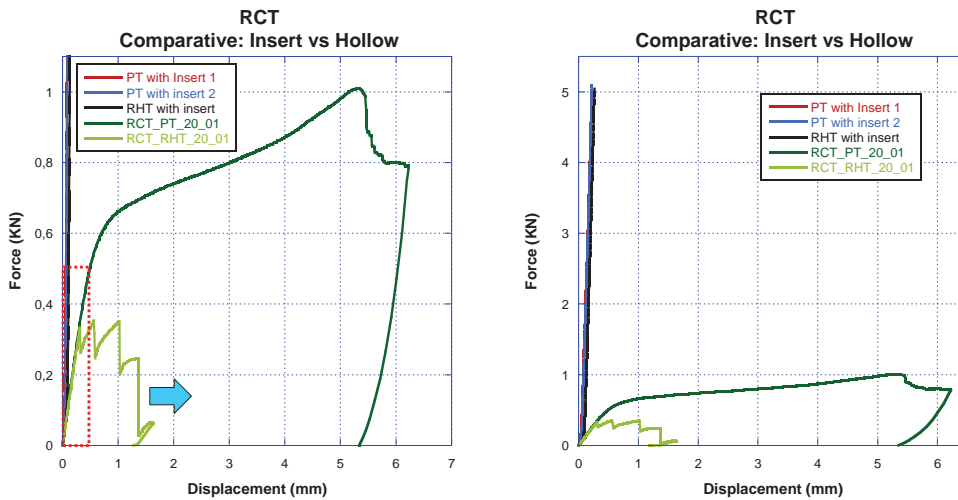
# RESULTS

## Ring compression tests (RCT): hollow samples



# RESULTS

## Ring compression tests (RCT): surrogate pellet





## RESULTS

### Ring compression tests (RCT)

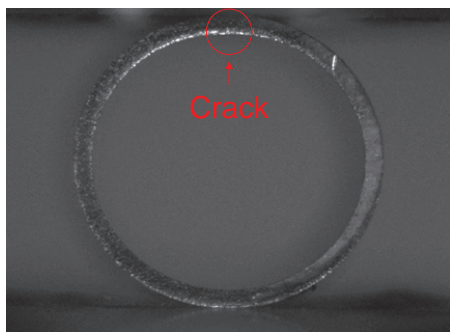


Image of hollow sample with radial hydrides during RCT at failure

**Max. Load: 0,33 KN**  
**Displacement: 0,32 mm**



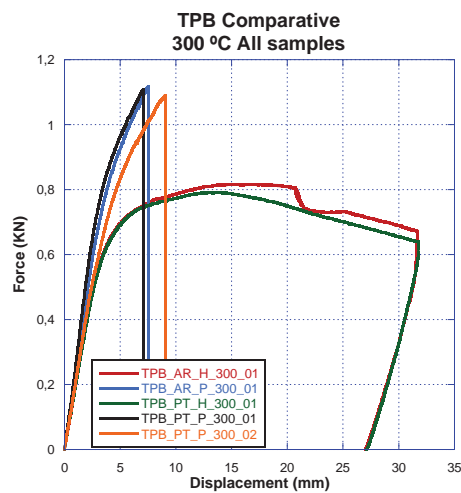
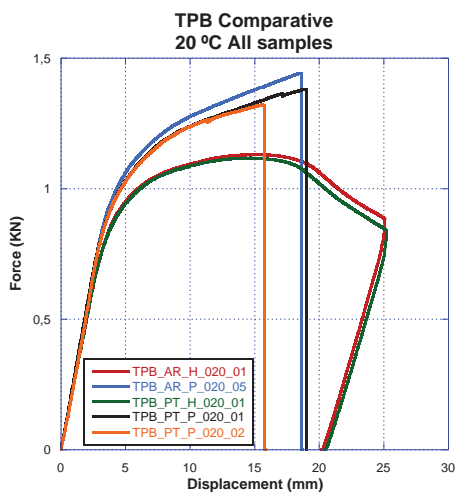
Image of sample with insert and circumferential hydrides during RCT at same load

**Load: 0,33 KN**  
**Displacement: 0,1 mm**



## RESULTS

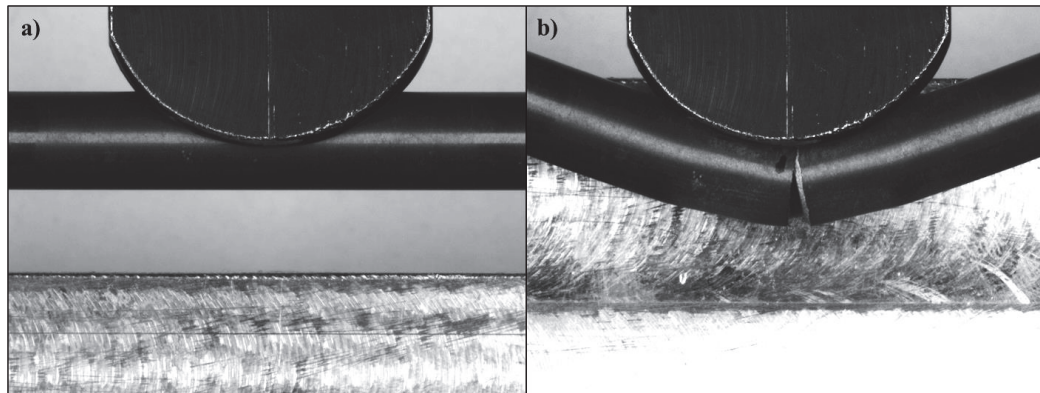
### Three point bending tests





## RESULTS

### Three point bending tests



Images taking during the TPB test of a sample with ceramic inserts at 20 °C at a) beginning of the test, and b) after max load



## CONCLUSIONS

- **ZIRLO ® samples were charged with  $\approx 100$  wppm hydrogen**
- **Hydrogen reorientation treatment (hoop stress=140 MPa)**
  - Almost full reorientation
  - Long radial hydrides: almost 100 % cladding thickness in some cases
- **RCT tests**
  - Hollow samples: brittle failure with radial hydrides (RT and 135°C)
  - Samples with inserts: no failure with radial hydrides
- **TPB tests**
  - Cladding behavior dominated by inserts
  - Failure mode: cladding cracking in the boundary between pellets
  - Increasing temperature decreases displacement at failure



## 2. External training course

- Characterization of spent nuclear fuel for intermediate storage and final disposal; P. Schillebeeckx, JRC Geel; ANNETTE school "Final stage of the nuclear lifecycle" KIT, Karlsruhe; 2 - 6/12/2019
- Characterization of spent nuclear fuel by theoretical calculations; P. Schillebeeckx, JRC Geel; Online available (JRC127309);
- Neutron resonance experiments; P. Schillebeeckx, JRC Geel; Summer school on neutron detectors and related applications, Riva del Garda; 30/06 - 04/07/2022
- Spent Nuclear Fuel Characterisation, P. Schillebeeckx, JRC Geel, Training for DG-ENER EURATOM; 28/06/2023
- SNF characterisation by NDA; P. Schillebeeckx, JRC Geel; School on "Nuclear data for depletion calculations; 11/09 - 15/09/2023
- Observables of interest (in spent fuel); G. Žerovnik, JSI-; School on "Nuclear data for depletion calculations" 11/09 - 15/09/2023



**2.1 Characterization of spent nuclear fuel for intermediate storage and final disposal; P. Schillebeeckx, JRC Geel; ANNETTE school "Final stage of the nuclear lifecycle" KIT, Karlsruhe; 2 - 6/12/2019**

# Characterisation of spent nuclear fuel for intermediate storage and final disposal

ANNETTE  
"Final stage of the nuclear lifecycle"

2 – 6 December 2019, Karlsruhe



## Contents

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- Introduction
- Source terms
  - Neutron
  - Gamma-ray
  - Heat
- Theoretical estimation of source terms
  - Principles
  - Nuclear data
  - Fuel properties and irradiation history
- Application: CLAB (SE)

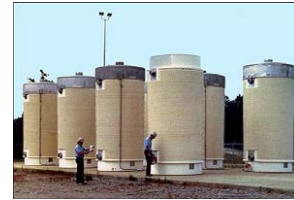
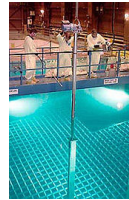


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## Spent Nuclear Fuel (SNF) intermediate storage or final disposal

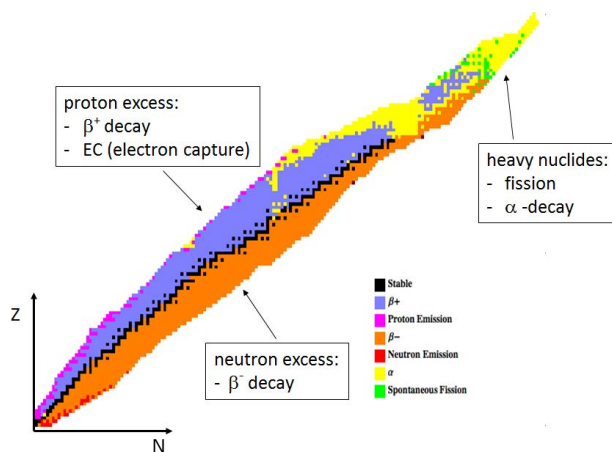
A **safe, secure, ecological** and **economic** transport, storage and final disposal requires that **SNF is characterised** for the main source terms of interest:

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity : R  
i.e. FP, actinides (Burn Up Credit)
- Fissile material (Nuclear Safeguards)  
i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- Specific nuclides (Long term safety)  
e.g.  $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$



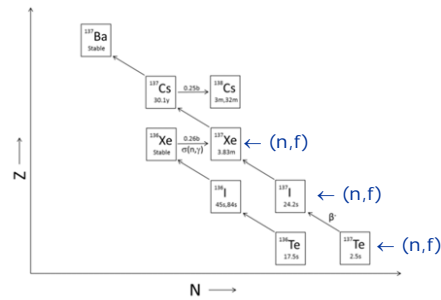
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## Nuclear spent fuel: nuclide inventory



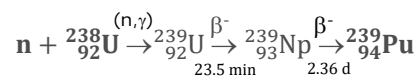
### • Fission products

e.g.  $^{99}\text{Tc}$ ,  $^{137}\text{Cs}$ ,  $^{154}\text{Eu}$ , ...



### • Actinides / minor actinides

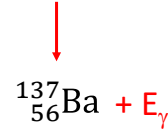
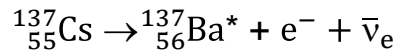
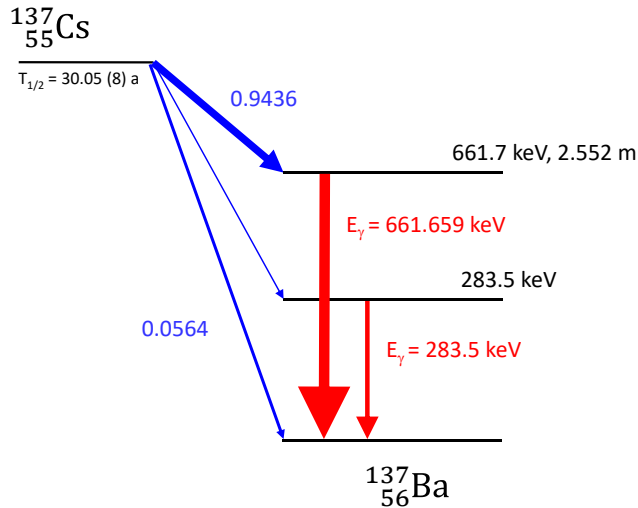
e. g.  $^{239}\text{Pu}$ ,  $^{241}\text{Am}$ ,  $^{244}\text{Cm}$ , ...



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### $\beta^-$ decay: $^{137}\text{Cs}$ (neutron rich)

- $T_{1/2} = 30.05$  (8) a
- $Q_{\beta^-} = 1175.73$  (17) keV



Gamma-ray emission probability:  $\beta$

$E_{\gamma}$	$\beta$
661.7 keV	<b>0.8436 (20)</b>
283.5 keV	5.8 (8) $\times 10^{-6}$

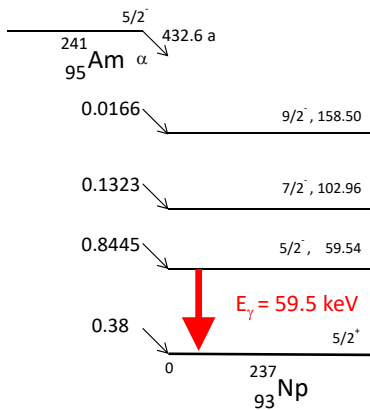
[http://www.nucleide.org/DDEP\\_WG/Nuclides/Cs-137\\_tables.pdf](http://www.nucleide.org/DDEP_WG/Nuclides/Cs-137_tables.pdf)



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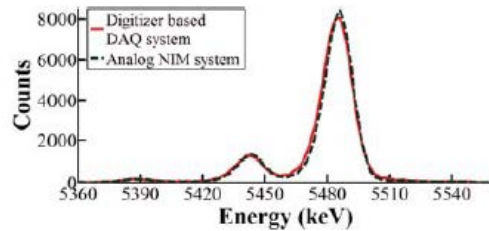
### $\alpha$ decay: $^{241}\text{Am}$

- $T_{1/2} = 432.6$  (6) a
- $Q_{\alpha} = 5637.82$  (12) keV



#### Emission of $\alpha$ -particles

P. Kandlakunta and L. Cao, Rad. Prot. Dos. 151 (2012) 586



$E_{\alpha}$ / keV	$P(E_{\alpha})$
5388.3	0.0166 (3)
5442.9	0.1323 (10)
<b>5485.6</b>	<b>0.8445 (10)</b>

[http://www.nucleide.org/DDEP\\_WG/Nuclides/Am-241\\_tables.pdf](http://www.nucleide.org/DDEP_WG/Nuclides/Am-241_tables.pdf)

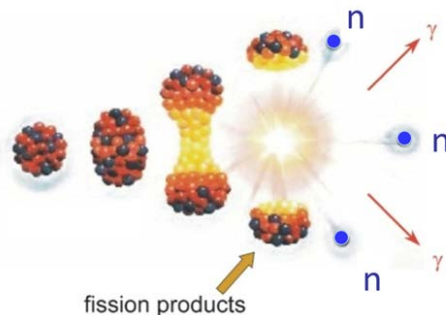


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## Spontaneous fission

Fission: nucleus splits up into fission products (FP)

e.g.  $^{238,240,242}\text{Pu(sf)}$ ,  $^{242,244,246}\text{Cm(sf)}$ ,  $^{252}\text{Cf(sf)}$

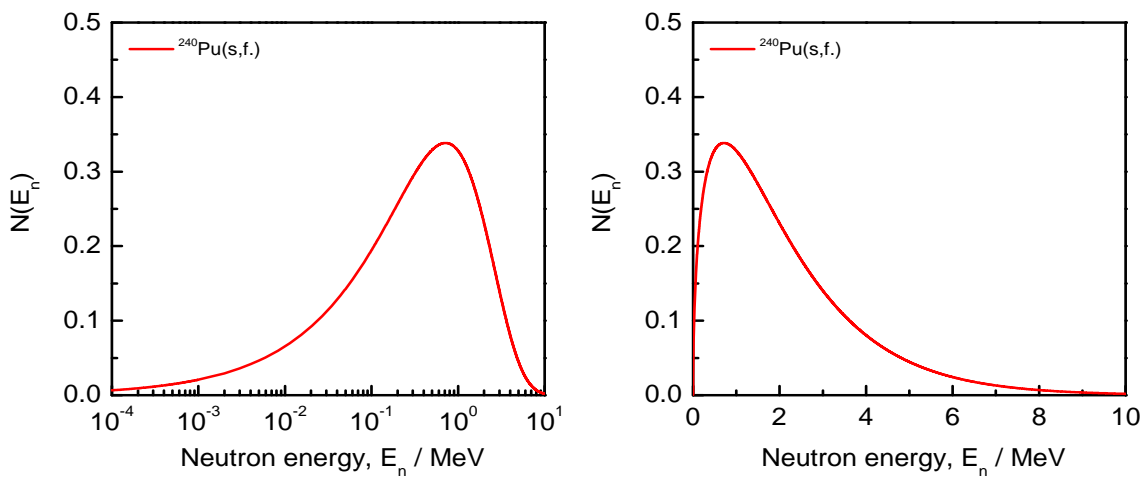


- FP : acceleration due to Coulomb repulsion
- FP : strongly excited, emission of
  - Prompt fission neutrons
  - Prompt fission  $\gamma$ -rays
- Prompt fission neutrons important for NDA (see K. Abbas)



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## Prompt fission neutron energy distribution

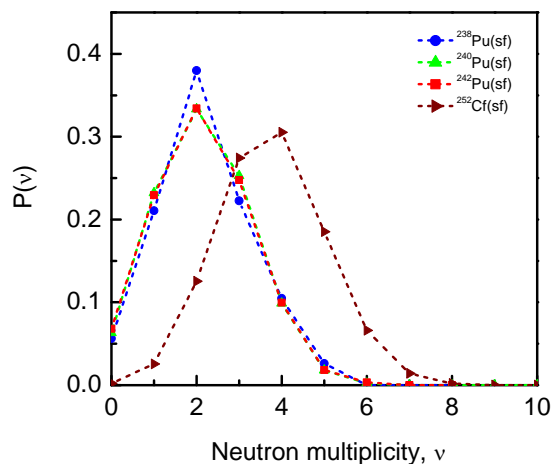


$$\langle E_n \rangle \approx 2 \text{ MeV}$$



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## Prompt fission neutron multiplicity



Emission of prompt fission neutrons:

- statistical process
- on average  $\nu > 1$

Nuclide	$\nu_{s(1)}$	$\nu_{s(2)}$	$\nu_{s(3)}$
$^{238}\text{Pu}$	2.210	1.978	0.933
$^{240}\text{Pu}$	2.154	1.895	0.868
$^{242}\text{Pu}$	2.145	1.882	0.867
$^{252}\text{Cf}$	3.756	5.978	5.287

$$\nu_{s(j)} = \sum_{v=j}^{\infty} \binom{v}{j} P_{sv}$$



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## Spontaneous fission: neutron emission

Nuclide	$T_{1/2} / a$	Main decay mode	(sf) branch x 100	$\langle \nu \rangle$	$S_{n,sf} (s^{-1}g^{-1})$
$^{238}\text{U}$	4.468 $10^9$	$\alpha$	5.45 $10^{-5}$	1.990	1.35 $10^{-2}$
<b><math>^{238}\text{Pu}</math></b>	<b>87.74</b>	<b><math>\alpha</math></b>	<b>1.85 <math>10^{-7}</math></b>	<b>2.21</b>	<b>2592</b>
$^{239}\text{Pu}$	24110	$\alpha$	3.1 $10^{-10}$	2.219	2.18 $10^{-2}$
<b><math>^{240}\text{Pu}</math></b>	<b>6561</b>	<b><math>\alpha</math></b>	<b>5.7 <math>10^{-6}</math></b>	<b>2.154</b>	<b>1023</b>
$^{241}\text{Pu}$	14.29	$\beta^-$	5.74 $10^{-13}$	2.27	4.5 $10^{-2}$
<b><math>^{242}\text{Pu}</math></b>	<b>373500</b>	<b><math>\alpha</math></b>	<b>5.49 <math>10^{-4}</math></b>	<b>2.145</b>	<b>1725</b>
$^{241}\text{Am}$	432.6	$\alpha$	4.30 $10^{-10}$	2.46	1.3
<b><math>^{242}\text{Cm}</math></b>	<b>0.446</b>	<b><math>\alpha</math></b>	<b>6.36 <math>10^{-4}</math></b>	<b>2.54</b>	<b>2.10 <math>10^7</math></b>
<b><math>^{244}\text{Cm}</math></b>	<b>18.1</b>	<b><math>\alpha</math></b>	<b>1.37 <math>10^{-4}</math></b>	<b>2.72</b>	<b>1.08 <math>10^7</math></b>
<b><math>^{252}\text{Cf}</math></b>	<b>2.645</b>	<b><math>\alpha</math></b>	<b>3.10</b>	<b>3.757</b>	<b>2.31 <math>10^{12}</math></b>



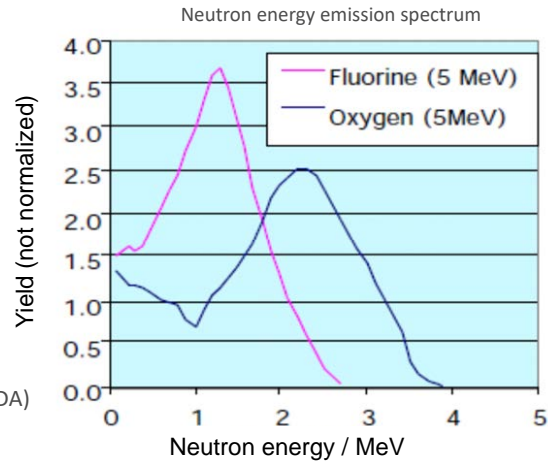
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## Neutron production by ( $\alpha,n$ )

### Additional neutron source, $S_{n,\alpha}$

SNF:  $\alpha$  - decay of actinides followed by ( $\alpha,n$ ) reaction in light elements

- ( $\alpha,n$ ) reactions
  - $^{18}\text{O}(\alpha,n)^{21}\text{Ne}$
  - $^{17}\text{O}(\alpha,n)^{20}\text{Ne}$
  - $^{19}\text{F}(\alpha,n)^{22}\text{Na}$
- Neutron energy (emission)
  - $\text{O}(\alpha,n)$  :  $\langle E_n \rangle \sim 2$  MeV
  - $\text{F}(\alpha,n)$  :  $\langle E_n \rangle \sim 1$  MeV
- $P(v) \equiv 1$   
used to separate prompt fission neutrons from ( $\alpha,n$ ) neutrons in neutron correlation counting (NDA)



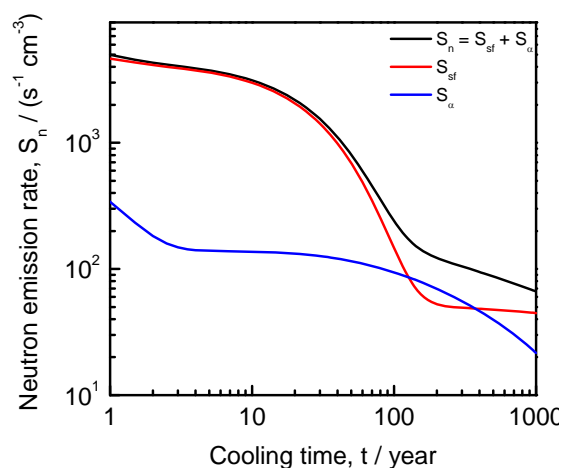
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## Neutron emission by SNF

$$S_n(t) = \sum_k S_{n,k}(t)$$

- $S_{n,k}(t)$  : contribution of radionuclide k
- $S_{n,k}(t) = (s_{sf,k} + s_{\alpha n,k}) N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $s_{sf,k}$  : specific neutron emission rate of nuclide k due to sf
  - $s_{\alpha,k}$  : specific neutron emission rate of nuclide k due to ( $\alpha,n$ ) reactions

PWR  $\text{UO}_2$  pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8\%$   
 burnup = 44 GWd/tU



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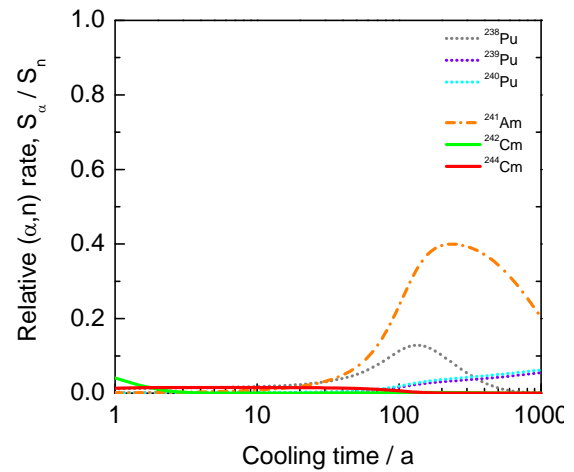
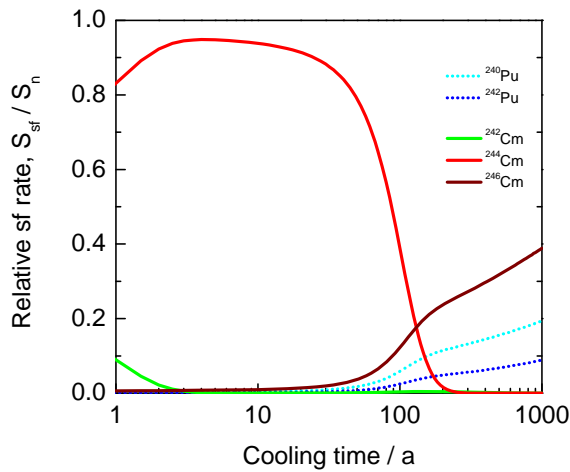
## Neutron emission by SNF

$$S_n(t) = \sum_k (s_{sf,k} + s_{\alpha n,k}) N_k(t)$$

PWR UO<sub>2</sub> pellet (5 g)

<sup>235</sup>U/U = 4.8 %

burnup = 44 GWd/tU



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## Gamma-ray emission by SNF

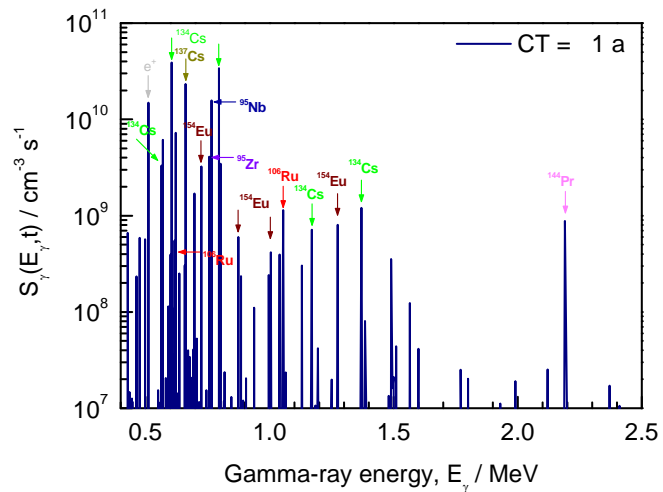
$$S_\gamma(t) = \sum_k S_{\gamma,k}(E_\gamma, t)$$

PWR UO<sub>2</sub> pellet (5 g)

<sup>235</sup>U/U = 4.8 %

burnup = 44 GWd/tU

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a



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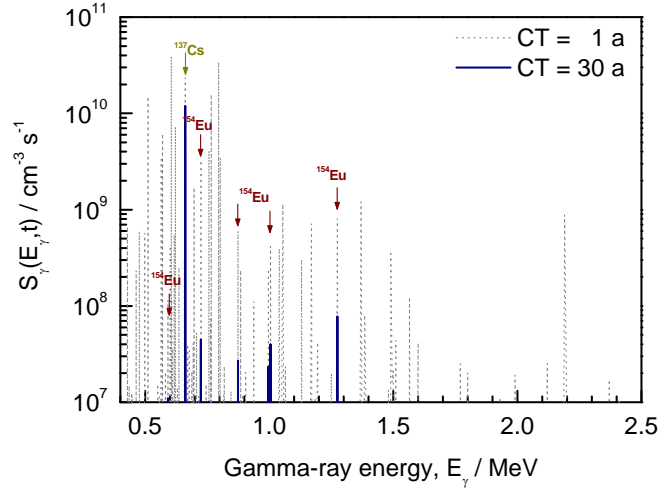


## Gamma-ray emission by SNF

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	<b>8.8 a</b>
<sup>137</sup> Cs/ <sup>137m</sup> Ba	<b>30.0 a</b>

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/tU



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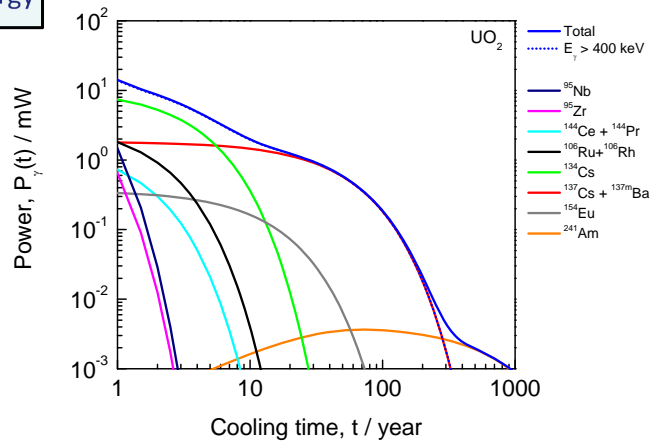
## Gamma-ray emission by SNF: recoverable thermal power

$$P_{\gamma}(t) = \sum_k \lambda_k N_k(t) \int E_{\gamma} S_{\gamma,k}(E_{\gamma}, t) dE_{\gamma}$$

Recoverable energy

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a
<sup>241</sup> Am	432.6 a

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/tU



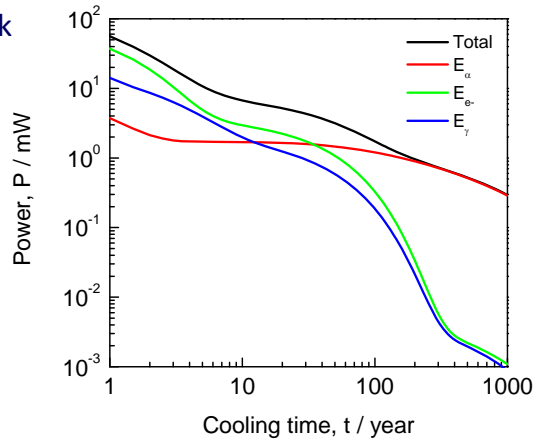
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## Thermal power produced by SNF (recoverable)

$$P(t) = \sum_k P_k(t)$$

- $P_k(t)$  : contribution of radionuclide k
- $P_k(t) = p_k N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $p_k$  : specific decay heat rate of nuclide k

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/tU

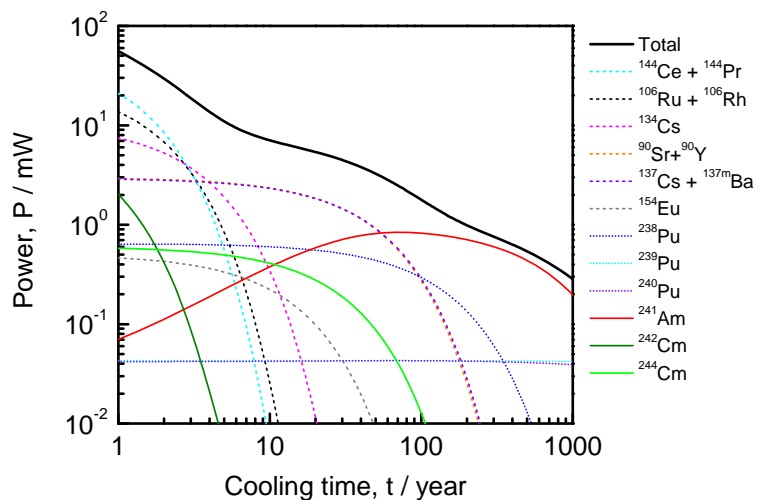


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## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - <sup>144</sup>Ce / <sup>144</sup>Pr
  - <sup>106</sup>Ru / <sup>106</sup>Rh
  - <sup>134</sup>Cs
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
  - <sup>238</sup>Pu
  - <sup>241</sup>Am
  - <sup>244</sup>Cm
- $100 \text{ a} \leq t$ 
  - <sup>241</sup>Am
  - <sup>238</sup>Pu
  - <sup>239,241</sup>Pu

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/tU



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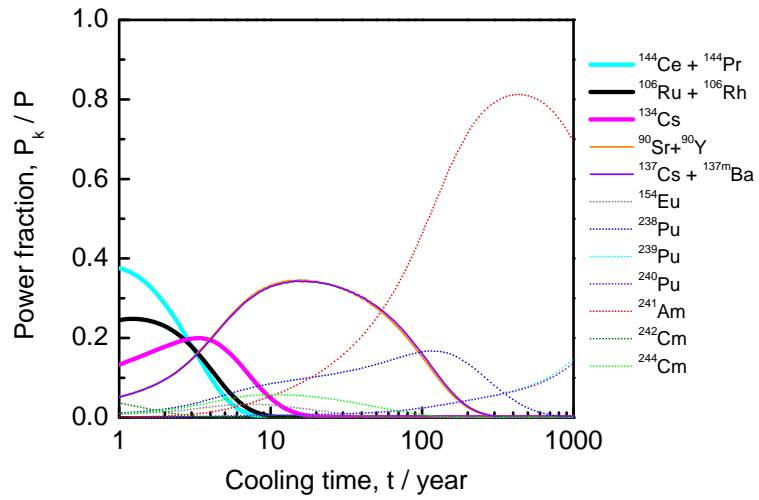
## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

PWR UO<sub>2</sub> pellet (5 g)

<sup>235</sup>U/U = 4.8 %

burnup = 44 GWd/tU



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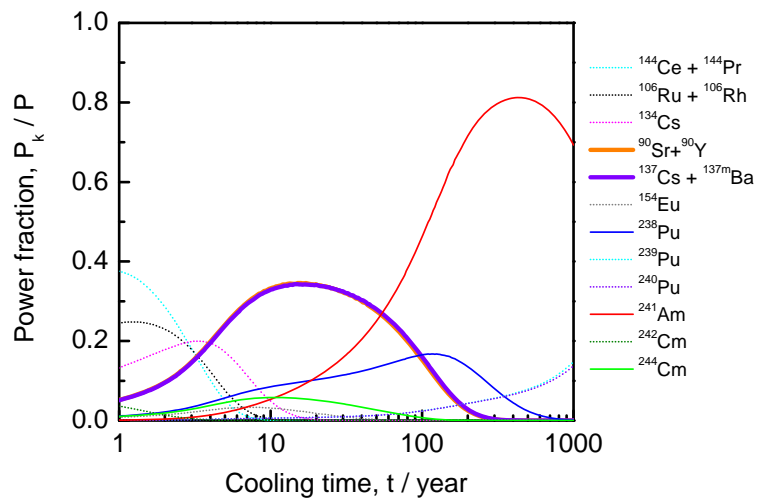
## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

PWR UO<sub>2</sub> pellet (5 g)

<sup>235</sup>U/U = 4.8 %

burnup = 44 GWd/tU

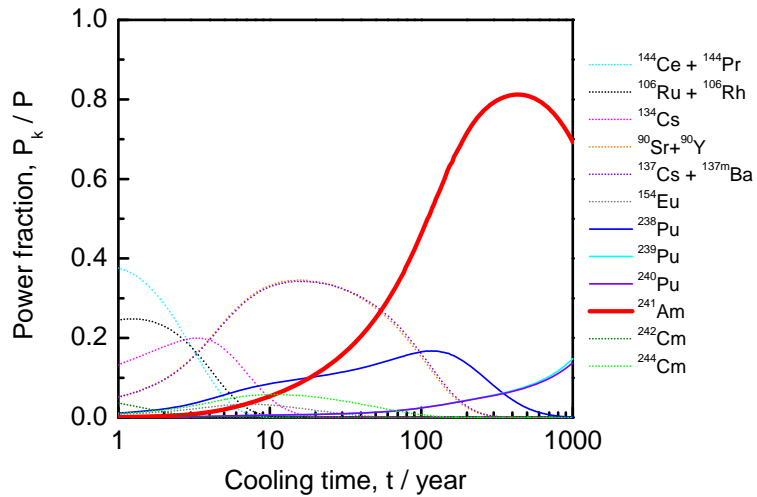


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## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/tU



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## Thermal power produced by SNF

$$P(t) = \sum_k p_k N_k(t)$$

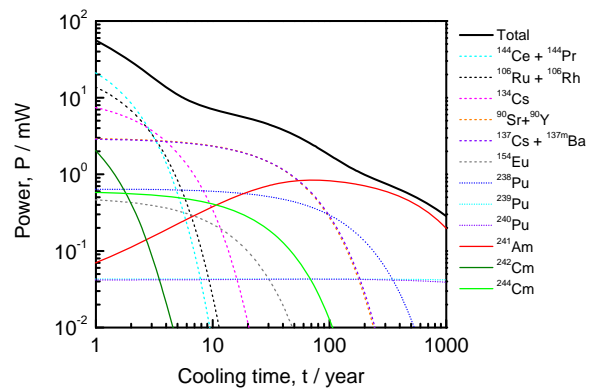
$P(t_2 > t_1)$  cannot be extrapolated from  $P(t_1)$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/tU

$N_k(t)$  : number of nuclei at time t

- $N_k(t_0)$  : number of nuclei at time  $t_0$  with  $t > t_0$
- Nuclide vector at  $t > t_0$

$$\frac{dN_k}{dt} = \sum_i \lambda_i N_i - \lambda_k N_k$$



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## Characterisation of SNF

### Main source terms of SNF are

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ , Fission Products (BUC)
- Fissile material :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- Long-term safety : e.g.  $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$

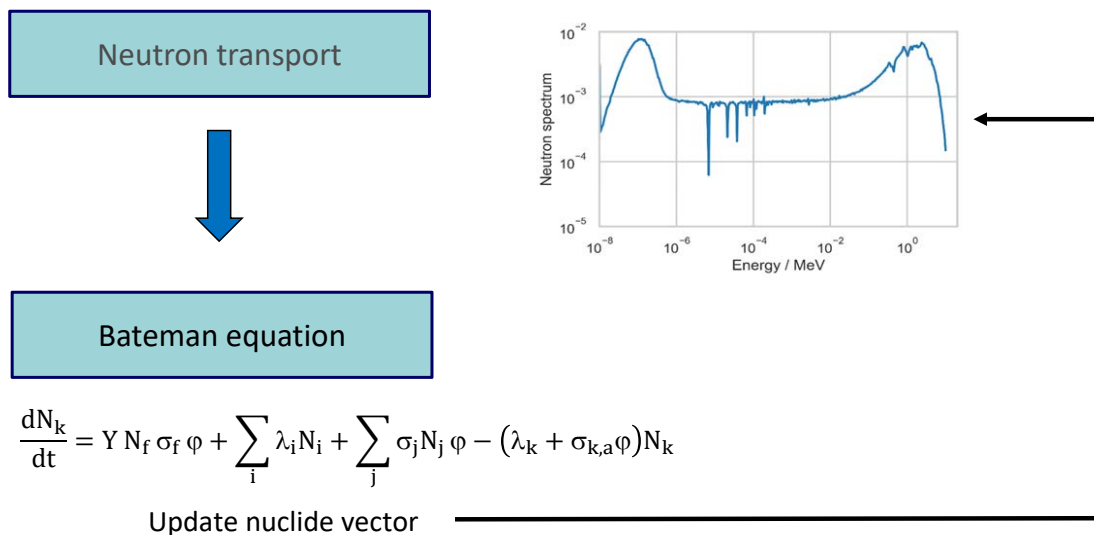
- a complex contribution of different nuclides
  - prediction at cooling time t requires nuclide vector  $N_k(t)$ ,  $k = 1, \dots, n$
  - difficult to be measured directly, in particular during industrial operation (e.g. decay heat, reactivity)
- ⇒ Determined/estimated by theoretical calculations using a burnup code  
Neutron transport + depletion/creation code



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## Burn-up calculations

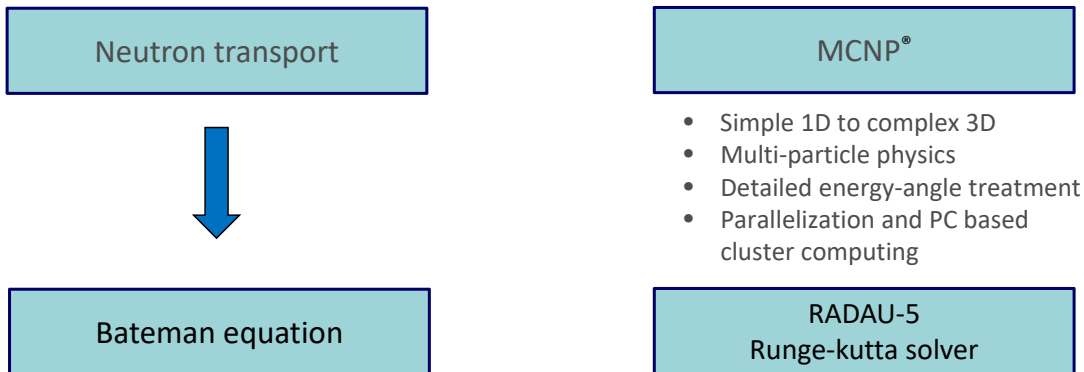
### Coupled neutron transport – nuclide depletion/creation calculation



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## ALEPH-2 (SCK•CEN)

### Coupled neutron transport – fuel depletion calculation



$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

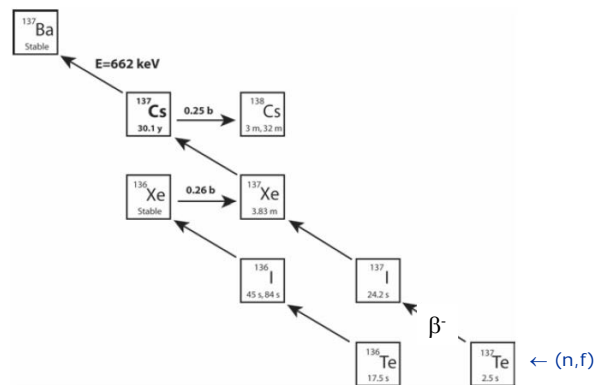
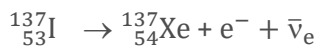
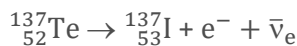
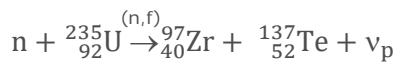


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## Production of <sup>137</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)



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## Production of <sup>137</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)

$$N_k(t) \approx \frac{Y_c \sigma_f N_f \phi}{\lambda_k + \sigma_{k,\gamma} \phi} [1 - e^{-(\lambda_k + \sigma_{k,\gamma} \phi)t}]$$

$(\lambda_k + \sigma_{k,\gamma} \phi) \ll 1$

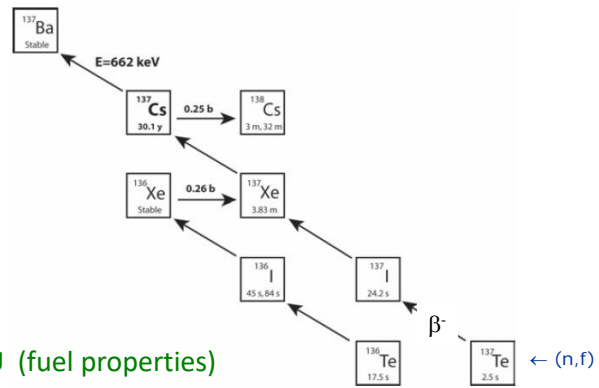
$$N_k(t) \approx Y_c \sigma_f N_f \phi t$$

$Y_c$  : cumulative fission yield

$\sigma_f$  : fission cross section

$N_f$  : number of fissile nuclei, i.e. <sup>235</sup>U (fuel properties)

$\phi t$  : total neutron fluence (operation history)



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## Estimation of SNF nuclide inventory by theoretical calculations

• Burn up code: Neutron transport + nuclear fuel depletion

• Input data:

– Nuclear Data (ND)

- Cross sections (neutron interactions)
- Fission yields
- Neutron emission probabilities
- Decay data

– Fuel History (FH)

- Fuel fabrication data (design, composition) e.g. Initial enrichment (IE)
- Reactor operation and irradiation conditions e.g. Burnup (BU)
- Cooling time (CT)

BurnUp (BU):

time integrated power per mass of initial fuel (MWd/kg)

$\propto$  total number of fission  $\times$  energy per fission event



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## Estimation of SNF nuclide vector and source terms by theory

• Nuclide vector  $N(t_0)$  at time  $t_0$  after irradiation : burn-up code

– Nuclear Data (ND)

- Cross sections
- Fission yields
- Neutron emission probabilities
- Decay data

– Fuel History (FH)

- Fuel fabrication data (design, composition)  
e.g. Initial enrichment (IE)
- Reactor operation and irradiation conditions  
e.g. Burnup (BU)
- Cooling time (CT)

• Nuclide vector at  $t > t_0$

$$\frac{dN_k}{dt} = \sum_i \lambda_i N_i - \lambda_k N_k$$

• Source terms at  $t > t_0$

e.g.  $P(t) = \sum_k p_k N_k(t)$

Depends on **well-known decay data**  
(except for reactivity relying on BUC)



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### $^{137}\text{Cs}$ : gamma-ray emission + decay heat

• Production :  $\sigma(n,f) + \text{Fission yields}$

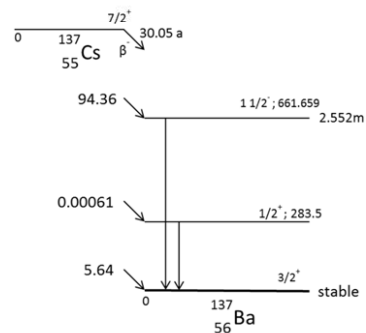
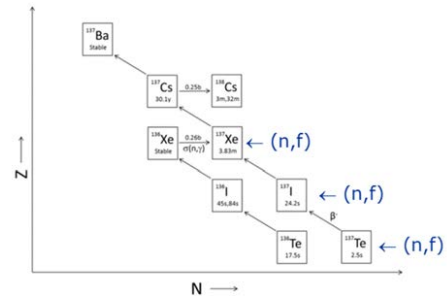
- $^{235}\text{U}(n,f)$  : 1.0 %
- Fission yields : 1.5 %

• Gamma-ray emission :

- $T_{1/2}$  : 30.18 (15) a
- $P(E_\gamma = 661.66\text{keV})$  : 0.851 (2)

• Decay heat: specific decay heat rate,  $p_k = E_{dk} \lambda_k$

- $T_{1/2}$  : 30.18 (15) a
- $Q_{\beta^-}$  : 1175.63 (17) keV
- Recoverable energy
  - Average electron + recoil energy : 247.9 (12) keV
  - $\langle E_\gamma \rangle$  : 565.4 (13) keV



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## Decay heat: <sup>90</sup>Sr and <sup>137</sup>Cs

- Production :  $\sigma(n,f) +$  fission yields
  - <sup>235</sup>U(n,f) : 1.0 %
  - Fission yields

Library	Cumulative yield x 100	
	<sup>90</sup> Sr	<sup>137</sup> Cs
<b>IAEA</b>	<b>5.730 (130)</b>	<b>6.221 (69)</b>
JEF-2.2	5.847 (188)	6.244 (54)
JEFF-3.1.1	5.729 (132)	6.221 (69)
JENDL-4.0	5.772 (59)	6.175 (34)
ENDF/B-V	5.913 (42)	6.220 (31)
ENDF/B-VI.8	5.782 (58)	6.188 (31)
ENDF/B-VII.1	5.782 (58)	6.188 (31)

- Specific decay heat rate (recoverable)

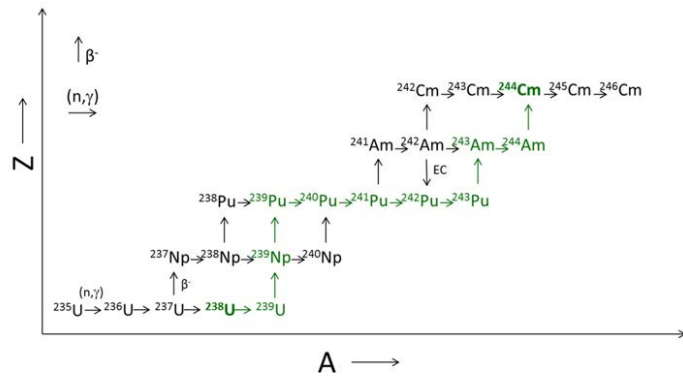
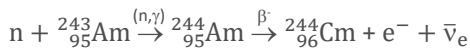
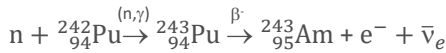
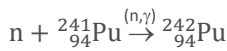
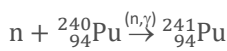
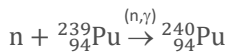
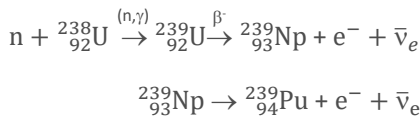
	<sup>90</sup> Sr + <sup>90</sup> Y		<sup>137</sup> Cs + <sup>137m</sup> Ba		
	<E <sub>e</sub> >/keV	E <sub>γ</sub> /keV	<E <sub>e</sub> >/keV	<E <sub>γ</sub> >/keV	<E <sub>e</sub> + E <sub>γ</sub> >/keV
Exp. (Ramthun)	1147 (9)				
Theory (Collé)	1130				
Decay data	1129.4 (14)	~ 0.0	247.9 (12)	565.4 (13)	813.3 (18)
JEFF-3.1.1	1107	0.0	245	567	812
JENDL/FPD-2011	1130	0.0	248	563	811
ENDF/B-VII.1	1129	0.0	240	566	806

	Rel. Uncertainties	
	<sup>90</sup> Sr	<sup>137</sup> Cs
– Cross section	1.0 %	1.0 %
– Fission yield	2.3 %	1.5 %
– Specific heat	0.8 %	0.2 %
	2.6 %	1.8 %



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## Production <sup>244</sup>Cm



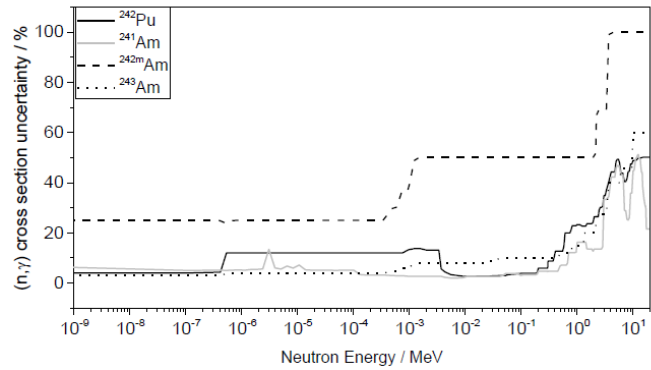
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## 242, 244Cm : production in MOX

Borella et al. MC 2017, Jeju, Korea

- MOX

- PWR: 17 x 17
- Single pin model



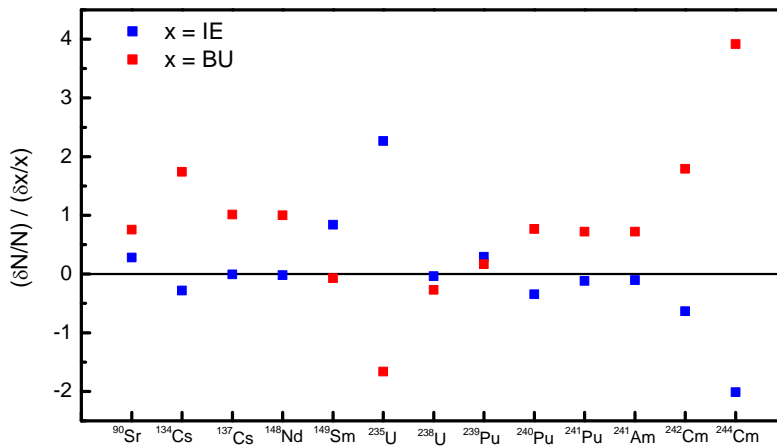
- Production :  $\sigma(n,\gamma)$

- <sup>242</sup>Cm : 2.5 %     <sup>241</sup>Am(n,γ), <sup>242m</sup>Am(n,γ)
- <sup>244</sup>Cm : 10 %     <sup>242</sup>Pu(n,γ), <sup>243</sup>Am(n,γ)



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## Fuel design and irradiation history: initial enrichment and burnup



PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/tU



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## Production of <sup>137</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

$$N_k(t) \approx a \text{ BU}$$

<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)

$$N_k(t) \approx \frac{Y_c N_f \sigma_f \varphi}{\lambda_k + \sigma_{k,\gamma} \varphi} [1 - e^{-(\lambda_k + \sigma_{k,\gamma} \varphi)t}]$$

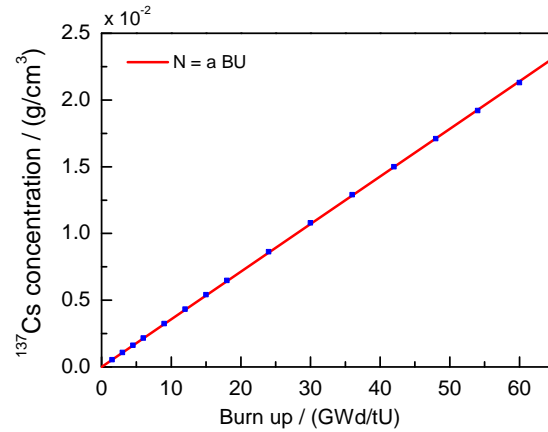
$(\lambda_k + \sigma_{k,\gamma} \varphi) \ll 1$

$$N_k(t) \approx Y_c \sigma_f N_f \varphi t$$

$(\sigma_f N_f \varphi t)$  : total number of fissions

$(\sigma_f N_f \varphi t) \times E_f$  : time integrated power

$$\Rightarrow N_k(t) \propto \text{BU}$$



$E_f$  : recoverable energy per fission



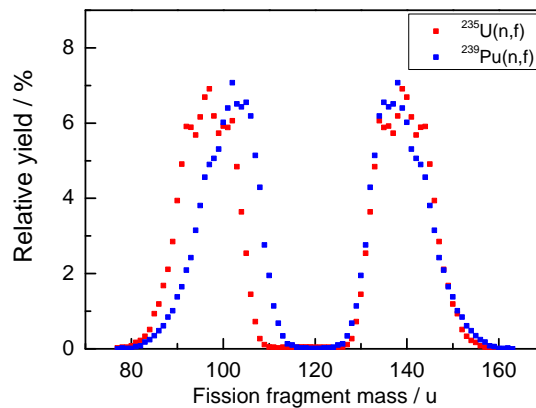
ANNETTE, 2 - 6 December 2019, Karlsruhe

## <sup>137</sup>Cs used as burn-up indicator

$$N_k(t) \approx Y_c N_f \sigma_f \varphi t$$

- $N \propto \text{BU}$   
(long half-life, small  $\sigma_\gamma$ )
- Fixed BU: not sensitive to IE
- Cumulative fission yields (x 100)

	<sup>235</sup> U(n,f)	<sup>239</sup> Pu(n,f)
<sup>106</sup> Ru	0.41 (1)	4.19 (9)
<sup>137</sup> Cs	<b>6.22 (7)</b>	<b>6.59 (8)</b>



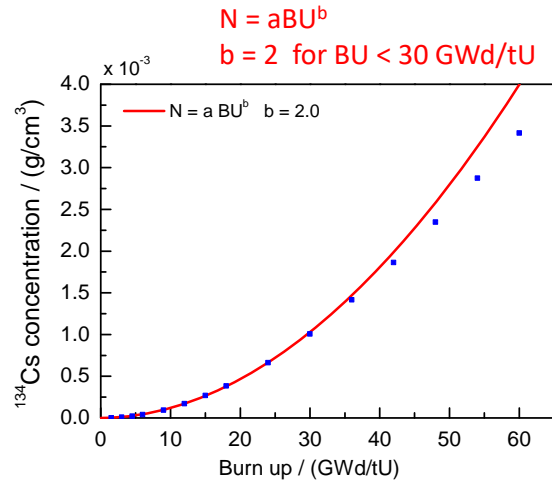
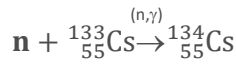
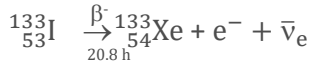
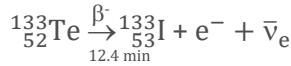
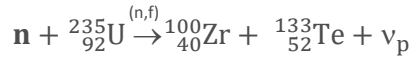
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## Production of <sup>134</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

<sup>134</sup>Cs production:

(n,f) followed by β<sup>-</sup> and (n,γ)



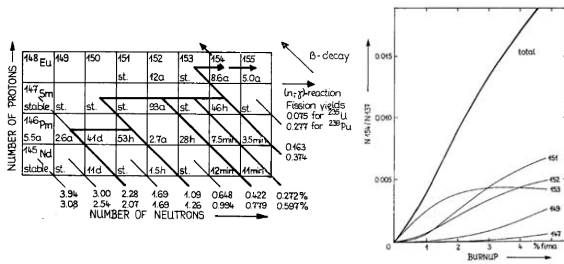
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## Production of <sup>154</sup>Eu

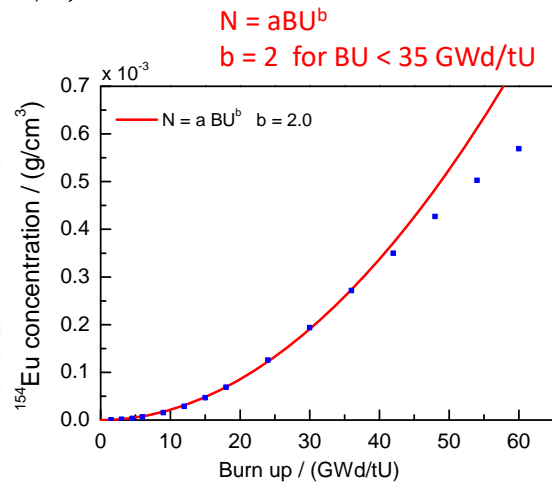
$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

<sup>154</sup>Eu production: complex

(n,f), β<sup>-</sup> and (n,γ) from 5 mass chains



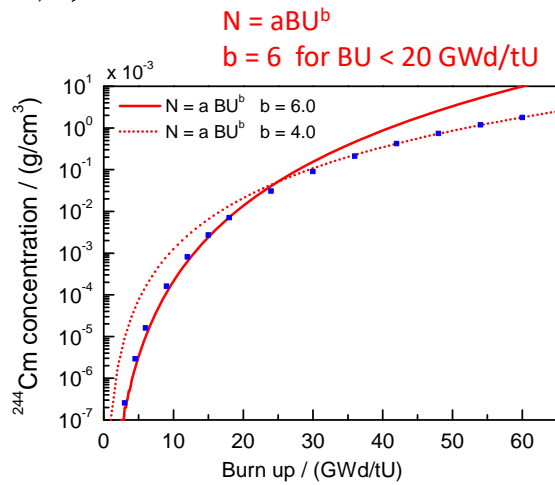
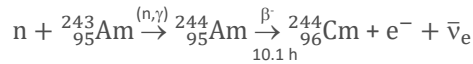
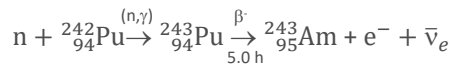
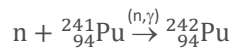
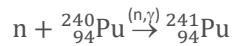
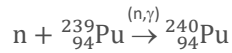
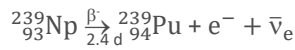
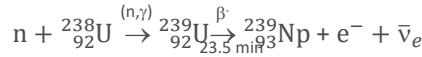
R. Berndt, Kernenergie 31 (1988) 59



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## Production of <sup>244</sup>Cm

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$



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## Experimental characterisation

- Code validation

- Radiochemical analysis of pin segments (KIT, JRC Karlsruhe) (chemistry + mass spectrometry and  $\alpha$  and  $\gamma$ -spectrometry)
- Calorimetric measurements of fuel assemblies (CLAB)

- Verification of input parameters (fuel design and irradiation history) by NDA (see S. Vaccaro)

- Gamma-ray spectroscopic measurements
- Neutron counting
- Advanced systems developed at LANL (simulations) and tested at CLAB

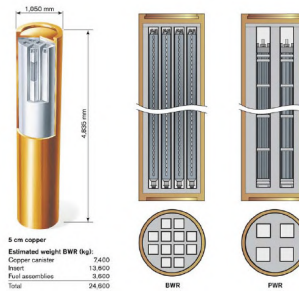
EURAD/SFC:

develop NDA methods to characterise fuel assemblies under industrial operation conditions



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## EURAD: relies on experiments at CLAB (intermediate storage SE)



### Installed systems

- Calorimeter
- Gamma-ray spectroscopic scanner

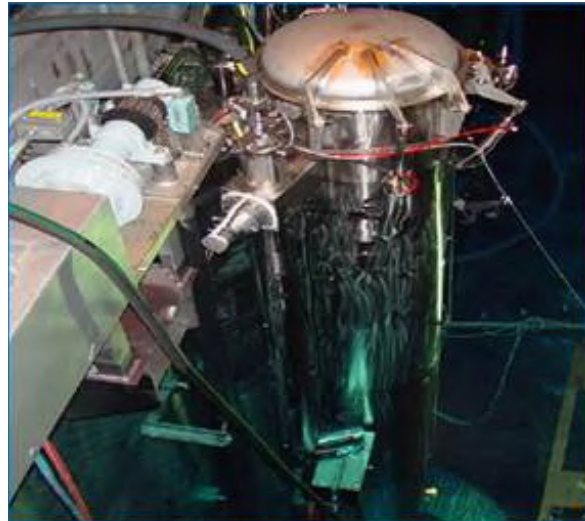
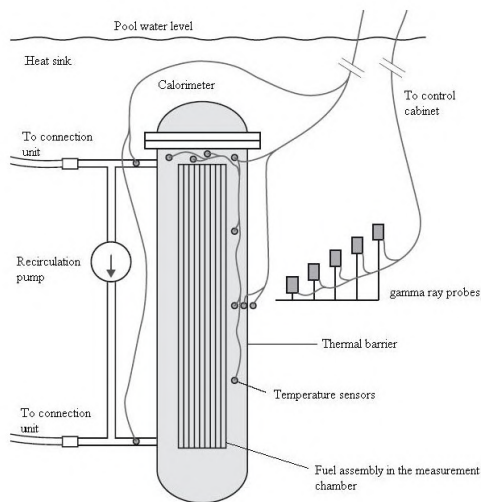
### Testing

- Differential Die-Away Self-Interrogation (DDSI)
- Differential Die-Away (DDA)



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## Calorimeter at CLAB

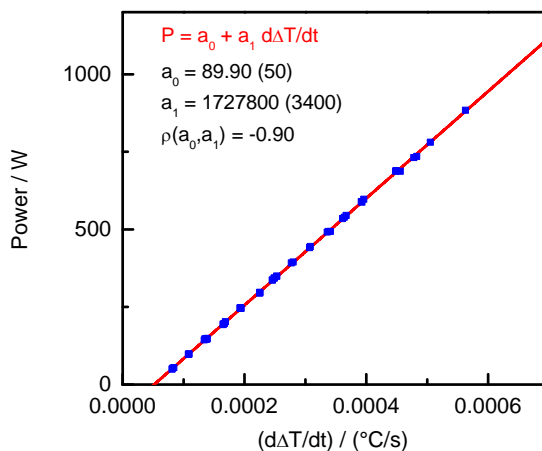
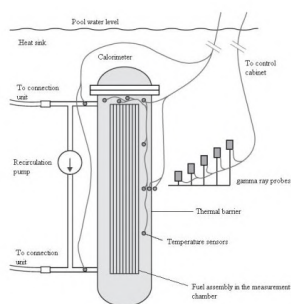


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## Calorimeter at CLAB: principle

### Calibration with an electrical heater

- Determine  $\Delta T = T_{cal} - T_{pool}$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$
- Fit to data:  $P = a_0 + a_1 d\Delta T/dt$

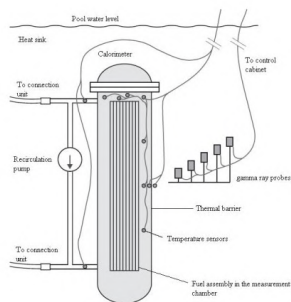


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## Calorimeter at CLAB: principle

### Calibration with an electrical heater

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- Fit to data:  $P = a_0 + a_1 d\Delta T/dt$



### Spent nuclear fuel assembly

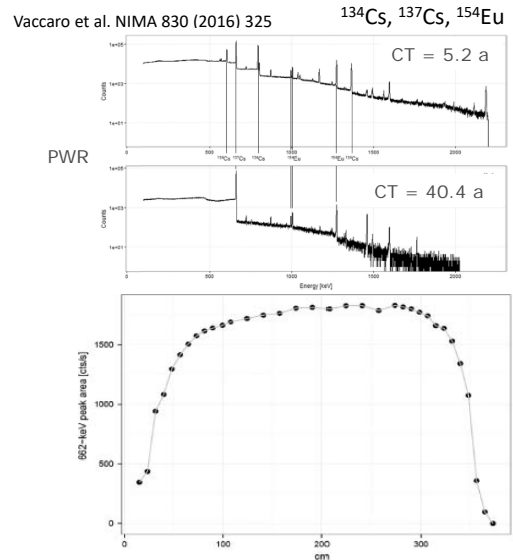
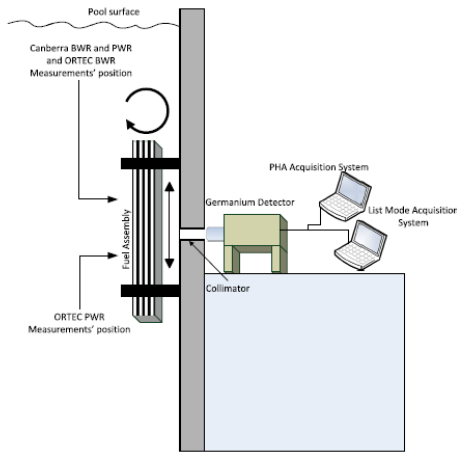
- Determine  $\Delta T = T_{cal} - T_{pool}$  vs time
- Determine  $d\Delta T/dt$  when  $\Delta T = 0$
- $Q = a_0 + a_1 K d\Delta T/dt$
- $P = Q + P_e$ 
  - $K$  : correction factor due to thermal capacity difference between electrical heater and fuel assembly
  - $P_e$  : heat loss due to  $\gamma$ -rays escaping from the calorimeter



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## Gamma-ray spectroscopic scanning system at CLAB



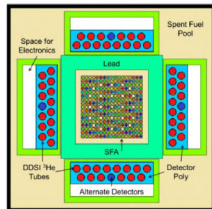
**Fig. 8.** Count rate for the 662-keV  $^{137}\text{Cs}$  net peak area as a function of axial location along BWR9. These data were measured with the ORTEC GMX detector and Canberra Lynx MCA from the 45° corner. The axial location is specified as downward along the uranium containing portion of the fuel (The indicated absolute positions are accurate to  $\pm 10$  cm, the error bars are much smaller than the data points).



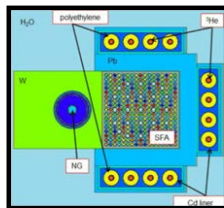
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## Fuel assemblies: DDSI and DDA (LANL development, NGS)

- Differential Die Away Self-Interrogation (DDSI, passive) *A.C. Trahan, LA-UR\_16\_20026*  
LANL, Kaplan et al., NIMA 764 (2014) 347 - 351



- Differential Die Away (DDA, active) *V. Henzl, LANL-UR-123025*



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## Thank you for the attention

- EURAD project (SNF characterisation)
  - PhD position at Uppsala University  
<https://www.uu.se/en/about-uu/join-us/details/?positionId=300024>
  - NUGENIA  
<http://nugenia.org/call-for-mobility-grants-open/>
- JRC Geel and Karlsruhe: open access
  - <https://ec.europa.eu/jrc/en/research-facility/open-access>



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**2.2 Characterization of spent nuclear fuel by theoretical calculations; P. Schillebeeckx, JRC Geel; Online available (JRC127309).**



## CHARACTERISATION OF SPENT NUCLEAR FUEL BY THEORETICAL CALCULATIONS

PWR UO<sub>2</sub> SNF

P. Schillebeeckx, L. Fiorito, P. Romojaro, G. Žerovnik • WP 8 Task 2



This project has received funding from the European Union's Horizon 2020 research and innovation programme 2014-2018 under grant agreement N°847593

Training material

1



### KEY WORDS

- Actinides
- Alpha-decay
- Bateman equation
- Beta-decay
- Burnup
- Cooling time
- Decay heat
- Depletion codes
- Final disposal
- Fission product
- Gamma-ray emission
- Initial enrichment
- Light water reactor
- Irradiation history
- Neutron transport
- Pressurised water reactor
- Spent nuclear fuel
- Spontaneous fission
- Thermal power

Training material



2



## CONTENTS

- Learning outcomes
- Introduction
- Radioactive decay
  - $\beta$  decay
  - $\alpha$  decay
  - spontaneous fission (sf)
- Source terms
  - Neutron emission
  - Gamma-ray emission
  - Decay heat rate (thermal power)
- Theoretical estimation of source terms
  - Principles
  - Nuclear data
  - Fuel properties and irradiation history
  - Examples:  $^{137}\text{Cs}$  and  $^{244}\text{Cm}$
- Summary and conclusions
- Bibliography and References

Training material



## LEARNING OUTCOMES

After the completion of this training lesson, the participants should be able to

- identify the observables or source terms that are important for the transport, handling, intermediate storage and final disposal of spent nuclear fuel
- identify key nuclides determining the observables
- breakdown the complexity to theoretically estimate the observables
- identify the different components involved in the theoretical calculations of the observables
- understand the importance of nuclear data and operational history for an accurate theoretical estimation of the observables
- realise the need of more accurate data to improve the theoretical calculations

Training material

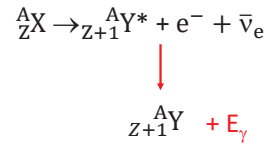
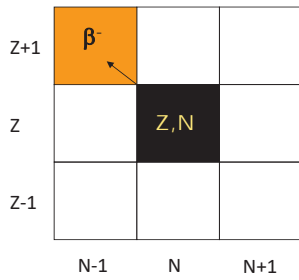






### $\beta^-$ - DECAY BY NEUTRON RICH NUCLIDES

Isobaric transition in which a neutron is transformed into a proton and an electron + anti-neutrino are emitted

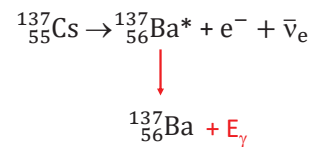
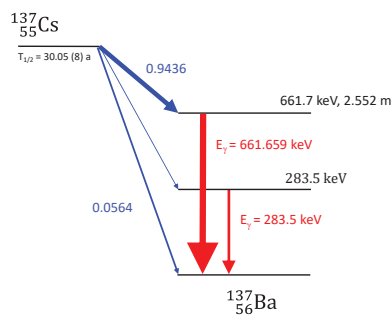


Training material



### $\beta^-$ - DECAY BY NEUTRON RICH NUCLIDES: e.g. $^{137}\text{Cs}$

- $T_{1/2} = 30.05 (8) \text{ a}$
- $Q_{\beta^-} = 1175.73 (17) \text{ keV}$



Gamma-ray emission probability:  $P_\gamma$

$E_\gamma$	$P_\gamma$
661.7 keV	0.8499 (20)
283.5 keV	$5.8 (8) \times 10^{-6}$

[http://www.nucleide.org/DDEP\\_WG/Nuclides/Cs-137\\_tables.pdf](http://www.nucleide.org/DDEP_WG/Nuclides/Cs-137_tables.pdf)

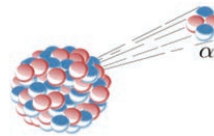
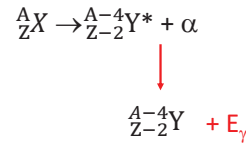
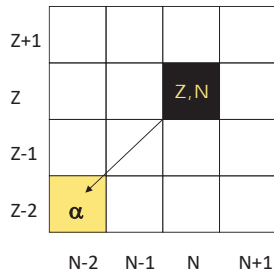
Training material





**α - DECAY**

Radioactive decay in which a nucleus emits an **α-particle** (<sup>4</sup>He nucleus) and transforms into a nucleus with 4 less nucleons (2n, 2p)



*in heavy nuclei*

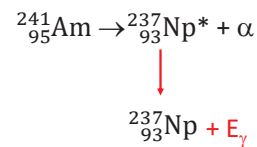
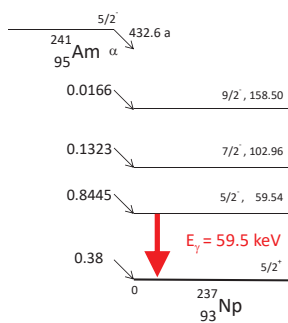


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**α - DECAY BY ACTINIDES: e.g. <sup>241</sup>Am**

- T<sub>1/2</sub> = 432.6 (6) a
- Q<sub>α</sub> = 5637.82 (12) keV



α -particle emission probability:

E <sub>α</sub>	P(E <sub>α</sub> )
5388.3 keV	0.0166 (3)
5442.9 keV	0.1323 (10)
<b>5485.6 keV</b>	<b>0.8445 (10)</b>

[http://www.nucleide.org/DDEP\\_WG/Nuclides/Am-241\\_tables.pdf](http://www.nucleide.org/DDEP_WG/Nuclides/Am-241_tables.pdf)



Training material



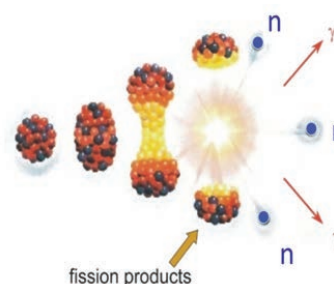


### SPONTANEOUS FISSION

Fission: nucleus splits up into fission products (FP)

e.g.  $^{238,240,242}\text{Pu(sf)}$ ,  $^{242,244,246}\text{Cm(sf)}$ ,  $^{252}\text{Cf(sf)}$

- FP : acceleration due to Coulomb repulsion
- FP : strongly excited, emission of
  - Prompt fission neutrons (PFN)
  - Prompt fission  $\gamma$ -rays (PFG)
- Prompt fission neutrons important for Non-Destructive Analysis (NDA)



Training material



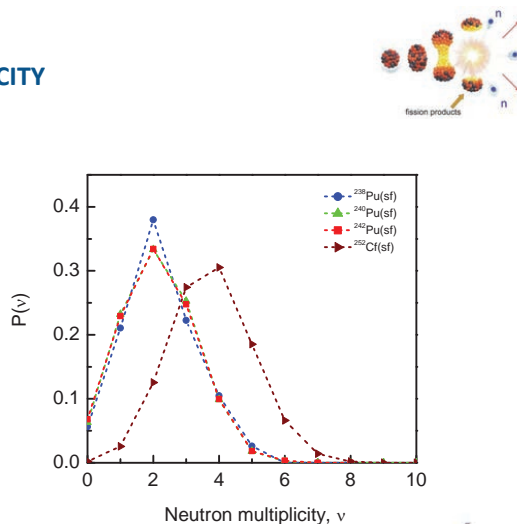
### PROMPT FISSION NEUTRONS: MULTIPLICITY

Emission of prompt fission neutrons:

- statistical process
- on average  $\nu > 1$

Nuclide	$\nu_{s(1)}$	$\nu_{s(2)}$	$\nu_{s(3)}$
$^{238}\text{Pu}$	2.210	1.978	0.933
$^{240}\text{Pu}$	2.154	1.895	0.868
$^{242}\text{Pu}$	2.145	1.882	0.867
$^{252}\text{Cf}$	3.756	5.978	5.287

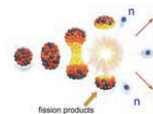
$$\nu_{s(j)} = \sum_{v=j}^{\infty} \binom{v}{j} P_{sv}$$



Training material



PROMPT FISSION NEUTRONS: DATA



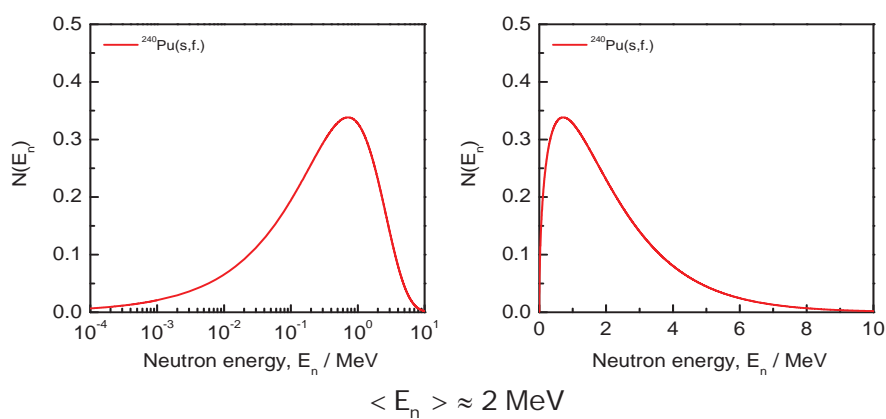
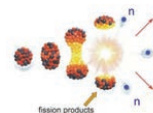
Nuclide	$T_{1/2}$	(sf) branching	$\langle v \rangle$	$S_{sf} / (s^{-1} g^{-1})$
$^{238}\text{Pu}$	$8.774 (3) \times 10^4 \text{ a}$	$1.85 (5) \times 10^{-9}$	1.980 (30)	$2.59 (11) \times 10^3$
$^{240}\text{Pu}$	$6.561 (7) \times 10^3 \text{ a}$	$5.70 (20) \times 10^{-8}$	2.154 (5)	$1.031 (36) \times 10^3$
$^{242}\text{Pu}$	$3.73 (3) \times 10^5 \text{ a}$	$5.49 (9) \times 10^{-6}$	2.149 (8)	$1.728 (32) \times 10^3$
$^{242}\text{Cm}$	162.86 (8) d	$6.36 (14) \times 10^{-8}$	2.540 (20)	$1.980 (46) \times 10^7$
$^{244}\text{Cm}$	$1.811 (3) \times 10^4 \text{ a}$	$1.36 (1) \times 10^{-6}$	2.710 (10)	$1.107 (10) \times 10^7$
$^{246}\text{Cm}$	$4.72 (3) \times 10^3 \text{ a}$	$2.61 (4) \times 10^{-6}$	2.930 (30)	$8.70 (13) \times 10^6$

Decay data from Nichols et al., INDC-2453, INDC(NDS)-0534, August 2008  
 $\langle v \rangle$  from Santi and Miller, Nucl. Sci. Eng. 160 (2017) 190

Training material



PROMPT FISSION NEUTRONS: ENERGY DISTRIBUTION



Training material

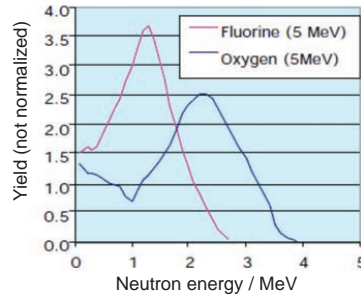




### NEUTRON PRODUCTION BY (α,n) REACTIONS

- (α,n) reaction with light nuclides
  - $^{18}\text{O}(\alpha,n)^{21}\text{Ne}$
  - $^{17}\text{O}(\alpha,n)^{20}\text{Ne}$
  - $^{19}\text{F}(\alpha,n)^{22}\text{Na}$
- Neutron energy (emission)
  - $\text{O}(\alpha,n)$  :  $\langle E_n \rangle \sim 2 \text{ MeV}$
  - $\text{F}(\alpha,n)$  :  $\langle E_n \rangle \sim 1 \text{ MeV}$
- $P(\nu) = 1$ 

used to separate prompt fission neutrons from (α,n) neutrons in neutron correlation counting (NDA)



⇒ in SNF: α - decay of actinides followed by (α,n) reaction in light elements

Training material

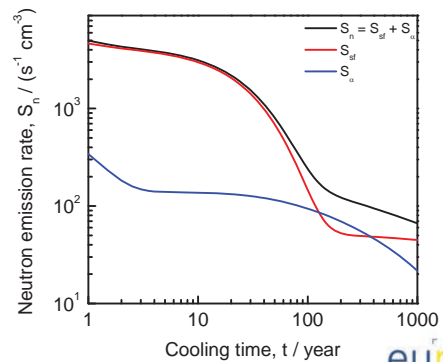


### NEUTRON EMISSION BY SPENT NUCLEAR FUEL

$$S_n(t) = \sum_k S_{n,k}(t)$$

- $S_{n,k}(t)$  : contribution of radionuclide k
- $S_{n,k}(t) = (s_{sf,k} + s_{\alpha n,k}) N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $s_{sf,k}$  : specific neutron emission rate of nuclide k due to **spontaneous fission**
  - $s_{\alpha,k}$  : specific neutron emission rate of nuclide k due to **(α,n) reactions**

PWR  $\text{UO}_2$  pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8 \%$   
 burnup = 45 GWd/t

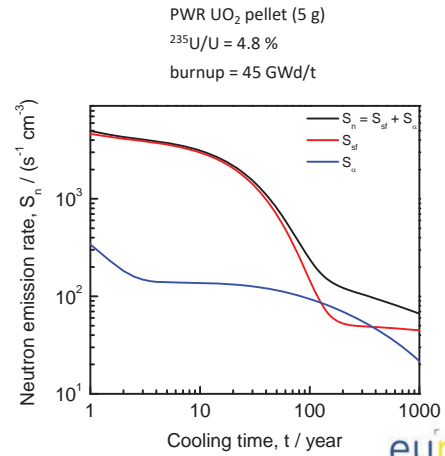
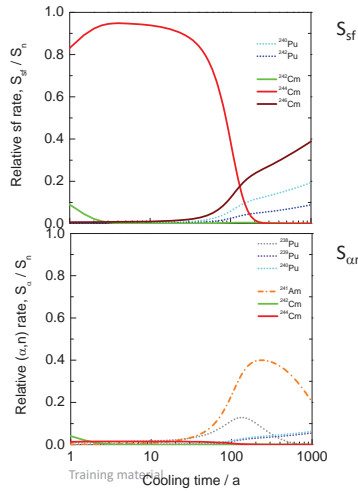


Training material

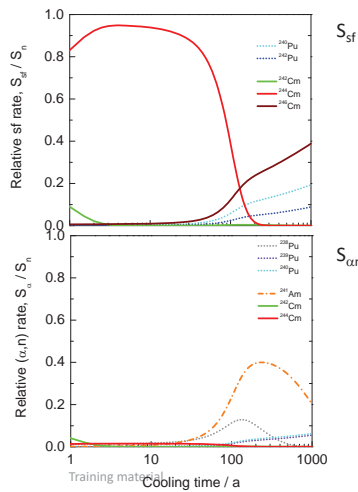




NEUTRON EMISSION BY SPENT NUCLEAR FUEL



NEUTRON EMISSION BY SPENT NUCLEAR FUEL



PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t

Nuclide	T <sub>1/2</sub>	(sf) branching	<v>	S <sub>sf</sub> / (s <sup>-1</sup> g <sup>-1</sup> )
<sup>238</sup> Pu	8.774 (3) × 10 <sup>4</sup> a	1.85 (5) × 10 <sup>-9</sup>	1.980 (30)	2.59 (11) × 10 <sup>3</sup>
<sup>240</sup> Pu	6.561 (7) × 10 <sup>3</sup> a	5.70 (20) × 10 <sup>-8</sup>	2.154 (5)	1.031 (36) × 10 <sup>3</sup>
<sup>242</sup> Pu	3.73 (3) × 10 <sup>5</sup> a	5.49 (9) × 10 <sup>-6</sup>	2.149 (8)	1.728 (32) × 10 <sup>3</sup>
<sup>242</sup> Cm	162.86 (8) d	6.36 (14) × 10 <sup>-8</sup>	2.540 (20)	1.980 (46) × 10 <sup>7</sup>
<sup>244</sup> Cm	<b>1.811 (3) × 10<sup>4</sup> a</b>	<b>1.36 (1) × 10<sup>-6</sup></b>	<b>2.710 (10)</b>	<b>1.107 (10) × 10<sup>7</sup></b>
<sup>246</sup> Cm	4.72 (3) × 10 <sup>3</sup> a	2.61 (4) × 10 <sup>-6</sup>	2.930 (30)	8.70 (13) × 10 <sup>6</sup>

Decay data from Nichols et al., INDC-2453, INDC(NDS) – 0534, August 2008  
 <v> from Santi and Miller, Nucl.; Sci. Eng. 160 (2017) 190



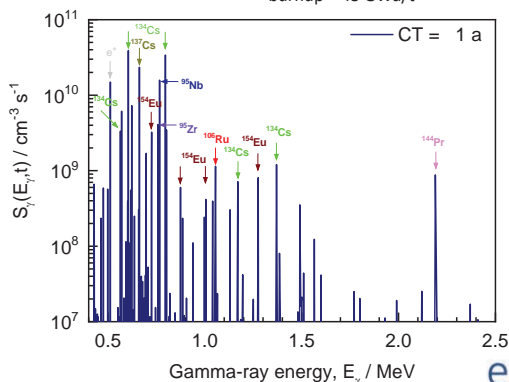


**GAMMA-RAY EMISSION BY SPENT NUCLEAR FUEL**

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t



Training material

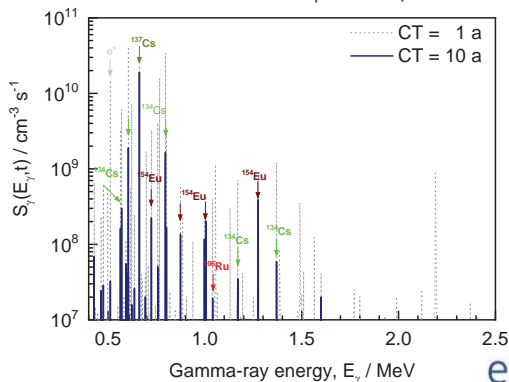


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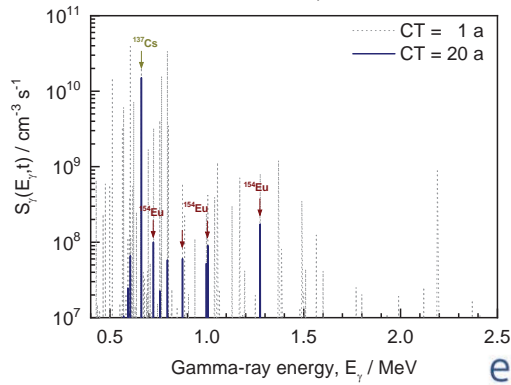


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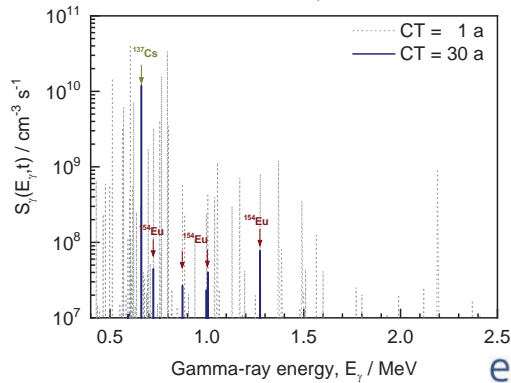


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Training material



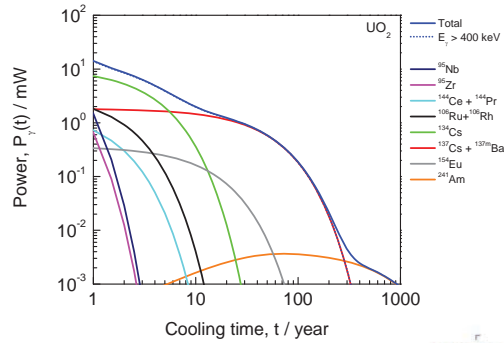


**GAMMA-RAY EMISSION BY SNF: CONTRIBUTION TO THERMAL POWER**

$$P_{\gamma}(t) = \sum_k \lambda_k N_k(t) \int E_{\gamma} S_{\gamma,k}(E_{\gamma}, t) dE_{\gamma}$$

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a
<sup>241</sup> Am	432.6 a

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t



Training material

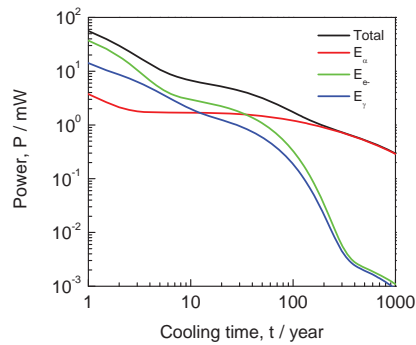


**THERMAL POWER PRODUCED BY SNF**

$$P(t) = \sum_k P_k(t)$$

- $P_k(t)$  : contribution of radionuclide k
- $P_k(t) = p_k N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $p_k$  : specific decay heat rate of nuclide k

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t



Training material

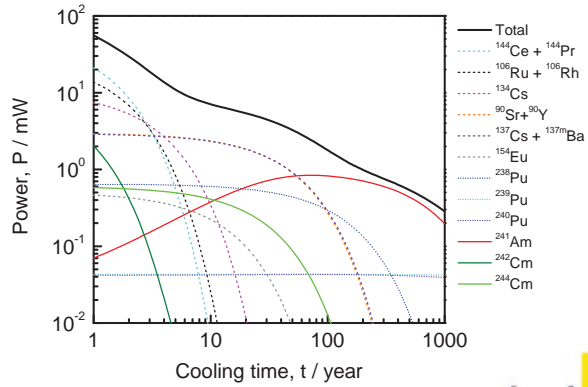




**THERMAL POWER PRODUCED BY SNF**

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

PWR  $\text{UO}_2$  pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8 \%$   
 burnup = 45 GWd/t



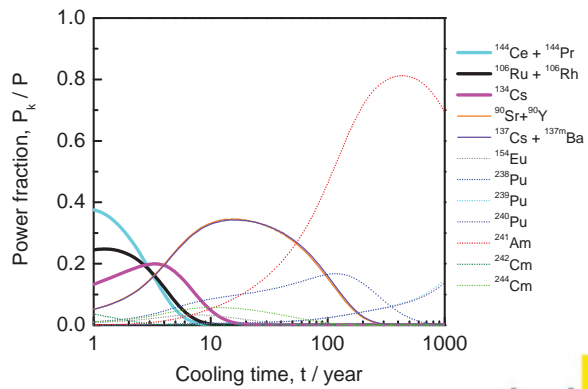
Training material



**THERMAL POWER PRODUCED BY SNF**

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
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Training material



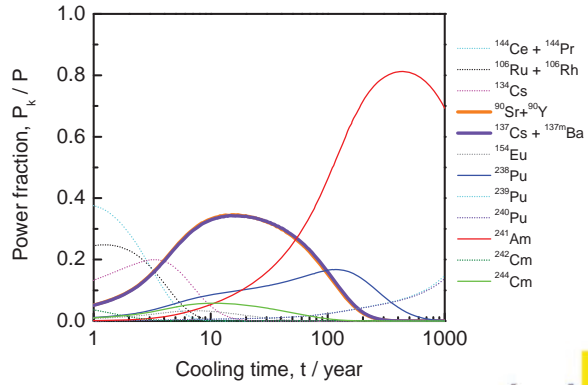




**THERMAL POWER PRODUCED BY SNF**

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 burnup = 45 GWd/t



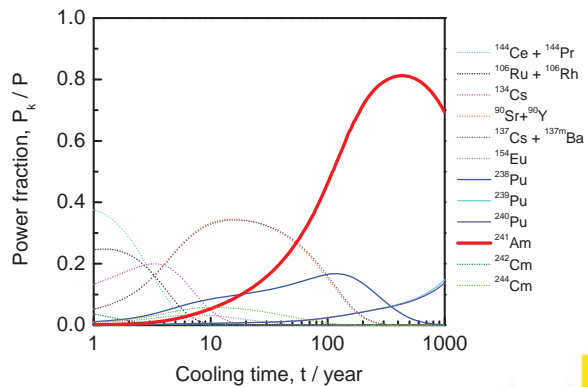
Training material



**THERMAL POWER PRODUCED BY SNF**

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
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PWR  $\text{UO}_2$  pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8 \%$   
 burnup = 45 GWd/t



Training material





### THERMAL POWER PRODUCED BY SNF

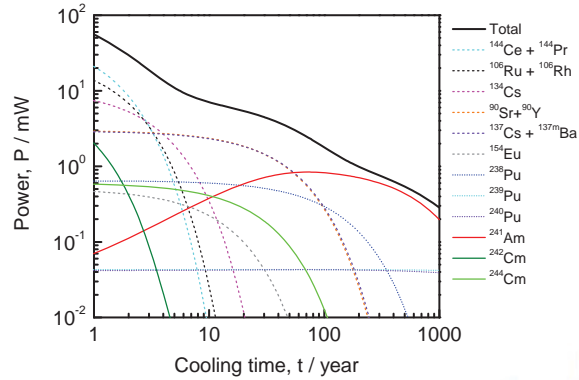
$$P(t) = \sum_k p_k N_k(t)$$

$N_k(t)$  : number of nuclei at time t

- $N_k(t_0)$  : number of nuclei at time  $t_0$  with  $t > t_0$
- Nuclide vector at  $t > t_0$

$$\frac{dN_k}{dt} = \sum_{i \rightarrow k} \lambda_i N_i - \lambda_k N_k$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t



Training material



### SNF SOURCE TERMS

Main **observables** or **source terms** of interest:

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity : <sup>235</sup>U, <sup>239</sup>Pu, Fission Products (BUC)
- Fissile material : <sup>235</sup>U, <sup>239</sup>Pu
- Long-term safety : e.g. <sup>14</sup>C, <sup>36</sup>Cl, <sup>79</sup>Se, <sup>94</sup>Nb, <sup>99</sup>Tc, <sup>129</sup>I, <sup>226</sup>Ra, <sup>237</sup>Np

**difficult to be measured directly, in particular during industrial operation**

- Decay heat by **calorimetry** at CLAB: accurate but **long measurement times**
- Criticality safety analysis: calculations required to account for **burn-up credit** (MA, FP)
- **Prediction at long cooling times** only possible by theoretical calculations

⇒ Determined/estimated by **theoretical calculations** using a burnup code  
 Neutron transport + depletion/creation code

Training material





### SNF SOURCE TERMS: NUCLIDE INVENTORY

Nuclide	Source term	CT
<sup>90</sup> Sr	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a
<sup>106</sup> Ru	H	1 a ≤ t ≤ 10 a
<sup>134</sup> Cs	H	1 a ≤ t ≤ 10 a
<sup>137</sup> Cs	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a
<sup>144</sup> Ce	H	1 a ≤ t ≤ 10 a
<sup>148</sup> Nd	Burn-up	stable
<sup>149</sup> Sm	Power	stable
<sup>154</sup> Eu	H, S <sub>γ</sub>	1 a ≤ t ≤ 10 a

Nuclide	Source term	CT
<sup>235</sup> U	R, S <sub>γ</sub>	10 <sup>5</sup> a ≤ t
<sup>238</sup> U	R, S <sub>γ</sub>	10 <sup>5</sup> a ≤ t
<sup>238</sup> Pu	H, S <sub>γ</sub>	10 a ≤ t
<sup>239</sup> Pu	R, S <sub>γ</sub>	100 a ≤ t ≤ 10 <sup>4</sup> a
<sup>240</sup> Pu	R, S <sub>γ</sub>	100 a ≤ t ≤ 10 <sup>4</sup> a
<sup>241</sup> Pu	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a
<sup>241</sup> Am	H	10 a ≤ t
<sup>242</sup> Cm	H, S <sub>n</sub>	1 a ≤ t ≤ 10 a
<sup>244</sup> Cm	H, S <sub>n</sub>	10 a ≤ t ≤ 100 a

H : thermal power or decay heat  
 S<sub>n</sub> : neutron emission  
 S<sub>γ</sub> : γ-ray emission  
 R : reactivity (criticality safety)

Criticality safety (Burn Up Credit, BUC):

<sup>95</sup>Mo, <sup>99</sup>Tc, <sup>101</sup>Ru, <sup>103</sup>Rh, <sup>109</sup>Ag, <sup>133</sup>Cs, <sup>143</sup>Nd, <sup>147,149,150,151,152</sup>Sm, <sup>155</sup>Gd

Long term safety:

<sup>14</sup>C, <sup>36</sup>Cl, <sup>79</sup>Se, <sup>94</sup>Nb, <sup>99</sup>Tc, <sup>129</sup>I, <sup>226</sup>Ra, <sup>237</sup>Np

⇒ Requires complex nuclide inventory which can only be obtained by theoretical calculations



Training material



### BURNUP CALCULATIONS: COUPLED NEUTRON TRANSPORT – NUCLIDE DEPLETION/CREATION

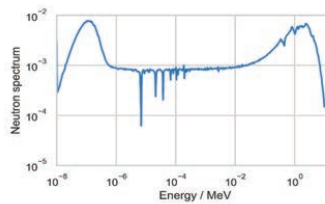
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

Update nuclide vector



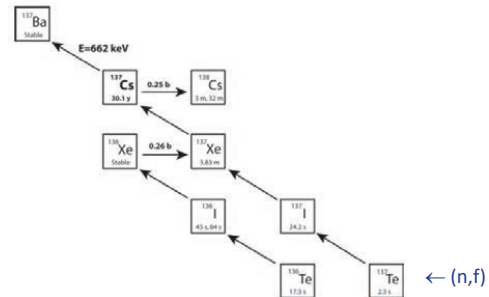
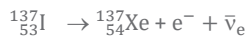
Training material



**PRODUCTION OF <sup>137</sup>Cs**

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)



Training material



**PRODUCTION OF <sup>137</sup>Cs**

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

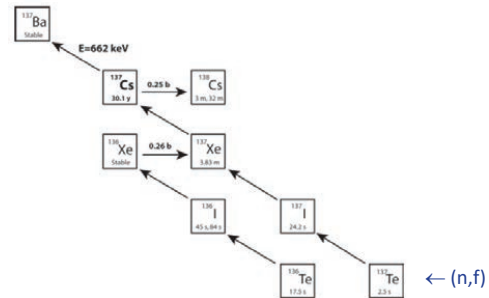
<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)

$$N_k(t') \approx \frac{Y_c \sigma_f N_f \varphi}{\lambda_k + \sigma_{k,\gamma} \varphi} [1 - e^{-(\lambda_k + \sigma_{k,\gamma} \varphi) t'}]$$

$(\lambda_k + \sigma_{k,\gamma} \varphi) t' \ll 1$

$$N_k(t') \sim Y_c \sigma_f N_f \varphi t'$$

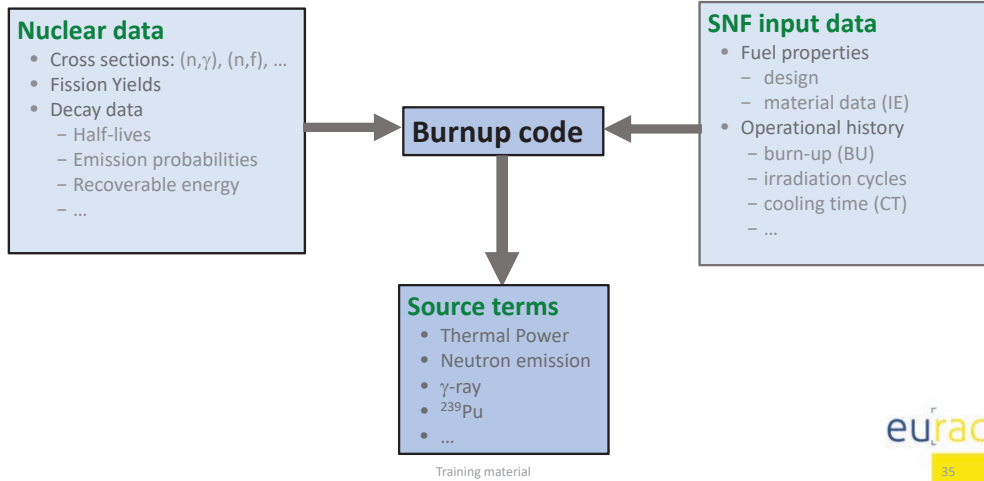
- $Y_c$  : cumulative fission yield
- $\sigma_f$  : fission cross section
- $N_f$  : number of fissile nuclei, i.e. <sup>235</sup>U (fuel properties)
- $\varphi t'$  : total (time integrated) neutron fluence (operation history)
- $\sigma_f N_f \varphi t'$  : total number of fissions



Training material



**BURNUP CODES: THEORETICAL CALCULATION OF SNF NUCLIDE INVENTORY AND OBSERVABLES**



Training material



**BURNUP CODES: THEORETICAL CALCULATION OF SNF NUCLIDE INVENTORY AND OBSERVABLES**

• **Burnup code: Neutron transport + nuclear fuel depletion**

- Deterministic ↔ stochastic
- Approach to solve the Bateman equation
- Geometry

• **Input data:**

- **Nuclear Data (ND)**

- Cross sections
- Fission yields
- Decay data
- (α,n) production yields
- ...

- **Fuel History (FH)**

- Fuel fabrication data (design, composition)  
e.g. Initial enrichment (IE)
- Reactor operation and irradiation conditions  
e.g. Burnup (BU)
- Cooling time (CT)

Burnup (BU):  
time integrated power per mass of initial fuel (MWd/kg)

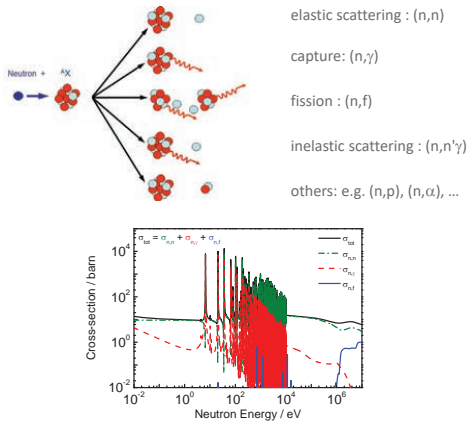
Training material



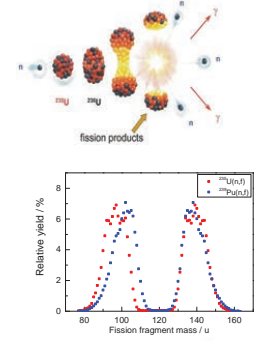


**BURNUP CODES: NUCLEAR DATA**

**Neutron induced interaction cross sections**



**Fission process**



**BURNUP CODES**

**Nuclide vector  $N(t_0)$  at time  $t_0$  after irradiation : burn-up code**

– **Nuclear Data (ND)**

- Cross sections
- Fission yields
- Neutron emission probabilities
- Decay data

– **Fuel History (FH)**

- Fuel fabrication data (design, composition)  
e.g. Initial enrichment (IE)
- Reactor operation and irradiation conditions  
e.g. Burnup (BU)
- Cooling time (CT)

**Nuclide vector at  $t > t_0$**

$$\frac{dN_k}{dt} = \sum_{i \rightarrow k} \lambda_i N_i - \lambda_k N_k$$

**Source terms at  $t > t_0$**

e.g.  $P(t) = \sum_k p_k N_k(t)$

Depends on **well-known decay data**

Training material



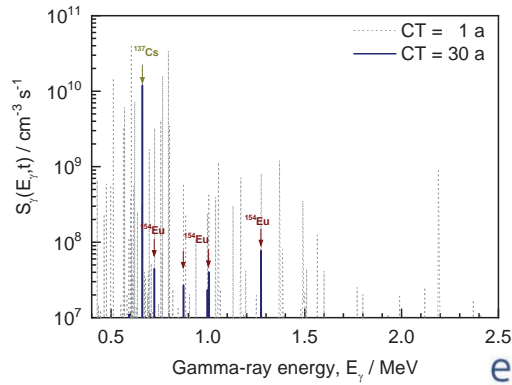


### GAMMA-RAY EMISSION BY SNF

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PWR UO<sub>2</sub> pellet (5 g)  
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 burnup = 45 GWd/t



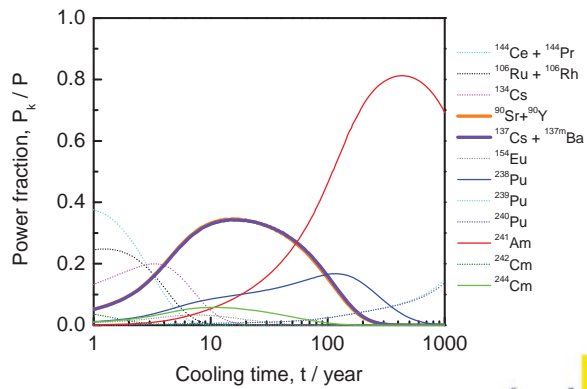
Training material



### THERMAL POWER PRODUCED BY SNF

- 1 a ≤ t ≤ 10 a
  - <sup>144</sup>Ce / <sup>144</sup>Pr
  - <sup>106</sup>Ru / <sup>106</sup>Rh
  - <sup>134</sup>Cs
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
- 10 a ≤ t ≤ 100 a
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
  - <sup>238</sup>Pu
  - <sup>241</sup>Am
  - <sup>244</sup>Cm
- 100 a ≤ t
  - <sup>241</sup>Am
  - <sup>238</sup>Pu
  - <sup>239,241</sup>Pu

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t



Training material





**<sup>137</sup>Cs: γ-RAY EMISSION AND THERMAL POWER**

- Production :

$$N_k(t') \sim Y_c \sigma_f N_f \varphi t'$$

- Gamma-ray emission : (decay data)

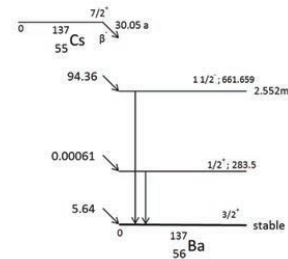
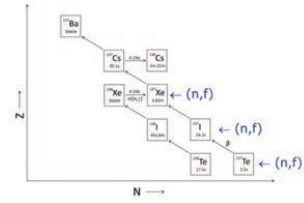
- $T_{1/2}$  : 30.05 (8) a
- $P(E_\gamma = 661.66\text{keV})$  : 0.8499 (20)

- Thermal power: specific decay heat rate,  $p_k = E_{dk} \lambda_k$  (decay data)

- $T_{1/2}$  : 30.18 (15) a
- $Q_{\beta^-}$  : 1175.63 (17) keV
- Recoverable energy
  - Average electron + recoil energy : 247.9 (12) keV
  - $\langle E_\gamma \rangle$  : 565.4 (13) keV

Decay data from DDEP (Decay Data Evaluation Project) : <http://www.nucleide.org/DDEP.htm>

Training material



**<sup>137</sup>Cs: PRODUCTION**

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

$$N_k(t') \approx \frac{Y_c \sigma_f N_f \varphi}{\lambda_k + \sigma_{k,\gamma} \varphi} [1 - e^{-(\lambda_k + \sigma_{k,\gamma} \varphi) t'}]$$

$(\lambda_k + \sigma_{k,\gamma} \varphi) \ll 1$

$$N_k(t') \sim Y_c \sigma_f N_f \varphi t'$$

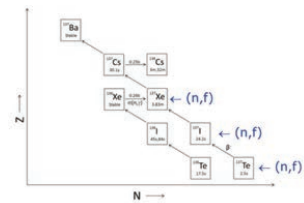
$(\sigma_f N_f \varphi t')$  : total number of fissions

$(\sigma_f N_f \varphi t') \times E_f$  : time integrated reactor power = burnup (BU)

$E_f$  = recoverable energy per fission

$$\Rightarrow N_k(t_0) \propto \text{BU}$$

$$N_k(t_0) \propto Y_c \text{BU}$$



<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> (decay of short lived precursors)

- Relatively long lived
- Small capture cross section



Training material





### <sup>137</sup>Cs: CONTRIBUTION TO THERMAL POWER

- Production : cumulative fission yields + burnup

$$N_k(t_0) \propto Y_c \text{ BU}$$

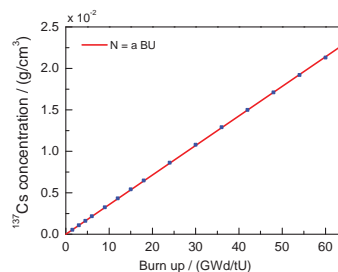
- Thermal power after cooling time t by <sup>137</sup>Cs

$$P_k(t) = p_k N_k(t_0) e^{-\lambda_k (t-t_0)} \quad p_k = E_{dk} \lambda_k$$

⇒ Nuclear data

- $Y_c$  : cumulative fission yields
- $\lambda_k$  : decay constant
- $E_{dk}$  : recoverable energy

⇒ Operational history : BU



Training material



### <sup>137</sup>Cs: γ-RAY EMISSION AND THERMAL POWER

- Production : cumulative fission yields + burnup

$$N_k(t_0) \propto Y_c \text{ BU}$$

- Gamma-ray emission : (decay data)

- $T_{1/2}$  : 30.05 (8) a
- $P(E_\gamma = 661.66\text{keV})$  : 0.8499 (20)

- Thermal power: specific decay heat rate,  $p_k = E_{dk} \lambda_k$  (decay data)

- $T_{1/2}$  : 30.18 (15) a
- $Q_{\beta^-}$  : 1175.63 (17) keV
- Recoverable energy
  - Average electron + recoil energy : 247.9 (12) keV
  - $\langle E_\gamma \rangle$  : 565.4 (13) keV

Decay data from DDEP (Decay Data Evaluation Project) : <http://www.nucleide.org/DDEP.htm>

Training material





### <sup>137</sup>Cs and <sup>90</sup>Sr: CONTRIBUTION TO THERMAL POWER (UNCERTAINTY EVALUATION)

$$P_k(t) = p_k N_k(t_0) e^{-\lambda_k (t-t_0)}$$

$$N_k(t_0) \propto Y_c BU$$

$$p_k = E_{dk} \lambda_k$$

$$\Rightarrow \frac{u_{P_k}}{P_k} = \sqrt{\left(\frac{u_{BU}}{BU}\right)^2 + \left(\frac{u_{Y_c}}{Y_c}\right)^2 + \left(\frac{u_{E_{dk}}}{E_{dk}}\right)^2}$$

⇒ Nuclear data

- $Y_c$  : cumulative fission yields
- $\lambda_k$  : decay constant
- $E_{dk}$  : recoverable energy

⇒ Operational history : BU

Note:

- Contribution of <sup>137</sup>Cs and <sup>90</sup>Sr: similar
  - simple cases
  - with relatively well determined nuclear data
- Production of e.g <sup>134</sup>Cs ore complex  $\propto BU^b$  with  $b \sim 2$

$$\Rightarrow \frac{u_{N_k}}{N_k} = 2 \frac{u_{BU}}{BU}$$



Training material



### <sup>137</sup>Cs : NUCLEAR DATA ( $Y_c, E_d$ )

Library	$E_d$ / keV	Ratio	<sup>137</sup> Cs		$(Y_c \times E_d)$ / keV	Ratio
			$100 \times Y_c$	Ratio		
DDEP/IAEA	811.8 (18)	1	6.221 (69)	1	50.5 (6)	1
JEF-2.2	812.0 (69)	1.000 (8)	6.244 (54)	1.004 (9)	50.7 (6)	1.004 (12)
JEFF-3.1.1	<b>810.1 (23)</b>	<b>0.998 (3)</b>	<b>6.221 (69)</b>	<b>1.000 (11)</b>	<b>50.4 (6)</b>	<b>0.998 (11)</b>
JEFF-3.3	<b>801.8 (23)</b>	<b>0.988 (3)</b>	<b>6.090 (63)</b>	<b>0.979 (10)</b>	<b>48.8 (5)</b>	<b>0.967 (10)</b>
ENDF/B-VI.8	813.4 (41)	1.002 (5)	6.188 (31)	0.995 (5)	50.3 (4)	0.997 (7)
ENDF/B-VII.0	805.7 (16)	0.992 (2)	6.188 (31)	0.995 (5)	49.9 (3)	0.987 (5)
ENDF/B-VIII.0	<b>805.8 (18)</b>	<b>0.993 (2)</b>	<b>6.188 (31)</b>	<b>0.995 (5)</b>	<b>49.9 (3)</b>	<b>0.987 (5)</b>

DDEP: <http://www.nucleide.org/DDEP.htm>  
 Evaluated data libraries: [https://www.oecd-nea.org/jcms/pl\\_39910/janis](https://www.oecd-nea.org/jcms/pl_39910/janis)



Training material



**<sup>90</sup>Sr : NUCLEAR DATA ( $Y_c, E_d$ )**

Library	$E_d$ / keV	Ratio	<sup>90</sup> Sr		$(Y_c \times E_d)$ / keV	Ratio
			$100 \times Y_c$	Ratio		
DDEP/IAEA	1129.4 (14)	1	5.730 (130)	1	64.7 (15)	1
JEF-2.2	1129.6 (7)	1.000 (1)	<b>5.847 (188)</b>	<b>1.020 (33)</b>	<b>66.0 (21)</b>	<b>1.021 (33)</b>
JEFF-3.1.1	1107.8 (13)	0.981 (1)	5.729 (132)	1.000 (23)	63.5 (15)	0.981 (23)
JEFF-3.3	1127.3 (13)	0.998 (1)	<b>5.676 (131)</b>	<b>0.991 (23)</b>	<b>64.0 (15)</b>	<b>0.989 (23)</b>
ENDF/B-VI.8	1129.9 (12)	1.000 (1)	5.782 (58)	1.009 (10)	65.3 (7)	1.010 (10)
ENDF/B-VII.0	1129.4 (13)	1.000 (1)	5.782 (58)	1.009 (10)	65.3 (7)	1.009 (10)
ENDF/B-VIII.0	1128.8 (11)	0.999 (1)	<b>5.782 (58)</b>	<b>1.009 (10)</b>	<b>65.3 (7)</b>	<b>1.009 (10)</b>
<b>Ramthum (Exp. 1967)</b>	<b>1147.0 (90)</b>					

DDEP: <http://www.nucleide.org/DDEP.htm>  
 Evaluated data libraries: [https://www.oecd-nea.org/jcms/pl\\_39910/janis](https://www.oecd-nea.org/jcms/pl_39910/janis)  
 H. Ramthum, Proc. Symp. Standardization of radionuclides, Oct. (1966) (IAEA, 1967), p. 589

Training material



**<sup>90</sup>Sr and <sup>137</sup>Cs: NUCLEAR DATA ( $Y_c, E_d$ )**

Library	<sup>90</sup> Sr		<sup>137</sup> Cs	
	$(E_d \times Y_c)$ / keV	Ratio	$(Y_c \times E_d)$ / keV	Ratio
DDEP/IAEA	64.7 (15)	1	50.5 (6)	1
JEF-2.2	<b>66.0 (21)</b>	<b>1.021 (33)</b>	<b>50.7 (7)</b>	<b>1.004 (12)</b>
JEFF-3.1.1	63.5 (15)	0.981 (23)	50.4 (6)	0.998 (11)
JEFF-3.3	<b>64.0 (15)</b>	<b>0.989 (23)</b>	<b>48.8 (5)</b>	<b>0.967 (10)</b>
ENDF/B-VI.8	65.3 (7)	1.010 (10)	50.3 (4)	0.997 (7)
ENDF/B-VII.0	65.3 (7)	1.009 (10)	49.9 (3)	0.987 (5)
ENDF/B-VIII.0	<b>65.3 (7)</b>	<b>1.009 (10)</b>	<b>49.9 (3)</b>	<b>0.987 (5)</b>

Ilas et al., Nucl. Eng. Des. 319 (2017) 176  
 $u_p/P = 1.3\%$ , is this realistic? No

Data set	Data set	Uncertainty (1σ) (%)
Modeling data	Fuel design	0.20
	Operating data	0.85
	Total	0.87
Nuclear data	Cross sections	0.88
	Fission yields	0.26
	Total	0.92
Overall effect	Total	1.27

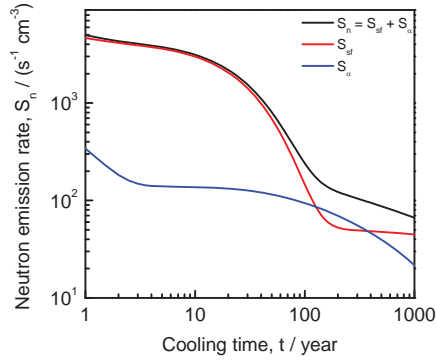
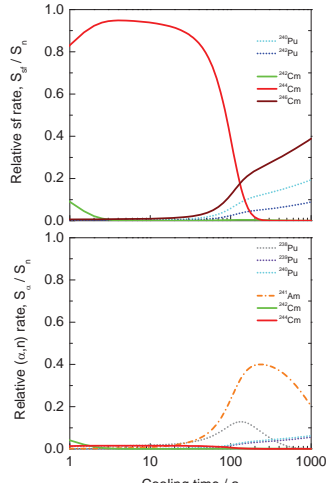
Training material





### NEUTRON EMISSION BY SPENT NUCLEAR FUEL

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t



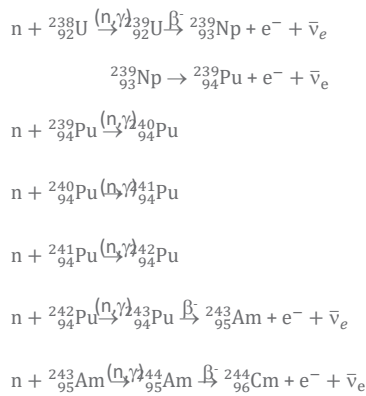
⇒ Main contribution from <sup>244</sup>Cm(sf)

Training material



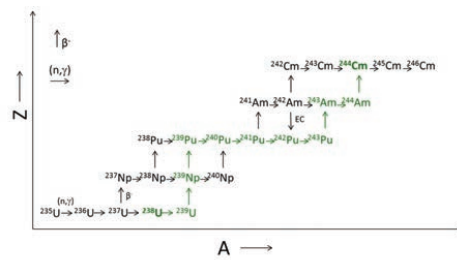
### <sup>244</sup>Cm : NEUTRON EMISSION

- Production



Sequence of

- (n,γ) reactions (6)
- β<sup>-</sup> decays (4)



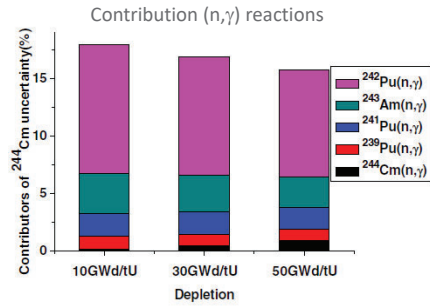
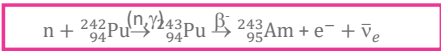
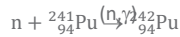
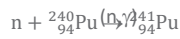
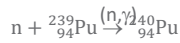
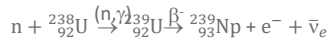
Training material





**<sup>244</sup>Cm : UNCERTAINTY OF INVENTORY DUE TO NUCLEAR DATA**

• Production



Burnup	Relative uncertainty
10 GWD/t	12.1 %
30 GWD/t	11.1 %
50 GWD/t	10.0 %

Tiejun Zu et al., Annals of Nuclear Energy 94 (2016) 399

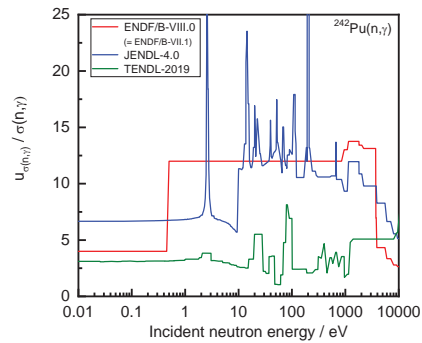
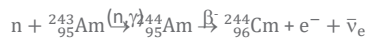
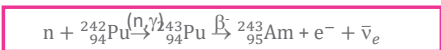
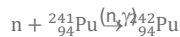
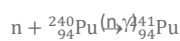
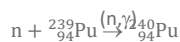
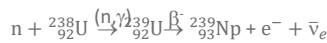


Training material



**<sup>244</sup>Cm : UNCERTAINTY OF INVENTORY DUE TO NUCLEAR DATA**

• Production

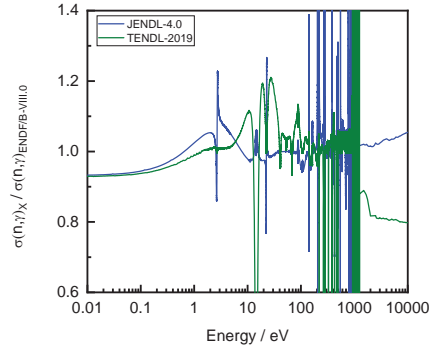
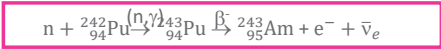
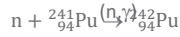
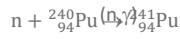
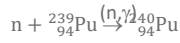
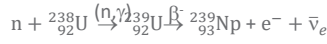


Training material



**<sup>244</sup>Cm : DIFFERENCES IN INVENTORY DUE TO NUCLEAR DATA**

- Production



Training material



**<sup>244</sup>Cm : UNCERTAINTY OF INVENTORY DUE TO FUEL HISTORY**

- Production

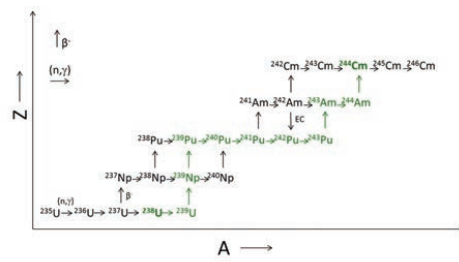
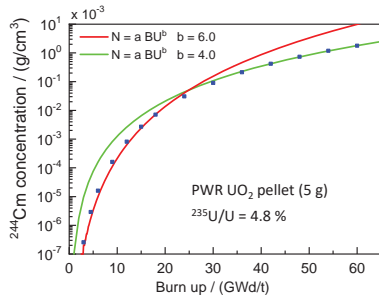
$$N = aBU^b$$

$b = 6$  for  $BU < 20$  GWd/tU

$$\frac{\delta N}{N} = b \frac{\delta BU}{BU}$$

Sequence of

- (n,γ) reactions (6)
- β decays (4)

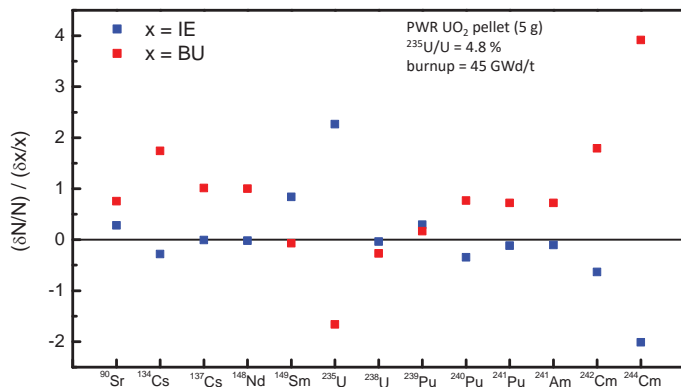


Training material





### NUCLIDE INVENTORY: DESIGN AND OPERATIONAL HISTORY



$$^{244}\text{Cm} : N = a\text{BU}^b$$

$$b \approx 4 \text{ for BU} = 45 \text{ GWd/t}$$

$$\frac{\delta N}{N} = b \frac{\delta \text{BU}}{\text{BU}}$$

0.5 % uncertainty on BU  
 ⇒ 2 % uncertainty on <sup>244</sup>Cm inventory



Training material



### SUMMARY AND CONCLUSIONS

- The main observables of interest for a safe handling, transport, intermediate storage and final disposal were identified and discussed
- A characterisation of SNF for these observables requires the inventory of some key nuclides with different characteristics
- The inventory of the key nuclides can only be obtained by theoretical calculations using burnup code which rely on a combination of neutron transport and nuclide depletion and creation calculations
- The quality of the theoretical calculations strongly depends on the quality of the nuclear data and design and irradiation history of the SNF
- Some key nuclear data (including their uncertainties) such as cumulative fission yields and neutron induced capture cross sections need to be improved to allow an accurate estimation of the main observables of interest including reliable confidence limits



Training material



## BIBLIOGRAPHY AND REFERENCES

### Spent nuclear fuel observables and key nuclides

- Broadhead et al., "Investigation of nuclide importance to functional requirements related to transport and long-term storage of LWR spent fuel", Report ORNL/TM-12742 (1995)
- Gauld et al., "Nuclide importance to criticality safety, decay heating and source terms related to transport and interim storage of high-burnup LWR fuel", Report NUREG/CR-6700, ORNL/TM-2000/284 (2001)
- Žerovnik et al., "Observables of interest for the characterisation of Spent Nuclear Fuel", EUR 29301 EN (2018), JRC112361
- Schillebeeckx et al., "Characterisation of spent nuclear fuel by theoretical calculations and non-destructive analysis", see JRC114178 (2019)

### Burnup codes

- Stankovskiy and Van den Eynde, "Advanced method for calculations of core burn-up, activation of structural materials and spallation products accumulation in accelerator driven system", Science and Technology of Nuclear Installations 2012 (2012) 545103
- Álvarez-Velarde, "Validation of the burn-up code EVOLCODE 2.0 with PWR experimental data and with a Sensitivity/Uncertainty analysis", Annals of Nuclear Energy 73 (2014) 175
- Leppänen et al., "The Serpent Monte Carlo code: status, development and applications in 2013", Annals of Nuclear Energy 82 (2015) 142
- Kashima et al., "Validation of burnup calculation code SWAT4 by evaluation of isotopic composition data of mixed oxide fuel irradiated in pressurized water reactor", Energy Procedia 71 (2015) 159
- Rearden and Jessee, "SCALE Code System", ORNL/TM-2005/39 Version 6.2, April 2016
- Gauld et al., "Isotopic depletion and decay methods and analysis capabilities in SCALE", Nuclear Technology 174 (2017) 169
- Ebiwonjumi et al., "Verification and validation of radiation source term capabilities in STREAM", Annals of Nuclear Energy 124 (2019) 80

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## BIBLIOGRAPHY AND REFERENCES

### Bateman equation

- Jerzy Cetnar, "General solution of Bateman equations for nuclear transmutation", Annals of Nuclear Energy 33 (2006) 640
- Maren Vranckx, "Implementation, validation and comparison of different algorithms to solve the Bateman equations for very large systems", Thesis Msc, Univ. Gent, June 2016
- Isotalo and Aarnio, "Comparison of depletion algorithms for large systems of nuclides", Annals of Nuclear Energy 38 (2011) 261
- Maria Pusa, "Numerical methods for nuclear fuel depletion calculations", PhD Thesis, Aalto University, May 2013
- Calvin and Hart, "Architecture for the performance of nuclear fuel depletion calculations", INL/MIS-19-56187, November 2019

### Nuclear data

- Nuclear data libraries at JANIS NEA, [https://www.oecd-nea.org/jcms/pl\\_39910/janis](https://www.oecd-nea.org/jcms/pl_39910/janis)
- Decay data, <http://www.nucleide.org/DDEP.htm>
- Nichols et al., "Handbook of nuclear data for safeguards: database extensions, august 2008", INDC-2453, INDC(NDS) – 0534

Training material





**2.3 Neutron resonance experiments; P. Schillebeeckx, JRC Geel;  
Summer school on neutron detectors and related applications,  
Riva del Garda; 30/06 - 04/07/2022**



# Neutron Resonance Experiments

P. Schillebeeckx

European Commission

Joint Research Centre, Geel (BE)

*Summer School on Neutron Detectors and Related Applications  
Riva del Garda, 2022*



## Joint Research Centre

Headquarters in Brussels  
and research facilities located  
in 5 Member States:

- **Belgium (Geel)**
- Germany (Karlsruhe)
- Italy (Ispra)
- The Netherlands (Petten)
- Spain (Seville)



## Nuclear facilities at JRC - Geel



**GELINA**  
neutron time-of-flight facility for high-resolution neutron measurements



**MONNET**  
tandem accelerator based fast neutron source



**TARGET**  
nuclear target preparation laboratories



**RADMET**  
laboratories for standardisation of radionuclide activity



**HADES**  
low-level gamma-spectrometry laboratory



**METRO**  
nuclear reference material and measurement facility

Operated by JRC.G.2 Unit (SN3S)  
“Standards for Nuclear Safety, Security and Safeguards”

- Nuclear data
- Radionuclide measurements
- Nuclear safeguards metrology



## Nuclear data



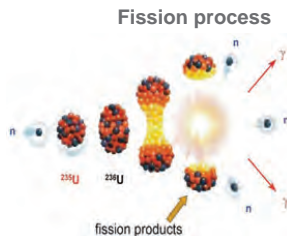
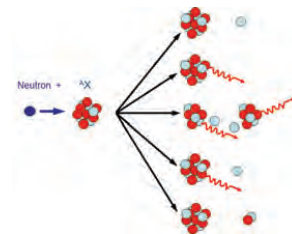
**GELINA** (this presentation)  
neutron time-of-flight facility for high-resolution neutron measurements



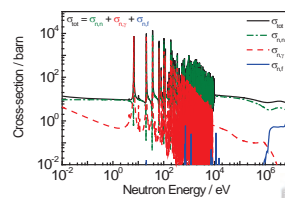
**MONNET** (S. Oberstedt)  
tandem accelerator based fast neutron source



**TARGET**  
nuclear target preparation laboratories



Neutron induced interaction cross sections



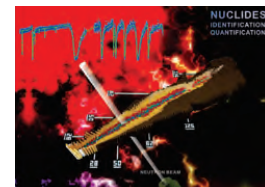
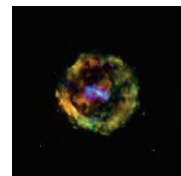
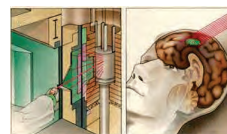
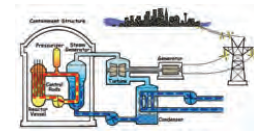
## Contents

- Neutron induced interactions: basic principles
- Neutron resonance spectroscopy
  - Neutron Time-Of-Flight measurements
  - Transmission measurements
  - Reaction cross section measurements
- Applications
  - Neutron Resonance Analysis (NRA)
  - Characterisation of Spent Nuclear Fuel (SNF)



## Nuclear data

- **Nuclear data for energy technology**
  - Safety of current systems
  - Back-end: Spent Nuclear Fuel (Burn Up Credit, Decay heat, ...)
  - Development of innovative systems (e.g. MYRRHA)
- Nuclear physics
- Nuclear medicine: diagnostics and therapy
- Nucleosynthesis and nuclear astrophysics
- Detector development
- Materials research (NAA, PGAA, Neutron Resonance Analysis, ...)
- ....

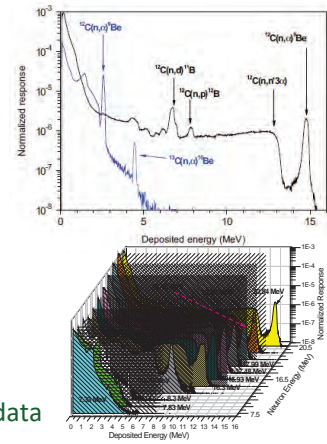


## Nuclear data: response functions of neutron detectors

- For EJ301(NE213), EJ315 type and stilbene well established
  - H(n,n)H, D(n,n)D based
- CVD diamond (Chemical Vapour Deposition)
  - Fast neutron detector
  - $^{12}\text{C}(n,p)^{12}\text{B}$ ,  $^{12}\text{C}(n,d)^{11}\text{B}$ ,  $^{12}\text{C}(n,\alpha)^9\text{Be}$ ,  $^{12}\text{C}(n,n')^3\alpha$
- Elpasolite crystals
  - Dual mode (neutron +  $\gamma$ -ray detection)
  - CLYC ( $\text{Cs}_2\text{LiYCl}_6$ ), CLLBC ( $\text{Cs}_2\text{LiLaBr}_6\text{Cl}_6$ ) with  $^6\text{Li}$  or  $^7\text{Li}$
  - Thermal:  $^6\text{Li}(n,\alpha)t$
  - Fast :  $^{35}\text{Cl}(n,p)$  and  $^{35}\text{Cl}(n,\alpha)$
  - Also needed for sodium cooled reactor concepts
- ...

⇒ simulation of response function requires accurate cross section data (see A. Ferrari)

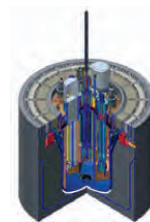
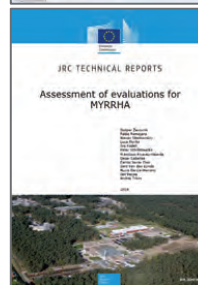
Diamond detector  
Pillon et al., NIMA 640 (2011) 185



## Nuclear data: MYRRHA

“Multi-purpose hYbrid Research Reactor for High-tech Applications”

Nuclide	Quantity/reaction	Energy region
$^{16}\text{O}$	$\sigma(n,n)$	continuum (fast)
	$\sigma(n,n)$	resonance and continuum
$^{56}\text{Fe}$	$\sigma(n,n')$	continuum
	$\sigma(n,\gamma)$	resonance and continuum
	$\sigma(n,n)$	resonance and continuum
$^{208}\text{Pb}$	$\sigma(n,n)$	resonance and continuum
	$\sigma(n,n')$	resonance and continuum
$^{209}\text{Bi}$	$\sigma(n,n')$	resonance and continuum
	$\sigma(n,\gamma)$	resonance and continuum
$^{235}\text{U}$	$\bar{\nu}$	resonance and continuum
	$\sigma(n,f)$	resonance and continuum
	$\sigma(n,\gamma)$	resonance and continuum
$^{238}\text{U}$	$\sigma(n,n)$	continuum
	$\sigma(n,n')$	resonance and continuum
	$\sigma(n,\gamma)$	resonance and continuum
$^{238}\text{Pu}$	$\sigma(n,f)$	resonance and continuum
	$\bar{\nu}$	continuum
$^{239}\text{Pu}$	$\chi$	continuum
	$\sigma(n,f)$	continuum
$^{240}\text{Pu}$	$\sigma(n,\gamma)$	resonance and continuum
	$\bar{\nu}$	continuum
$^{241}\text{Pu}$	$\sigma(n,f)$	resonance and continuum
$^{242}\text{Pu}$	$\sigma(n,f)$	continuum



## Nuclear data: back-end of the fuel cycle

- **Criticality safety** for Spent Nuclear Fuel (SNF)
  - Original procedures : conservative based on fresh fuel (< 4%)
  - Fuel cycle extension : increase of initial enrichment (IE) and burnup (BU)
- ⇒ **Burn Up Credit (BUC)** approach:
  - “Account for reactivity loss due to **(n,γ)** reactions in actinides and fission products”
- **Nuclear data** are required to **optimise** transport, handling, intermediate storage and **final disposal of SNF**



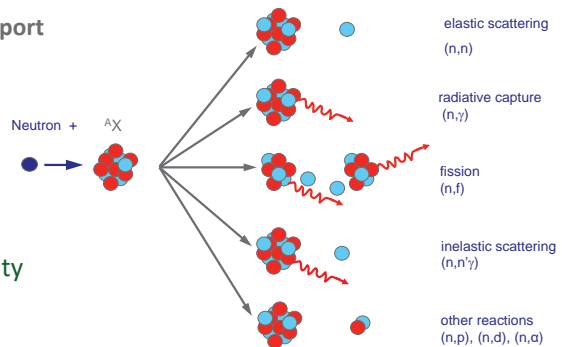
## Neutron transport calculations

Majority of the applications require **neutron transport** calculations

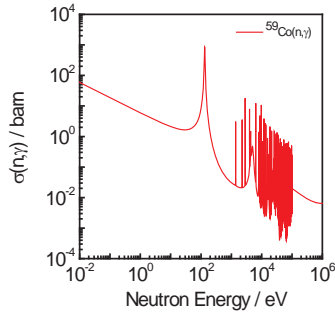
- deterministic (Boltzman)
- stochastic (Monte Carlo), e.g. FLUKA, MCNP, SERPENT

relying on **neutron interaction cross sections**

⇒ **Quality of the output depends on the quality of the nuclear data**



## Cross section: definition



- Cross section is a quantity that is used to calculate the probability that a neutron interaction occurs:
  - symbol :  $\sigma$
  - dimension : area, unit barn,  $1 \text{ b} = 10^{-28} \text{ m}^2$
- Reaction rate per target nucleus for a specific interaction (n,r) :



$$r_r = \sigma_r \varphi$$

- $r_r$  : reaction rate per nucleus (s<sup>-1</sup>)
- $\varphi$  : neutron fluence rate (s<sup>-1</sup> cm<sup>-2</sup>)
- $\sigma_r$  : cross section for (n,r) reaction (cm<sup>-2</sup>)



## Cross section: definition

Reaction:  $X + a \rightarrow Y + b$

$X(a,b)Y$



- Cross section  $\sigma(E_a)$  : **energy dependent** cross section

$E_a$  : kinetic energy of **incident particle a**

$$\sigma(E_a) = \int \int \frac{d^2\sigma(E_a, E_b, \Omega)}{dE_b d\Omega} dE_b d\Omega$$

- **Differential** cross section (**product particle**)

$E_b$  : kinetic energy of product particle b

$\Omega$  : emission (solid) angle of product particle b

$$\frac{d\sigma(E_a, E_b)}{dE_b} \quad \frac{d\sigma(E_a, \Omega)}{d\Omega}$$

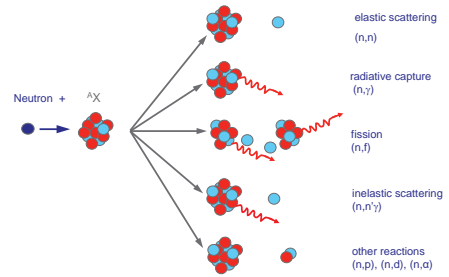
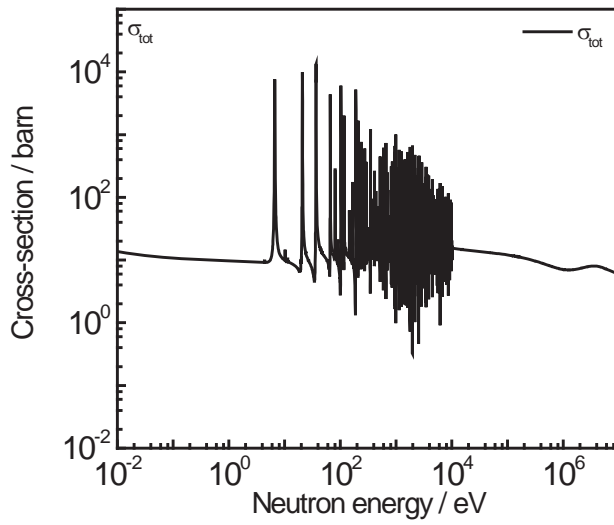
- **Double differential** cross section (**product particle**)

$E_b$  and  $\Omega$

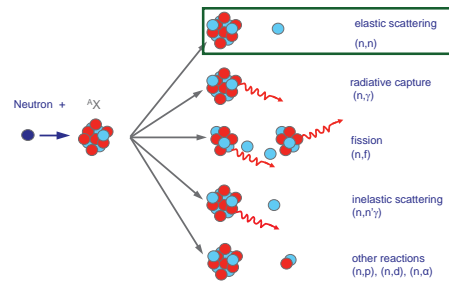
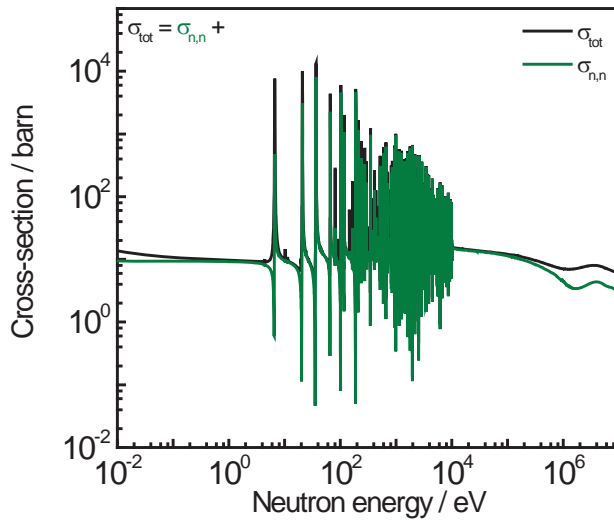
$$\frac{d^2\sigma(E_a, E_b, \Omega)}{dE_b d\Omega}$$



## Neutron interaction cross sections: e.g. $^{238}\text{U}$

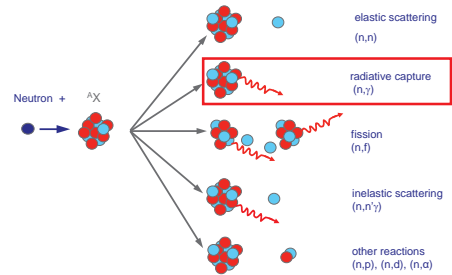
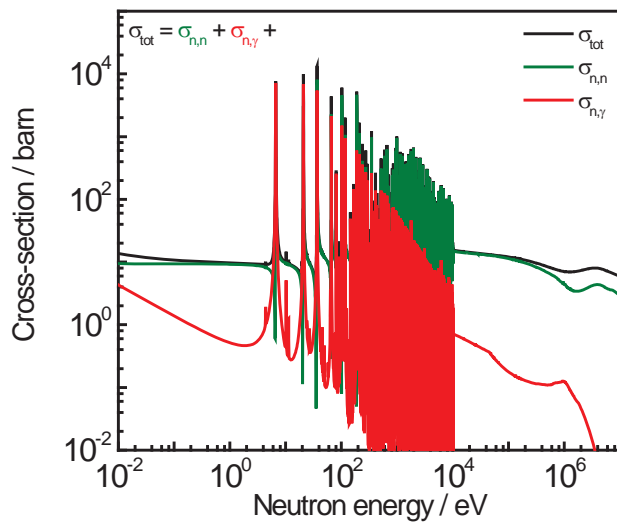


## Neutron interaction cross sections: e.g. $^{238}\text{U}$

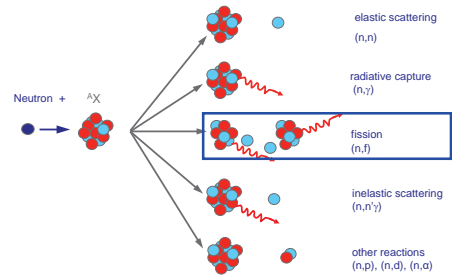
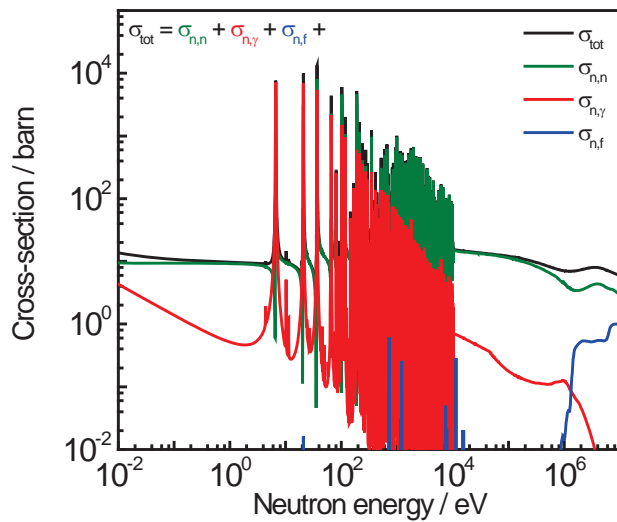




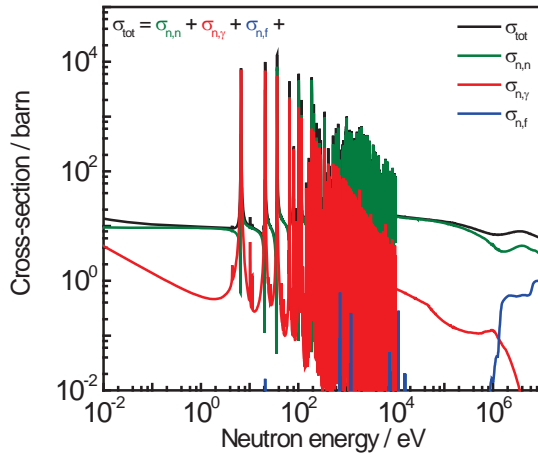
### Neutron interaction cross sections: e.g. <sup>238</sup>U



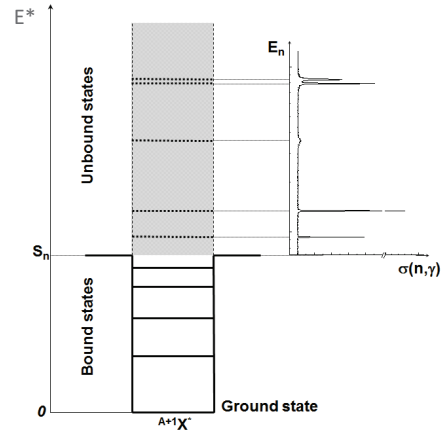
### Neutron interaction cross sections: e.g. <sup>238</sup>U



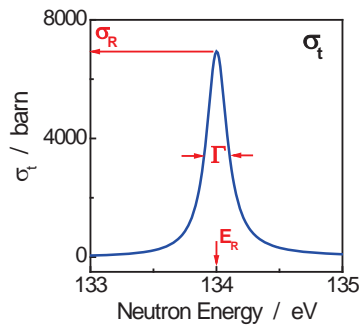
## Resonance structures: compound nucleus



$$E^* = S_n + \frac{A}{A+1} E_n$$



## Resonance structures: compound nucleus



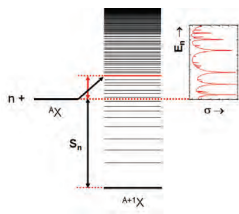
The resonant structure can be approximated by a Lorentzian shape:

$$\text{with } \sigma_{\text{tot}} \sim \frac{1}{(E_n - E_R)^2 + (\Gamma/2)^2}$$

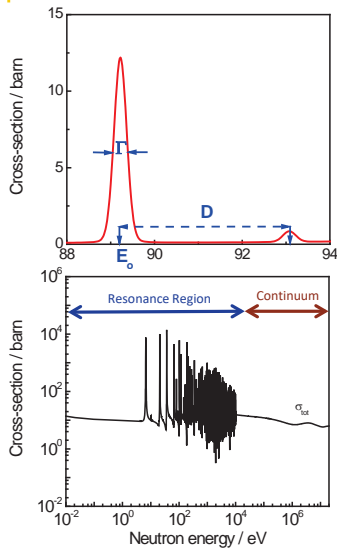
$\Gamma$  total width (FWHM)  
 $E_R$  resonance energy

Heisenberg uncertainty principle

$$\Delta E \Delta t \geq \frac{\hbar}{2} \quad \Gamma \tau \geq \frac{\hbar}{2}$$



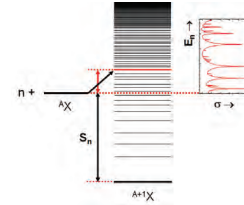
## Neutron interactions cross sections



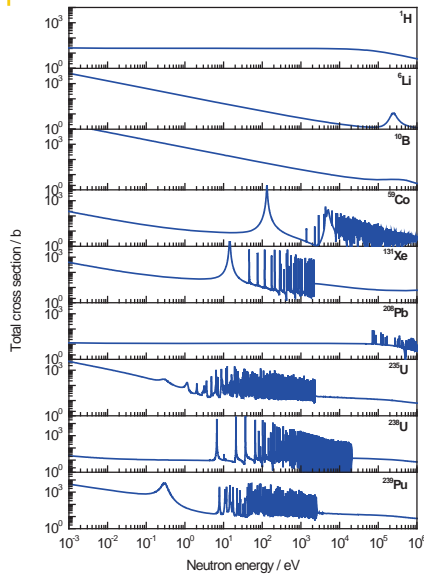
$D$  : level distance (distance between resonances)  
 $\Gamma$  : resonance width

Increasing  $E_n \nearrow$   
 $\Rightarrow$  Level density increases :  $D \searrow$   
 $\Rightarrow$  Resonance width increases :  $\Gamma \nearrow$

- Resonance region :  $D > \Gamma$
- Continuum region :  $D < \Gamma$



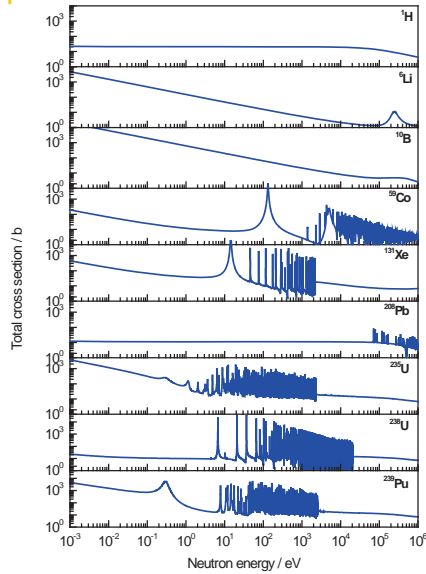
## Neutron interaction cross sections



- Cross sections are different for each nuclide
- Cross sections are strongly energy dependent
  - Low energy region:  $1/v$  dependence
  - Resonance structures
- Level density increases with increasing  $A$ 
  - Except for nuclei with a magic neutron or proton number
- Upper energy of resonance region decreases with increasing  $A$ 
  - Except for nuclei with a magic neutron or proton number



## Neutron interaction cross sections below 20 MeV

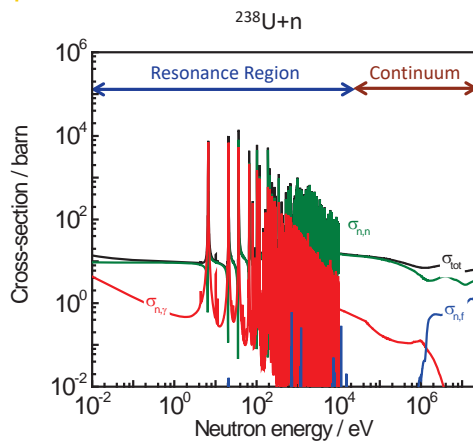


Fröhner, JEFF Report 18



- **Theoretical cross sections** required for nuclear energy applications
  - Ensures full consistency, e.g.  $\sigma_{tot} = \sum_j \sigma_j$
  - Consistency between energy regions
  - Inter- and extrapolation in regions where no data are available
  - **Doppler broadening**
- **Cross sections** for neutron induced interactions **cannot be predicted** by theory based on first principles
- **Cross sections** in evaluated data libraries are **parameterized by nuclear reaction models**

## Neutron interaction cross sections below 20 MeV



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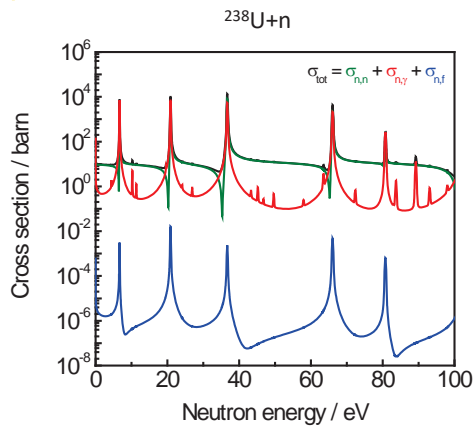


**Parameterised** by nuclear reaction models  
 Different energy regions : different theories

- **Resonance region**
  - R-matrix formalism
- **Continuum**
  - Hauser-Feshbach
  - Statistical level theories
  - Optical model
  - Pre-equilibrium theories
  - ...

⇒ **Model parameters** determined by an **adjustment to experimental data**

## Resonance region: R – matrix formalism



R-matrix

Lane and Thomas, Rev. Mod. Phys. 30 (1958) 257

Model parameters derived from experimental data

R and  $(E_R, J^\pi, \Gamma_n, \Gamma_\gamma, \Gamma_f, \dots)_j$

- $E_R$  resonance energy
- $\Gamma_n, \Gamma_\gamma, \Gamma_f, \dots$  partial widths
- $\Gamma$  total width  
( $\Gamma = \Gamma_n + \Gamma_\gamma + \Gamma_f \dots$ )
- R scattering radius

Partial widths ( $\Gamma_n, \Gamma_\gamma, \Gamma_f, \dots$ ) reflect the probability that a specific reaction occurs

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## Single Level Breit Wigner (SLBW) approximation

$(E_R, \Gamma_n, \Gamma_\gamma, J^\pi, R)$

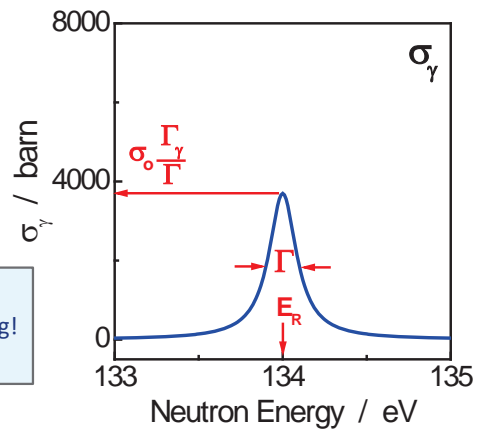
$g$ : statistical factor  $g = \frac{1+2J}{2(1+2I)}$

$k_n$ : neutron wave number

- $(n, \gamma)$

$$\sigma_\gamma(E_n) = g \frac{\pi}{k_n^2} \frac{\Gamma_n \Gamma_\gamma}{(E_n - E_R)^2 + (\Gamma/2)^2}$$

- ⇒  $\sigma_\gamma = 0$  when  $\Gamma_n = 0$
- ⇒ No resonance capture without resonance elastic scattering!
- $\Gamma_n$  reflects the probability to form the compound nucleus



Note: resonance energy related to incident neutron energy

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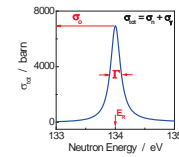
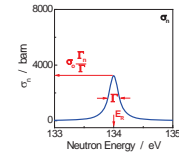
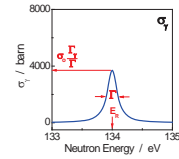
## Single Level Breit Wigner (SLBW) approximation

$(E_R, \Gamma_n, \Gamma_\gamma, J^\pi, R)$

- $(n, \gamma) \quad \sigma_\gamma(E_n) = g \frac{\pi}{k_n^2} \frac{\Gamma_n \Gamma_\gamma}{(E_n - E_R)^2 + (\Gamma/2)^2}$

- $(n, n) \quad \sigma_n(E_n) = g \frac{\pi}{k_n^2} \frac{\Gamma_n \Gamma_n}{(E_n - E_R)^2 + (\Gamma/2)^2} + g \frac{4\pi}{k_n} \frac{\Gamma_n (E_n - E_R) R}{(E_n - E_R)^2 + (\Gamma/2)^2} + 4\pi g R^2$

- $(n, \text{tot}) \quad \sigma_{\text{tot}}(E_n) = g \frac{\pi}{k_n^2} \frac{\Gamma_n \Gamma}{(E_n - E_R)^2 + (\Gamma/2)^2} + g \frac{4\pi}{k_n} \frac{\Gamma_n (E_n - E_R) R}{(E_n - E_R)^2 + (\Gamma/2)^2} + 4\pi g R^2$

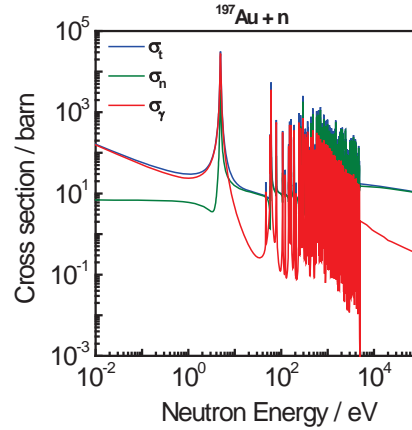
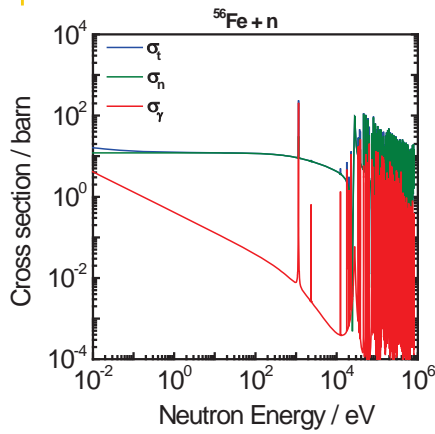


Note: resonance energy related to incident neutron energy

Fröhner, JEFF Report 18



## Neutron interaction cross sections in resonance region



- No capture without scattering
- Relative contribution of  $\sigma_n$  and  $\sigma_\gamma$  to  $\sigma_{\text{tot}}$  may be different

Fröhner, JEFF Report 18



### 1/v behaviour of reaction cross section, e.g. (n,γ)

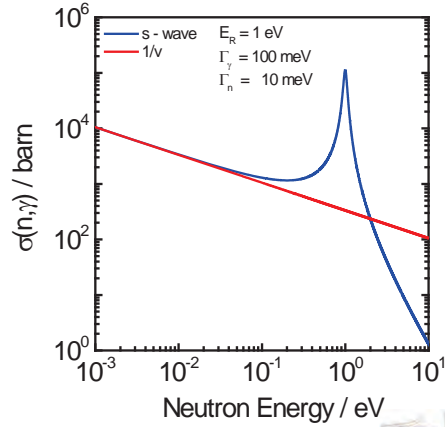
Neutron width  $\Gamma_n$  depends on  $\ell$  and  $E_n$  due to centrifugal-barrier penetrability

- s - wave ( $\ell = 0$ )

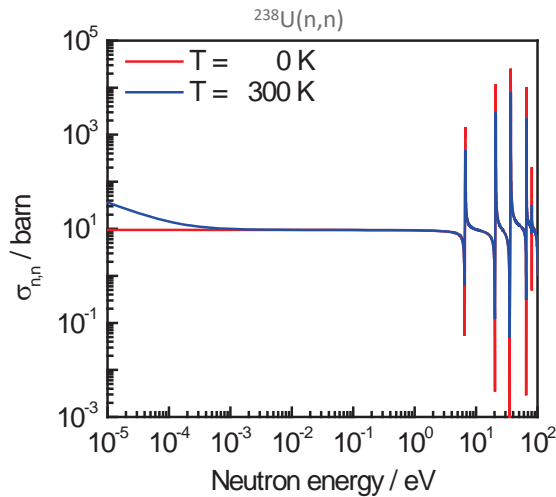
$$\Gamma_n(E_n) = \Gamma_n^0 \sqrt{\frac{E_n}{1\text{eV}}} \quad k_n = \frac{2\pi p}{\lambda} = \frac{p}{\hbar}$$

1/v dependence in thermal region

$$\sigma_\gamma(E_n) = g \frac{\pi}{k_n^2} \frac{\Gamma_n \Gamma_\gamma}{(E_n - E_R)^2 + (\Gamma/2)^2}$$



### 1/v behaviour of (n,n) in extreme low energy region



$$\bar{\sigma}(v, T) = \frac{1}{v} \int |v - V| \sigma(|v - V|) P(V) dV$$

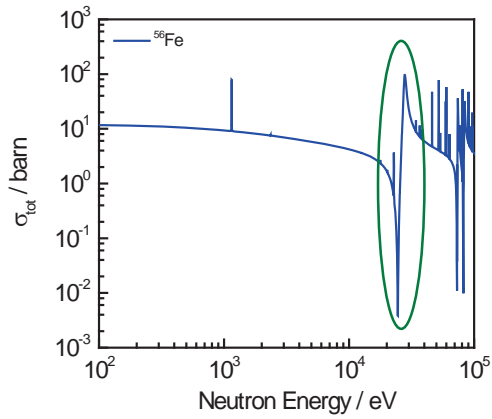
$$\begin{aligned} \sigma(|v - V|) &= k \text{ and } v \ll V \\ \Rightarrow \bar{\sigma}(v, T) &\approx \frac{1}{v} \int k V P(V) dV \\ \Rightarrow \bar{\sigma}(v, T) &= \frac{K'}{v} \end{aligned}$$

Cross sections in data bases such as JANIS are mostly Doppler broadened



## Neutron interaction cross sections in resonance region

$$\sigma_{\text{tot}}(E_n) = g \frac{\pi}{k_n^2} \frac{\Gamma_n \Gamma}{(E_n - E_R)^2 + (\Gamma/2)^2} + g \frac{4\pi}{k_n} \frac{\Gamma_n (E_n - E_R) R}{(E_n - E_R)^2 + (\Gamma/2)^2} + 4\pi g R^2$$



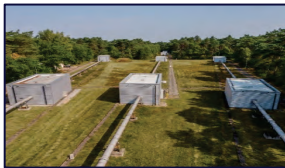
Interference term :  $\ell = 0$

- Filtered neutron beams, e.g.
  - Fe + Al : 24 keV
  - Si + Ti : 144 keV
- Shielding and collimation of fast neutrons
  - several materials required

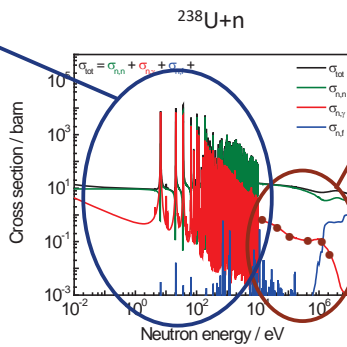


## Neutron facilities: GELINA and MONNET

GELINA



White neutron source  
+  
Time-of-flight (TOF)



MONNET



Mono-energetic neutrons  
(cp,n) reactions

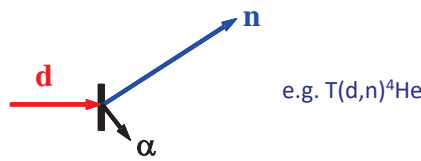




# MONNET

Quasi mono-energetic neutrons produced  
By charged particle induced reactions

${}^7\text{Li}(p,n){}^7\text{Be}$	$E_n: 0 - 5.3 \text{ MeV}$
$\text{T}(p,n){}^3\text{He}$	$E_n: 0 - 6.2 \text{ MeV}$
$\text{D}(d,n){}^3\text{He}$	$E_n: 1.8 - 10.1 \text{ MeV}$
$\text{T}(d,n){}^4\text{He}$	$E_n: 12.1 - 24.1 \text{ MeV}$



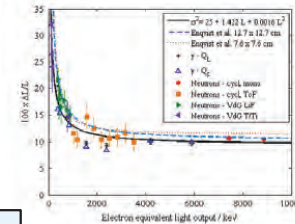
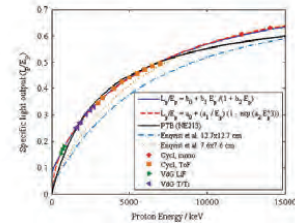
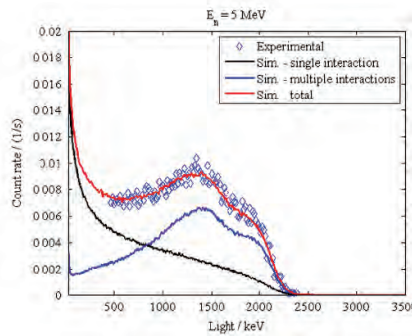
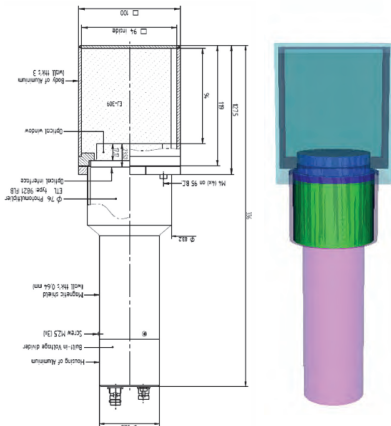
## MONNET



Mono-energetic neutrons  
(cp,n) reactions



## E.g. response functions for a EJ309 scintillator



Light output functions for protons are strongly non-linear and different for each system  
Require experimental verification

Tomanin et al., NIMA 756 (2014) 45



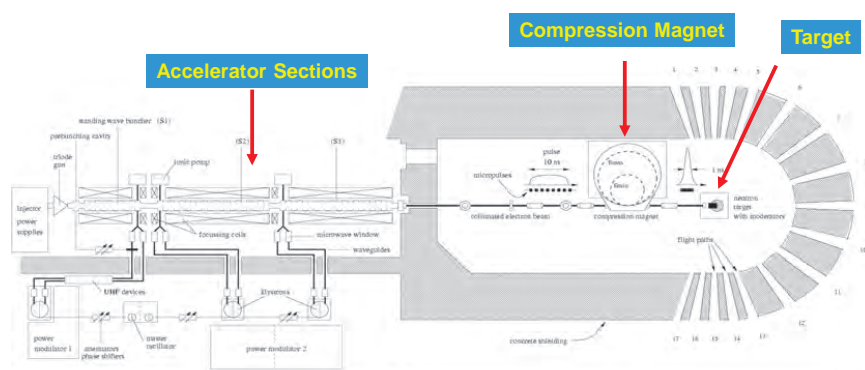
## GELINA: TOF – facility



- Pulsed white neutron source  
( $10 \text{ meV} < E_n < 20 \text{ MeV}$ )
- Neutron energy : time – of – flight (TOF)
- Multi-user facility: 10 flight paths (10 m – 400 m)
- Measurement stations with special equipment:
  - Total cross section measurements
  - Reaction (partial) cross section measurements



## GELINA: linear accelerator

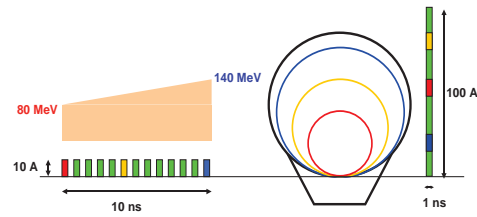
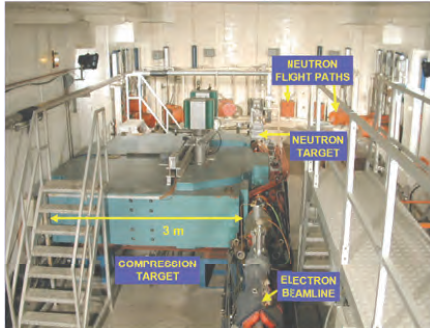


Normal operating parameters

Average Current	: 50 $\mu\text{A}$	Frequency	: 400 Hz
Average Electron Energy	: 100 MeV	Pulse Width	: 2 ns
Mean Power	: 5.0 kW	Neutron Flux	: $1 \times 10^{13} \text{ 1/s}$



## GELINA: compression magnet



$$B\rho = \frac{p}{q}; E \approx pc; q = e$$

$$\Rightarrow \rho = \frac{1}{B} \frac{E}{qc}$$

$$\Rightarrow B = \frac{2\pi}{qc^2} \frac{\Delta E}{\Delta\tau}$$

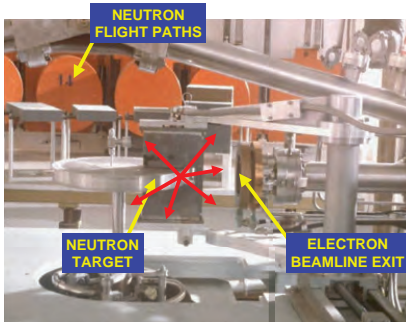
$$\Delta E = 60 \text{ MeV}$$

$$\Delta\tau = 10 \text{ ns}$$

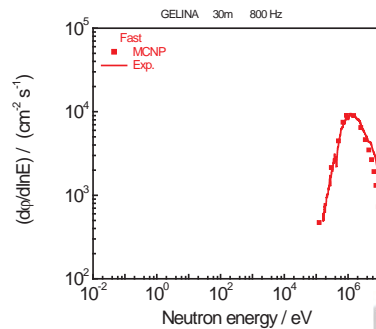
⇒ compressed pulse width ~ 1 ns



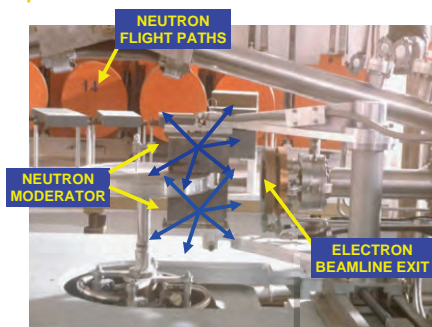
## GELINA: neutron production



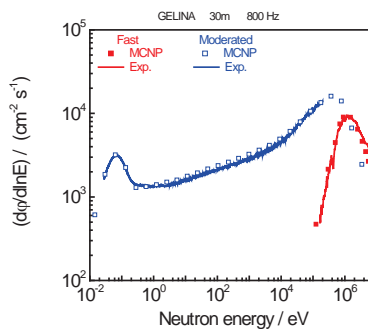
- $e^-$  accelerated to  $E_{e-,max} \approx 140 \text{ MeV}$
- Bremsstrahlung in U-target (rotating & cooled with liquid Hg)
- $(\gamma, n), (\gamma, f)$  in U-target



## GELINA: neutron production



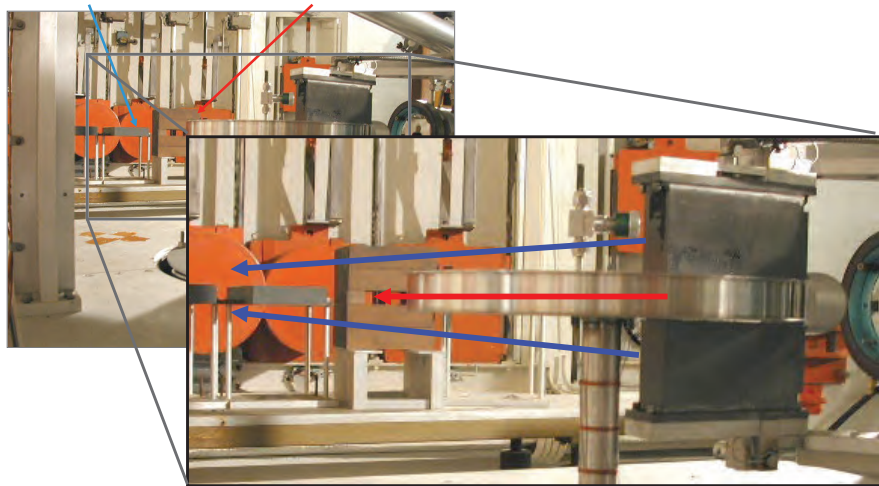
- $e^-$  accelerated to  $E_{e^-,max} \approx 140$  MeV
- Bremsstrahlung in U-target (rotating & cooled with liquid Hg)
- $(\gamma, n)$ ,  $(\gamma, f)$  in U-target
- Low energy neutrons by moderation (water moderator in Be-canning)



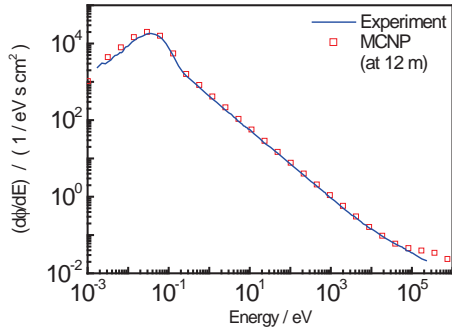
## GELINA: fast and moderated neutron beam

SHIELDING for MODERATED SPECTRUM

SHIELDING for FAST SPECTRUM



## GELINA: neutron fluence moderated beam



- Energy distribution ("white neutron spectrum")

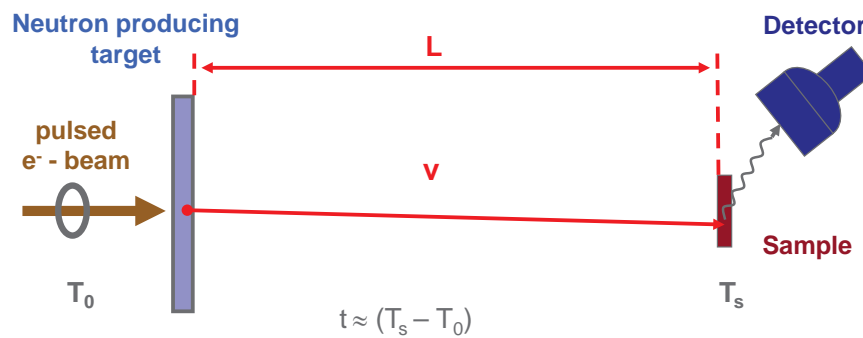
Maxwellian + 1/E

- Isotropic emission

$$\phi(L) \propto \frac{1}{L^2}$$



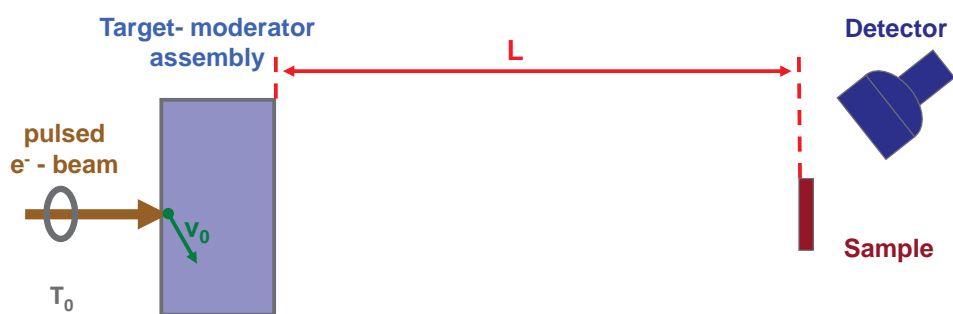
## Time-of-flight measurement



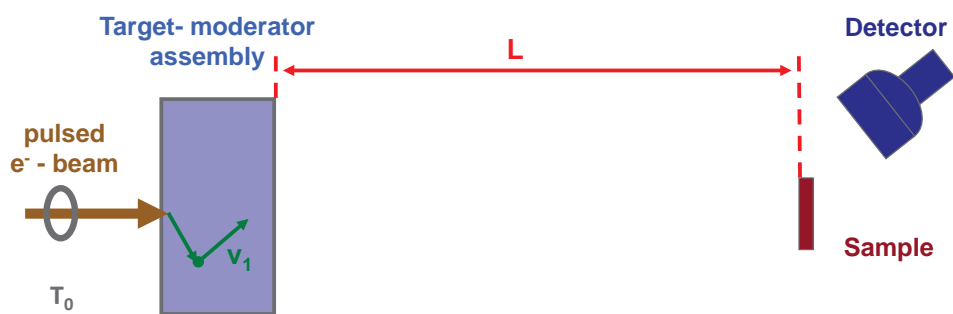
$$v = \frac{L}{t} \quad \Rightarrow \quad E = mc^2(\gamma - 1) \cong \frac{1}{2}mv^2$$



## Time-of-flight measurement



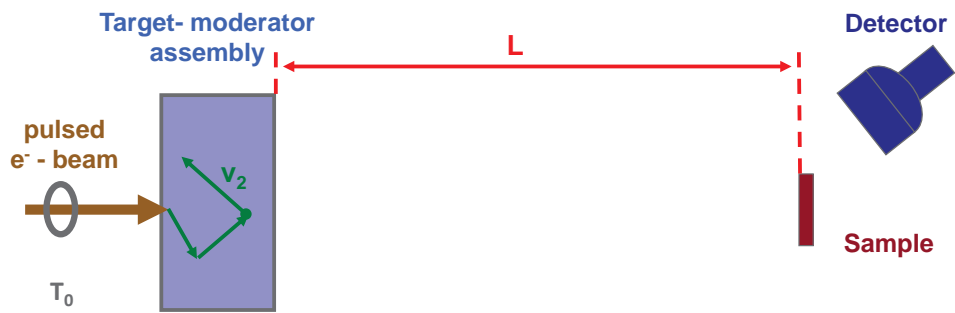
## Time-of-flight measurement



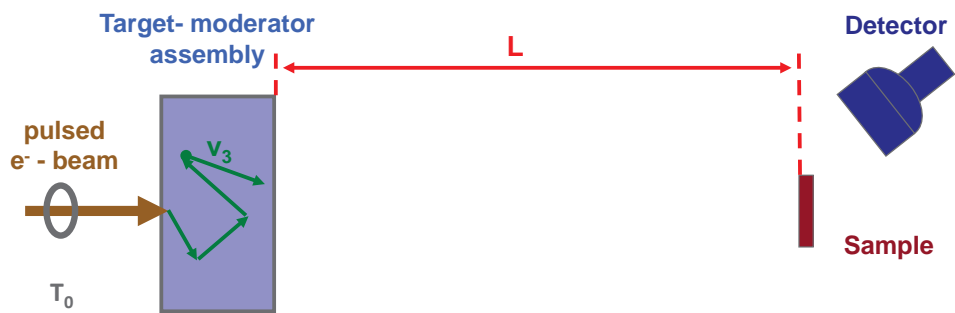
$E$  kinetic energy before scattering  
 $E'$  kinetic energy after H(n,n)H scattering  
 $E'_{max} = E$   
 $\langle E' \rangle = \frac{E}{2}$



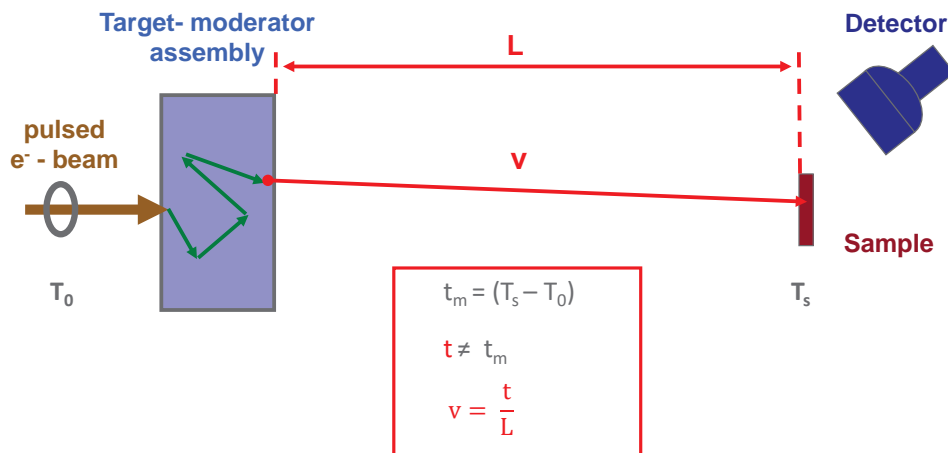
## Time-of-flight measurement



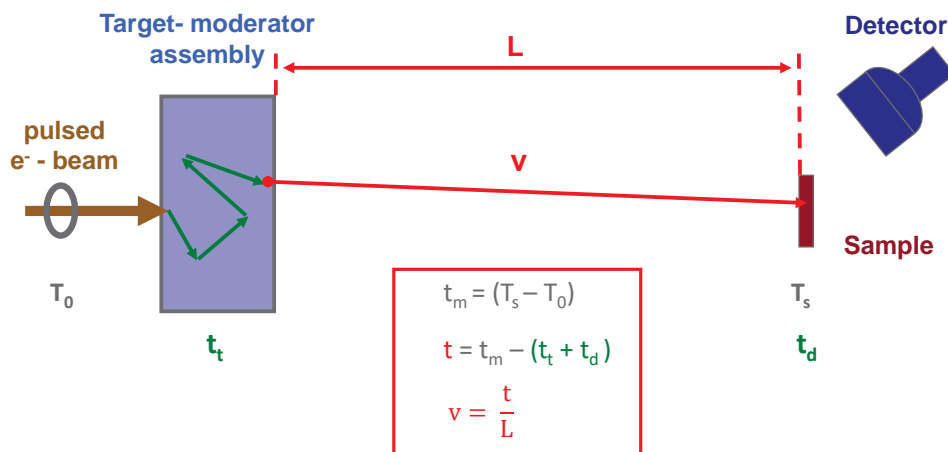
## Time-of-flight measurement



## Time-of-flight measurement



## Time-of-flight measurement





## Response of time-of-flight spectrometer

$$v = \frac{t}{L} \quad \Rightarrow E = m^2(\gamma - 1) \cong \frac{1}{2}mv^2$$

$$\frac{\Delta v}{v} = \sqrt{\frac{\Delta t^2}{t^2} + \frac{\Delta L^2}{L^2}} \quad \Rightarrow E = \gamma(\gamma + 1) \frac{\Delta v}{v} \cong 2 \frac{\Delta v}{v}$$

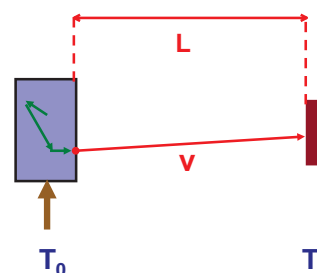
$$\frac{\Delta v}{v} = \frac{1}{L} \sqrt{v^2 \Delta t^2 + \Delta L^2}$$

- $\Delta L$  :  $\sim 1$  mm, independent of  $v$  (or  $E$ )
- $\Delta t$  :
  - Start pulse (GELINA:  $\Delta T_0 \approx 2$  ns)  $\Delta T_0$
  - Time jitter detector & electronics  $\Delta T_s$

$\Rightarrow$  Mostly lumped into one component

Gaussian distribution (depending on start pulse structure)

Independent of  $E$  (neutron energy or velocity)



$$t_m = (T_s - T_0)$$

$$t = t_m - (t_t + t_d)$$

$$v = \frac{t}{L}$$



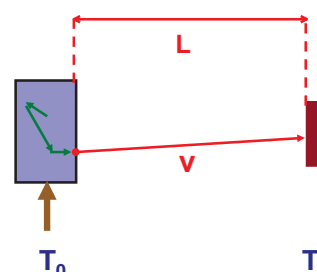
## Response of time-of-flight spectrometer

$$v = \frac{t}{L} \quad \Rightarrow E = m^2(\gamma - 1) \cong \frac{1}{2}mv^2$$

$$\frac{\Delta v}{v} = \sqrt{\frac{\Delta t^2}{t^2} + \frac{\Delta L^2}{L^2}} \quad \Rightarrow E = \gamma(\gamma + 1) \frac{\Delta v}{v} \cong 2 \frac{\Delta v}{v}$$

$$\frac{\Delta v}{v} = \frac{1}{L} \sqrt{v^2 \Delta t^2 + \Delta L^2}$$

- $\Delta L$  :  $\sim 1$  mm, independent of  $v$  (or  $E$ )
- $\Delta t$  :
  - Start pulse (GELINA:  $\Delta T_0 \approx 2$  ns)  $\Delta T_0$
  - Time jitter detector & electronics  $\Delta T_s$
  - Neutron transport in target - moderator  $\Delta t_t$
  - Neutron transport in detector  $\Delta t_d$



$$t_m = (T_s - T_0)$$

$$t = t_m - (t_t + t_d)$$

$$v = \frac{t}{L}$$

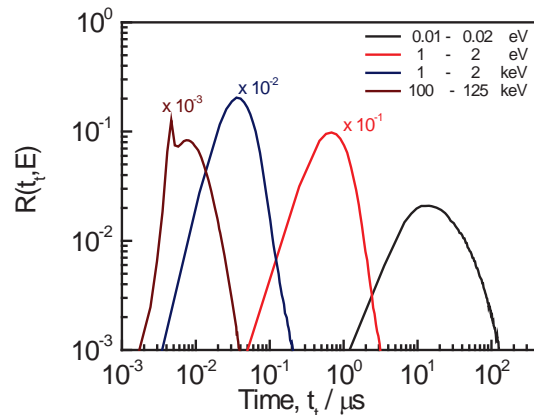


## Probability distribution of $t_t$ for GELINA

$R(t_t, E)$  : TOF-response function

Probability that a neutron escaping from the moderator with an energy  $E$  spends a time  $t_t$  in the target moderator assembly

⇒ strongly depends on neutron energy



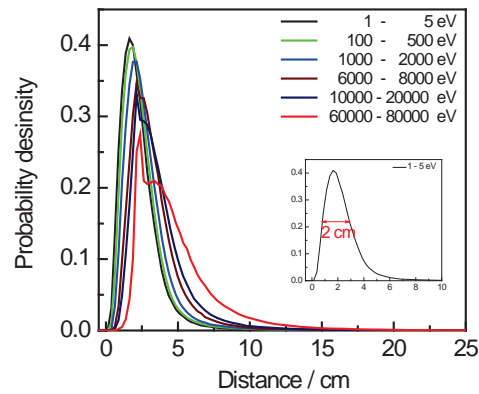
## Probability distribution of $t_t$ for GELINA

$$R(t_t, E) = R'(L_t, E) \left| \frac{dL_t}{dt_t} \right|$$

Transformation of variables :

$$L_t = v t_t$$

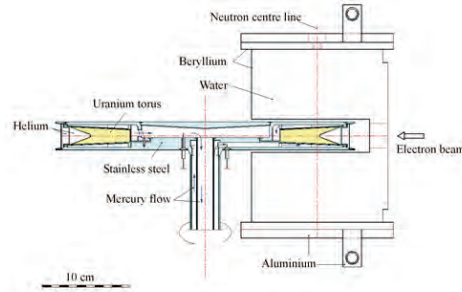
- $L_t$  : equivalent distance
- $v$  : neutron velocity when leaving the moderator
- $t_t$  : time difference between neutron creation and moment it leaves the moderator



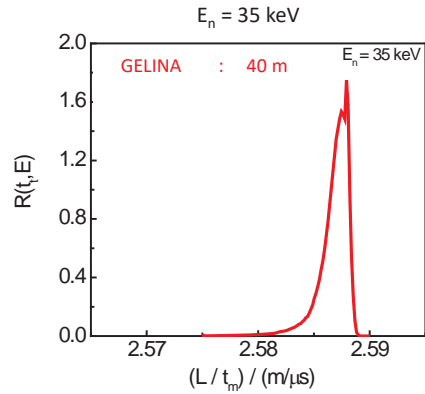
GELINA : FWHM ~ 2 cm



### P( $t_f$ , E) : photonuclear GELINA



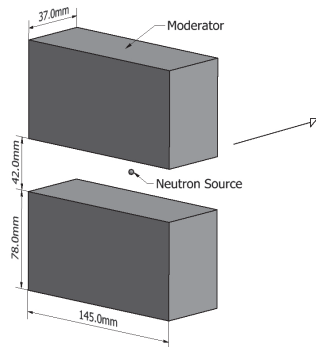
Resolution :  $\Delta L$  (FWHM)  
 GELINA : 2 cm



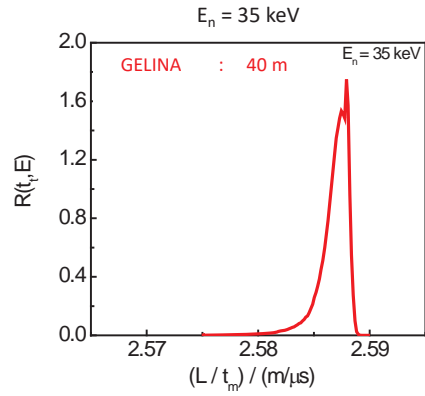
Resolution :  $\Delta L$  (FWHM)  
 GELINA : 2 cm



### P( $t_f$ , E) : photonuclear GELINA



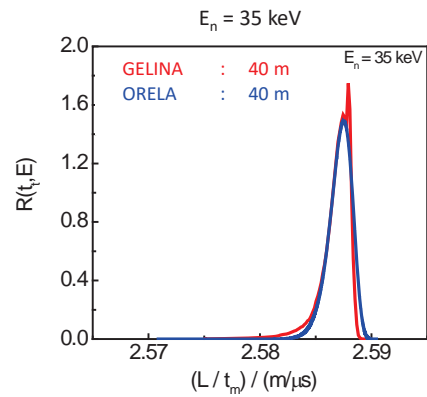
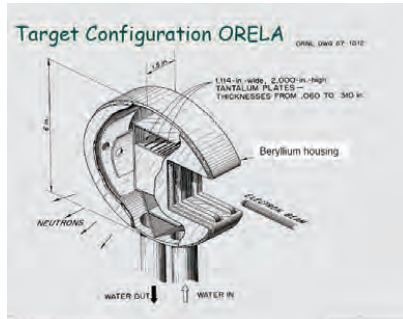
$\Delta L$  (FWHM) = 2 cm  
 $\Rightarrow$  about half of the moderator thickness



Resolution :  $\Delta L$  (FWHM)  
 GELINA : 2 cm



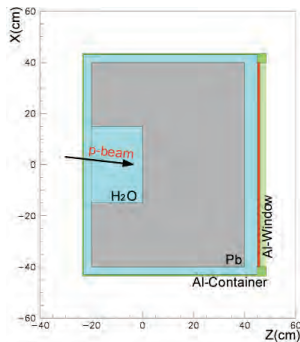
## $P(t, E)$ : photonuclear GELINA and ORELA



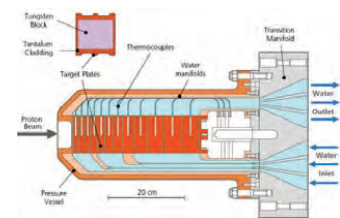
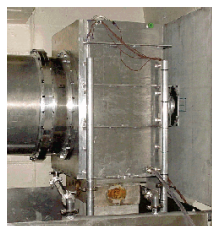
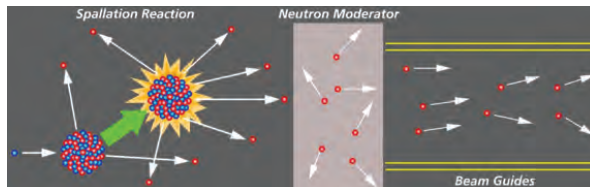
Resolution :  $\Delta L$  (FWHM)  
 GELINA : 2 cm  
 ORELA : 2 cm



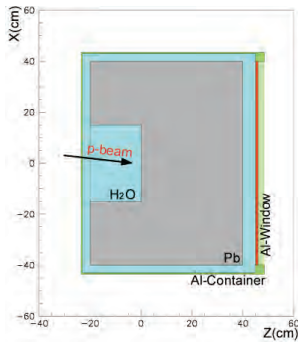
## Neutron production at spallation sources, e.g. n\_TOF, ISIS



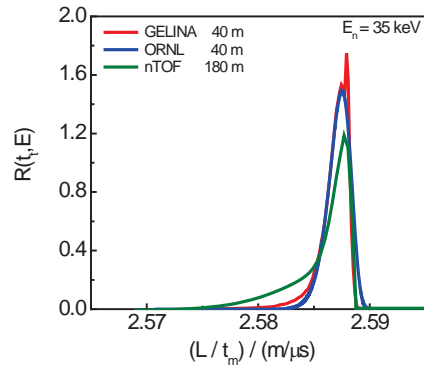
Dimensions :  $80 \times 80 \times 60 \text{ cm}^3$   
 Pure Lead : 4 t  
 H<sub>2</sub>O moderator : 5 cm  
 Al-window : 1.6 mm  
 Al-container : 140 l



## Neutron production at spallation sources, e.g. n\_TOF, ISIS



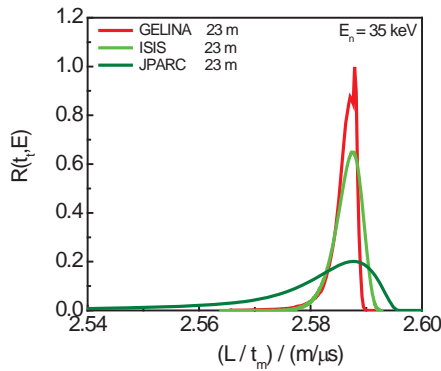
Dimensions :  $80 \times 80 \times 60 \text{ cm}^3$   
 Pure Lead : 4 t  
 H<sub>2</sub>O moderator : 5 cm  
 Al-window : 1.6 mm  
 Al-container : 140 l



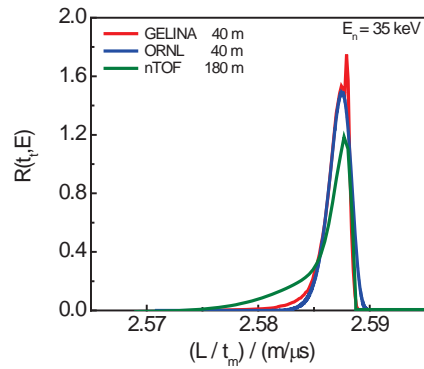
Resolution :  $\Delta L$   
 GELINA : 2 cm  
 ORELA : 2 cm  
 nTOF : 10 cm



## Neutron production at spallation sources, e.g. n\_TOF, ISIS, J-PARC



Resolution :  $\Delta L$   
 ISIS (INES) : 5 cm  
 J-PARC (MLF/ANNRI) : 12 cm  
 Strongly depend on target/moderator configuration (coupled/decoupled)



Resolution :  $\Delta L$   
 GELINA : 2 cm  
 ORELA : 2 cm  
 nTOF : 10 cm



## GELINA - Experimental set-ups

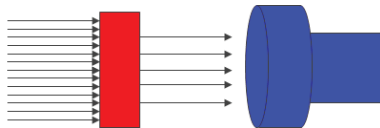


- Transmission
  - 10 m, 30 m, 50 m
- Capture
  - 10 m, 30m, 60 m
- Elastic, in-elastic scattering
  - 30 m
- In-elastic scattering ( $n, n'\gamma$ )
  - 30 m, 100 m
- Fission, ( $n, p$ ), ( $n, \alpha$ ),
  - 10 m

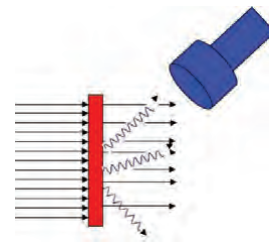


## Cross section measurements

- Transmission measurement



- Reaction cross section measurement



## Transmission measurement

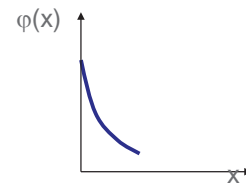
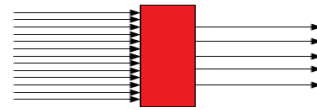
**Transmission:** fraction of the beam traversing a sample without any interaction

Parallel neutron beam, perpendicular to a slab of material : **Lambert-Beer law**

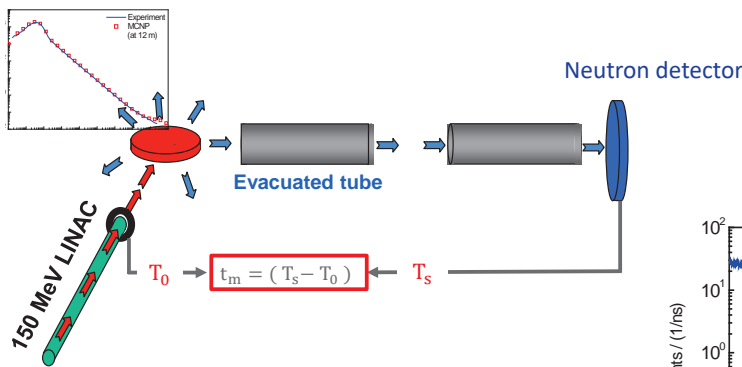
Transmission  
Lambert-Beer law

$$T = \frac{\varphi(d)}{\varphi(0)} = e^{-n \sigma_{tot} d}$$

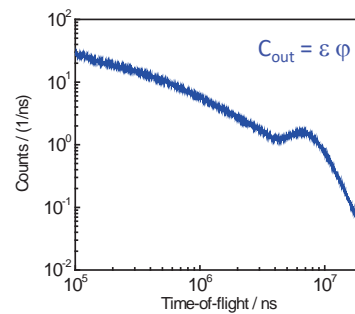
$\sigma_{tot}$ : total cross section  
 $n$  : areal number density  
 total number of atoms per unit area



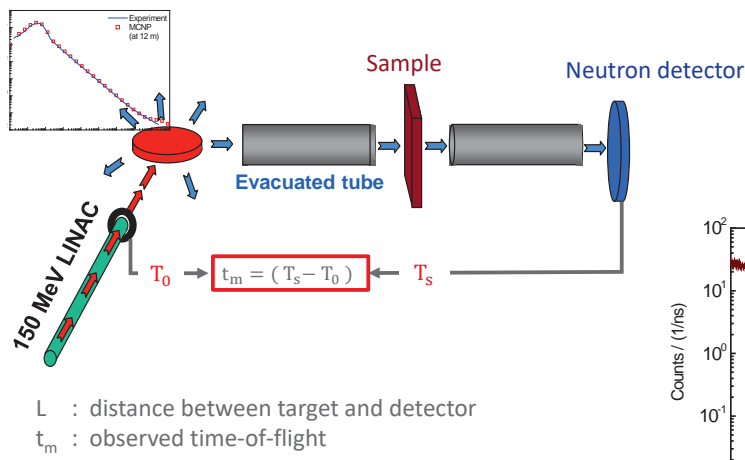
## Transmission measurement



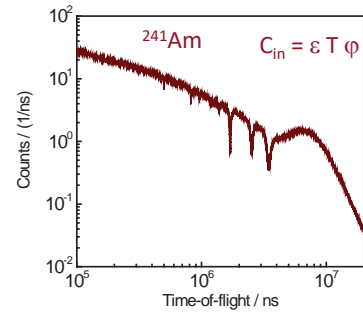
$L$  : distance between target and detector  
 $t_m$  : observed time-of-flight



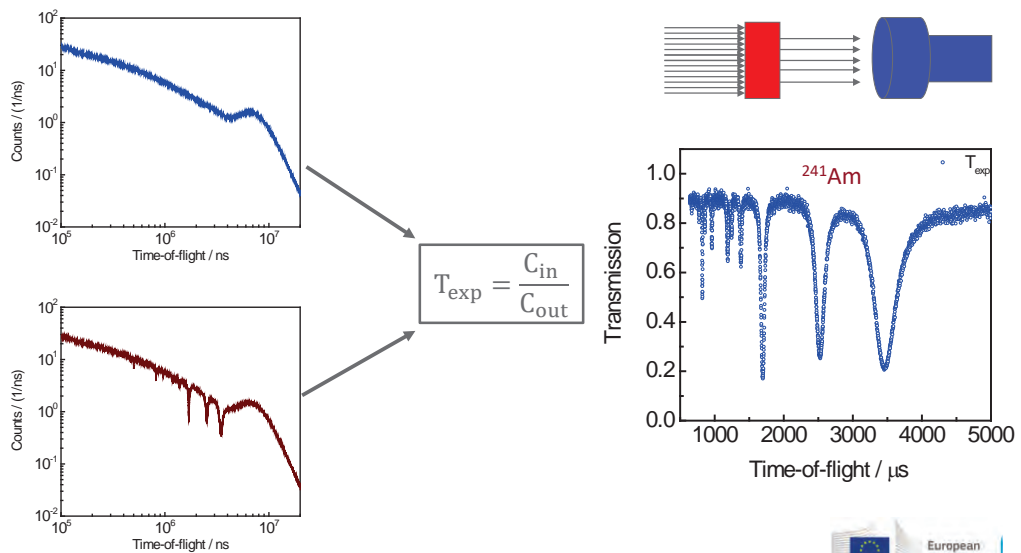
### Transmission measurement



L : distance between target and detector  
 $t_m$  : observed time-of-flight



### Transmission measurement





## Transmission measurement

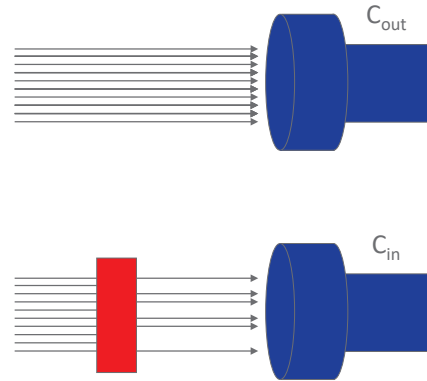
Transmission

$$T_{exp} = \frac{C_{in}}{C_{out}} \propto e^{-n \sigma_{tot}}$$

- Incoming neutron fluence rate cancels
- Detection efficiency cancels

⇒ Absolute measurement

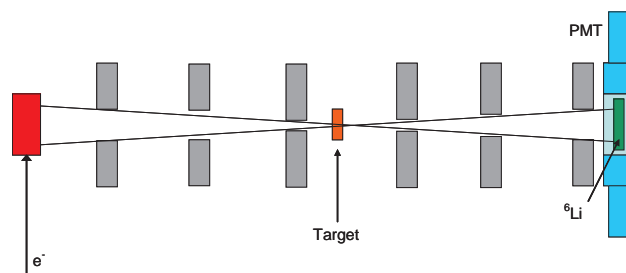
⇒ Direct relation between  $T_{exp}$  and  $\sigma_{tot}$



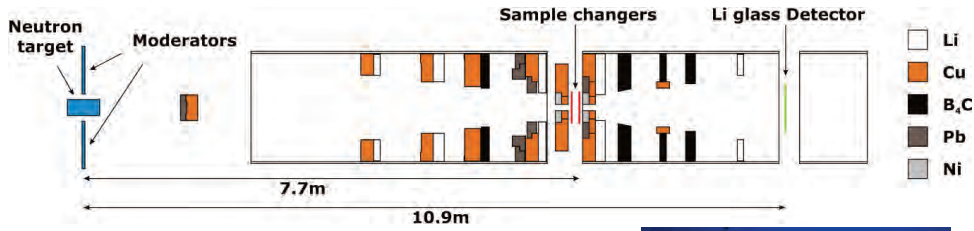
## Transmission: principle

$$T_{exp} = \frac{C_{in}}{C_{out}} \propto e^{-n \sigma_{tot}}$$

- (1) All detected neutrons passed through the sample
- (2) Neutrons scattered in the target do not reach detector
- (3) Sample perpendicular to parallel neutron beam  
⇒ Good transmission geometry (collimation)
- (4) Homogeneous target (no spatial distribution of n)



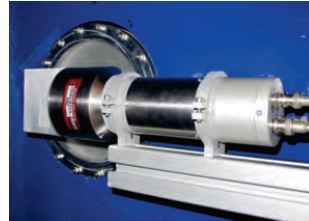
## GELINA – Transmission at 10 m, 25 m and 50 m



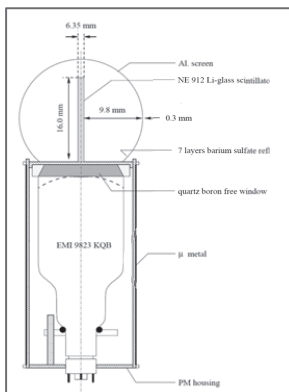
Neutron detectors

Low energy :  ${}^6\text{Li}(n,t)\alpha$   
Li-glass (enriched in  ${}^6\text{Li}$ ) scintillator

High energy :  $\text{H}(n,n)\text{H}$   
Plastic or NE213 type scintillator

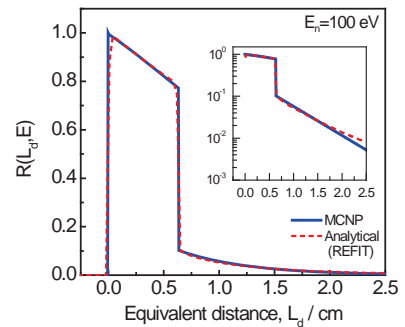
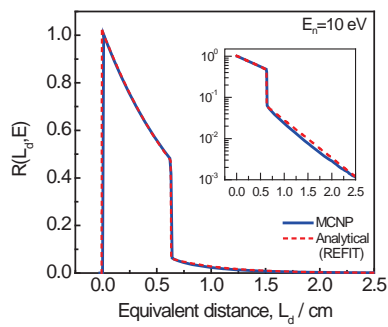


## Neutron detector: TOF-response, equivalent distance



Detector thickness 6.35 mm!

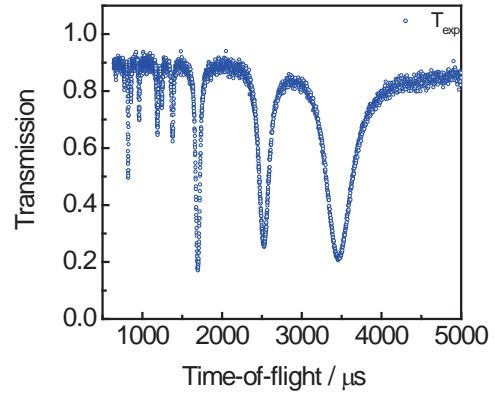
Sensitive to  $\gamma$ -rays



### Transmission: resonance parameters for $^{241}\text{Am} + n$

$$T_{\text{exp}} = N \frac{C_{\text{in}} - B_{\text{in}}}{C_{\text{out}} - B_{\text{out}}} \quad \frac{u_{T_{\text{exp}}}}{T_{\text{exp}}} \leq 0.25\%$$

- ⇒ absolute measurement
- ⇒ no calibration measurement required



### Transmission: resonance parameters for $^{241}\text{Am} + n$

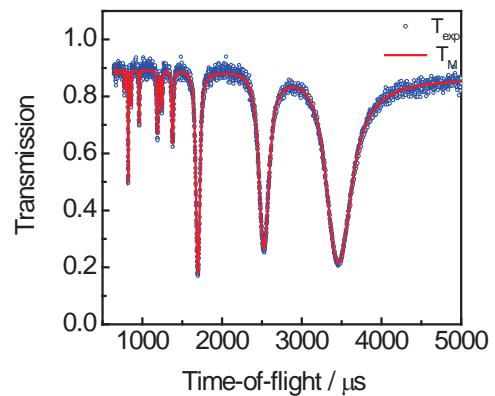
$$T_{\text{exp}} = N \frac{C_{\text{in}} - B_{\text{in}}}{C_{\text{out}} - B_{\text{out}}} \quad \frac{u_{T_{\text{exp}}}}{T_{\text{exp}}} \leq 0.25\%$$

- ⇒ absolute measurement
- ⇒ no calibration measurement required

$$T_M(t_m) = \int R(t_m, E) e^{-n \bar{\sigma}_{\text{tot}}(E_n)} dE_n$$

- $R(t_m, E)$  : response of TOF-spectrometer + detector
- $\bar{\sigma}_{\text{tot}}$  : Doppler broadened total cross section
- $n$  : areal number density  
total number of atoms per unit area

$$\chi^2(\mathbf{RP}) = (T_{\text{exp}} - T_M)^T V_{T_{\text{exp}}}^{-1} (T_{\text{exp}} - T_M)$$



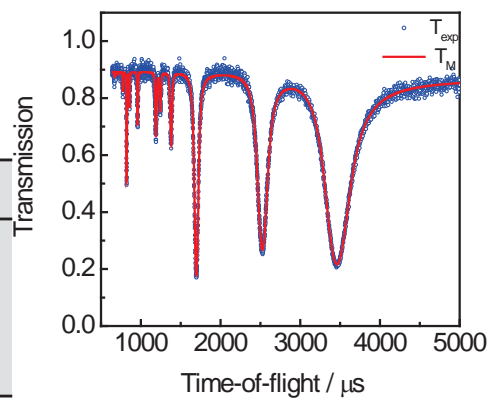
### Transmission: resonance parameters for $^{241}\text{Am} + n$

$$T_{\text{exp}} = N \frac{C_{\text{in}} - B_{\text{in}}}{C_{\text{out}} - B_{\text{out}}} \quad \frac{u_{T_{\text{exp}}}}{T_{\text{exp}}} \leq 0.25\%$$

- ⇒ absolute measurement
- ⇒ no calibration measurement required

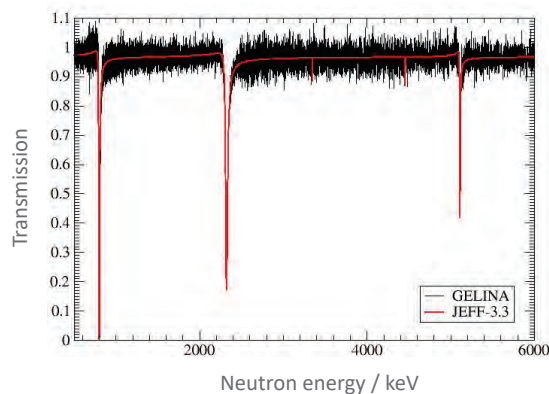
Energy /eV	J/h	g	$g\Gamma_n$ / meV	$\Gamma_\gamma$ / meV
0.306	3	7/12	0.0373 (2)	41.6 (4)
0.574	2	5/12	0.0629 (4)	42.1 (6)
1.271	3	7/12	0.2176 (23)	41.7 (8)

$$\chi^2(\mathbf{RP}) = (T_{\text{exp}} - T_M)^T V_{T_{\text{exp}}}^{-1} (T_{\text{exp}} - T_M)$$



### Improve nuclear data for $^{206}\text{Pb}$ , $^{208}\text{Pb}$ and $^{209}\text{Bi}$ (MYRRHA)

- Transmission measurements at 50 m
  - $^{209}\text{Bi}$
  - $^{206,208,\text{nat}}\text{Pb}$
- Capture measurements at 60 m
  - $^{209}\text{Bi}$



## Reaction cross section measurement

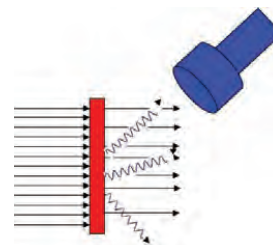
**Reaction yield:** fraction of the beam creating a (n,r) reaction in the sample

Parallel neutron beam, perpendicular to a slab of material : Lambert-Beer law

Reaction yield

$$Y_r \cong (1 - e^{-n \sigma_{\text{tot}}}) \frac{\sigma_r}{\sigma_{\text{tot}}}$$

$$Y_r \approx n \sigma_r \text{ for } n \sigma_r \ll 1$$



$$1 - e^{-n \sigma_{\text{tot}}} \cong 1 - (1 - n \sigma_{\text{tot}}) = n \sigma_{\text{tot}}$$



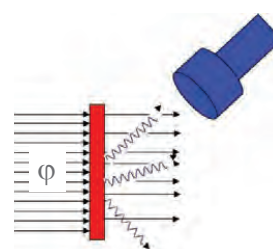
## Reaction cross section measurement

Reaction yield: fraction of the beam creating a (n,r) reaction in the sample

**Experimental response :**

$$C_r = \varepsilon_r Y_r \varphi$$

- $C_r$  experimental response
- $\varphi$  neutron fluence rate
- $Y_r$  reaction yield
- $\varepsilon_r$  overall detection efficiency (including solid angle)



## Cross section measurements

### Transmission

$$T = e^{-n \sigma_{tot}}$$

$$T_{exp} = \frac{C_{in}}{C_{out}}$$

- Absolute measurement
- No additional measurements

+ direct relation:  $T \leftrightarrow \sigma_{tot}$   
 good geometry  
 homogeneous sample

### Reaction

$$Y_r \approx (1 - e^{-n \sigma_{tot}}) \frac{\sigma_r}{\sigma_{tot}}$$

$$Y_{exp} = \frac{C_r}{\epsilon_r \phi}$$

- Detection efficiency
- Fluence rate: additional measurement

+ complex relation:  $Y_r \leftrightarrow \sigma_r$   
 $Y_r = f(\sigma_r, \sigma_{tot} \text{ \& } \sigma_n)$   
 only for  $n\sigma_{tot} \ll 1$ :  $Y_r \cong n \sigma_r$



## Cross section measurements

### Transmission

$$T = e^{-n \sigma_{tot}}$$

$$T_{exp} = \frac{C_{in}}{C_{out}}$$

Transmission most accurate cross section measurement

<sup>10</sup>B(n,α) from transmission:  $\sigma(n_{th}, \alpha) = 3838 (6) \text{ b}$

Axton, Nucl. Sci. Techn. 5 (1984) 609

<sup>197</sup>Au(n,γ) from transmission:  $\sigma(n_{th}, \gamma) = 98.7 (1) \text{ b}$

Dilg et al., Z. Phys. 264 (1973) 427

### Reaction

$$Y_r \approx (1 - e^{-n \sigma_{tot}}) \frac{\sigma_r}{\sigma_{tot}}$$

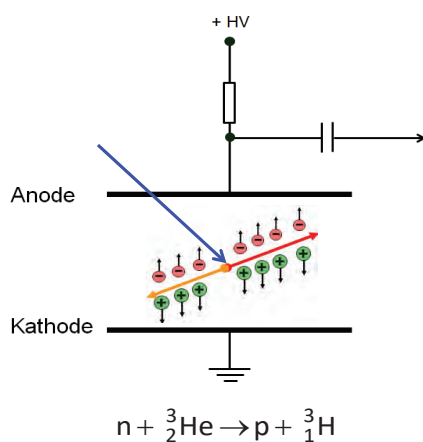
$$Y_{exp} = \frac{C_r}{\epsilon_r \phi}$$

- Detection efficiency
- Fluence rate: additional measurement

+ complex relation:  $Y_r \leftrightarrow \sigma_r$   
 $Y_r = f(\sigma_r, \sigma_{tot} \text{ \& } \sigma_n)$   
 only for  $n\sigma_{tot} \ll 1$ :  $Y_r \cong n \sigma_r$



## Neutron fluence measurements



Neutron: electrical neutral

- No direct ionisation or excitation
- *Transfer reaction is required to transform neutron energy into charged particle energy*

⇒ Transfer reaction required with well-known cross section



## Neutron fluence measurements: standard reactions

**Neutron Cross-section Standards**

Neutron cross section standards are important in the measurement and evaluation of all other neutron reaction cross sections.

Not many cross sections can be defined as absolute - most are measured relative to the cross section standards. The most recent evaluations were completed in 2005 and a report was published in 2007 (STI/PUB/1291). Further information can be found in Nuclear Data Sheets Volume 110, Issue 12, December 2009, Pages 3215-3324.

**Resource Information**

- Quality Level:** Quality-checked by the IAEA Secretariat
- Completeness:** Comprehensive
- Update Frequency:** Static
- Last Resource Update:** 2015
- Subject:** Nuclear Physics
- Organizational Source:** Nuclear Applications
- Data Type:** Nuclear data, cross sections, Standards
- Keywords:** NDS,Contact: Pons@iaea.org
- Contact point:** NATHAN, Bira Nicole; VRAPCENJAK, Lidija; VERPELLI, Marco
- Page Authors:** ZERIN, Viktor

Neutron transfer reactions with an accurate cross section:

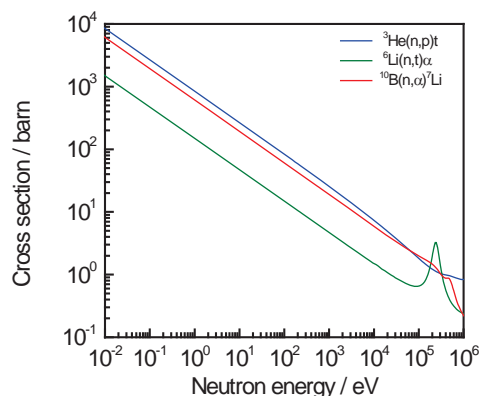
- Neutron standard and reference reactions with recommended cross sections
- <https://www-nds.iaea.org/standards>



## Neutron fluence measurements: standard reactions

Reaction	2200 m/s	Energy region	
		E <sub>low</sub>	E <sub>high</sub>
<sup>1</sup> H(n,n)		1 keV	20 MeV
<sup>3</sup> He(n,p)	X	25.3 meV	50 keV
<sup>6</sup> Li(n,t)	X	25.3 meV	1 MeV
<sup>10</sup> B(n,α)	X	25.3 meV	1 MeV
<sup>10</sup> B(n,α;γ)	X	25.3 meV	1 MeV
<sup>nat</sup> C(n,n)		25.3 meV	1.8 MeV
<sup>197</sup> Au(n,γ)	X	0.2 MeV	2.8 MeV
<sup>235</sup> U(n,f)	X	0.15 MeV	200 MeV (1 GeV)
<sup>238</sup> U(n,f)		2 MeV	200 MeV (1 GeV)
<sup>238</sup> U(n,γ)		150 eV	2.2 MeV
<sup>239</sup> Pu(n,f)		25.3 meV	300 MeV
<sup>209</sup> Bi(n,f)		34 MeV	1 GeV
<sup>nat</sup> Pb(n,f)		34 MeV	1 GeV

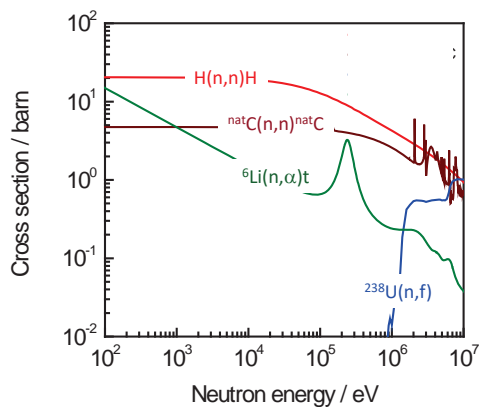
Standard  
Reference



## Neutron fluence measurements: standard reactions

Reaction	2200 m/s	Energy region	
		E <sub>low</sub>	E <sub>high</sub>
<sup>1</sup> H(n,n)		1 keV	20 MeV
<sup>3</sup> He(n,p)	X	25.3 meV	50 keV
<sup>6</sup> Li(n,t)	X	25.3 meV	1 MeV
<sup>10</sup> B(n,α)	X	25.3 meV	1 MeV
<sup>10</sup> B(n,α;γ)	X	25.3 meV	1 MeV
<sup>nat</sup> C(n,n)		25.3 meV	1.8 MeV
<sup>197</sup> Au(n,γ)	X	0.2 MeV	2.8 MeV
<sup>235</sup> U(n,f)	X	0.15 MeV	200 MeV (1 GeV)
<sup>238</sup> U(n,f)		2 MeV	200 MeV (1 GeV)
<sup>238</sup> U(n,γ)		150 eV	2.2 MeV
<sup>239</sup> Pu(n,f)		25.3 meV	300 MeV
<sup>209</sup> Bi(n,f)		34 MeV	1 GeV
<sup>nat</sup> Pb(n,f)		34 MeV	1 GeV

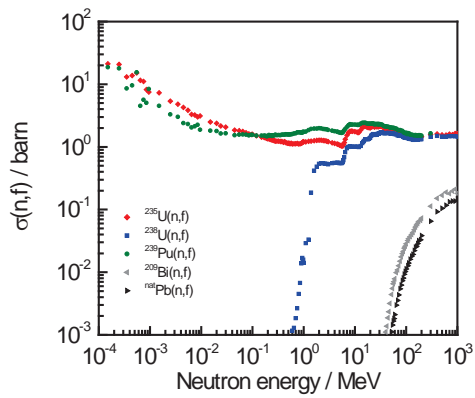
Standard  
Reference





## Neutron fluence measurements: standard reactions

Reaction	2200 m/s	Energy region	
		$E_{low}$	$E_{high}$
$^1\text{H}(n,n)$		1 keV -	20 MeV
$^3\text{He}(n,p)$	X	25.3 meV -	50 keV
$^6\text{Li}(n,t)$	X	25.3 meV -	1 MeV
$^{10}\text{B}(n,\alpha)$	X	25.3 meV -	1 MeV
$^{10}\text{B}(n,\alpha;\gamma)$	X	25.3 meV -	1 MeV
$^{nat}\text{C}(n,n)$		25.3 meV -	1.8 MeV
$^{197}\text{Au}(n,\gamma)$	X	0.2 MeV -	2.8 MeV
$^{235}\text{U}(n,f)$	X	0.15 MeV -	200 MeV (1 GeV)
$^{238}\text{U}(n,f)$		2 MeV -	200 MeV (1 GeV)
$^{238}\text{U}(n,\gamma)$		150 eV -	2.2 MeV
$^{239}\text{Pu}(n,f)$		25.3 meV -	300 MeV
$^{209}\text{Bi}(n,f)$		34 MeV -	1 GeV
$^{nat}\text{Pb}(n,f)$		34 MeV -	1 GeV



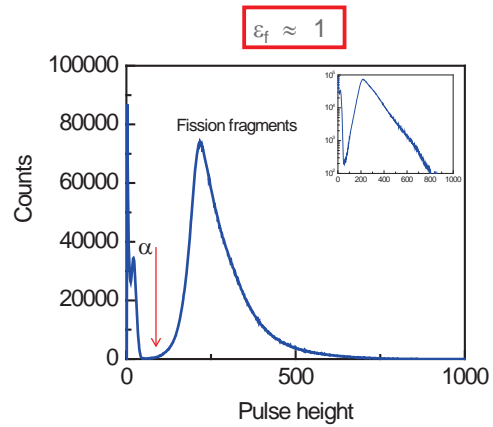
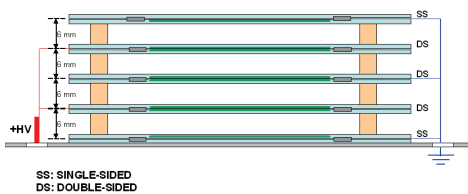
Standard  
Reference



## Neutron fluence measurements

Parallel plate ionisation chamber loaded with  $^{235}\text{U}$

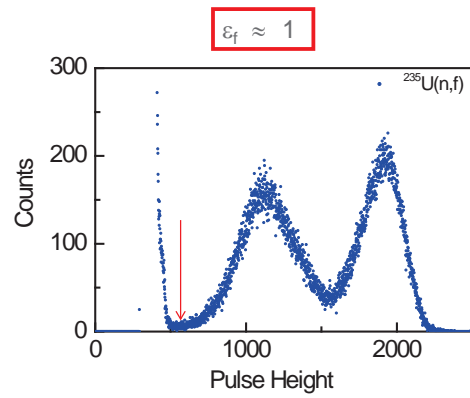
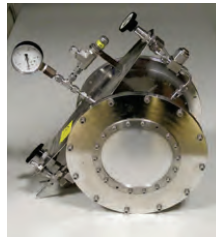
standard reaction:  $^{235}\text{U}(n,f)$



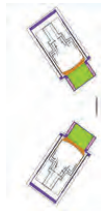
## Neutron fluence measurements

Frisch-gridded ionisation chamber loaded with  $^{235}\text{U}$

standard reaction:  $^{235}\text{U}(n,f)$



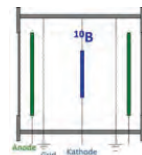
## Reaction cross section measurements



$$C_r = \varepsilon_r \varphi Y_r$$

- $Y$  reaction yield
- $\varphi$  Neutron fluence rate
- $\varepsilon$  Detection efficiency
- $C$  response

$$Y_{r,exp} = \frac{\varepsilon_\varphi C_r}{\varepsilon_r C_\varphi} Y_\varphi$$



$$C_\varphi = \varepsilon_\varphi \varphi Y_\varphi$$



## Reaction cross section measurements

- Absolute measurements
  - all parameters ( $\epsilon_r$ ,  $\epsilon_\phi$ ) have to be determined

$$Y_{r,exp} = \frac{\epsilon_\phi}{\epsilon_r} \frac{C_r}{C_\phi} Y_\phi$$

- Relative measurements based on normalisation factor **N**:
  - accounts for energy independent parameters ( $\epsilon_r$ ,  $\epsilon_\phi$ )
  - determined at energy where  $Y_r$  is accurately defined

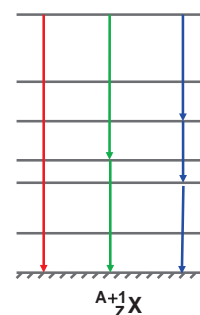
$$Y_{r,exp} = N \frac{C_r}{C_\phi} Y_\phi$$



## Capture cross section measurements

Efficiency to detect capture event  $\epsilon_c$  independent of gamma-ray cascade

- Gamma-ray spectroscopy  
good resolution for  $E_\gamma$  e.g. Ge-detectors
- Total absorption detectors  
 $4\pi$  &  $\epsilon_\gamma \approx 100\%$  e.g. BaF<sub>2</sub>
- Total energy detection principle  
 $\epsilon_\gamma \propto E_\gamma$  &  $\epsilon_\gamma \ll 1$  e.g. C<sub>6</sub>D<sub>6</sub> scintillators



$$\Rightarrow \epsilon_c = k \sum_i E_{\gamma,i} = k(S_n + E_n \frac{A}{1+A})$$

Schillebeeckx et al., Nuclear Data Sheets 113 (2012) 3054



## GELINA – (n,γ) at 12.5 m and 60 m

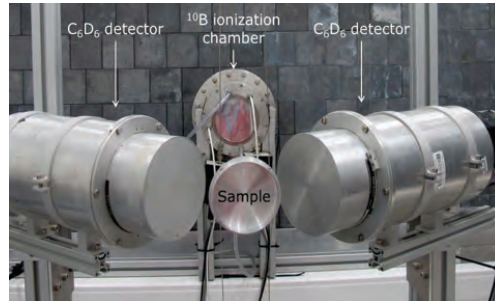
- Total energy detection principle
  - C<sub>6</sub>D<sub>6</sub> liquid scintillators (Boron free quartz window!)
  - 125°
  - Pulse Height Weighting Technique

$$C_w = \int C_c(E_d) WF(E_d) dE_d$$

$$\epsilon_\gamma \propto E_\gamma \Rightarrow \epsilon_c \propto S_n + E_n \frac{A}{1+A}$$

- Fluence rate measurements (IC)

- <sup>10</sup>B(n,α)
- <sup>235</sup>U(n,f)



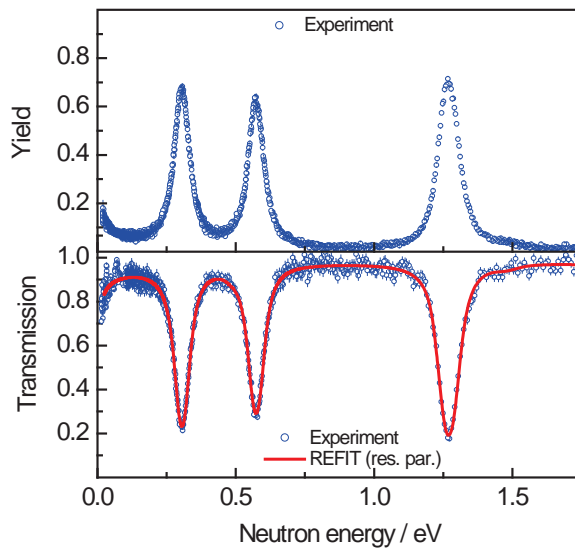
$$Y_{exp} = N \frac{C_w - B_w}{C_\phi - B_\phi} Y_\phi$$



Borella et al., NIMA 577 (2007) 626



## <sup>241</sup>Am + n in RRR

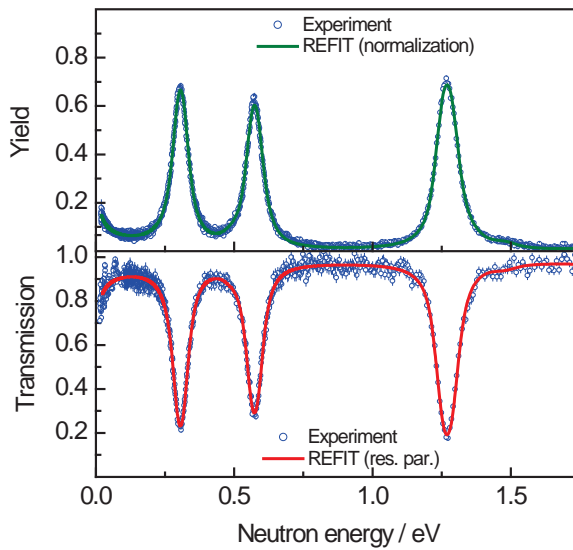


**No reference cross section required**

Energy / eV	J/ħ	g	gΓ <sub>n</sub> /meV	Γ <sub>γ</sub> /meV
0.306	3	7/12	0.0373 (2)	41.6 (4)
0.574	2	5/12	0.0629 (4)	42.1 (6)
1.271	3	7/12	0.2176 (23)	41.7 (8)



### $^{241}\text{Am} + n$ in RRR



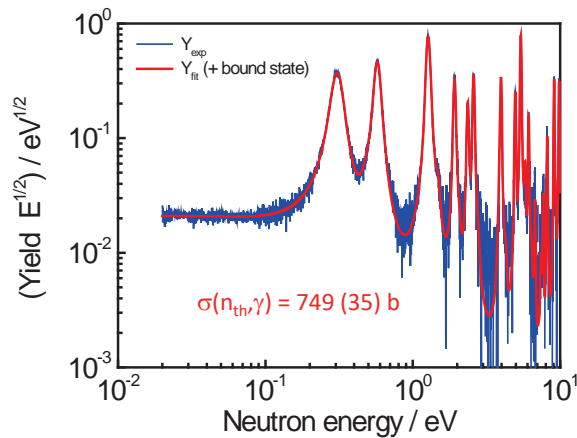
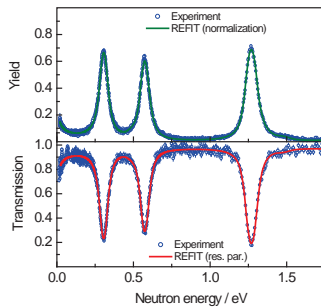
$N = 1.00 (2)$

No reference cross section required

Energy / eV	$J/\hbar$	$g$	$g\Gamma_n/\text{meV}$	$\Gamma_\gamma/\text{meV}$
0.306	3	7/12	0.0373 (2)	41.6 (4)
0.574	2	5/12	0.0629 (4)	42.1 (6)
1.271	3	7/12	0.2176 (23)	41.7 (8)



### $^{241}\text{Am} + n$ in RRR



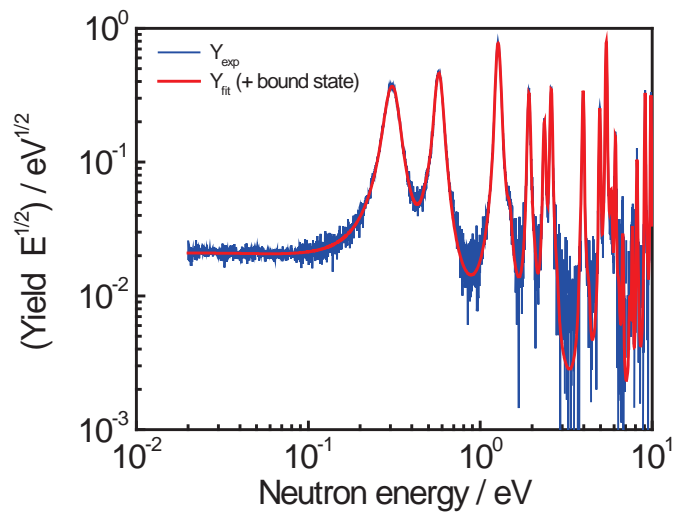
This work = 749 (35) b  
 JEFF-3.3 = 752.7 b

JENDL-4.0 = 684.2 b  
 ENDF/B-VIII.0 = 684.2 b

Lampoudis et al., Eur. Phys. J. Plus 128 (2013) 86



<sup>241</sup>Am + n in RRR

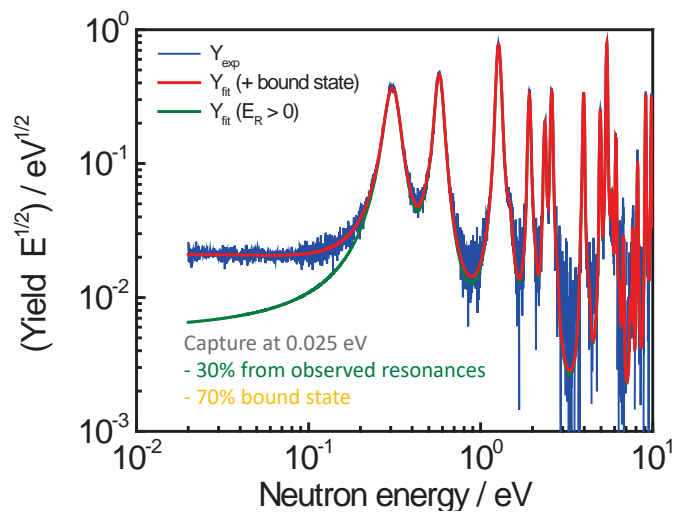


$\sigma(n_{th}, \gamma) = 749 (35) \text{ b}$

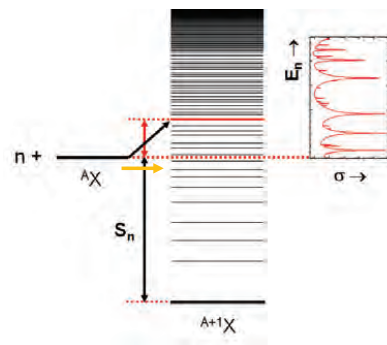
Lampoudis et al., Eur. Phys. J. Plus 128 (2013) 86



<sup>241</sup>Am + n in RRR



$\sigma(n_{th}, \gamma) = 749 (35) \text{ b}$



Lampoudis et al., Eur. Phys. J. Plus 128 (2013) 86



## GELINA: resonance parameters for $^{107,109}\text{Ag} + n$ (BUC)

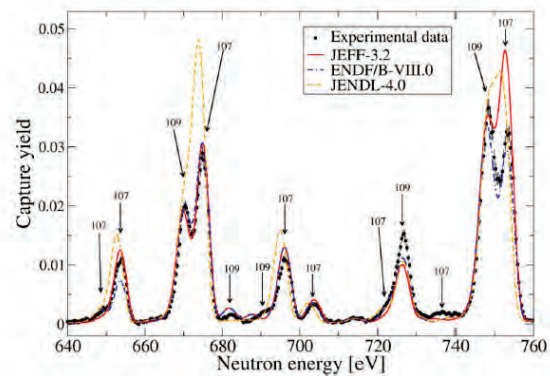
Collaboration CEA (FR)

- Experiments at GELINA
  - Transmission (T) measurements at 10 m
  - Capture (C) measurements at 12.5 m

- Metallic discs of  $^{\text{nat}}\text{Ag}$

Thickness

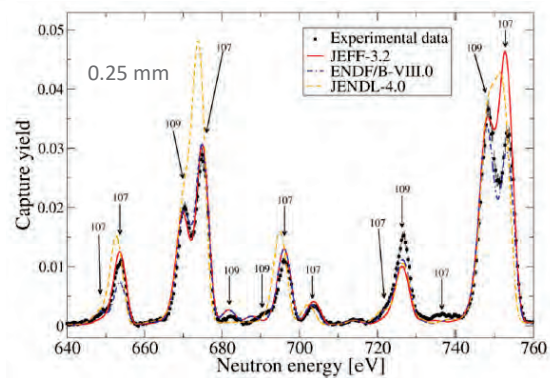
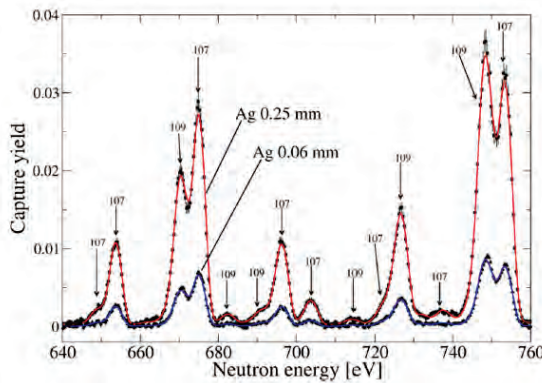
- 0.06 mm T, C
- 0.126 mm T, C
- 0.25 mm T, C
- 0.5 mm T, C



Šalamon et al., Nucl. Instr. Meth. B446 (2019) 19



## GELINA: resonance parameters for $^{107,109}\text{Ag} + n$ (BUC)



⇒ Improved RP file for  $^{107,109}\text{Ag} + n$

E [eV]	l	J <sup>π</sup>	gΓ <sub>n</sub> [meV]	Γ <sub>γ</sub> [meV]
5.195 (1)	0	1 <sup>-</sup>	9.928 (9)	130.3 (2)
30.565 (1)	0	1 <sup>-</sup>	5.533 (9)	125.5 (5)
40.342 (1)	0	1 <sup>-</sup>	3.568 (8)	139.7 (9)
55.81 (1)	0	0 <sup>-</sup>	9.02 (3)	131 (1)
71.06 (1)	0	1 <sup>-</sup>	20.61 (7)	130.0 (9)
87.69 (1)	0	1 <sup>-</sup>	4.44 (2)	128 (2)

Šalamon et al., Nucl. Instr. Meth. B446 (2019) 19



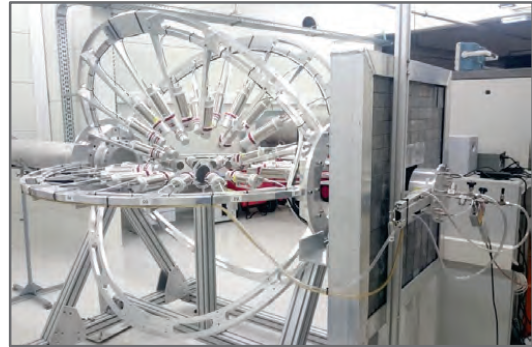
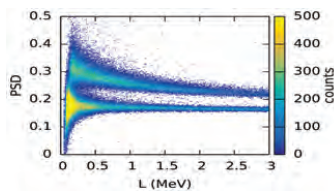


## GELINA – ELISA (Elastic and inelastic scattering array)

(n,n) and (n,n' $\gamma$ ) cross sections at L = 30m  
 Collaboration PTB (GE)

e.g. <sup>nat</sup>Fe(n,n)  
 Pirovano et al. Phys. Rev. C 99 (2019) 024601

- Neutron and  $\gamma$ -ray detection by
  - 16 EJ301 (NE213 equivalent)
  - 16 EJ315 (C<sub>6</sub>D<sub>6</sub> based)
- (n/ $\gamma$ ) pulse shape discrimination
- Fluence rate measurements (IC) : <sup>235</sup>U(n,f)



More info:  
 Georgios Gkatis (PhD)  
 Andreea Oprea

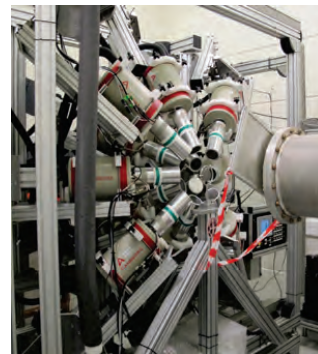
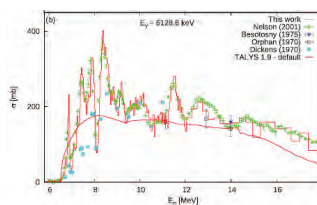
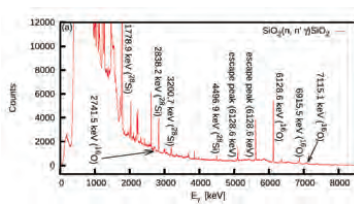


## GELINA – GAINS (Gamma Array for Inelastic Neutron Scattering)

(n,n' $\gamma$ ):  $\gamma$ -ray production cross sections at L = 100 m  
 Collaboration IFIN-HH (RO)

e.g. <sup>16</sup>O(n,n' $\gamma$ ) and <sup>28</sup>Si(n,n' $\gamma$ )  
 Boromiza et al. Phys. Rev. C 101 (2020) 024604

- $\gamma$ -ray detection by
  - 12 HPGe detectors at 110°, 125° and 150°
  - Digital acquisition system
- Fluence rate measurements (IC) : <sup>235</sup>U(n,f)



More info:  
 Andreea Oprea



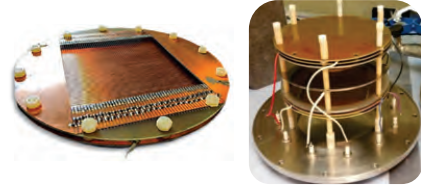


## GELINA – Fission studies

(n,f) cross sections and FF properties and prompt fission neutrons and  $\gamma$ -rays

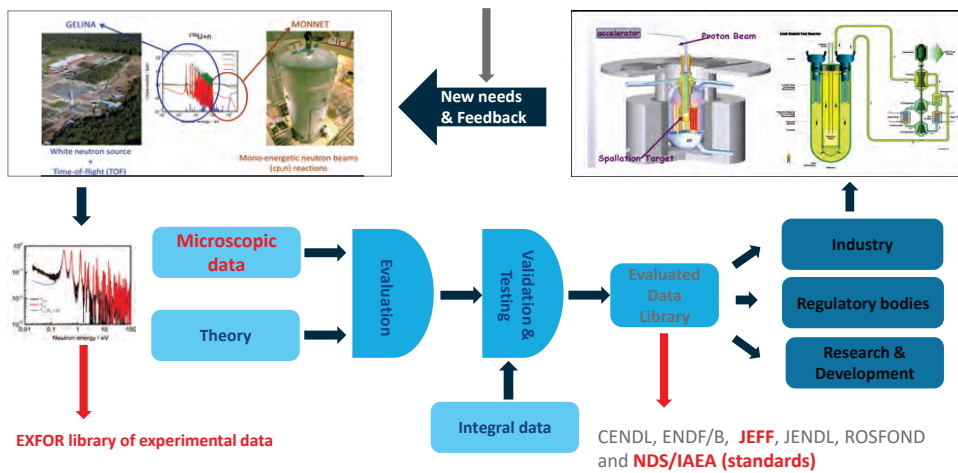
- Fission fragments by Twin Frisch-Gridded IC
  - Fragment energy
  - Fragment masses - 2E-technique
  - Fission axis orientation
- Prompt fission neutrons
  - 12 x Scintillators (NE213 equivalent)
  - Energy : time-of-flight
- Prompt fission  $\gamma$ -rays
  - LaBr, CeBr scintillators

Position sensitive electrode



## Nuclear data libraries for nuclear applications

NEA/OECD High Priority Request List  
IAEA Coordinated Research Projects

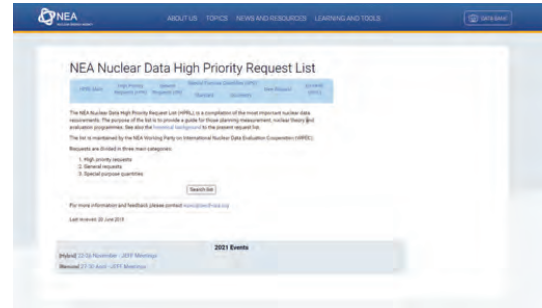


## Nuclear data services: Nuclear Energy Agency (NEA/OECD)

JANIS



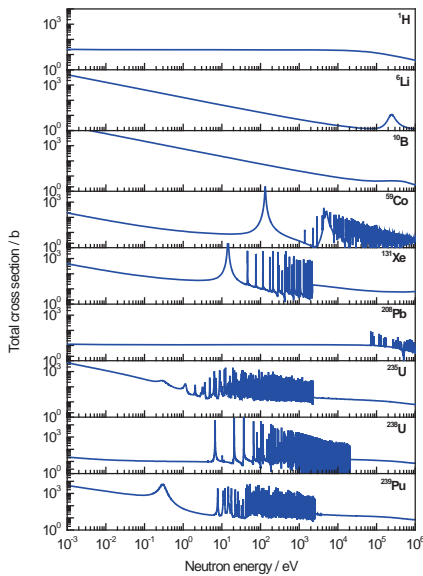
High Priority Request List



<https://www.oecd-nea.org>



## Neutron Resonance Analysis (NRCA & NRTA)



- Resonances appear at energies that are specific for each nuclide
- Position and amplitude of resonances can be used as fingerprints to
  - identify and quantify nuclides
  - elemental & isotopic composition
- Neutron Resonance Capture and Transmission Analysis (NRCA & NRTA)
  - Non-Destructive Analysis (NDA)
  - no sample preparation required
  - sensitive to almost all nuclides (except light)
  - **requirements: TOF-measurements at a white neutron source** (e.g. GELINA, LANSCE, J-PARC, ISIS)

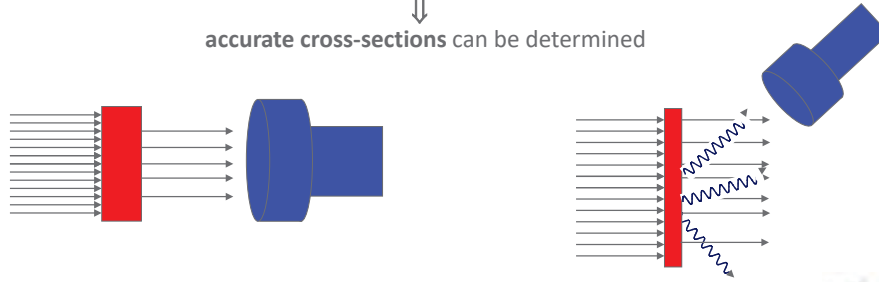


## Cross section measurements

<p><b>Total cross section</b></p> $T \cong e^{-n \sigma_{\text{tot}}}$	<p><b>Capture cross section</b></p> $Y_\gamma \approx (1 - e^{-n \sigma_{\text{tot}}}) \frac{\sigma_\gamma}{\sigma_{\text{tot}}}$
--	---

**Well-characterised (reference) samples**  
 n: total number of atoms per unit area is well-known

↓  
**accurate cross-sections** can be determined



Schillebeeckx et al., Nuclear Data Sheets 113 (2012) 3054

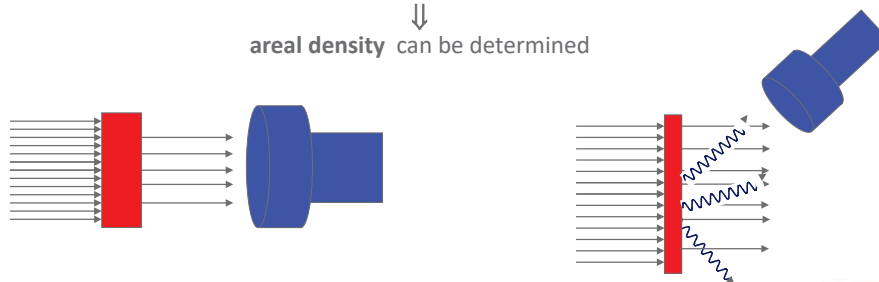


## Neutron resonance analysis (NRTA and NRCA)

<p><b>NRTA</b></p> $T \cong e^{-n \sigma_{\text{tot}}}$	<p><b>NRCA</b></p> $Y_\gamma \approx (1 - e^{-n \sigma_{\text{tot}}}) \frac{\sigma_\gamma}{\sigma_{\text{tot}}}$
---	--

**Well-known cross sections**

↓  
**areal density** can be determined



Schillebeeckx et al., Report EUR 26848-EN (2014)



## Neutron Resonance Analysis

**NRTA**

$$T_{\text{exp}} = \frac{C_{\text{in}}}{C_{\text{out}}}$$

Resonance Shape Analysis: REFIT

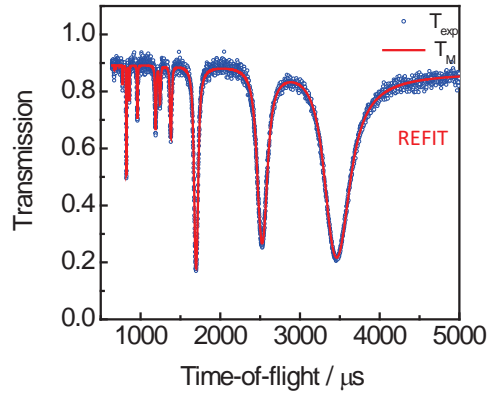
$$\chi^2(\vec{n}) = (T_{\text{exp}} - T_M(t, n))^T V_{T_{\text{exp}}}^{-1} (T_{\text{exp}} - T_M(t, n))$$

$$T_M(t) = \int R(t, E) T(E) dE$$

$$T(E) = e^{-n \sigma_{\text{tot}}(E)}$$

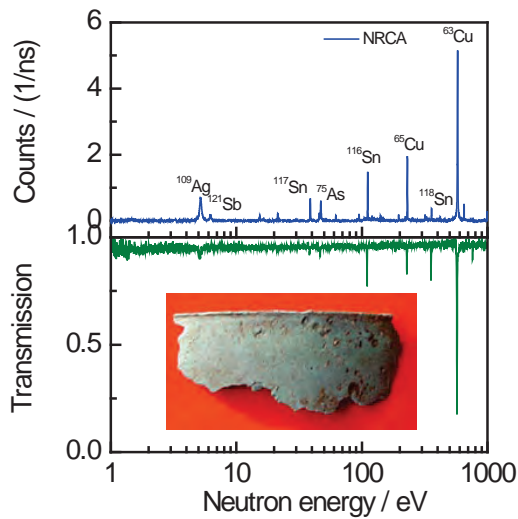
n : areal density

total number of nuclei per unit area



## NRTA and NRCA

Transmission: areal density Cu: 0.55 (2) g/cm<sup>2</sup>



Element	Isotope	E <sub>r</sub> / eV	wt%
Cu	<sup>63</sup> Cu	579.0	77.76 (11)
	<sup>65</sup> Cu	230.0	
Sn	<sup>112</sup> Sn	94.8	20.85 (10)
	<sup>116</sup> Sn	111.2	
	<sup>117</sup> Sn	38.8	
	<sup>118</sup> Sn	45.7	
	<sup>119</sup> Sn	222.6	
	<sup>120</sup> Sn	427.5	
	<sup>124</sup> Sn	62.0	
Fe	<sup>56</sup> Fe	1147.4	0.77 (1)
As	<sup>75</sup> As	47.0	0.34 (1)
Sb	<sup>121</sup> Sb	6.2	0.20 (2)
	<sup>123</sup> Sb	21.4	
Ag	<sup>107</sup> Ag	16.3	0.09 (1)
	<sup>109</sup> Ag	5.2	
In	<sup>115</sup> In	1.46	0.0061 (3)

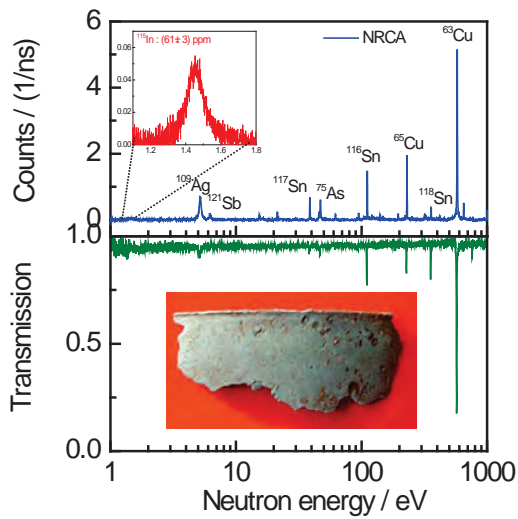
Uncertainties: only counting statistics



H. Postma and P. Schillebeeckx, in Neutron Methods for Archaeology and Cultural Heritage (Springer)

### NRTA and NRCA

Transmission: areal density Cu: 0.55 (2) g/cm<sup>2</sup>



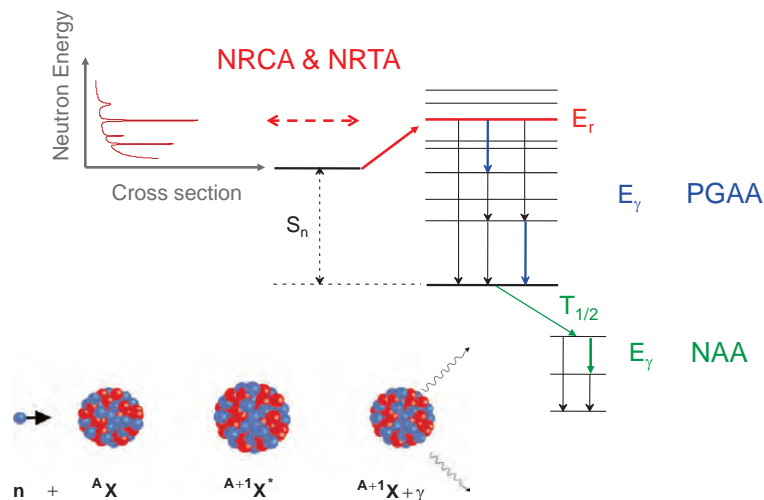
Element	Isotope	E <sub>r</sub> / eV	wt%
Cu	<sup>63</sup> Cu	579.0	77.76 (11)
	<sup>65</sup> Cu	230.0	
Sn	<sup>112</sup> Sn	94.8	20.85 (10)
	<sup>116</sup> Sn	111.2	
	<sup>117</sup> Sn	38.8	
	<sup>118</sup> Sn	45.7	
	<sup>119</sup> Sn	222.6	
	<sup>120</sup> Sn	427.5	
Fe	<sup>56</sup> Fe	1147.4	0.77 (1)
	<sup>75</sup> As	47.0	0.34 (1)
Sb	<sup>121</sup> Sb	6.2	0.20 (2)
	<sup>123</sup> Sb	21.4	
Ag	<sup>107</sup> Ag	16.3	0.09 (1)
	<sup>109</sup> Ag	5.2	
In	<sup>115</sup> In	1.46	0.0061 (3)

Uncertainties: only counting statistics



H. Postma and P. Schillebeeckx, in Neutron Methods for Archaeology and Cultural Heritage (Springer)

### NRA ⇔ NAA & PGAA



## NRA $\Leftrightarrow$ NAA & PGAA

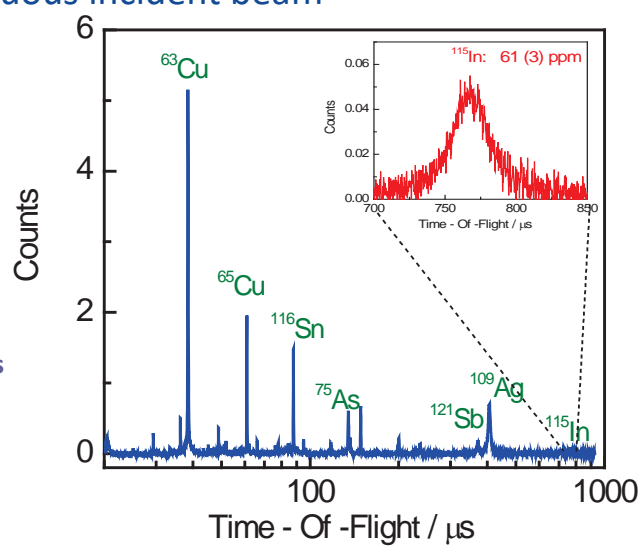
- NRCA & NRTA
  - Pulsed white neutron beam
  - Gamma/Neutron detector: good time resolution  $\Rightarrow$  scintillators
- NAA
  - Intense neutron beam (irradiation in core)
  - Gamma detector:  $\gamma$  - ray energy resolution  $\Rightarrow$  Ge-detectors
- PGNAA
  - Intense neutron beam (mostly cold: Budapest, NIST, FRM-II)
  - Gamma detector:  $\gamma$  - ray energy resolution  $\Rightarrow$  Ge-detectors



## NRCA $\Leftrightarrow$ PGAA at continuous incident beam



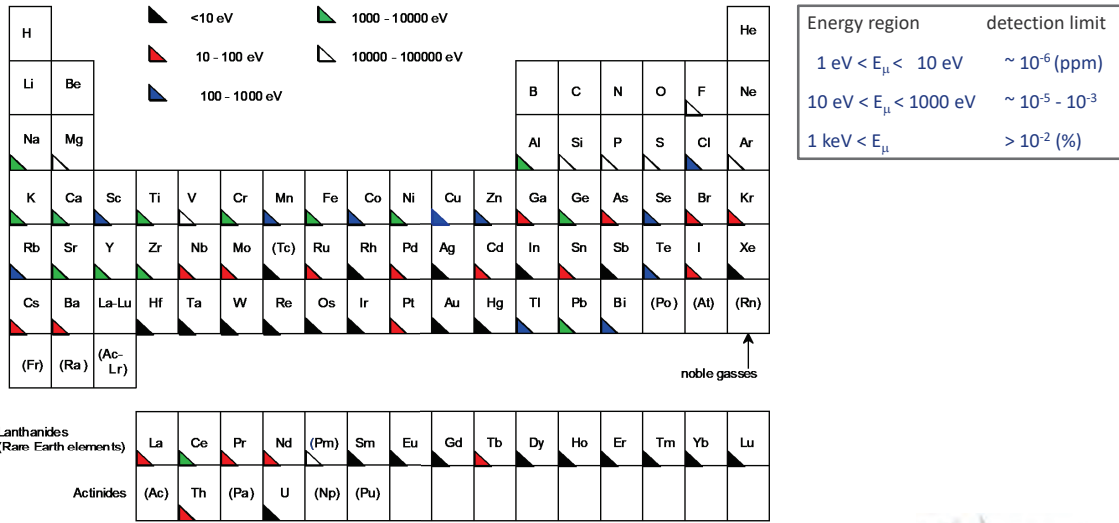
$\Rightarrow$  detection of In is **not hindered** by strong resonances of **other elements** (e.g. Cu)



Postma et al., Czech. J. Phys. 53 (2003) A233



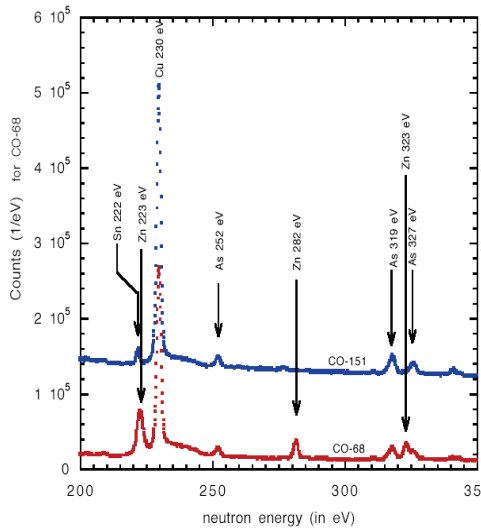
## NRA: which elements can be detected?



H. Postma and P. Schillebeeckx, in Neutron Methods for Archaeology and Cultural Heritage (Springer)



## NRCA: Authenticity of Etruscan artefacts

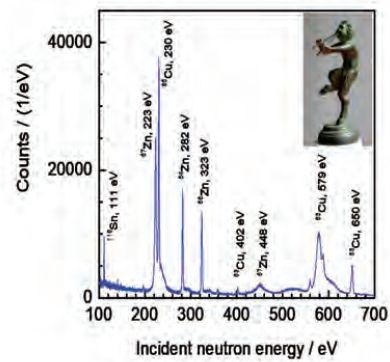
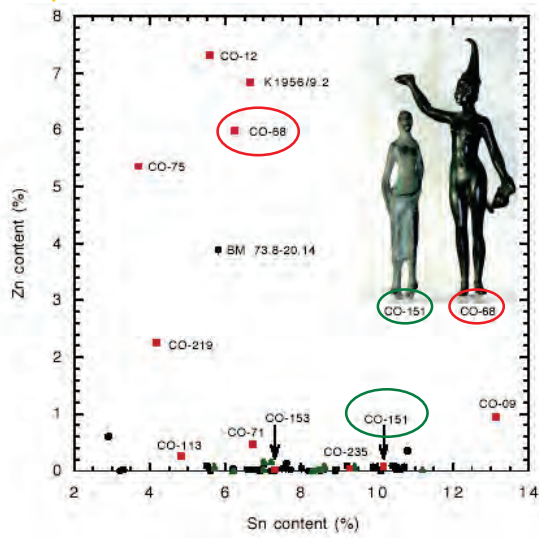


Statuettes from a collection assembled in the 18<sup>th</sup> century by count Corazzi of Cortona (It).  
Now at the National Museum of Antiquities in Leiden (NL).

Postma et al., Archaeometry, 46 (2004) 635



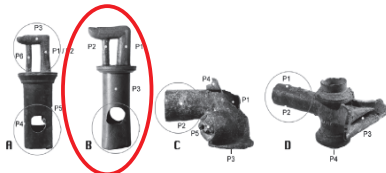
### NRCA: Authenticity of artefacts



NRCA measurements at a 12.5 m station of GELINA of a figurine that is supposed to present the Greek god Pan.  
Zn/Cu ratio: replica

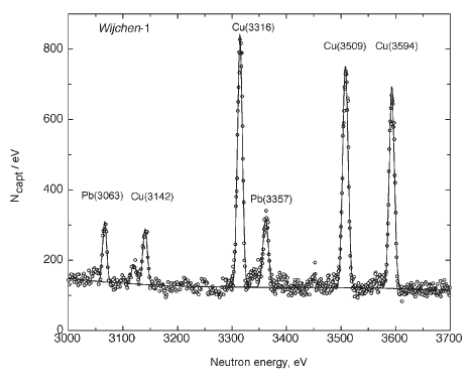


### Roman water taps: NRCA combined with Neutron Diffraction (ND)



NRCA : material composition  
ND : fabrication process

NRCA: 4.8 (5) g/cm<sup>2</sup> Cu



Element weight ratio	NRCA (GELINA)		Neutron diffraction (ISIS)		
			P1	P2	P3
Pb/Cu	0.335	(34)	0.415	0.337	0.402
Sn/Cu	0.0868	(25)	0.094	0.098	0.094
Zn/Cu	0.0036	(3)			
Sb/Cu	0.00167	(3)			
Fe/Cu	0.0012	(3)			
As/Cu	0.00098	(3)			
Ag/Cu	0.00096	(3)			

Schut et al., J. Radioanal. Nucl. Chem. 278 (2008) 151





## NRA for cultural heritage and archaeology

Started in 2000 by a collaboration between Univ. Delft and JRC Geel initiated by **Prof. H. Postma**

### Journal papers

- Postma et al., J. Radioanal. Nucl. Chem. 248 (2001) 115  
 Postma et al., Czech. J. Phys. 53 (2003) A233 – A240  
 Postma et al., Archaeometry, 46 (2004) 635  
 Postma and Schillebeeckx, J. Radioanal. Nucl. Chem. 265 (2005) 297  
 Postma et al., Il Nuovo Cimento, 30C (2007) 105  
 Perego et al., J. Radioanal. Nucl. Chem. 271 (2007) 89  
 Postma et al., J. Radioanal. Nucl. Chem. 271 (2007) 95  
 Schut et al., J. Radioanal. Nucl. Chem. 278 (2008) 151  
 Postma et al., J. Radioanal. Nucl. Chem. 283 (2010) 641  
 Perelli et al., Nucl. Instr. Meth. Phys. Res. A 623 (2010) 693  
 Perelli et al., J. Anal. At. Spectrom. 26 (2011) 992  
 Postma et al., J. Archaeol. Sci. 38 (2011) 1810  
 Schillebeeckx et al., J. Instrumentation, 7 (2012) C03009  
 Postma et al., Analecta Praehistorica Leidensia, 47 (2017) 37



† April 2021



## NRA for cultural heritage and archaeology

Started in 2000 by a collaboration between Univ. Delft and JRC Geel initiated by **Prof. H. Postma**

### Chapters in books

- H. Postma and P. Schillebeeckx, "Neutron resonance capture and transmission analysis"  
 In: Encyclopedia of analytical chemistry (chapter a9070),  
 R.A. Meyers (Ed.), John Wiley & Sons Ltd. (2009)
- H. Postma and P. Schillebeeckx, "Neutron Resonance Analysis"  
 In: Neutron Methods for Archaeology and Cultural Heritage (chapter 12),  
 N. Kardjilov and G. Festa (Eds.), Springer International Publishing Switzerland (2017)
- P. Schillebeeckx and H. Postma, "Neutron resonance analysis (NRA)"  
 In: The SAS Encyclopedia of Archaeological Sciences,  
 S.L. Lopez Varela (Ed.), Wiley –Blackwell (2018)
- P. Schillebeeckx and H. Postma, "Neutron Resonance Analysis methods for archaeological and cultural heritage applications"  
 In: Handbook of Cultural Heritage Analysis (pp. 145 – 187)  
 S. D'Amico and V. Venuti (Eds.), Springer International Publishing Switzerland (2022)

† April 2021

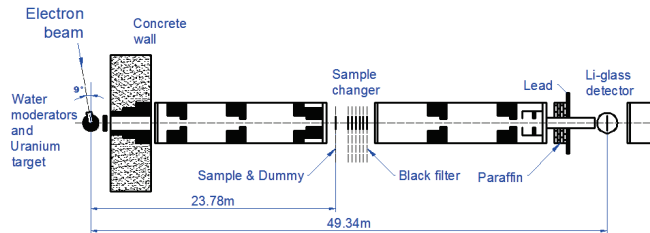


## Characterisation of $PbI_2$ by NRTA at GELINA

- JRC Geel target preparation group extracted:
  - 150 g Iodine (powder) from 210 liter from **reprocessed waste** (Le Hague)
  - (1.3 g/l Iodine and 40 MBq/l)
- Sample characterisation: by mass spectrometry , NAA and **NRTA**



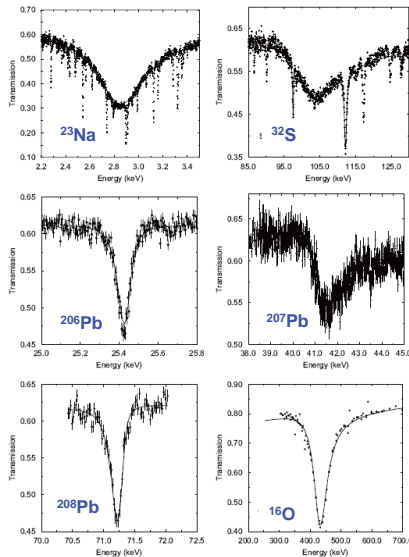
Fig. 3. Addition of  $Pb(NO_3)_2$  to the iodide solution to precipitate lead iodide.



Noguere et al., Nucl. Instr. Meth. Phys. Res. A 575 (2007) 476

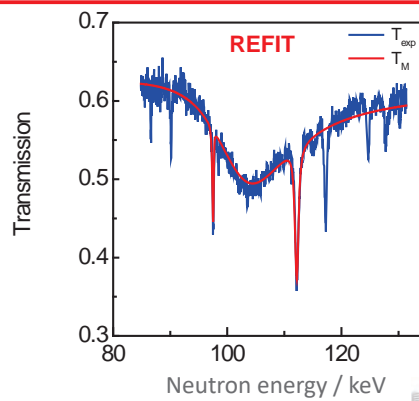


## Characterisation of $PbI_2$ by NRTA at GELINA



$$T_M(t_m, n) = \int R(t_m, E) e^{-n \sigma_{tot}(E)} dE$$

$$\chi^2(n) = (T_{exp} - T_M(t_m, n))^T V_{T_{exp}}^{-1} (T_{exp} - T_M(t_m, n))$$



## NRTA compared with NAA and ICP-MS

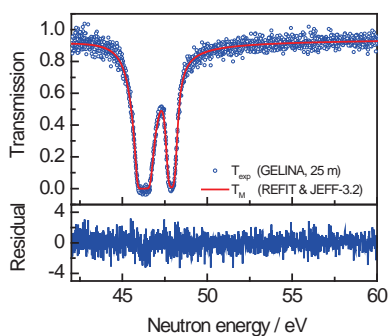
Element		NRTA	NAA	Mass spectrometry (PSI)
Iodine	total	20.24 (41)	19.75 (61)	19.86 (41)
	<sup>127</sup> I	3.44 (5)	3.35 (10)	3.36 (8)
	<sup>129</sup> I	16.80 (40)	16.40 (60)	16.50 (40)
Lead	Total	52.3 (17)	51.1 (1.8)	
	<sup>206</sup> Pb	12.8 (5)		
	<sup>207</sup> Pb	11.5 (1)		
	<sup>208</sup> Pb	27.1 (17)		
Sulfur		5.44 (3)		
Sodium		0.72 (2)		1.0 (2)
Oxygen		13.92 (5)		14.5 (15)
Hydrogen		<0.13		0.020 (2)
Nitrogen				1.2 (4)

NRTA ↔ NAA, ICPMS :

- more elements analysed
- isotopic composition of Pb



## NRTA of W sample: validation of resonance parameters



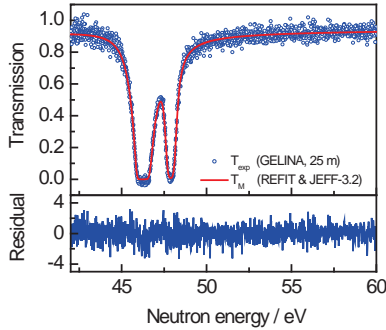
- Sample: metallic disc of <sup>nat</sup>W (1 mm thick)
  - homogeneous sample
  - areal density n : from weight and area  
⇒  $u_n/n < 0.2\%$
- Transmission : absolute measurement
  - absolute measurement
  - methodology well understood (background, dead time correction,...)  
Schillebeeckx et al., Nuclear Data Sheets 113 (2012) 3054 – 3100  
⇒  $u_{T_{exp}}/T_{exp} < 0.3\%$

- ⇒ NRTA: derive  $n_{NRTA}$  from the transmission data and compare with  $n_{REF}$
- ⇒ one of the most accurate benchmark experiments to validate resonance parameters



## NRTA of W sample: validation of resonance parameters

<sup>183</sup>W



Reference	$E_r = 46.26$ eV		$E_r = 47.80$ eV		$n_{NRTA}/n_{REF}$
	$\Gamma_n$ / meV	$\Gamma_\gamma$ / meV	$\Gamma_n$ / meV	$\Gamma_\gamma$ / meV	
Lynn et al. 2002	162 (1)	72	126 (2)	72	0.983 (10)
Mughabghab 1984	140 (4)	77 (8)	108 (10)	78 (10)	1.198 (34)
Mughabghab 2006	162 (2)	77 (8)	122 (2)	78 (10)	0.992 (14)
JEFF-3.2	163.4	75.3	120.8	61.5	1.002 (5)
JENDL-3.3	154.0	46.0	119.0	81.0	1.113 (5)
<b>ENDF/B-VII.1</b>	<b>154.0 (8)</b>	<b>46.0 (21)</b>	<b>119.0 (12)</b>	<b>81.0 (51)</b>	<b>1.113 (11)</b>

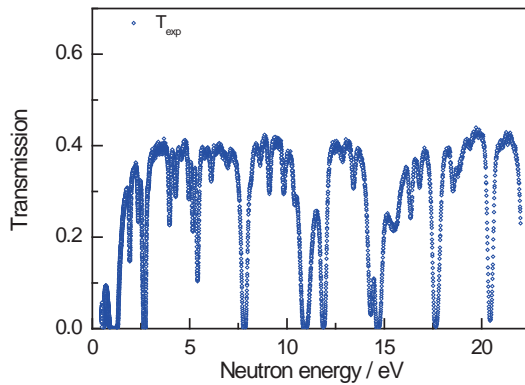
$$\chi^2(n_{NRTA}) = (T_{exp} - T_M)^T V_{T_{exp}}^{-1} (T_{exp} - T_M)$$

⇒ Parameters in ENDF/B-VII.1 (JENDL-3.3) strongly biased and covariance data not reliable

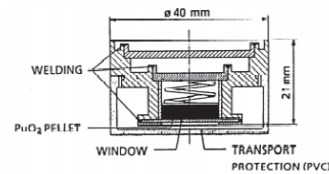
Becker et al., Nuclear Data Sheets 123 (2015) 171



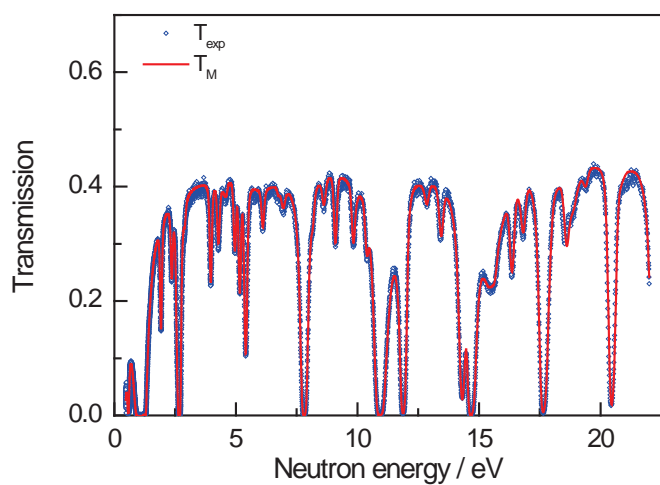
## NRTA of PuO<sub>2</sub> sample: validation of resonance parameters



CBNM - 271



### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



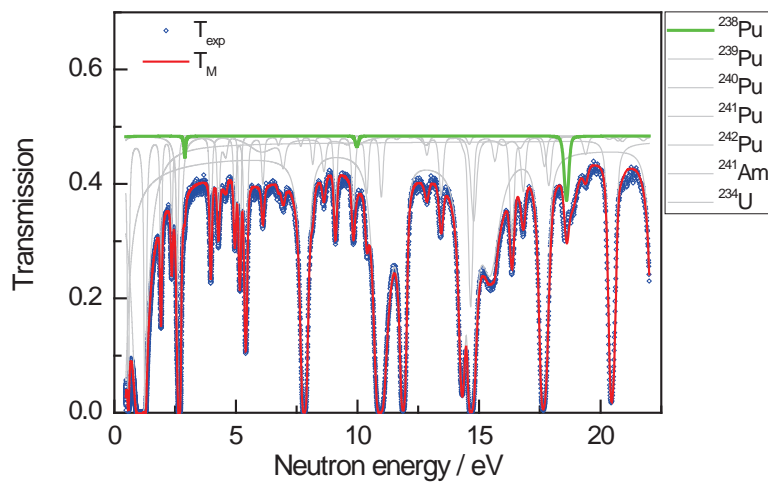
$$T_M(t_m, n) = \int R(t_m, E) e^{-n \sigma_{tot}(E)} dE$$

$$\chi^2(n) = (T_{exp} - T_M(t_m, n))^T V_{T_{exp}}^{-1} (T_{exp} - T_M(t_m, n))$$

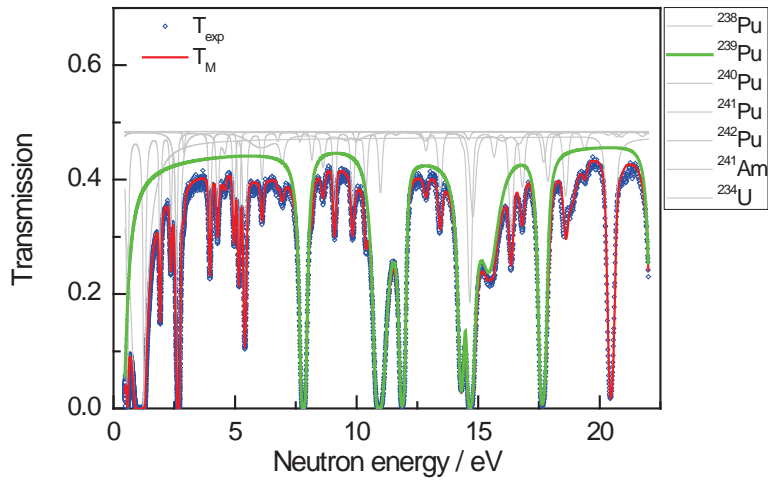
REFIT



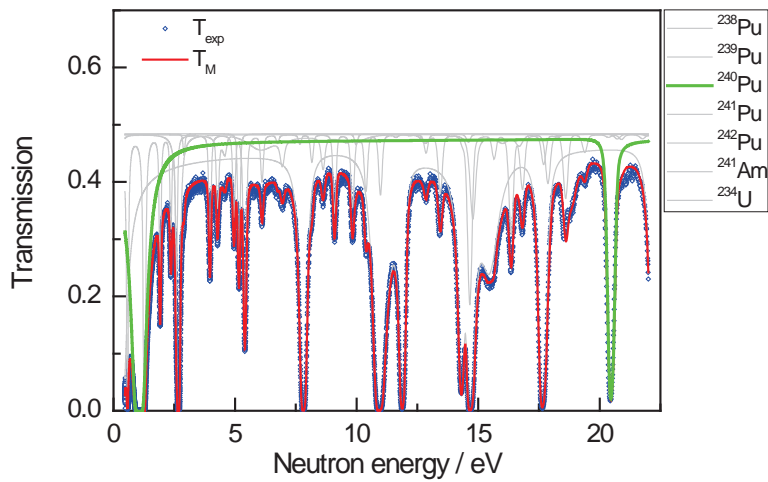
### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



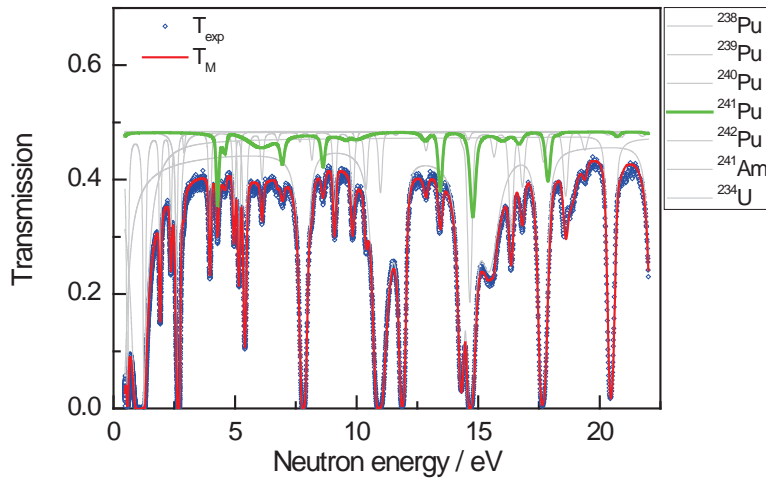
### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



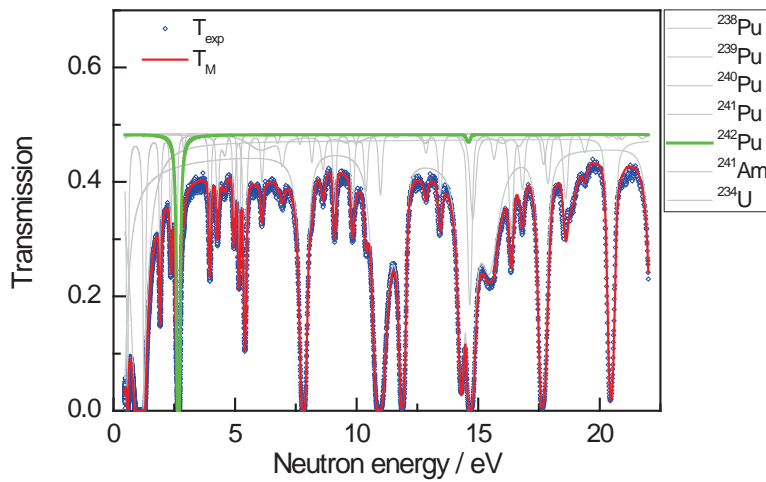
### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



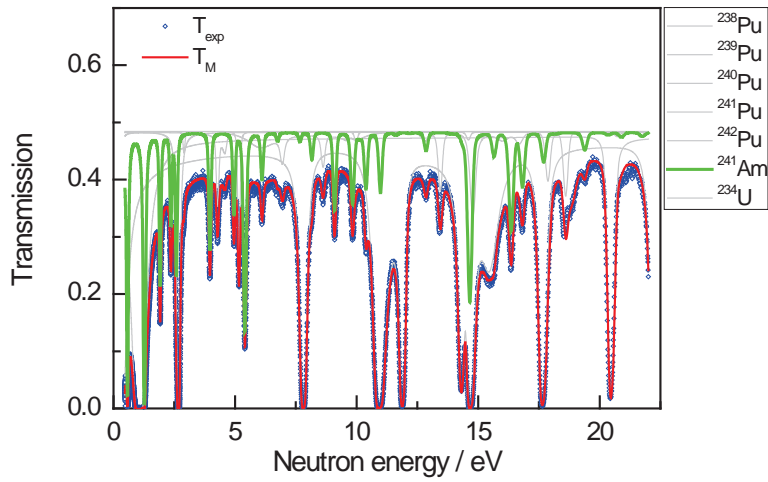
### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



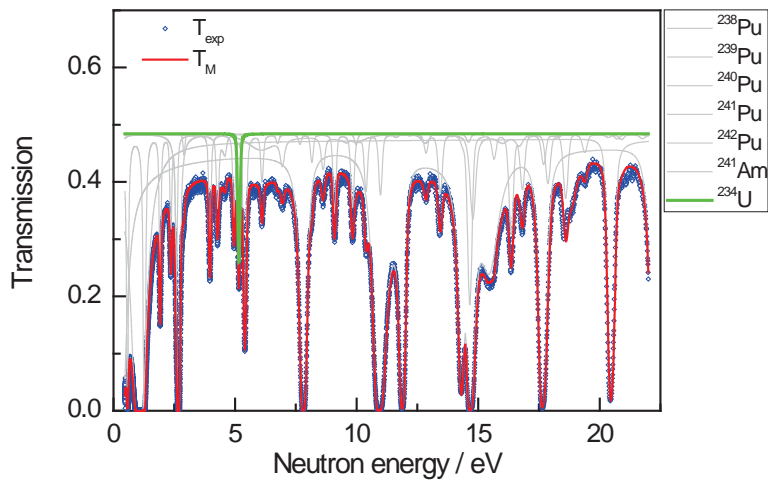
### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)





## NRTA of PuO<sub>2</sub> sample: validation of resonance parameters

Nuclide	n <sub>REF</sub>	n <sub>NRTA</sub>		n <sub>NRTA</sub> / n <sub>REF</sub>	
		ENDF/B-VIII.0	JEFF-3.2	ENDF/B-VIII.0	JEFF-3.2
<sup>238</sup> Pu	0.009514 (20)	0.00783 (70)	0.00898 (70)	0.823 (74)	0.944 (74)
<sup>239</sup> Pu	0.62603 (28)	0.62154 (90)	0.61530 (95)	0.9928 (14)	0.9829 (15)
<sup>240</sup> Pu	0.25273 (24)	0.25699 (36)	0.26240 (32)	1.0169 (14)	1.0383 (13)
<sup>241</sup> Pu	0.015697 (20)	0.01574 (10)	0.01577 (10)	1.0028 (64)	1.0045 (65)
<sup>242</sup> Pu	0.041489 (60)	0.04334 (10)	0.04300 (10)	1.0447 (25)	1.0365 (24)
<sup>241</sup> Am	0.06290 (63)	0.07236 (21)	0.06059 (20)	1.1503 (33)	0.9633 (32)
<sup>234</sup> U	0.002918 (10)	0.00289 (10)	0.00287 (10)	0.989 (34)	0.982 (35)

RP in ENDF/B-VIII.0 for <sup>241</sup>Am are strongly biased:  
 $\sigma(n,\gamma)$  underestimated

n: atomic abundance relative to total Pu  
 NRTA uncertainties only due to counting statistics

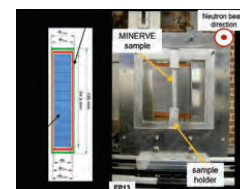


## NRTA: MINERVE samples

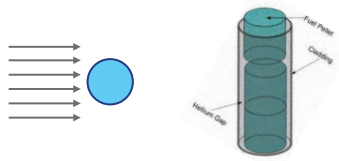
Collaboration with CEA Cadarache

- MAESTRO project: determine data for FP important for BUC applications
  - Production of pellet samples
    - mixture: depleted uranium + material enriched in specific FP
  - Pile oscillator measurements at MINERVE
    - Validate absorption cross sections of FP and determine correction factors
- NRTA of irradiated MINERVE pellet samples at GELINA (part of MAESTRO)
  - Identification and quantification of impurities
  - Validation of resonance parameters of FP

<sup>103</sup>Rh  
<sup>107,109</sup>Ag  
<sup>133</sup>Cs  
<sup>143,145</sup>Nd  
<sup>147,149,152</sup>Sm,  
<sup>151,153</sup>Eu  
<sup>161,162,163,164</sup>Dy  
<sup>168,170</sup>Er  
<sup>180</sup>Hf

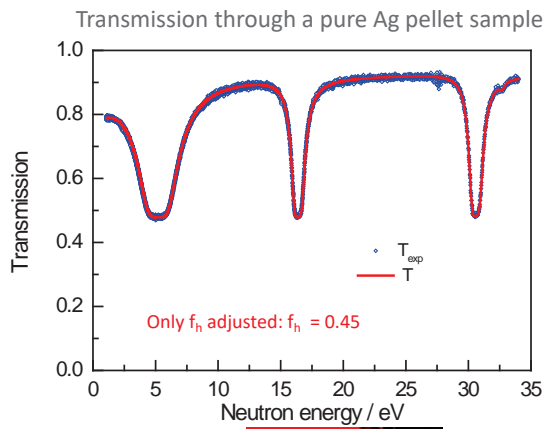


## NRTA model for pellet samples



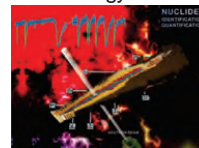
$$T(E) = f_h + (1 - f_h) \int_0^1 \frac{x}{\sqrt{1-x^2}} e^{-\rho \sigma_{tot}(E) x} dx$$

- REFIT**
- $x$  : track length (divided by  $2R$ )
  - $f_h$  : holes fraction
  - $\rho$  : volume number density
  - $R$  : radius



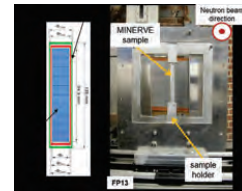
Model developed, implemented and validated at JRC Geel (S. Kopecky)

Fei Ma et al., J. Anal. At. Spectrom. 35 (2020) 478

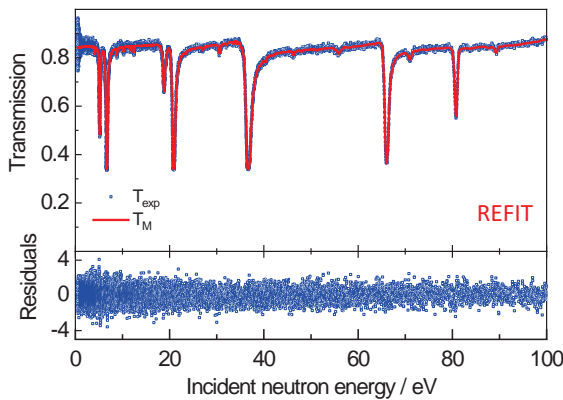


## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA
  - Identification and quantification of impurities



$^{109}\text{Ag}$



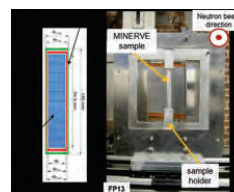
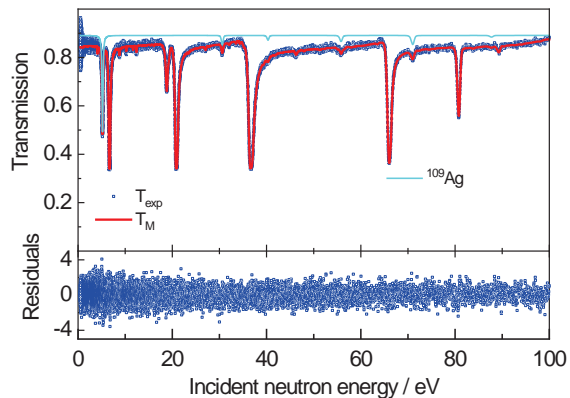
Note:  
 RP used result from a new evaluation for  $^{107,109}\text{Ag}$  based on capture and transmission experiments at GELINA

Šalamon et al., Nucl. Instr. Meth. B 446 (2019) 19



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA
  - Identification and quantification of impurities

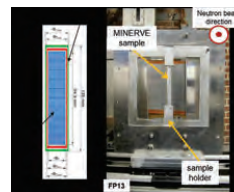
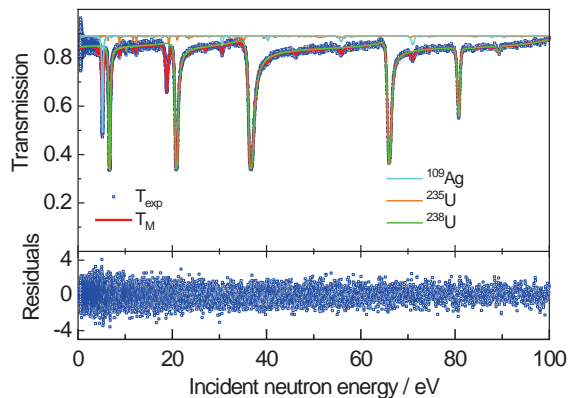


$^{109}\text{Ag}$



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA
  - Identification and quantification of impurities

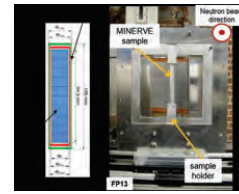
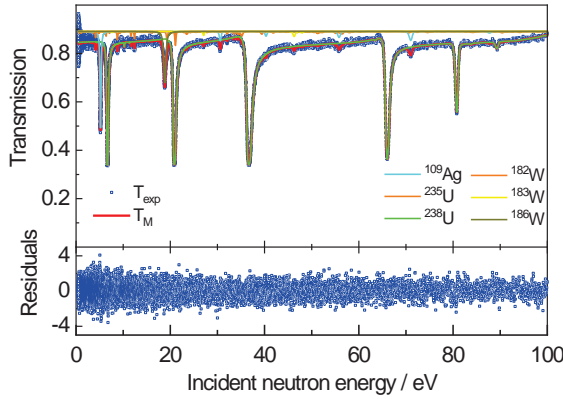


$^{109}\text{Ag}$



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA
  - Identification and quantification of impurities



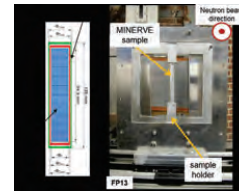
$^{109}\text{Ag}$

Presence of strong neutron absorber W:  
Not declared by supplier



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA
  - Identification and quantification of impurities
- Presence of strong neutron absorbing elements such as W important for the interpretation pile oscillator measurements



$^{109}\text{Ag}$

$10^{24} \text{ at/cm}^3$

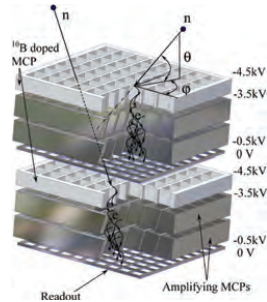
	AG9C1		AG9C2	
	ICPMS	This work	ICPMS	This work
$^{109}\text{Ag}$	6.30 (8) $\times 10^{-4}$	6.03 (2) $\times 10^{-4}$	6.82 (8) $\times 10^{-5}$	6.54 (2) $\times 10^{-5}$
$^{235}\text{U}$	8.31 (10) $\times 10^{-5}$	8.35 (20) $\times 10^{-5}$	8.39 (10) $\times 10^{-5}$	8.45 (20) $\times 10^{-6}$
$^{238}\text{U}$	1.119 (14) $\times 10^{-2}$	1.126 (5) $\times 10^{-2}$	1.129 (14) $\times 10^{-2}$	1.136 (5) $\times 10^{-2}$
$^{182}\text{W}$		1.30 (4) $\times 10^{-5}$		6.1 (3) $\times 10^{-6}$
$^{183}\text{W}$		6.6 (2) $\times 10^{-6}$		3.1 (2) $\times 10^{-6}$
$^{186}\text{W}$		1.36 (1) $\times 10^{-5}$		6.11 (3) $\times 10^{-6}$

Šalamon et al., J. Radioanal. Nucl. Chem. 321 (2019) 519

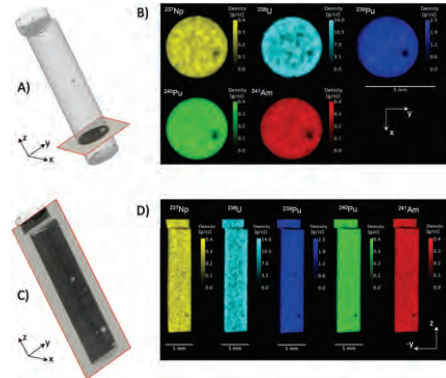


### 3D imaging (transmission)

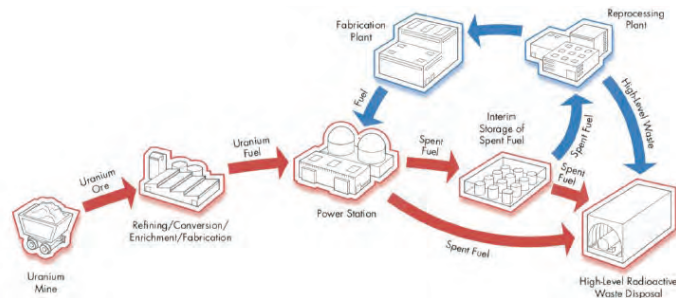
- GELINA: high resolution, relatively low intensity
- Imaging at spallation sources: ISIS, JPARC, LANSCE, ...  
E.g. Losko and Vogel, Scientific Report 12 (2022) 6648
  - LANSCE
  - Microchannel plate neutron imaging detector (<sup>10</sup>B)



Tremsin et al., NIMA 539 (2005) 278



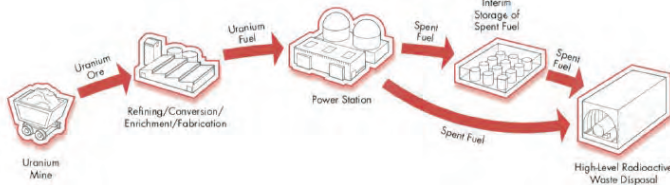
### Nuclear fuel cycle



Nuclear fuel cycle  
(open or closed)  
produces waste



## Open fuel cycle: final disposal of Spent Nuclear Fuel (SNF)



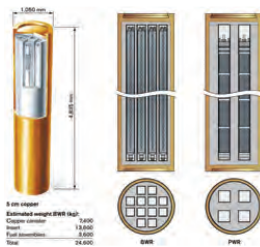
**Open fuel cycle**  
 Sweden : Forsmark  
 Finland : Onkalo

**Three barriers (SKB):**

- canister
- buffer (bentonite clay)
- rock



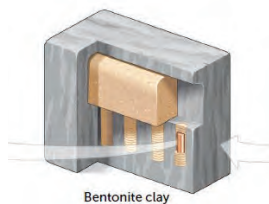
## Open fuel cycle: final disposal of SNF assemblies



**Open fuel cycle**  
 Sweden : Forsmark

Estimate of thermal power has a substantial impact on:

- the number of canisters (Cu mining)
- ecological and financial footprint



6000 canisters  
 12000 ton of spent fuel

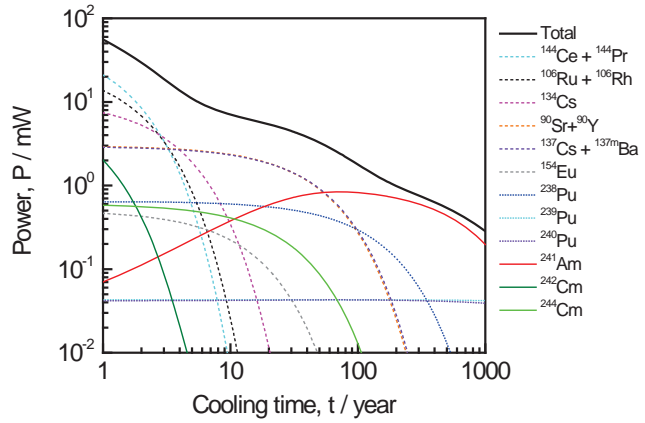
SKB : Swedish nuclear fuel and waste management company



## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 MWd/kg



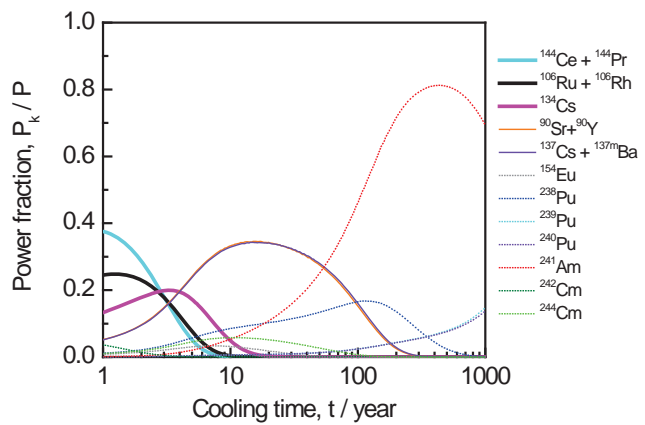
Žerovnik et al., JRC Technical Reports, EUR 29301 EN (2018)



## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

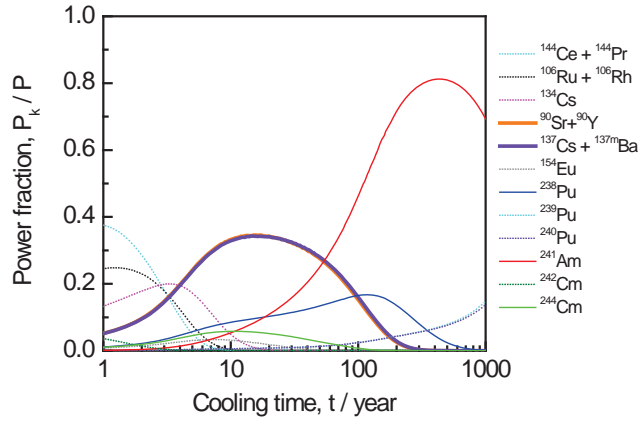
PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 MWd/kg



## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

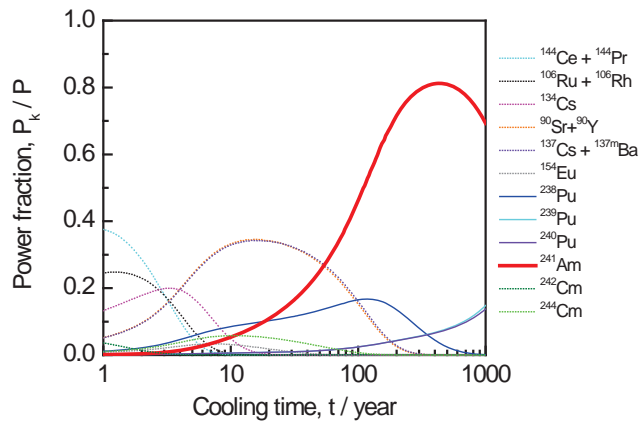
PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 MWd/kg



## Thermal power produced by SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 MWd/kg





## Back-end of the fuel cycle: spent fuel characterisation (SFC)

A **safe, secure, ecological** and **economic** handling, interim storage and final disposal requires that **Spent Nuclear Fuel (SNF)** is **characterised** for the main observables of interest:

- Decay heat
- Neutron emission
- $\gamma$ -ray emission
- Reactivity (BurnUp Credit)  
(i.e. Fission Product (FP), actinides )
- Fissile material (Nuclear Safeguards, i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ )
- Specific nuclides (Long term safety)  
i.e.  $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$



## Spent fuel characterisation (SFC): nuclide inventory

Nuclide	Observable	Nuclide	Observable
$^{90}\text{Sr}$	H, $S_\gamma$	$^{235}\text{U}$	R, $S_\gamma$
$^{106}\text{Ru}$	H	$^{238}\text{U}$	R, $S_\gamma$
$^{134}\text{Cs}$	H	$^{238}\text{Pu}$	H, $S_\gamma$
$^{137}\text{Cs}$	H, $S_\gamma$	$^{239}\text{Pu}$	R, $S_\gamma$
$^{144}\text{Ce}$	H,	$^{240}\text{Pu}$	R, $S_\gamma$
$^{148}\text{Nd}$	Burn-up	$^{241}\text{Pu}$	H, $S_\gamma$
$^{149}\text{Sm}$	Power	$^{241}\text{Am}$	H, $S_\gamma$
$^{154}\text{Eu}$	H, $S_\gamma$	$^{242}\text{Cm}$	H, $S_n$
		$^{244}\text{Cm}$	H, $S_n$

H : thermal power or decay heat  
 $S_n$  : neutron emission  
 $S_\gamma$  :  $\gamma$ -ray emission  
 R : reactivity (criticality safety)

⇒ Requires **complex nuclide inventory** which can only be obtained by **theoretical calculations**

Criticality safety (BUC):

$^{95}\text{Mo}$ ,  $^{99}\text{Tc}$ ,  $^{101}\text{Ru}$ ,  $^{103}\text{Rh}$ ,  $^{109}\text{Ag}$ ,  $^{133}\text{Cs}$ ,  $^{143}\text{Nd}$ ,  $^{147,149,150,151,152}\text{Sm}$ ,  $^{155}\text{Gd}$

Long term safety:

$^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$



## Burnup calculations

Coupled neutron transport – nuclide depletion/production

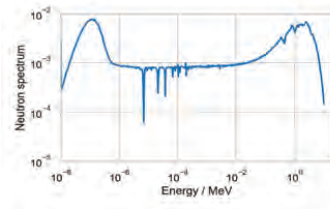
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

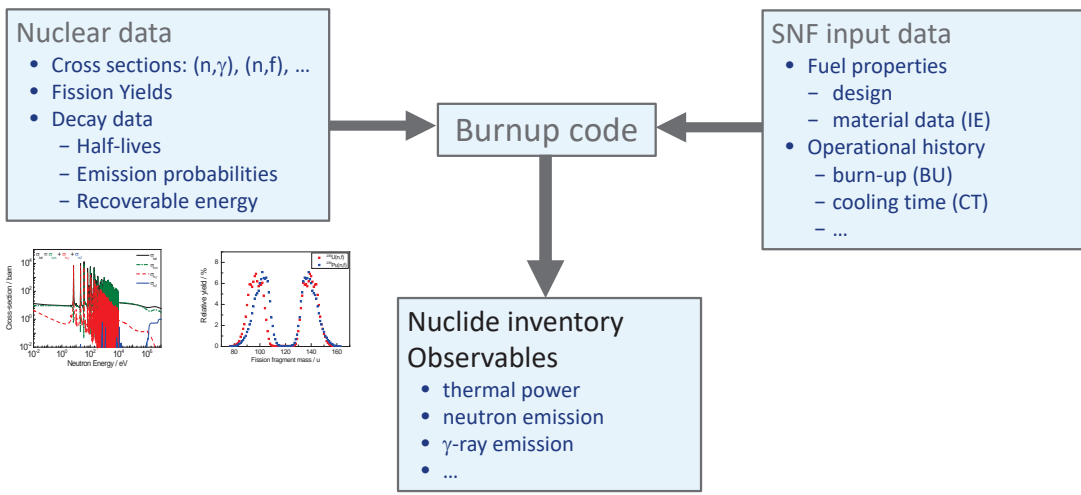
Update nuclide vector



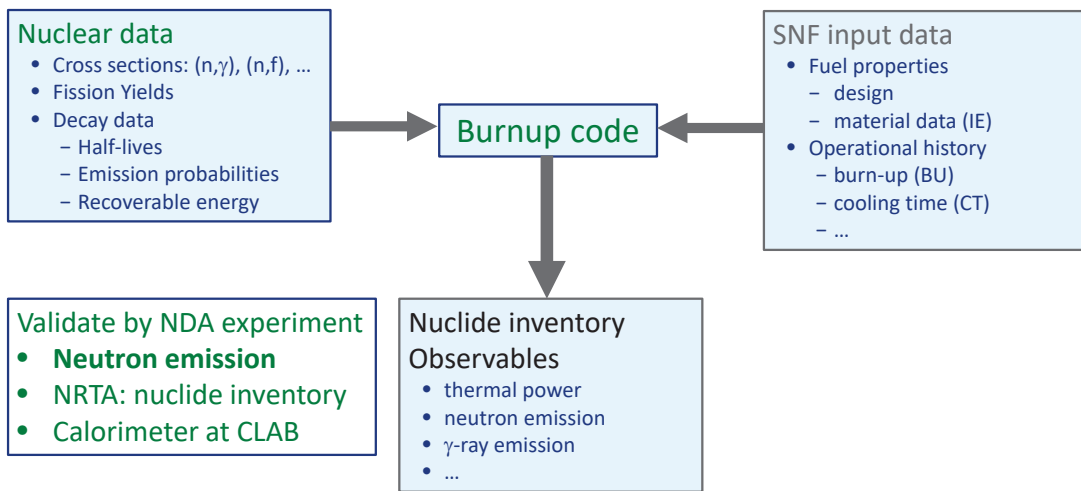
- ALEPH2 (SCK CEN)
- EVOLCODE (CIEMAT)
- SERPENT (VTT)
- SCALE (ORNL)
- VESTA (IRSN)



## Burnup calculations need to be validated

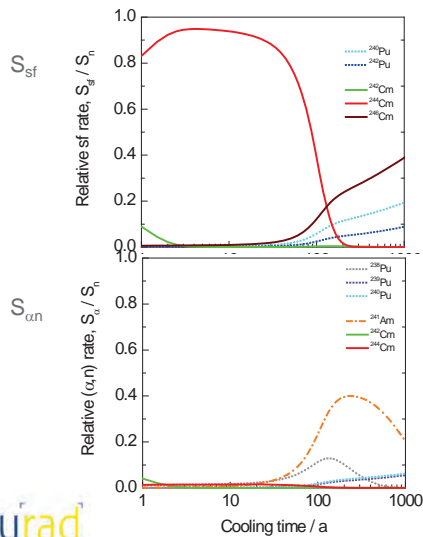


## Burnup calculations need to be validated

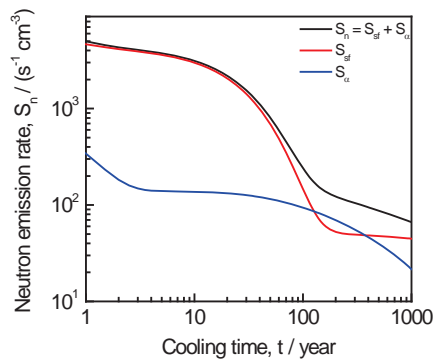


## Neutron emission by SNF

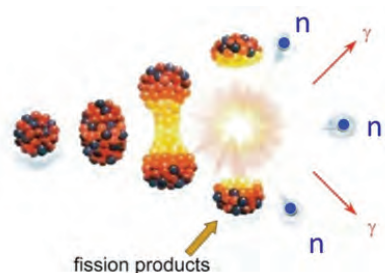
PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 45 GWd/t



⇒ Main contribution from <sup>244</sup>Cm(sf)



## Neutron emission by SNF: spontaneous fission

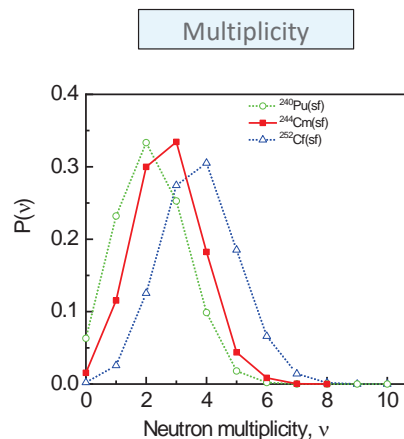
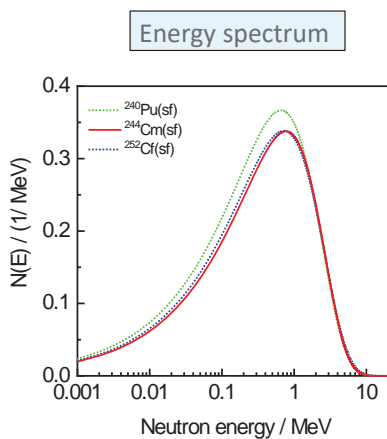


e.g.  $^{240}\text{Pu}(\text{sf})$ ,  $^{244}\text{Cm}(\text{sf})$ ,  $^{252}\text{Cf}(\text{sf})$

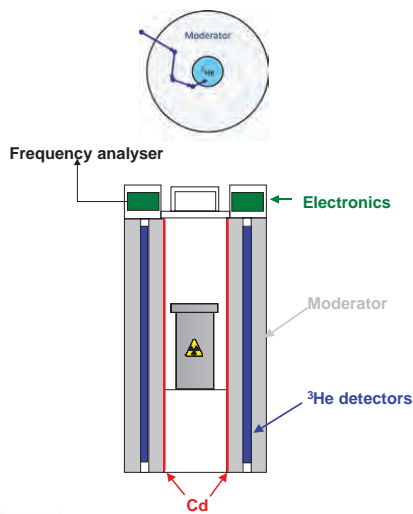
Fission: nucleus splits up into fission products (FP), which are strongly :

- Prompt fission  $\gamma$ -rays
- **Prompt fission neutrons**

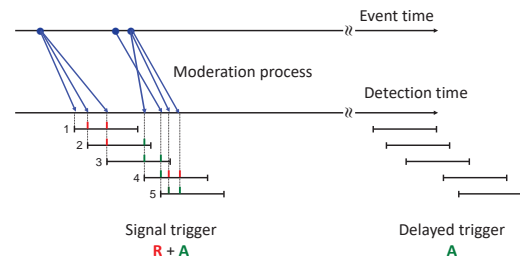
## Prompt neutron emission due to spontaneous fission



## Detection of prompt fission neutrons: correlation counting



Well-known for nuclear safeguards applications  
See S. Pozzi on Monday



Experimental observables:  
Total count rate: T  
Reals count rate:  $R = (R+A) - A$



## Neutron correlation counting: Hage's point model

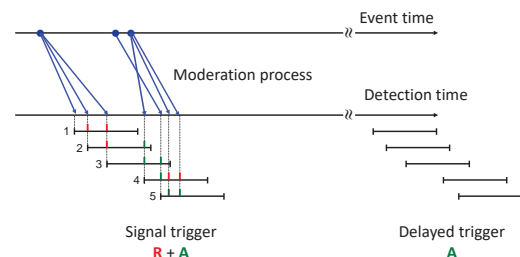
$$T = \epsilon_{sf} S_{sf} M [1 + \alpha]$$

W. Hage and D.M. Cifarelli, Nucl. Sci; Eng. 89 (1985) 159

W. Hage and D.M. Cifarelli, Nucl. Instr. Meth. A236 (1985) 165

$$R = \epsilon_{sf}^2 f S_{sf} M^2 \left[ \frac{v_{sf(2)}}{v_{sf(1)}} + \frac{p v_{nf(2)}}{1-p v_{nf(1)}} (1 + \alpha) \right]$$

- Neutron emission rate due to (sf) :  $F_s$
- Relative  $(\alpha, n)$  contribution :  $\alpha$
- Detection efficiency :  $\epsilon$
- Leakage multiplication :  $M$
- Probability for a (n, f) reaction :  $p$
- Factorial moments multiplicity distribution



Experimental observables:  
Total count rate: T  
Reals count rate:  $R = (R+A) - A$

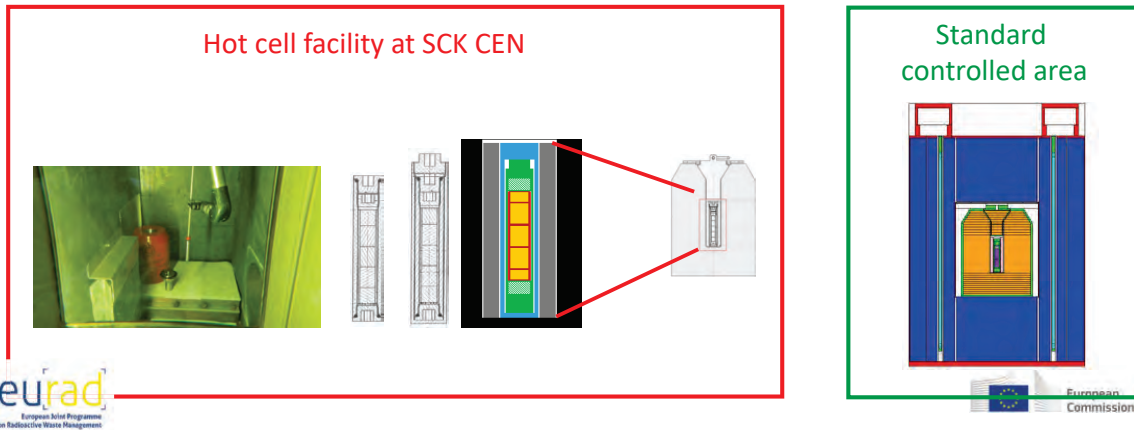
$$v_{sf(j)} = \sum_{v=j}^{\infty} \binom{v}{j} P_{sf}(v) \quad v_{nf(j)} = \sum_{v=j}^{\infty} \binom{v}{j} P_{nf}(v)$$



## Validation of depletion codes: neutron emission rate of SNF

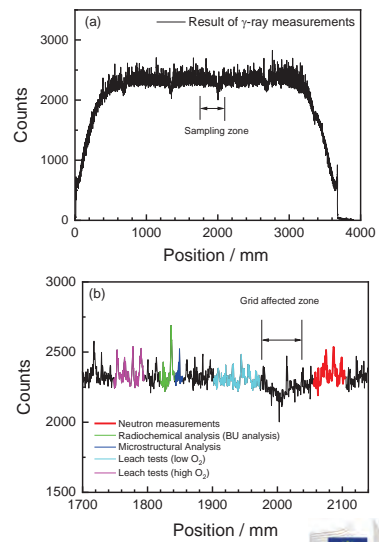
**NDA method** to determine the neutron output of a **SNF** sample under **standard controlled area** conditions

Collaboration SCK CEN



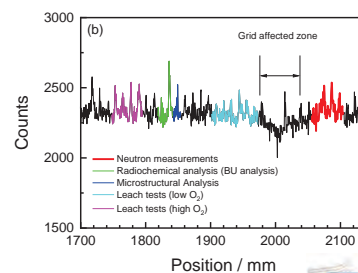
## EURAD: Validation of depletion codes

- **Irradiation history of the SNF**
  - Segment (~ 50 mm) from rod D05 of FT1X57 (PWR)
  - PWR Assembly (15 x 15):  
188 UO<sub>2</sub> rod (4.5 wt% <sup>235</sup>U/U) and 16 (U,Gd)O<sub>2</sub> rods
  - Irradiated at Tihange 1
  - Rod used for other international project (First-Nuclides, REGAL, WETFUEL & AGAF, SF-ALE)
- **SNF segment sample by NDA**  
Part of a set of 4 samples (**REGAL project**)
  - **Radiochemical analysis (BU)**
  - Microstructural analysis
  - Leach tests (low O<sub>2</sub>)
  - Leach tests (high O<sub>2</sub>)



## Results of radiochemical analysis

BU indicator	Date of analysis	Nuclide inventory mg/g	Cumulative fission yield (x 100)	Burnup Gwd/t
$^{137}\text{Cs}$	10/21/2013	1.288 (28)	6.334	52.6 (11)
$^{143}\text{Nd} + ^{144}\text{Nd}$	02/05/2014	3.029 (32)	10.158	53.95 (56)
$^{145}\text{Nd} + ^{146}\text{Nd}$	02/05/2014	1.962 (21)	6.479	53.05 (56)
$^{148}\text{Nd}$	02/05/2014	0.534 (12)	1.724	53.3 (12)
$^{150}\text{Nd}$	02/05/2014	0.257 (11)	0.836	52.2 (23)
Average:				52.78 (37)



Schillebeeckx et al., JRC Technical Reports, EUR 30379 EN (2020)



## Absolute neutron output of SNF segment sample: results

- SNF segment sample: characteristics

Parameter	Value
Length	52.01 (4) mm
Segment weight	42.616 (1) g
Cladding weight	6.71 (4) g
Net fuel weight	35.91 (4) g

- Neutron emission rate (exp) <sup>CT 18 a</sup>

$$S_{sf} = 682 (10) \text{ g}^{-1} \text{ s}^{-1}$$

$$S_{\alpha n} / S_{sf} = 0.036 (15)$$

$$\rho(S_{sf}, \alpha) = -0.972$$

Note: neutron emission rate reflects  $^{244}\text{Cm}$  inventory  
radiochemical analysis uncertainty > 3%

- Detector calibrated with certified  $^{252}\text{Cf}(sf)$  sources (Mn bath)
- Hage's point model



Schillebeeckx et al., JRC Technical Reports, EUR 30379 EN (2020)



### Absolute neutron output of SNF segment sample: code validation

Code	Library	$(\alpha, n)$		$S_{sf} / (g^{-1}s^{-1})$	$S_{\alpha} / (g^{-1}s^{-1})$	Calculation/Experiment	
		Method	Library			$S_{sf}$	$S_{\alpha n}$
SCALE	ENDF/B-VII.1	$Y(\alpha, n)$		653	11.0	0.96	0.45
SERPENT(1)	ENDF/B-VII.1	$Y(\alpha, n)$		689	14.3	1.01	0.58
SERPENT(2)	ENDF/B-VII.1	$Y(\alpha, n)$		694	14.2	1.02	0.58
	ENDF/B-VIII.0	$Y(\alpha, n)$		691	14.1	1.01	0.57
	JEFF-3.1.2	$Y(\alpha, n)$		629	13.2	0.92	0.54
	JEFF-3.3	$Y(\alpha, n)$		654	13.7	0.96	0.56
	JEFF-4T0	$Y(\alpha, n)$		695	13.7	1.02	0.56
	JENDL-4.0	$Y(\alpha, n)$		719	14.5	1.05	0.59
ALEPH28	ENDF/B-VIII.0	$Y(\alpha, n)$		662	13.1	0.97	0.53
		$\sigma(\alpha, n)$	TENDL2015		12.6		0.51
		$\sigma(\alpha, n)$	JENDL_AN/500		10.6		0.43
	JEFF-3.3	$Y(\alpha, n)$		641	12.9	0.94	0.53
		$\sigma(\alpha, n)$	TENDL2015		12.7		0.52
		$\sigma(\alpha, n)$	JENDL_AN/500		10.5		0.43

All data normalised to  $^{148}\text{Nd}$  inventory

$$S_{sf} = 682 (10) \text{ g}^{-1} \text{ s}^{-1}$$

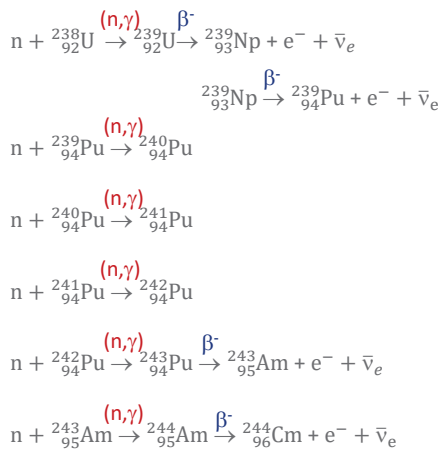
$$S_{\alpha n} / S_{sf} = 0.036 (15)$$

⇒ influence

- nuclear data
- burnup code

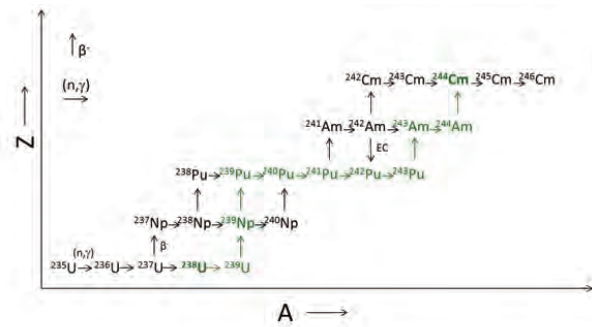


### Production of $^{244}\text{Cm}$



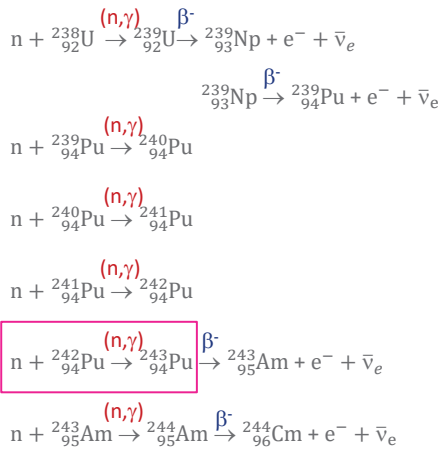
Main production root of  $^{244}\text{Cm}$  is a sequence of

- $(n,\gamma)$  reactions (6)
- $\beta^-$  decays (4)

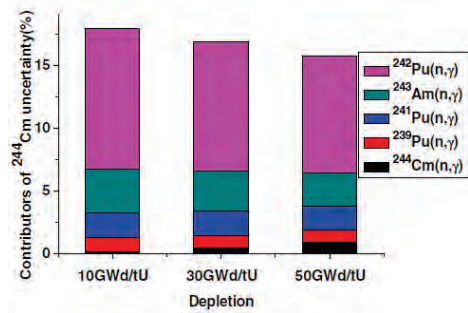




## Production of <sup>244</sup>Cm



Contribution (n,γ) reactions

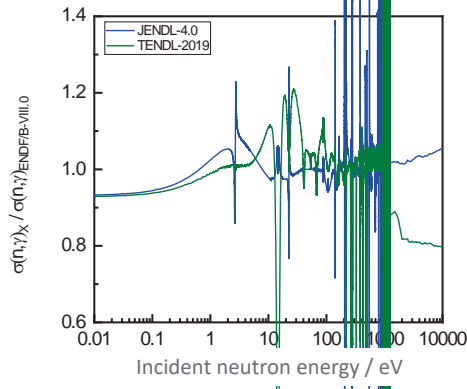
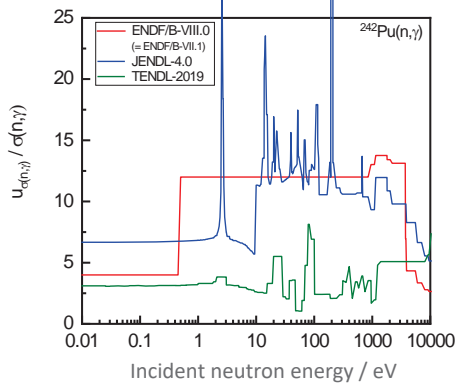


Burnup	Relative uncertainty
10 Gwd/t	12.1 %
30 GWD/t	11.1 %
50 Gwd/t	10.0 %

Tiejun Zu et al., Annals of Nuclear Energy 94 (2016) 399



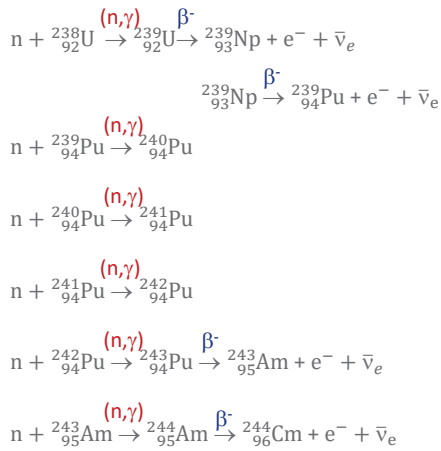
## Calculation of <sup>244</sup>Cm inventory: impact <sup>242</sup>Pu(n,γ)



⇒ Improved evaluation for the <sup>242</sup>Pu(n,γ) cross section required  
 ⇒ New experimental data required

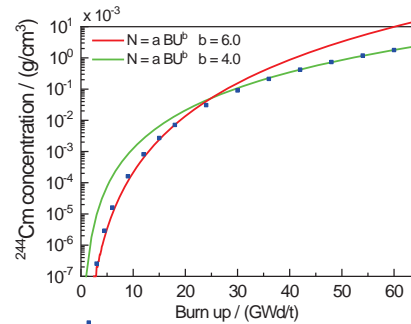


## Production of <sup>244</sup>Cm



Main production root of <sup>244</sup>Cm is a sequence of

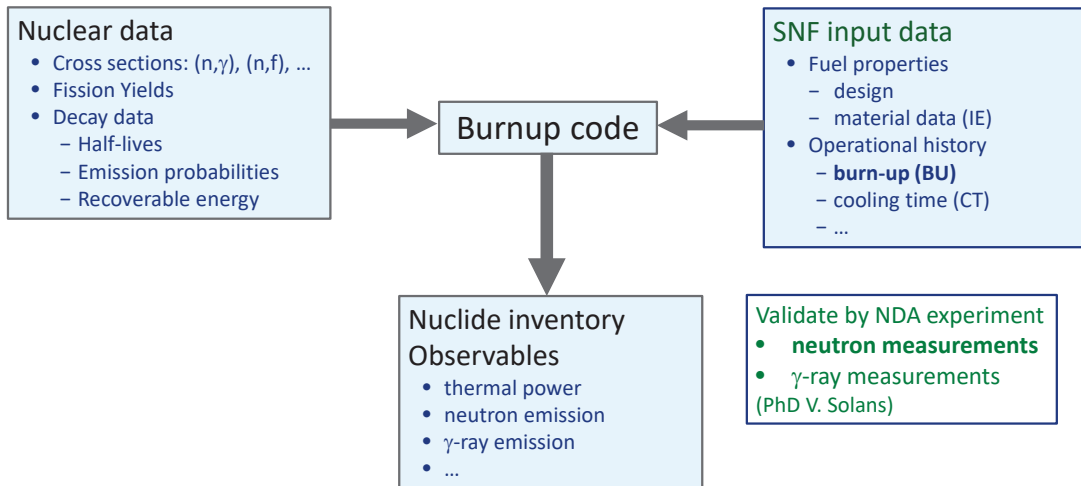
- (n,γ) reactions (6)
- β<sup>-</sup> decays (4)



⇒ Total neutron emission extremely sensitive to BU



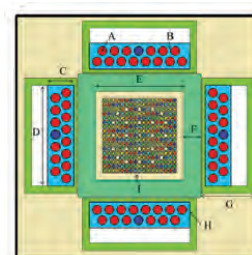
## Burnup calculations need to be validated



## Differential Die-away Self-Interrogation (DDSI)

Passive NDA: detection of neutrons emitted by SNF assembly  
 Developed at LANL for nuclear safeguards applications

- Neutron production
  - Primary neutrons: mainly prompt fission neutrons from  $^{244}\text{Cm}(sf)$
  - Prompt fission neutrons from neutron induced fission in fuel mainly after neutron moderation in the water of the pool
- Detection principle
  - $^3\text{He}$  in moderator
  - Detection of correlated neutrons: construct Rossi-alpha distribution

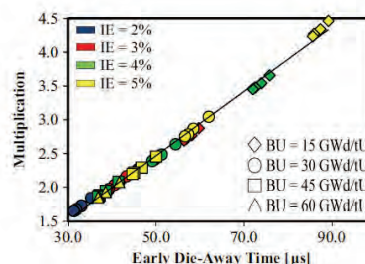
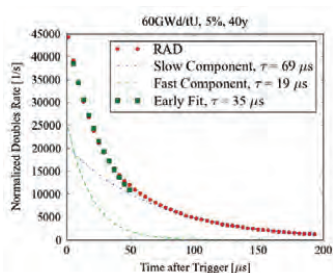


Kaplan et al., NIMA 764 (2014) 347



## DDSI: Rossi-alpha distribution

- 1) Total counts : burn-up
- 2) Rossi-alpha distribution : neutron multiplication (fissile material)



Kaplan et al., NIMA 764 (2014) 347

⇒ Poster V. Solans “Rossi-Alpha distribution analysis of DDSI data for spent nuclear fuel characterization”  
 main objective: improve analysis procedures for DDSI



## Summary and conclusions

- GELINA: TOF-facility for cross section measurements in the resonance region
- Importance of transmission measurements for an accurate determination of cross section data
- NRA: powerful tool for characterisation of objects and materials
- Improved neutron interaction cross section data are still needed for various energy and non-energy applications
- Importance of nuclear data and neutron detection for SNF characterisation



## Mobility projects and access to nuclear infrastructures

- EUFRAT (open access to JRC Geel nuclear infrastructure)  
[https://joint-research-centre.ec.europa.eu/knowledge-research/open-access-jrc-research-infrastructures\\_en](https://joint-research-centre.ec.europa.eu/knowledge-research/open-access-jrc-research-infrastructures_en)
- ARIEL (Accelerator and research reactor infrastructures for education and learning)  
<https://www.ariel-h2020.eu/index.php/en/call-for-proposals>
- EURAD (European joint programme on radioactive waste management)  
<https://euradschool.eu/application-guidelines/>
- ENEN2plus  
First call mobility grants expected fall 2022



## Keep in touch



EU Science Hub: [ec.europa.eu/jrc](https://ec.europa.eu/jrc)



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EU Science, Research and Innovation



EU Science Hub



EU science



# Thank you



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**2.4 Spent Nuclear Fuel Characterisation, P. Schillebeeckx, JRC  
Geel, Training for DG-ENER EURATOM; 28/06/2023**

# Spent Nuclear Fuel Characterisation

Peter Schillebeeckx

JRC Directorate G, Nuclear Safety and Security

Unit G.II.5 Nuclear Data and Measurement Standards

28 June 2023, DG-ENER, Luxembourg

*The project leading to this application has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement n° 847593.*



## CONTENTS

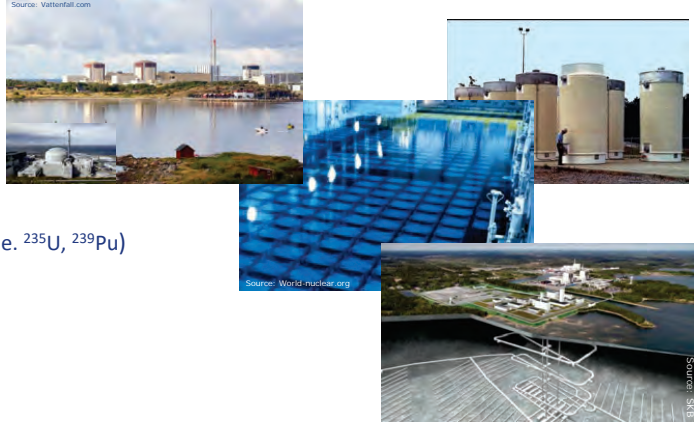
- Introduction
- Radioactive decay
  - $\beta$ - decay
  - $\alpha$  decay
  - spontaneous fission (sf)
- SNF characteristics
  - Neutron emission
  - $\gamma$ -ray emission
  - Decay heat rate (decay power)
- Theoretical estimation of observables
  - Principle
  - Example:  $^{137}\text{Cs}$
- Code validation
  - Calorimetry
  - Neutron measurements
- Verification of SNF history
  - Neutron measurements
  - $\gamma$ -ray measurements
- Bibliography



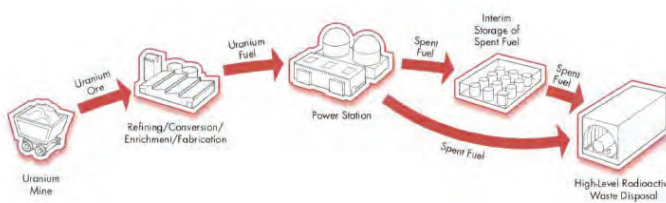
## BACK-END OF THE FUEL CYCLE: SPENT FUEL CHARACTERISATION (SFC)

A safe, secure, ecological and economic handling, interim storage and final disposal requires that **Spent Nuclear Fuel (SNF)** is characterised for the main observables of interest:

- Decay heat rate (power)
- Neutron emission
- $\gamma$ -ray emission
- Reactivity (BurnUp Credit)  
(i.e. Fission Product (FP), actinides)
- Fissile material (Nuclear Safeguards, i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ )
- Specific nuclides (Long term safety)  
i.e.  $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$



## OPEN FUEL CYCLE: DISPOSAL OF SPENT NUCLEAR FUEL (SNF)



SKB : Swedish nuclear fuel and waste management company

**Open fuel cycle**  
Sweden : Forsmark  
Finland : Onkalo

**Three barriers (SKB):**

- canister
- buffer (bentonite clay)
- rock





## SPENT NUCLEAR FUEL (SNF) DISPOSAL EXAMPLE: SWEDISH CONCEPT



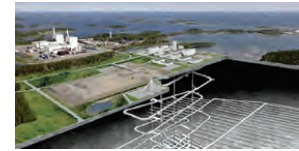
**CLAB**  
Central Interim Storage Facility for Spent Nuclear Fuel (SNF)



**CLINK**  
SNF encapsulation plant



**SIGRID**  
SNF carrier

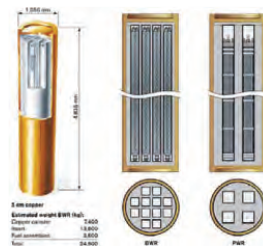


**FORSMARK bedrock**  
SNF disposal

www.skb.com



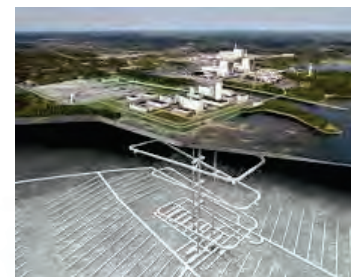
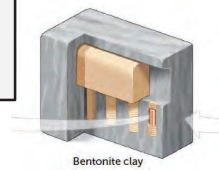
## OPEN FUEL CYCLE: DISPOSAL OF SNF ASSEMBLIES



Open fuel cycle  
Sweden : Forsmark

Estimate of decay heat rate (power) has a substantial impact on:

- the number of canisters (Cu mining)
- ecological and financial footprint



6000 canisters  
12000 ton of spent fuel

www.skb.com



## OPTIMISING CANISTER LOADING

Reduction of canisters and required disposal volume by

- Improved loading schemes algorithms  
e.g. Solans et al., Nucl. Eng. Des. 370 (220) 110897, reduction of 2% in number of canisters
- Improved decay power estimation  
Reduction of uncertainty of decay power estimation  
Seidl et al., Frontiers in Energy research 11 (2023) 1143312



One of the main objectives of EURAD WP8 Task 2

“Spent nuclear fuel characterisation and related uncertainty analysis”



www.skb.com



## SNF MANAGEMENT : STORAGE, TRANSPORT, REPROCESSING AND DISPOSAL

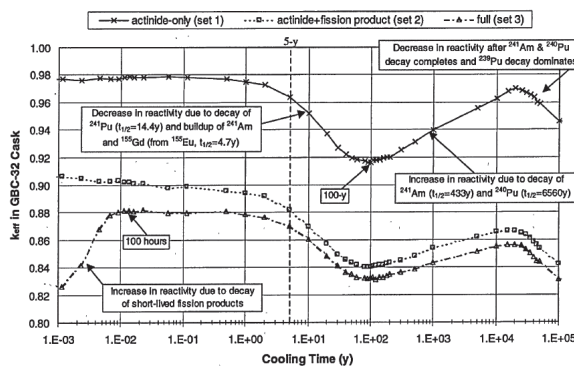


Figure 3 Reactivity behavior in the GBC-32 cask as a function of cooling time for the three classifications of burnup credit (defined in Table 1). The calculations correspond to fuel with 4.0 wt % <sup>235</sup>U initial enrichment that has accumulated 40 GWd/MTU burnup, and include an axial burnup distribution as described in Section 2.1.

Wagner and Parks, NUREG/CR-6781 (January 2003)

“Recommendations on the credit for cooling time in PWR burnup credit analysis”

Nuclear Criticality Safety (reactivity)

NEA: Working Party (WPNCs)

- Must be guaranteed based on reliable methods
- Burn-Up Credit (NEA: Expert group EGBUC)
  - Reactivity decreases as fuel BU proceeds: reduction of fissile material and increase of neutron absorbing fission products (FP)
  - Account for this reactivity decrease for criticality safety assessments

⇒ Requires **inventory of key nuclides** and accurate neutron **absorption cross sections**



## SNF CHARACTERISATION FOR THE BACK-END OF THE FUEL CYCLE

Main **observables** of interest:

- Decay heat rate (power) : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ , Fission Products (BUC)
- Fissile material :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- Long-term safety : e.g.  $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$

**difficult** to be **measured** directly, in particular during **industrial operation**

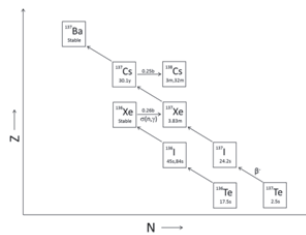
- Decay heat by **calorimetry** at CLAB: accurate but **long measurement times**
- Criticality safety analysis: calculations required to account for **burn-up credit** (MA, FP)
- **Prediction at long cooling times** only possible by theoretical calculations

⇒ requires knowledge of a **complex nuclide inventory** with strongly varying characteristics

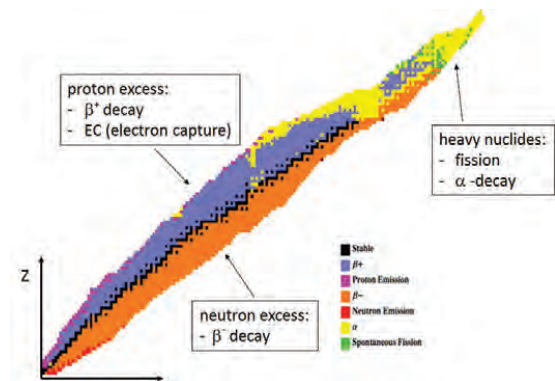
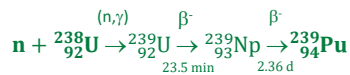


## SPENT NUCLEAR FUEL: NUCLIDE INVENTORY

- Fission products (FP): neutron induced fission (n,f)  
e.g.  $^{90}\text{Sr}$ ,  $^{134,137}\text{Cs}$ ,  $^{154}\text{Eu}$ , ...

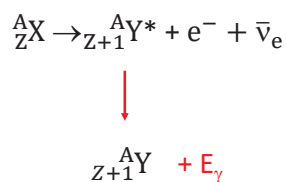
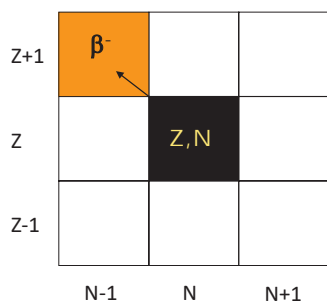


- Actinides: major and minor actinides  
e. g.  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$ ,  $^{241}\text{Am}$ ,  $^{244}\text{Cm}$ , ...



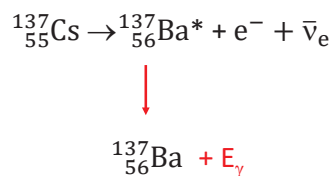
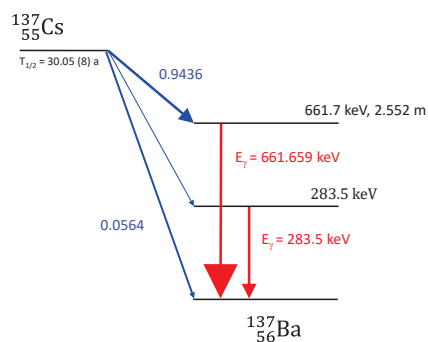
### β<sup>-</sup> - DECAY BY NEUTRON RICH NUCLIDES

Isobaric transition in which a neutron is transformed into a proton and an electron + anti-neutrino are emitted



### β<sup>-</sup> - DECAY BY NEUTRON RICH NUCLIDES: e.g. <sup>137</sup>Cs

- T<sub>1/2</sub> = 30.05 (8) a
- Q<sub>β<sup>-</sup></sub> = 1175.73 (17) keV



Gamma-ray emission probability: P<sub>γ</sub>

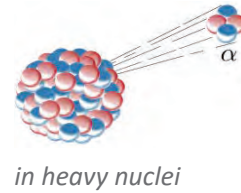
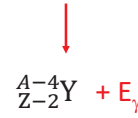
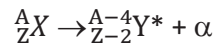
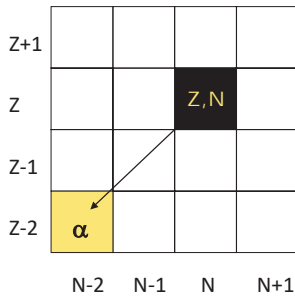
E <sub>γ</sub>	P <sub>γ</sub>
661.7 keV	0.8499 (20)
283.5 keV	5.8 (8) x 10 <sup>-6</sup>

<http://www.lnhb.fr/donnees-nucleaires/donnees-nucleaires-tableau/>



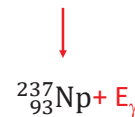
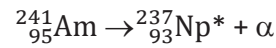
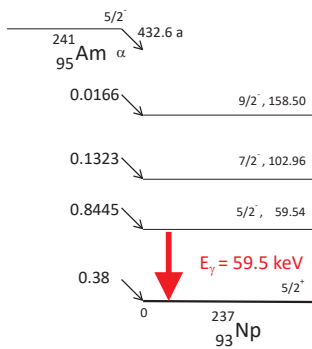
### α - DECAY

Radioactive decay in which a nucleus emits an **α-particle** (<sup>4</sup>He nucleus) and transforms into a nucleus with 4 less nucleons (2n, 2p)



### α - DECAY BY ACTINIDES: e.g. <sup>241</sup>Am

- T<sub>1/2</sub> = 432.6 (6) a
- Q<sub>α</sub> = 5637.82 (12) keV



α -particle emission probability:

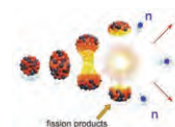
E <sub>α</sub>	P(E <sub>α</sub> )
5388.3 keV	0.0166 (3)
5442.9 keV	0.1323 (10)
<b>5485.6 keV</b>	<b>0.8445 (10)</b>

<http://www.lnhb.fr/donnees-nucleaires/donnees-nucleaires-tableau/>





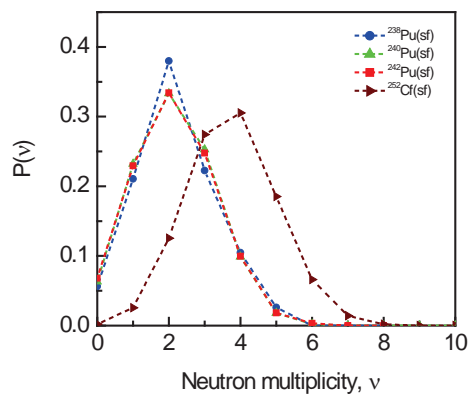
### PROMPT FISSION NEUTRONS: MULTIPLICITY



Emission of prompt fission neutrons:

- statistical process
- on average  $\langle v \rangle = v_{s(1)} > 1$

Nuclide	$v_{s(1)}$	$v_{s(2)}$	$v_{s(3)}$
$^{238}\text{Pu}$	2.210	1.978	0.933
$^{240}\text{Pu}$	2.154	1.895	0.868
$^{242}\text{Pu}$	2.145	1.882	0.867
$^{252}\text{Cf}$	3.756	5.978	5.287

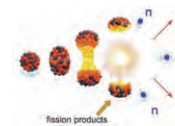


$$v_{s(j)} = \sum_{v=j}^{\infty} \binom{v}{j} P_{sv}$$

Normalised factorial moments



### PROMPT FISSION NEUTRONS: DATA



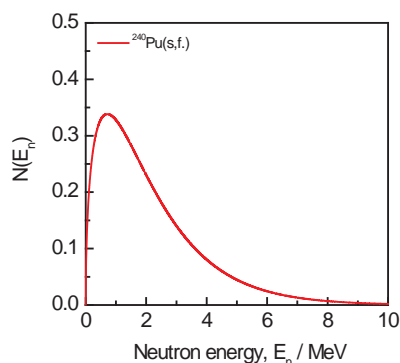
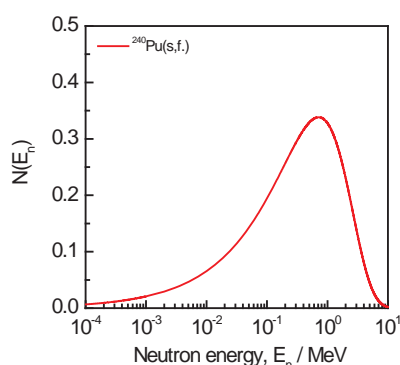
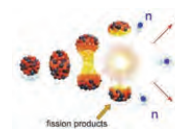
Nuclide	$T_{1/2}$	(sf) branching	$\langle v \rangle$	$S_{sf} / (s^{-1} g^{-1})$
$^{238}\text{Pu}$	$8.774 (3) \times 10^1 \text{ a}$	$1.85 (5) \times 10^{-9}$	1.980 (30)	$2.59 (11) \times 10^3$
$^{240}\text{Pu}$	$6.561 (7) \times 10^3 \text{ a}$	$5.70 (20) \times 10^{-8}$	2.154 (5)	$1.031 (36) \times 10^3$
$^{242}\text{Pu}$	$3.73 (3) \times 10^5 \text{ a}$	$5.49 (9) \times 10^{-6}$	2.149 (8)	$1.728 (32) \times 10^3$
$^{242}\text{Cm}$	162.86 (8) d	$6.36 (14) \times 10^{-8}$	2.540 (20)	$1.980 (46) \times 10^7$
$^{244}\text{Cm}$	$1.811 (3) \times 10^1 \text{ a}$	$1.36 (1) \times 10^{-6}$	2.710 (10)	$1.107 (10) \times 10^7$
$^{246}\text{Cm}$	$4.72 (3) \times 10^3 \text{ a}$	$2.61 (4) \times 10^{-6}$	2.930 (30)	$8.70 (13) \times 10^6$

Decay data from Nichols et al., INDC-2453, , INDC(NDS) – 0534, August 2008  
 $\langle v \rangle$  from Santi and Miller, Nucl; Sci. Eng. 160 (2017) 190





## PROMPT FISSION NEUTRONS: ENERGY DISTRIBUTION



$\langle E_n \rangle \sim 2 \text{ MeV}$

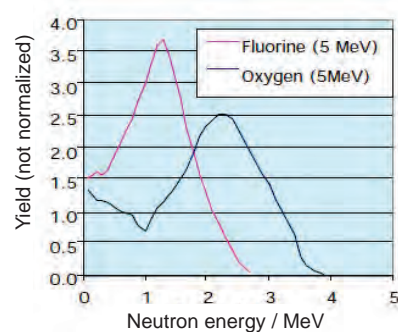
$N(E_n)$  can be parameterised by:

- a Maxwellian distribution in the CM system
- a Watt spectrum in the lab system



## NEUTRON PRODUCTION BY $(\alpha, n)$ REACTIONS

- $(\alpha, n)$  reaction with light nuclides
  - $^{18}\text{O}(\alpha, n)^{21}\text{Ne}$
  - $^{17}\text{O}(\alpha, n)^{20}\text{Ne}$
  - $^{19}\text{F}(\alpha, n)^{22}\text{Na}$
- Neutron energy (emission)
  - $\text{O}(\alpha, n) : \langle E_n \rangle \sim 2 \text{ MeV}$
  - $\text{F}(\alpha, n) : \langle E_n \rangle \sim 1 \text{ MeV}$
- $P(\nu) = 1$   
used to separate prompt fission neutrons from  $(\alpha, n)$  neutrons in neutron correlation counting (NDA)



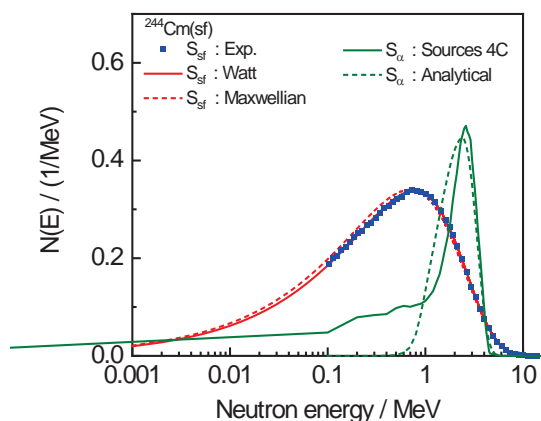
⇒ in SNF:  $\alpha$  - decay of actinides followed by  $(\alpha, n)$  reaction in light elements





### NEUTRON PRODUCTION BY SNF

- Prompt spontaneous fission neutrons
- $(\alpha, n)$  reaction with light nuclides

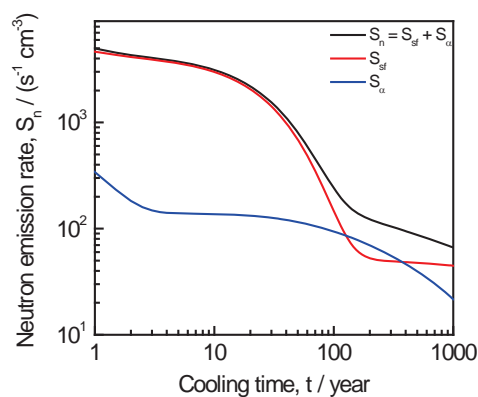


### NEUTRON EMISSION BY SNF

$$S_n(t) = \sum_k S_{n,k}(t)$$

- $S_{n,k}(t)$  : contribution of radionuclide k
- $S_{n,k}(t) = (s_{sf,k} + s_{\alpha n,k}) N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $s_{sf,k}$  : specific neutron emission rate of nuclide k due to (sf)
  - $s_{\alpha,k}$  : specific neutron emission rate of nuclide k due to  $(\alpha, n)$  reactions

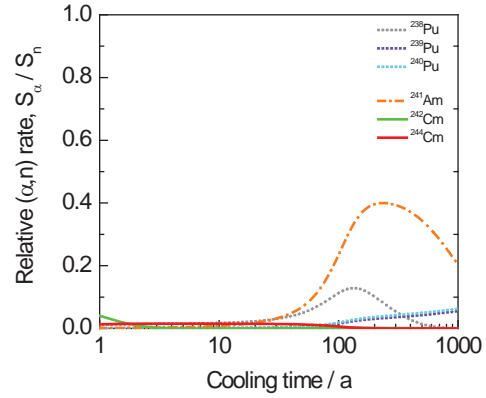
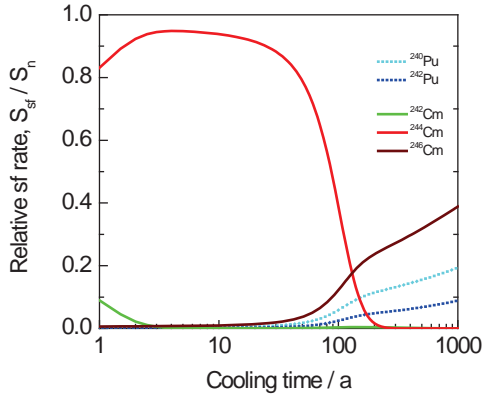
PWR  $UO_2$  pellet (5 g)  
 $^{235}U/U = 4.8\%$   
 burnup = 44 MWd/kg



### NEUTRON EMISSION BY SNF

$$S_n(t) = \sum_k (s_{sf,k} + s_{\alpha n,k}) N_k(t)$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg

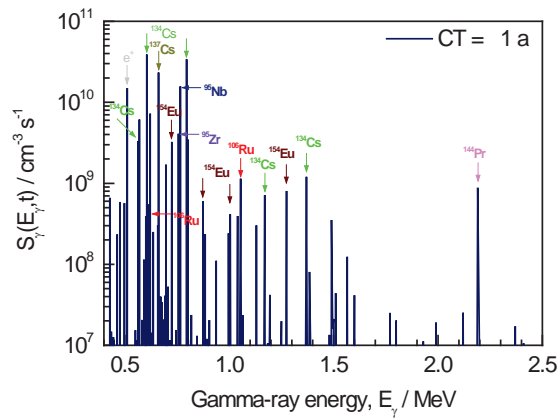


### GAMMA-RAY EMISSION BY SNF

$$S_\gamma(t) = \sum_k S_{\gamma,k}(E_\gamma, t)$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a

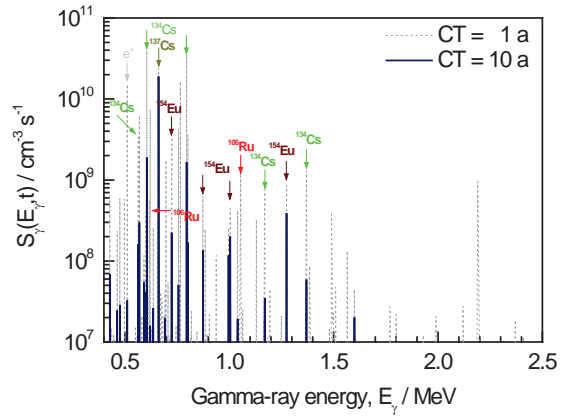


### GAMMA-RAY EMISSION BY SNF

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

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 burnup = 44 MWd/kg

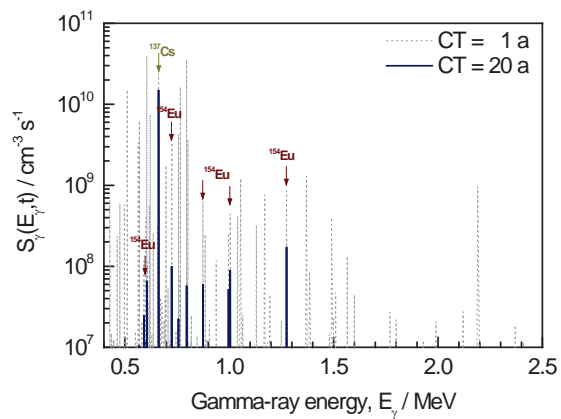


### GAMMA-RAY EMISSION BY SNF

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

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PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg

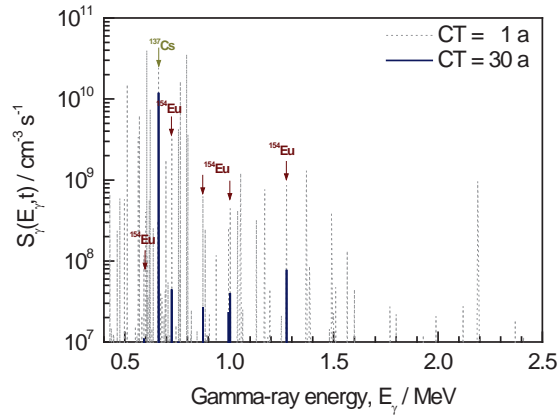


### GAMMA-RAY EMISSION BY SNF

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
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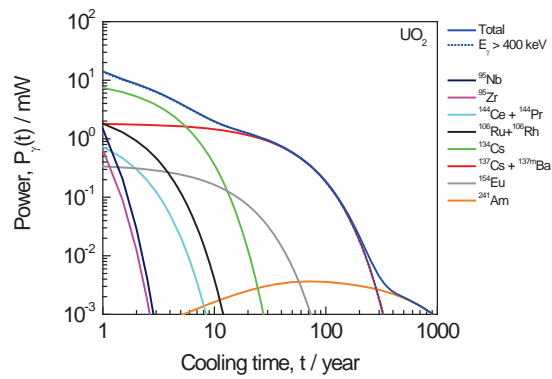


### GAMMA-RAY EMISSION BY SNF: DECAY POWER

$$P_{\gamma}(t) = \sum_k \lambda_k N_k(t) \int E_{\gamma} S_{\gamma,k}(E_{\gamma}, t) dE_{\gamma}$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a
<sup>241</sup> Am	432.6 a



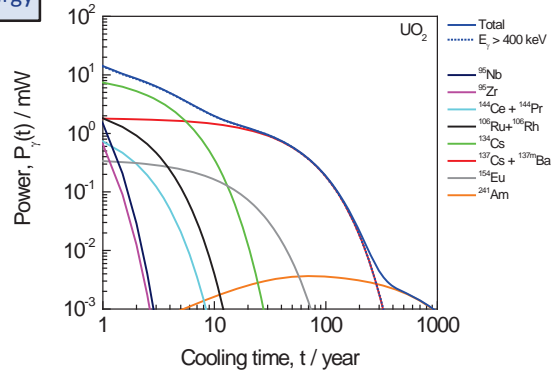
### GAMMA-RAY EMISSION BY SNF: DECAY POWER

$$P_\gamma(t) = \sum_k \lambda_k N_k(t) \int E_\gamma s_{\gamma,k}(E_\gamma, t) dE_\gamma$$

Recoverable energy

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a
<sup>241</sup> Am	432.6 a

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg

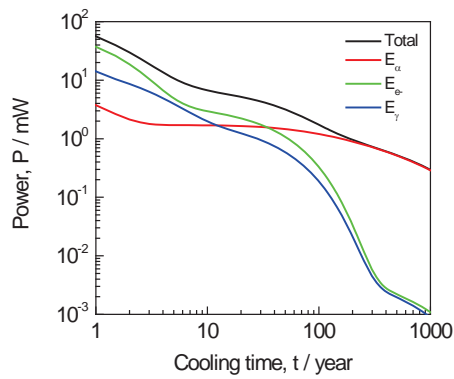


### DECAY POWER PRODUCED BY SNF (RECOVERABLE)

$$P(t) = \sum_k P_k(t)$$

- $P_k(t)$  : contribution of radionuclide k
- $P_k(t) = p_k N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $p_k$  : specific decay heat rate of nuclide k

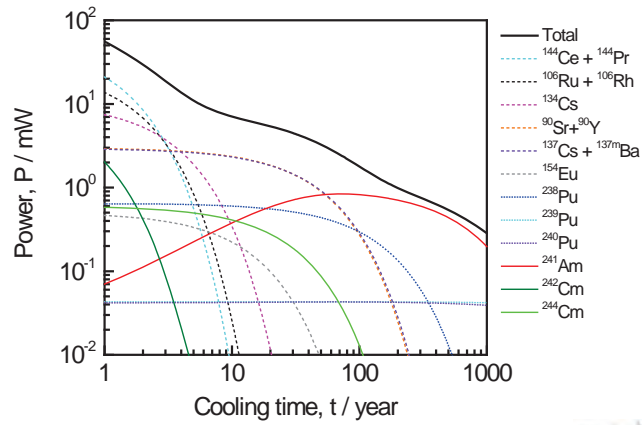
PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg



### DECAY POWER PRODUCED BY SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

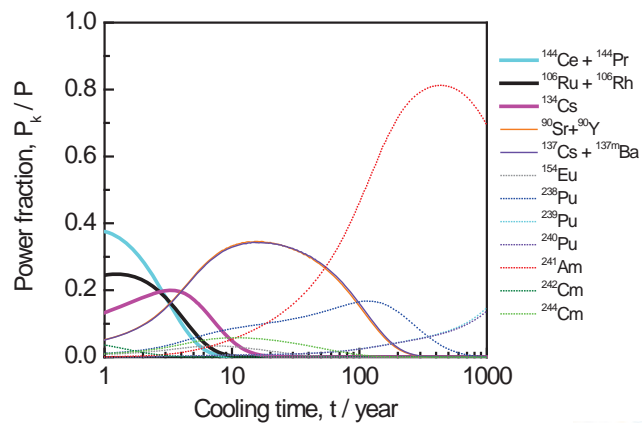
PWR UO<sub>2</sub> pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8 \%$   
 burnup = 44 MWd/kg



### DECAY POWER PRODUCED BY SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

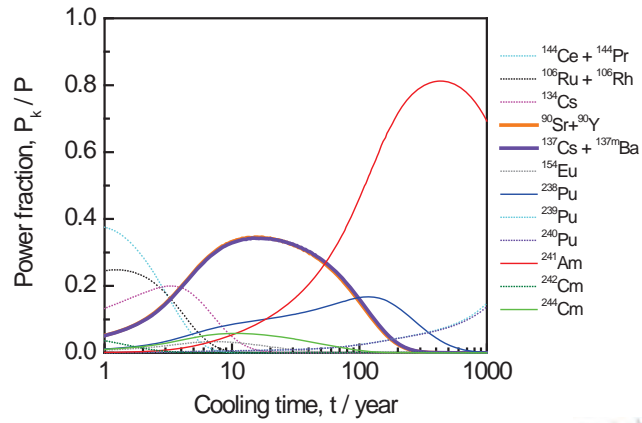
PWR UO<sub>2</sub> pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8 \%$   
 burnup = 44 MWd/kg



### DECAY POWER PRODUCED BY SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

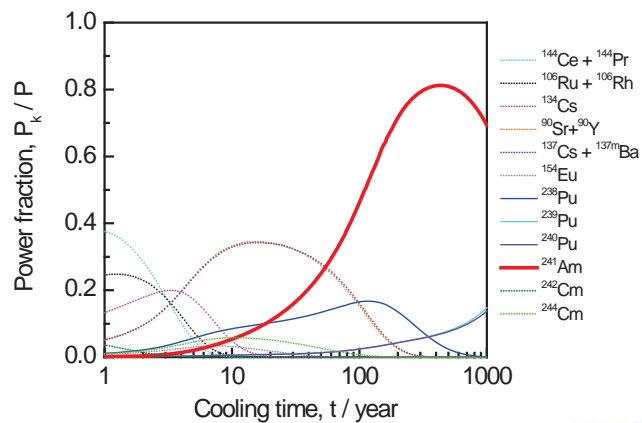
PWR UO<sub>2</sub> pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8 \%$   
 burnup = 44 MWd/kg



### DECAY POWER PRODUCED BY SNF

- $1 \text{ a} \leq t \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$

PWR UO<sub>2</sub> pellet (5 g)  
 $^{235}\text{U}/\text{U} = 4.8 \%$   
 burnup = 44 MWd/kg



### DECAY POWER PRODUCED BY SNF

$$P(t) = \sum_k p_k N_k(t)$$

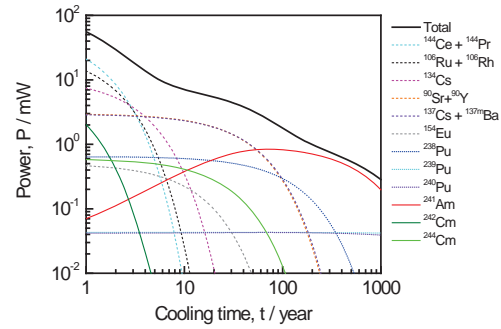
$P(t_2 > t_1)$  cannot be extrapolated from  $P(t_1)$

$N_k(t)$  : number of nuclei at time  $t$

- $N_k(t_0)$  : number of nuclei at time  $t_0$  with  $t > t_0$
- Nuclide vector at  $t > t_0$

$$\frac{dN_k}{dt} = \sum_i \lambda_i N_i - \lambda_k N_k$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 MWd/kg



### SNF SOURCE TERMS: NUCLIDE INVENTORY

Nuclide	Source term	CT
<sup>90</sup> Sr	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a
<sup>106</sup> Ru	H	1 a ≤ t ≤ 10 a
<sup>134</sup> Cs	H	1 a ≤ t ≤ 10 a
<sup>137</sup> Cs	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a
<sup>144</sup> Ce	H	1 a ≤ t ≤ 10 a
<sup>148</sup> Nd	Burn-up	stable
<sup>149</sup> Sm	Power	stable
<sup>154</sup> Eu	H, S <sub>γ</sub>	1 a ≤ t ≤ 10 a

Nuclide	Source term	CT
<sup>235</sup> U	R, S <sub>γ</sub>	10 <sup>5</sup> a ≤ t
<sup>238</sup> U	R, S <sub>γ</sub>	10 <sup>5</sup> a ≤ t
<sup>238</sup> Pu	H, S <sub>γ</sub>	10 a ≤ t
<sup>239</sup> Pu	R, S <sub>γ</sub>	100 a ≤ t ≤ 10 <sup>4</sup> a
<sup>240</sup> Pu	R, S <sub>γ</sub>	100 a ≤ t ≤ 10 <sup>4</sup> a
<sup>241</sup> Pu	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a
<sup>241</sup> Am	H	10 a ≤ t
<sup>242</sup> Cm	H, S <sub>n</sub>	1 a ≤ t ≤ 10 a
<sup>244</sup> Cm	H, S <sub>n</sub>	10 a ≤ t ≤ 100 a

H : decay heat rate (power)  
 S<sub>n</sub> : neutron emission  
 S<sub>γ</sub> : γ-ray emission  
 R : reactivity (criticality safety)

Nuclear safeguards

<sup>235</sup>U, Pu-isotopes

Criticality safety (Burn Up Credit, BUC):

<sup>95</sup>Mo, <sup>99</sup>Tc, <sup>101</sup>Ru, <sup>103</sup>Rh, <sup>109</sup>Ag, <sup>133</sup>Cs, <sup>143</sup>Nd, <sup>147,149,150,151,152</sup>Sm, <sup>155</sup>Gd

Long term safety:

<sup>14</sup>C, <sup>36</sup>Cl, <sup>79</sup>Se, <sup>94</sup>Nb, <sup>99</sup>Tc, <sup>129</sup>I, <sup>226</sup>Ra, <sup>237</sup>Np

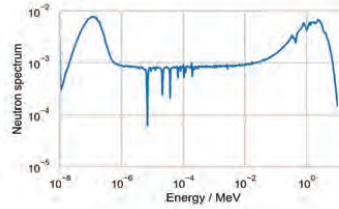
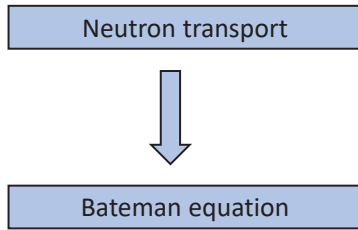
⇒ Requires **complex nuclide inventory** which can only be obtained by **theoretical calculations**





### THEORETICAL CALCULATIONS OF NUCLIDE INVENTORY

Depletion code: coupled neutron transport – nuclide depletion/creation calculations

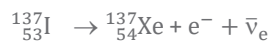
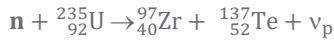


$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

Update nuclide vector

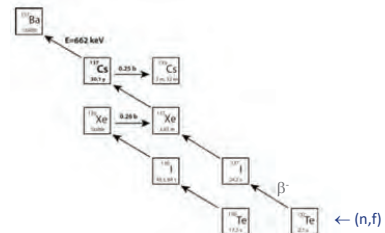


### EXAMPLE: PRODUCTION OF <sup>137</sup>Cs



<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> -decay (decay of short lived precursors)

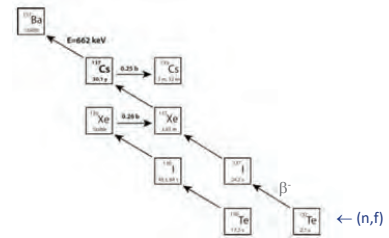
- Relatively long lived
- Small capture cross section



### PRODUCTION OF <sup>137</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

- $Y_c$  : cumulative fission yield
- $N_f$  : number of fissioning nuclei
- $N_i$  : number of nuclide i
- $\sigma_f$  : fission cross section
- $\sigma_{j \rightarrow k}$  : transmutation cross section (nuclide j to nuclide k)
- $\sigma_{k,a}$  : absorption cross section of nuclide k
- $\varphi$  : neutron fluence rate



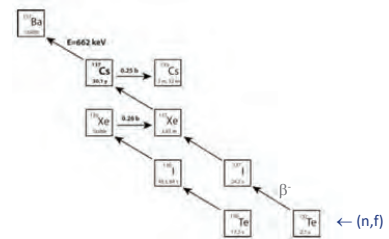
### PRODUCTION OF <sup>137</sup>Cs

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

$$N_k(t') \approx \frac{Y_c \sigma_f N_f \varphi}{\lambda_k + \sigma_{k,a} \varphi} [1 - e^{-(\lambda_k + \sigma_{k,a} \varphi)t'}]$$

<sup>137</sup>Cs production: only by (n,f) followed by β<sup>-</sup> -decay (decay of short lived precursors)

- $Y_c$  : cumulative fission yield
- $N_f$  : number of fissioning nuclei
- $N_i$  : number of nuclide i
- $\sigma_f$  : fission cross section
- $\sigma_{j \rightarrow k}$  : transmutation cross section (nuclide j to nuclide k)
- $\sigma_{k,a}$  : absorption cross section of nuclide k
- $\varphi$  : neutron fluence rate





### **<sup>137</sup>Cs: CONTRIBUTION TO DECAY HEAT RATE**

- Production at end of irradiation : cumulative fission yields + burnup

$$N_k(t_0) \propto Y_c \text{ BU}$$

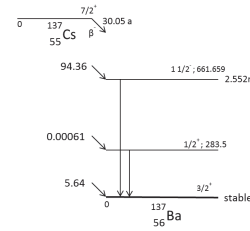
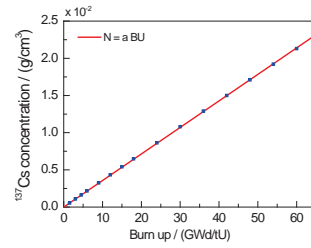
- Decay power after cooling time t by <sup>137</sup>Cs

$$P_k(t) = p_k N_k(t_0) e^{-\lambda_k (t-t_0)}$$

⇒ Nuclear data

- $Y_c$  : cumulative fission yields
- $\lambda_k$  : decay constant
- $E_{dk}$  : recoverable energy

⇒ Operational history : BU



### **<sup>137</sup>Cs : CONTRIBUTION TO THERMAL POWER (UNCERTAINTY EVALUATION)**

$$P_k(t) = p_k N_k(t_0) e^{-\lambda_k (t-t_0)}$$

$$N_k(t_0) \propto Y_c \text{ BU}$$

$$p_k = E_{dk} \lambda_k$$

$$\Rightarrow \frac{u_{P_k}}{P_k} = \sqrt{\left(\frac{u_{\text{BU}}}{\text{BU}}\right)^2 + \left(\frac{u_{Y_c}}{Y_c}\right)^2 + \left(\frac{u_{E_{dk}}}{E_{dk}}\right)^2}$$

• Nuclear data

- $Y_c$  : cumulative fission yields
- $E_{dk}$  : recoverable energy
- $\lambda_k$  : decay constant (small uncertainty)

• Operational history : BU

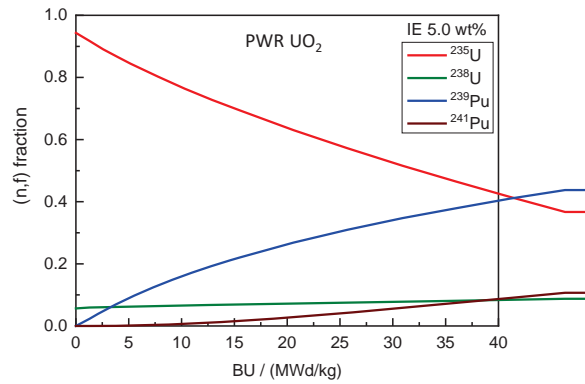
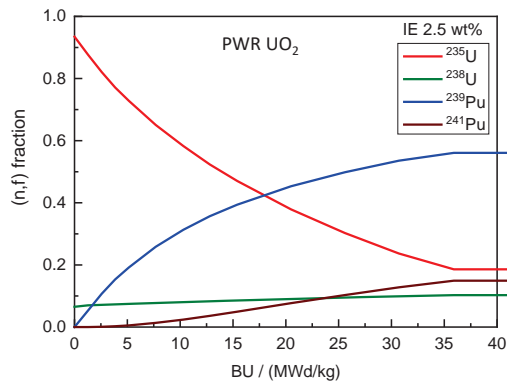
Note:

Production of e.g <sup>134</sup>Cs more complex  $\propto \text{BU}^b$  with  $b \sim 2$

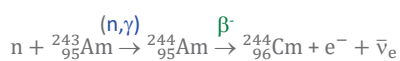
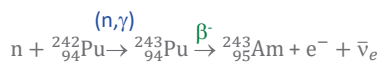
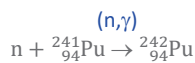
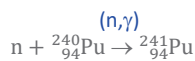
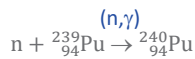
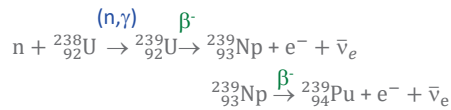
$$\Rightarrow \frac{u_{N_k}}{N_k} = 2 \frac{u_{\text{BU}}}{\text{BU}}$$



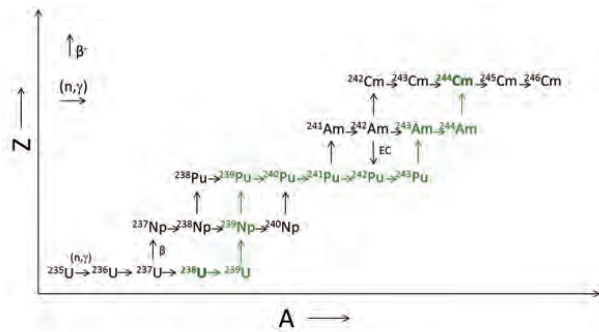
**<sup>137</sup>Cs: CONTRIBUTION OF <sup>235</sup>U, <sup>239</sup>Pu AND <sup>241</sup>Pu**



**<sup>244</sup>Cm PRODUCTION: COMPLEX PROCESS**



- Sequence of
- (n,γ) reactions (6)
  - β<sup>-</sup> decays (4)

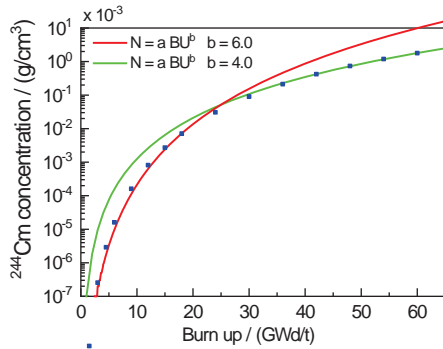


Training material

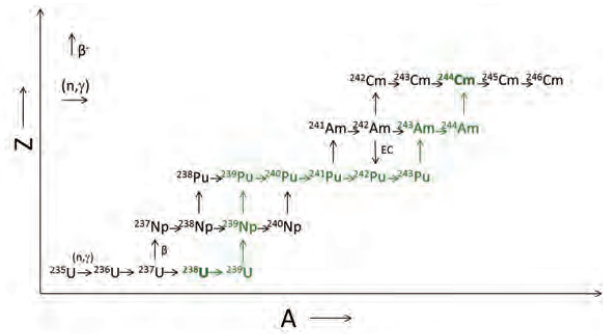


### <sup>244</sup>Cm PRODUCTION: COMPLEX PROCESS

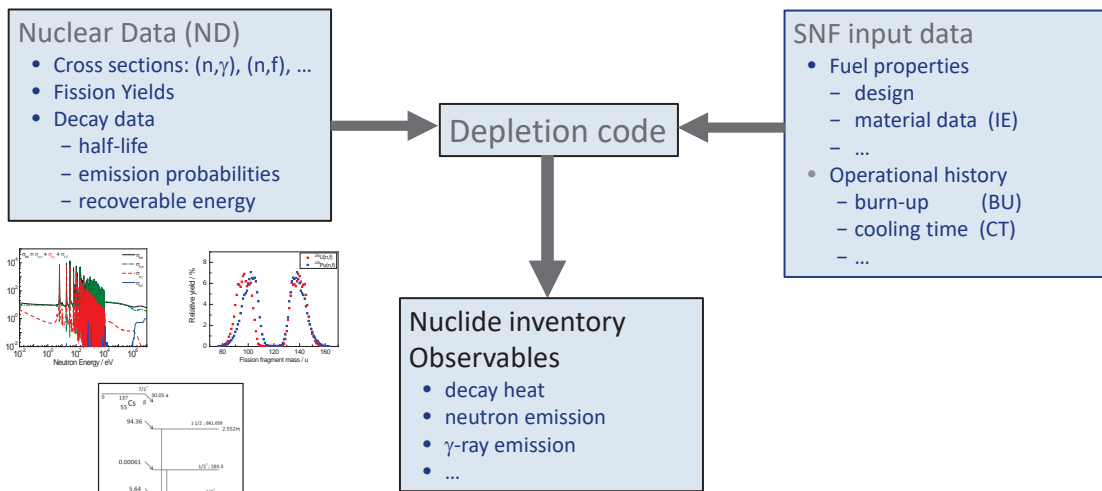
$$^{244}\text{Cm} : N = a\text{BU}^b \quad \frac{\delta N}{N} = b \frac{\delta \text{BU}}{\text{BU}}$$



- Sequence of
- (n,γ) reactions (6)
  - β<sup>-</sup> decays (4)



### TASK 2: PRODUCE VALIDATED DEPLETION CALCULATIONS WITH REALISTIC UNCERTAINTIES



## DEPLETION CODES

- SCALE System (ORNL)
  - Neutron transport : KENO (MC) and NEWT, POLARIS (deterministic)
  - Depletion/creation module : ORIGEN
- ALEPH2 (SCK CEN)
  - Neutron transport by MCNP
- SERPENT (VTT)
- DARWIN (CEA)
- EVOLCODE (CIEMAT)



## DEPLETION CODES

- Nuclide vector  $N(t_0)$  at time  $t_0$  (end of irradiation) by depletion calculations
  - **Nuclear Data (ND)**
    - Cross sections
    - Fission yields
    - Neutron emission probabilities
    - Decay data
  - **Fuel History (FH)**
    - Fuel fabrication data (design, composition) e.g. Initial enrichment (IE)
    - Reactor operation and irradiation conditions e.g. Burnup (BU)
    - Cooling time (CT)

- Nuclide vector at  $t > t_0$

$$\frac{dN_k}{dt} = \sum_{i \rightarrow k} \lambda_i N_i - \lambda_k N_k$$

- Observables at  $t > t_0$

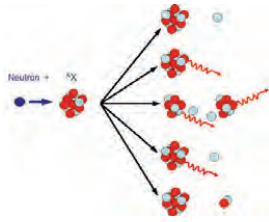
e.g.  $P(t) = \sum_k p_k N_k(t)$

Depends on **well-known decay data**

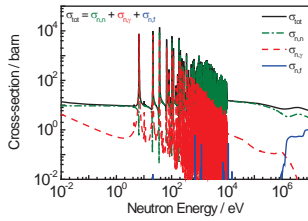


### BURNUP CODES: NUCLEAR DATA

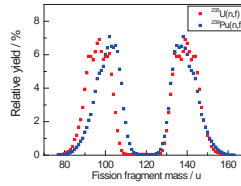
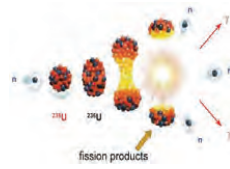
Neutron induced interaction cross sections



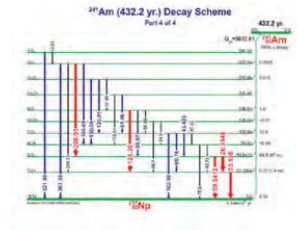
- elastic scattering : (n,n)
- capture: (n,γ)
- fission : (n,f)
- inelastic scattering : (n,n'γ)
- others: e.g. (n,p), (n,α), ...



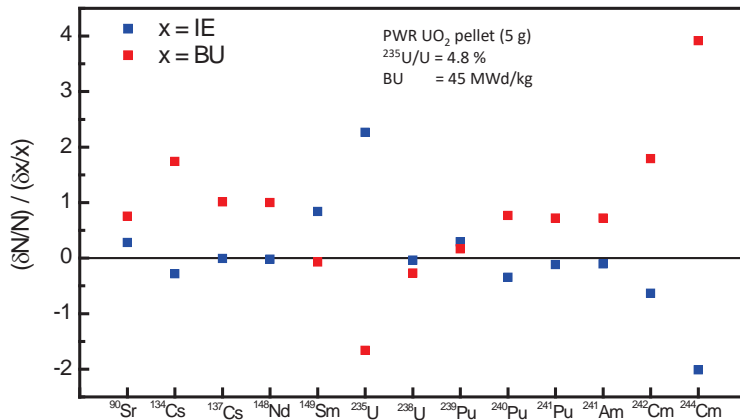
Fission process



Decay data



### NUCLIDE INVENTORY: DESIGN AND OPERATIONAL HISTORY



$$^{244}\text{Cm} : N = a\text{BU}^b$$

$$b \approx 4 \text{ for BU} = 45 \text{ MWd/kg}$$

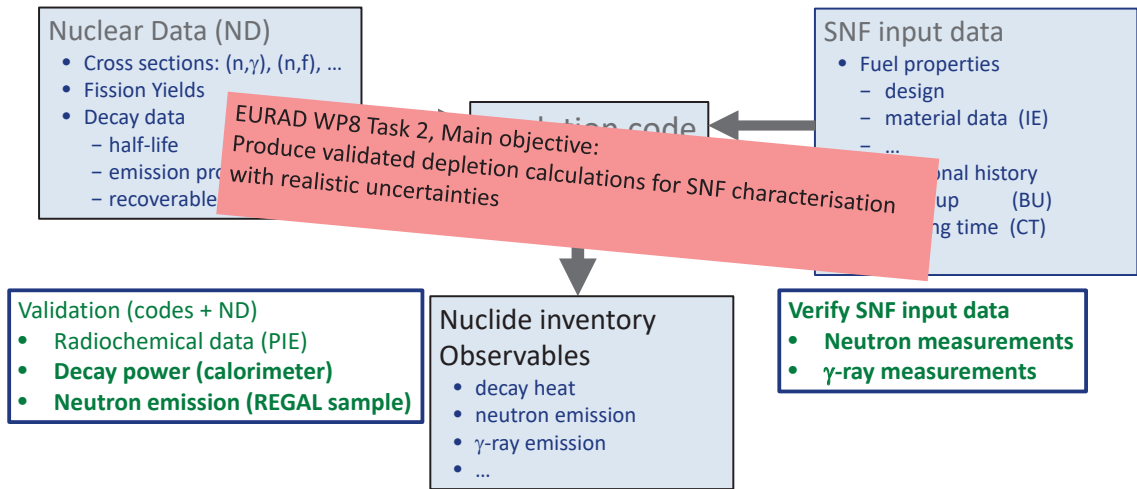
$$\frac{\delta N}{N} = b \frac{\delta \text{BU}}{\text{BU}}$$

0.5 % uncertainty on BU  
 ⇒ 2 % uncertainty on <sup>244</sup>Cm inventory

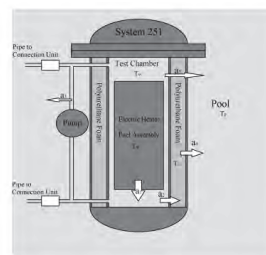
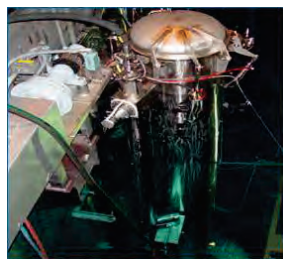




### TASK 2: PRODUCE VALIDATED DEPLETION CALCULATIONS WITH REALISTIC UNCERTAINTIES



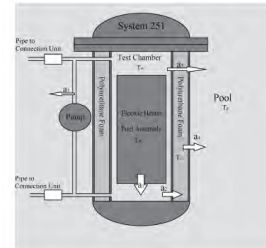
### CLAB CALORIMETER



### CLAB CALORIMETER: PRINIPLE

#### Measurement principle

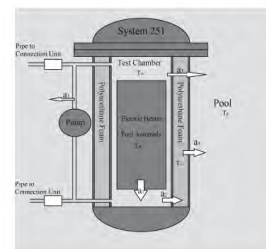
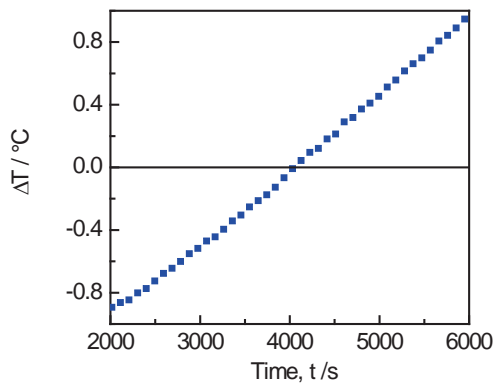
- Cool down the water in calorimeter
- Stop cooling (continue circulation)



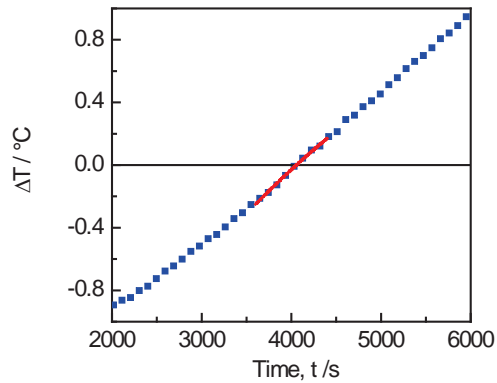
### CLAB CALORIMETER: PRINIPLE

#### Measurement principle

- Cool down the water in calorimeter
- Stop cooling (continue circulation)
- Measure  $T_c$  and  $T_p$ 
  - $T_c$  : temperature in calorimeter
  - $T_p$  : temperature in pool
- Determine  $\Delta T = T_c - T_p$  vs time

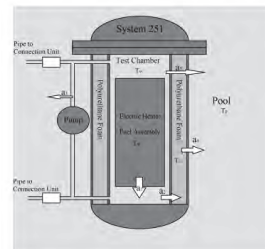


### CLAB CALORIMETER: PRINCIPLE

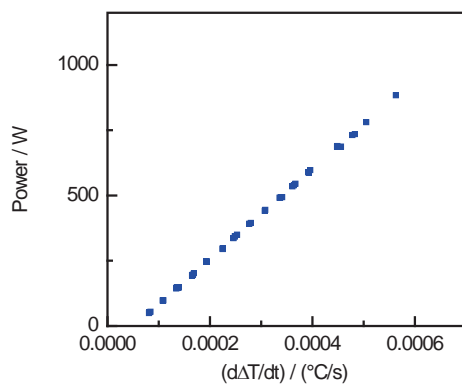


#### Measurement principle

- Cool down the water in calorimeter
- Stop cooling (continue circulation)
- Measure  $T_c$  and  $T_p$
- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$

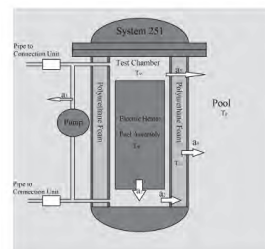


### CLAB CALORIMETER: PRINCIPLE

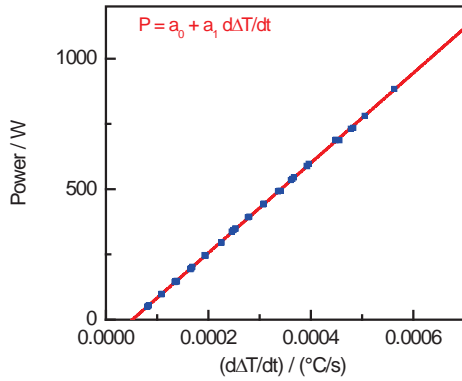


#### Calibration with an electrical heater

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$  for different P

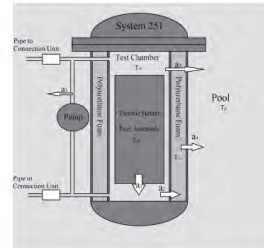


### CLAB CALORIMETER: PRINCIPLE

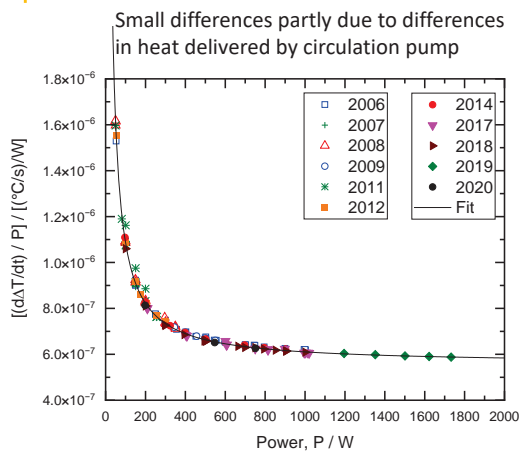


Calibration with an electrical heater

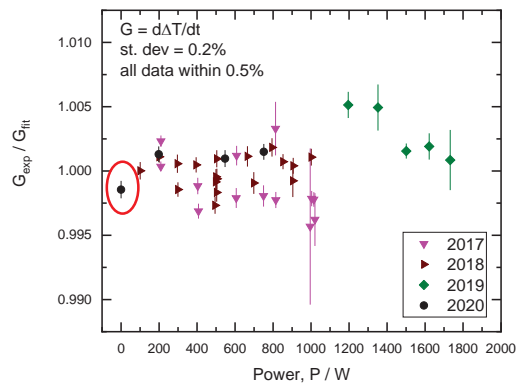
- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$
- Fit to data:  $P = a_0 + a_1 d\Delta T/dt$



### ELECTRICAL HEATER: CALIBRATION FUNCTION



Calibration for blind test and SKB-50 data



Perfect linear behaviour in whole range: from 0 W to 1800 W  
 Measurement without heater (heat delivered by circulation pump): fully consistent



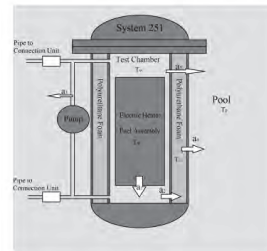
## CLAB CALORIMETER: PRINCIPLE

### Spent nuclear fuel assembly

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  when  $\Delta T = 0$
- $Q = a_0 + a_1 K d\Delta T/dt$
- $P = Q + P_\gamma$ 
  - $K$  : correction factor due to thermal capacity difference between electrical heater and fuel assembly
  - $P_\gamma$  : heat loss due to  $\gamma$ -rays escaping from the calorimeter

### Calibration with an electrical heater

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$
- Fit to data:  $P = a_0 + a_1 d\Delta T/dt$



## CLAB CALORIMETER: PRINCIPLE

### Spent nuclear fuel assembly

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  when  $\Delta T = 0$
- $Q = a_0 + a_1 K d\Delta T/dt$
- $P = Q + P_\gamma$ 
  - $K$  : correction factor due to thermal capacity difference between electrical heater and fuel assembly
  - $P_\gamma$  : heat loss due to  $\gamma$ -rays escaping from the calorimeter

- BWR:  $P = 140$  W
  - $P_\gamma = 3.3$  W (2.4%)
  - $K = 0.964$
- PWR:  $P = 450$  W
  - $P_\gamma = 11.8$  W (2.6%)
  - $K = 0.915$



### DATA FROM CLAB CALORIMETER: SOME RESULTS

Ref.	Year	Code	Library	PWR		BWR	
				<C/E>	St. dev	<C/E>	St. dev
Ilas and Gauld	2008	SCALE 5.1	ENDF/B-V	1.011	0.012	1.003	0.025
Ilas et al.	2014	SCALE 6.1.2	ENDF/B-VII.0	1.002	0.012	0.997	0.024
Ilas and Burns	2021	SCALE 6.2.4	ENDF/B-VII.0	1.013	0.013	1.002	0.012
	2021	SCALE 6.2.4	ENDF/B-VII.1	1.008	0.012	1.009	0.024
Ilas and Burns	2022	SCALE 6.3	ENDF/B-VIII.0	1.006	0.014	1.007	0.024
Shama et al.	2022	SCALE 6.2.3	ENDF/B-VII.1	1.019	0.012	1.003	0.025
		SCALE 6.2.3 (POLARIS)	ENDF/B-VII.1	1.015	0.012	1.010	0.026
Shama et al.	2022	CASMO5		1.009	0.013	1.008	0.025
Yamamoto	2016	CASMO5	JENDL-4.0	1.016	0.013	1.001	0.024
Haeck et al.	2022	VESTA 2.1	JEFF-3.1	0.978	0.012		
		VESTA 2.1	ENDF/B-VII.0	0.996	0.012		
San-Felice et al.	2012	DARWIN	JEFF-3.1.1	0.978	0.011		

Not blind!  
 Normalisation not specified  
 Adjustments not excluded



### BLIND TEST CLAB CALORIMETER

NUCLEAR SCIENCE AND ENGINEERING - VOLUME 196 - 1125-1145 - SEPTEMBER 2022  
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 DOI: <https://doi.org/10.1080/00295639.2022.2053489>

**Blind Benchmark Exercise for Spent Nuclear Fuel Decay Heat**



- PWR assemblies
- Decay heat rate determined at CLAB

Assembly ID	BU	CT	IE	Decay heat rate	Gamma-escape
BT01	53 MWd/kg	4.5 a	3.95 wt%	1662 W	58 W
BT02	55 MWd/kg	8.6 a	3.95 wt%	1068 W	30 W
BT03	50 MWd/kg	9.8 a	3.95 wt%	895 W	21 W
BT04	51 MWd/kg	13.5 a	3.70 wt%	768 W	15 W
BT05	50 MWd/kg	21.4 a	3.60 wt%	663 W	12 W



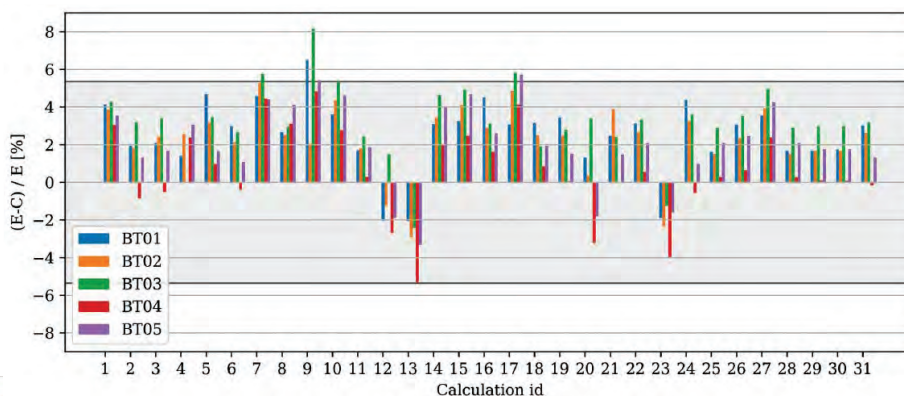
### BLIND TEST CLAB CALORIMETER: CODES + LIBRARIES

Code	Library	Appendix Section
ALEPH 2.7.2	ENDF/B-VII.1	A.I.A
APOLLO2.8/DARWIN2.3	JEFF-3.1.1	A.I.B
CASMO-4E + ORIGEN-S	JEFF-2.2	A.I.C
CASMO-5 (2.03)	ENDF/B-VII.1	A.I.D
CASMO-5 (2.12.00) + SNF (1.07.02)	ENDF/B-VII.1	A.I.E
DRAGON 4.0.5	ENDF/B-VII.1	A.I.F
EVOLCODE (MCNP + ACAB)	JEFF-3.3	A.I.G
MCNP-CINDER + Nukleonika (2D)	ENDF/B-VII.1	A.I.H
Monteburns v3 + CINDER	ENDF/B-VII.1	A.I.I
MOTIVE (KENO-VI + VENTINA)	ENDF/B-VII.1	A.I.J
MOTIVE (OpenMC + VENTINA)	ENDF/B-VIII	A.I.K
MVP 3	ENDF/B-VII.1	A.I.L
MVP 3	JEFF-3.2	A.I.M
MVP 3	JENDL-4.0	A.I.N
OREST	JEF-2.2 + ENDF/B-VI	A.I.O
SCALE 6.0: ORIGEN-ARP	ENDF/B-V	A.I.P
SCALE 6.1.3: ORIGEN-ARP	ENDF/B-V	A.I.Q
SCALE 6.2.3: ORIGAMI	ENDF/B-VII.1	A.I.P
SCALE 6.2.3: Polaris	ENDF/B-VII.1	A.I.R
SCALE 6.2.3: ORIGEN	ENDF/B-VII.1	A.I.R
SCALE 6.2.3: TRITON/KENO	ENDF/B-VII.1	A.I.S
SCALE 6.2.3: TRITON/NEWT	ENDF/B-VII.1	A.I.T
SEADep	JEFF-3.1.1	A.I.U
Serpent 2.1.29	ENDF/B-VII.1	A.I.V
Serpent 2.1.29	JEFF-3.1.1	A.I.W
Serpent 2.1.31	JEFF-3.2 + JEFF-3.1.1	A.I.X



### BLIND TEST CLAB CALORIMETER: RESULTS

Assembly ID	P	CT	<C/E>	St. dev
BT01	1662 W	4.5 a	0.975	0.019
BT02	1068 W	8.6 a	0.977	0.018
BT03 (+ Gd)	895 W	9.8 a	0.967	0.019
BT04	768 W	13.5 a	0.994	0.023
BT05	663 W	21.4 a	0.979	0.021



### DATA FROM CLAB CALORIMETER (R-05-62)

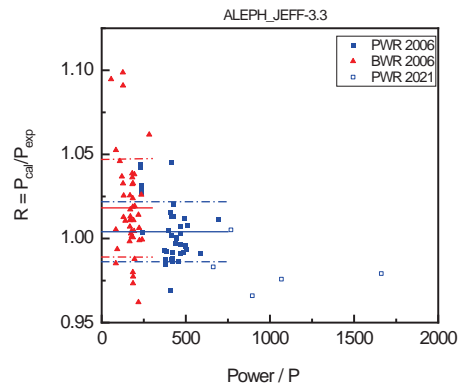
#### EURAD Task 2: systematic study of published calorimeter data

Compare different codes/libraries

- Total number of fissions
- Inventory of key nuclides
- Calculate decay power using recommended decay data

Paper in preparation  
 Romojaro et al., SCK CEN, CEA, GRS, IRSN, JSI, JRC, NAGRA, PSI

Code	Library	PWR		BWR	
		<C/E>	St. dev	<C/E>	St. dev
SCALE	(R-05-62)	1.011	0.012	1.003	0.025
ALEPH2	JEFF-3.1.2	1.001	0.020	1.013	0.031
ALEPH2	JEFF-3.3	1.004	0.018	1.018	0.029
ALEPH2	JEFF-4T0	1.006	0.018	1.020	0.030



EURAD Task 2:  
 additional blind test exercise using SKB-50 data



### <sup>137</sup>Cs : CONTRIBUTION TO THERMAL POWER (UNCERTAINTY EVALUATION)

$$P_k(t) = p_k N_k(t_0) e^{-\lambda_k (t-t_0)} \quad N_k(t_0) \propto Y_c BU \quad p_k = E_{dk} \lambda_k$$

$$\Rightarrow \frac{u_{P_k}}{P_k} = \sqrt{\left(\frac{u_{BU}}{BU}\right)^2 + \left(\frac{u_{Y_c}}{Y_c}\right)^2 + \left(\frac{u_{E_{dk}}}{E_{dk}}\right)^2}$$

- Nuclear data
  - $Y_c$  : cumulative fission yields
  - $E_{dk}$  : recoverable energy
  - $\lambda_k$  : decay constant (small uncertainty)

Note:

Production of e.g <sup>134</sup>Cs more complex  $\propto BU^b$  with  $b \sim 2$

$$\Rightarrow \frac{u_{N_k}}{N_k} = 2 \frac{u_{BU}}{BU}$$

- Operational history : BU





### <sup>137</sup>Cs: γ-RAY EMISSION AND DECAY HEAT RATE (POWER)

- Production : cumulative fission yields + burnup

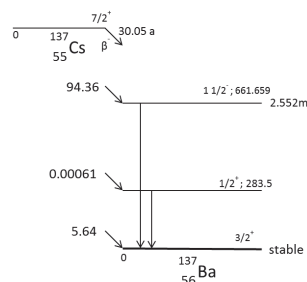
$$N_k(t_0) \sim Y_c \text{ BU}$$

- Gamma-ray emission : (decay data)

- $T_{1/2}$  : 30.05 (8) a
- $P(E_\gamma = 661.66\text{keV})$  : 0.8499 (20)

- Specific decay heat rate,  $p_k = E_{dk} \lambda_k$  (decay data)

- $T_{1/2}$  : 30.18 (15) a
- $Q_{\beta^-}$  : 1175.63 (17) keV
- Recoverable energy
  - Average electron + recoil energy : 247.9 (12) keV
  - $\langle E_\gamma \rangle$  : 565.4 (13) keV



Decay data from DDEP (Decay Data Evaluation Project) <http://www.nucleide.org/DDEP.htm>



### <sup>137</sup>Cs : NUCLEAR DATA ( $Y_c, E_d$ ) FOR <sup>235</sup>U(n,f) AT THERMAL ENERGY

Library	$E_d$ / keV	Ratio	<sup>137</sup> Cs		$(Y_c \times E_d)$ / keV	Ratio
			$100 \times Y_c$	Ratio		
DDEP/IAEA	811.8 (18)	1	6.221 (69)	1	50.5 (6)	1
JEF-2.2	812.0 (69)	1.000 (8)	6.244 (54)	1.004 (9)	50.7 (6)	1.004 (12)
JEFF-3.1.1	<b>810.1 (23)</b>	<b>0.998 (3)</b>	<b>6.221 (69)</b>	<b>1.000 (11)</b>	<b>50.4 (6)</b>	<b>0.998 (11)</b>
JEFF-3.3	<b>801.8 (23)</b>	<b>0.988 (3)</b>	<b>6.090 (63)</b>	<b>0.979 (10)</b>	<b>48.8 (5)</b>	<b>0.967 (10)</b>
ENDF/B-VI.8	813.4 (41)	1.002 (5)	6.188 (31)	0.995 (5)	50.3 (4)	0.997 (7)
ENDF/B-VII.0	805.7 (16)	0.992 (2)	6.188 (31)	0.995 (5)	49.9 (3)	0.987 (5)
ENDF/B-VIII.0	<b>805.8 (18)</b>	<b>0.993 (2)</b>	<b>6.188 (31)</b>	<b>0.995 (5)</b>	<b>49.9 (3)</b>	<b>0.987 (5)</b>



**<sup>90</sup>Sr and <sup>137</sup>Cs: NUCLEAR DATA ( $\gamma_c, E_d$ ) FOR <sup>235</sup>U(n,f) AT THERMAL ENERGY**

Library	<sup>90</sup> Sr		<sup>137</sup> Cs	
	( $E_d \times \gamma_c$ ) / keV	Ratio	( $\gamma_c \times E_d$ ) / keV	Ratio
DDEP/IAEA	64.7 (15)	1	50.5 (6)	1
JEF-2.2	<b>66.0 (21)</b>	<b>1.021 (33)</b>	<b>50.7 (7)</b>	<b>1.004 (12)</b>
JEFF-3.1.1	63.5 (15)	0.981 (23)	50.4 (6)	0.998 (11)
JEFF-3.3	<b>64.0 (15)</b>	<b>0.989 (23)</b>	<b>48.8 (5)</b>	<b>0.967 (10)</b>
ENDF/B-VI.8	65.3 (7)	1.010 (10)	50.3 (4)	0.997 (7)
ENDF/B-VII.0	65.3 (7)	1.009 (10)	49.9 (3)	0.987 (5)
ENDF/B-VIII.0	<b>65.3 (7)</b>	<b>1.009 (10)</b>	<b>49.9 (3)</b>	<b>0.987 (5)</b>



**<sup>90</sup>Sr and <sup>137</sup>Cs: NUCLEAR DATA ( $\gamma_c, E_d$ ) FOR <sup>235</sup>U(n,f) AT THERMAL ENERGY**

EPRI, PIRT, July 2020

Library	<sup>90</sup> Sr		<sup>137</sup> Cs	
	( $E_d \times \gamma_c$ ) / keV	Ratio	( $\gamma_c \times E_d$ ) / keV	Ratio
DDEP/IAEA	64.7 (15)	1	50.5 (6)	1
JEF-2.2	<b>66.0 (21)</b>	<b>1.021 (33)</b>	<b>50.7 (7)</b>	<b>1.004 (12)</b>
JEFF-3.1.1	63.5 (15)	0.981 (23)	50.4 (6)	0.998 (11)
JEFF-3.3	<b>64.0 (15)</b>	<b>0.989 (23)</b>	<b>48.8 (5)</b>	<b>0.967 (10)</b>
ENDF/B-VI.8	65.3 (7)	1.010 (10)	50.3 (4)	0.997 (7)
ENDF/B-VII.0	65.3 (7)	1.009 (10)	49.9 (3)	0.987 (5)
ENDF/B-VIII.0	<b>65.3 (7)</b>	<b>1.009 (10)</b>	<b>49.9 (3)</b>	<b>0.987 (5)</b>

Table 5.5  
Summary of Uncertainty in Calculated Decay Heat [17] for BWR Assembly at 37 GWd/MTU Burnup and 15.6 Years' Cooling Time

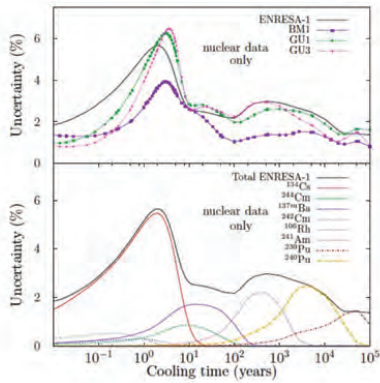
Perturbed Parameter Set	Relative Uncertainty (%)
Fuel design data	0.2
Operating history data	0.8
Nuclear cross-section data	0.9
Fission yield data	0.3
<b>Overall uncertainty</b>	<b>1.3</b>

$u_p/P = 1.3\%$ , is this realistic? **NO**



## <sup>90</sup>Sr and <sup>137</sup>Cs: NUCLEAR DATA ( $\gamma_c, E_d$ ) FOR <sup>235</sup>U(n,f) AT THERMAL ENERGY

Uncertainty only due to nuclear data > 2%



ENRESA-1: BWR  
 BM1 : MOX  
 GU1 : PWR  
 GU3 : PWR

EPRI, PIRT, July 2020

Table 5-5  
 Summary of Uncertainty in Calculated Decay Heat [17] for BWR Assembly at 37 GWd/MTU Burnup and 15.6 Years' Cooling Time

Perturbed Parameter Set	Relative Uncertainty (%)
Fuel design data	0.2
Operating history data	0.8
Nuclear cross-section data	0.9
Fission yield data	0.3
<b>Overall uncertainty</b>	<b>1.3</b>

$u_p/P = 1.3\%$ , is this realistic? **NO**

EURAD WP8 Task 2

- Rochman et al., Annals of Nuclear Energy 160 (2021) 108539
- Rochman et al., EPJ Nuclear Sci. Technol. 7 (2021) 18
- Rochman et al., EPJ Nuclear Sci. Technol. 8 (2022) 9



## UNCERTAINTY OF CALORIMETRY DATA

- Blind test paper (Jansson et al., Nucl. Sci. Eng. 196 (2022) 1125)

5% overall uncertainty

- SKB Document R-05-62 (also used in EPRI, PRIT report)

- PWR	
250 W	1.8 %
900 W	1.0 %
- BWR	
50 W	4.2 %
350 W	1.0 %

⇒ Performance assessment and uncertainty evaluation of CLAB calorimeter is required  
 ⇒ One of the main EURAD objectives of WP8 Task 2

Only total (combined uncertainties) are given  
 No separation between

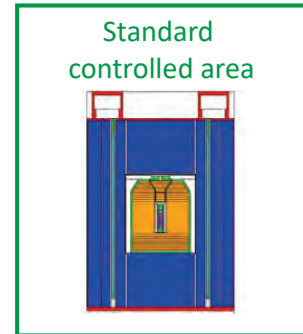
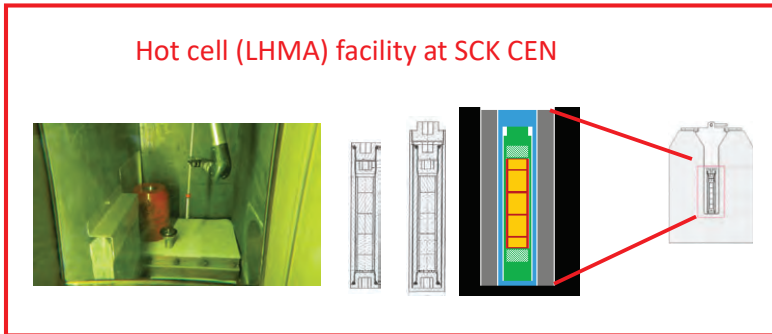
- Systematic and random effects
- Correlated and uncorrelated uncertainty components



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

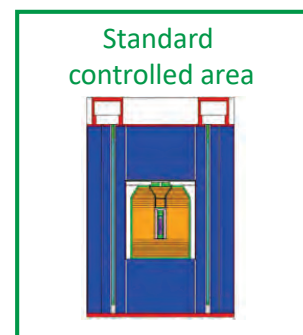
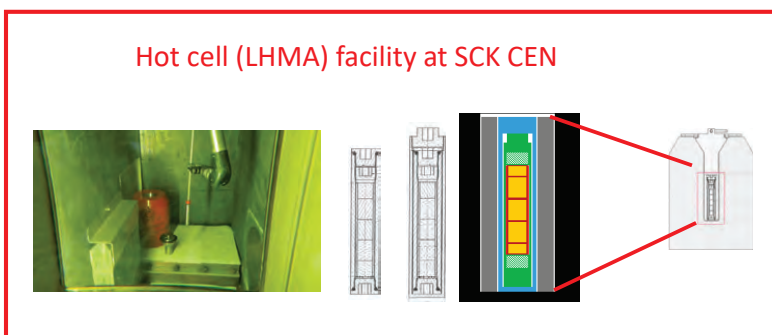
**Non Destructive Assay method** to determine the neutron output of a **SNF** sample under **standard controlled area** conditions

Collaboration SCK CEN



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

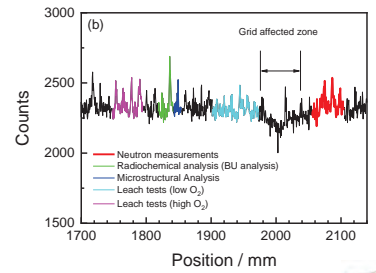
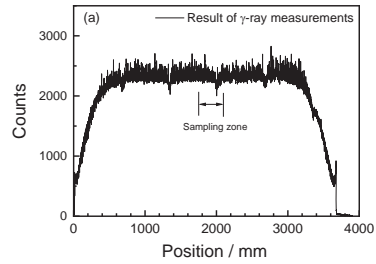
Databook of flat burnup samples from rod D05 extracted from fuel assembly FT1X57, Tihange 1 NPP  
Data on fuel initial composition and irradiation history  
Authors: S. Swinnen, M. Spasari  
Affiliation: IMGP/IMA SCK CEN



## EURAD: VALIDATION OF DEPLETION CODES USING THE REGAL SAMPLE

- **Irradiation history** of the SNF
  - Segment (~ 50 mm) from rod D05 of FT1X57 (PWR)
  - PWR Assembly (15 x 15):  
188 UO<sub>2</sub> rod (4.5 wt% <sup>235</sup>U/U) and 16 (U,Gd)O<sub>2</sub> rods
  - Irradiated at Tihange 1
  - Rod used for other international project (First-Nuclides, REGAL, WETFUEL & AGAF, SF-ALE)

- **SNF segment sample** by **NDA**  
Part of a set of 4 samples (REGAL project)
  - **Radiochemical analysis (BU)**
  - Microstructural analysis
  - Leach tests (low O<sub>2</sub>)
  - Leach tests (high O<sub>2</sub>)



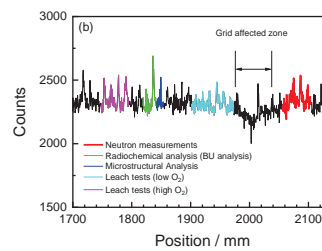
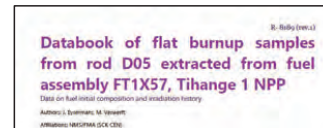
## NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

- Irradiation history burnup (REGAL project)

BU indicator	Analysis date	Nuclide Inventory N <sub>x</sub> /N <sub>0</sub>	BU MWd/kg
<sup>137</sup> Cs	21/10/2013	2.539 (55) × 10 <sup>-3</sup>	52.6 (11)
<sup>143+144</sup> Nd	05/02/2014	5.701 (60) × 10 <sup>-3</sup>	53.95 (56)
<sup>145+146</sup> Nd	05/02/2014	3.643 (38) × 10 <sup>-3</sup>	53.05 (56)
<sup>148</sup> Nd	05/02/2014	0.974 (21) × 10 <sup>-3</sup>	53.3 (12)
<sup>150</sup> Nd	05/02/2014	0.463 (21) × 10 <sup>-3</sup>	52.2 (23)
Average:			52.78 (37)

- SNF segment sample: characteristics

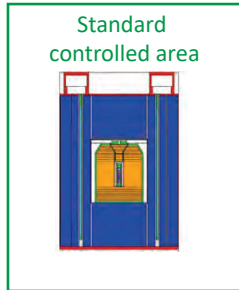
Parameter	Value
Segment length	52.01 (4) mm
Segment weight	42.616 (1) g
Cladding weight	6.71 (4) g
Net fuel weight	35.91 (4) g



⇒ Accurate information about design and operational history

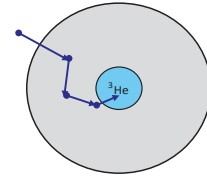


## NEUTRON EMISSION MEASUREMENT: CONVENTIONAL WELL COUNTER (AWCC)

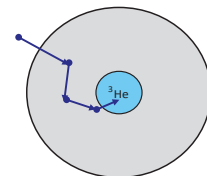
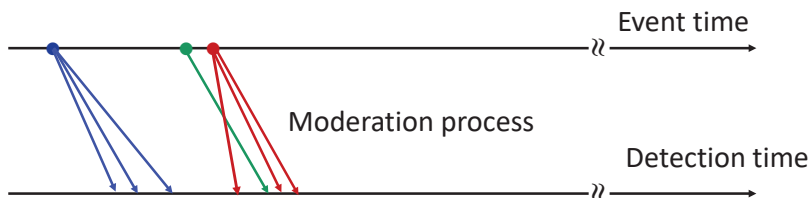


- Neutron detection
  - Modified AWCC (only internal cavity)
  - $^3\text{He}$  detectors in polyethylene
  - Detection efficiency for  $^{252}\text{Cf(sf)}$ :  $\epsilon = 0.28$
- Signal processing: shift register
  - Totals, reals and accidentals
- Data analysis: Hage’s point model (JRC Ispra)

W. Hage and D.M. Cifarelli, NSE 89 (1985) 159 – 176  
 W. Hage and D.M. Cifarelli, NIMA 236 (1985) 165 – 177  
 D.M. Cifarelli and W. Hage, NIMA 251 (1986) 550 – 563



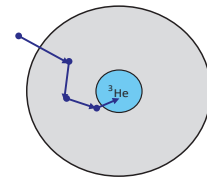
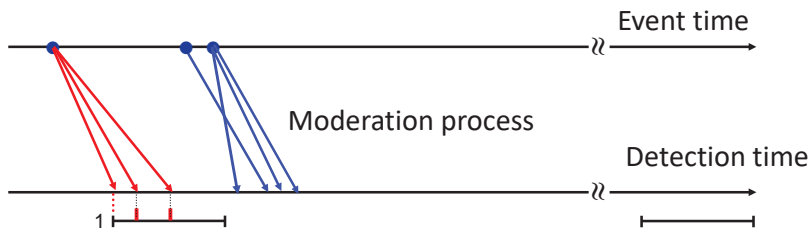
## SHIFT – REGISTER: PRINCIPLE



- Every detected neutron will trigger the opening of two gates
- Gate close to the signal (signal trigger)
  - Delayed gate



**SHIFT – REGISTER: PRINCIPLE**

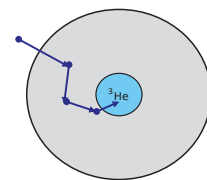
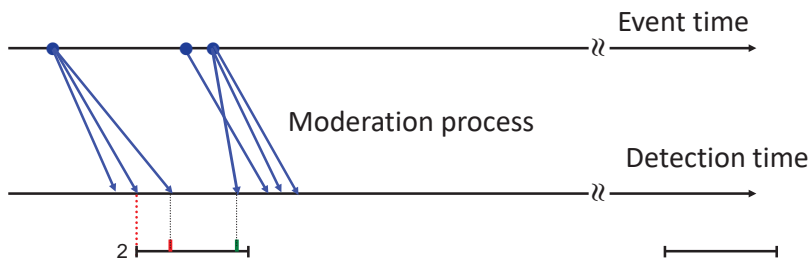


Signal trigger  
**R + A**

Delayed trigger  
**A**



**SHIFT – REGISTER: PRINCIPLE**

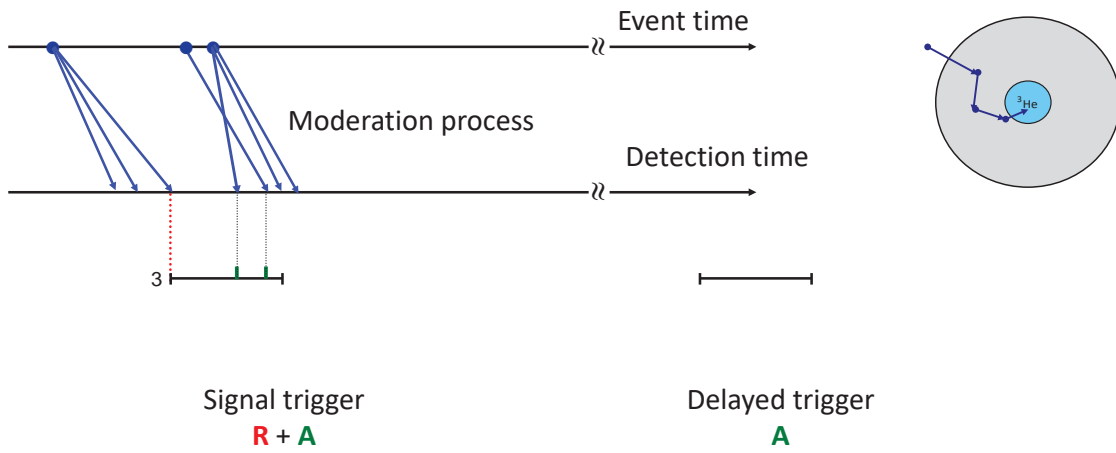


Signal trigger  
**R + A**

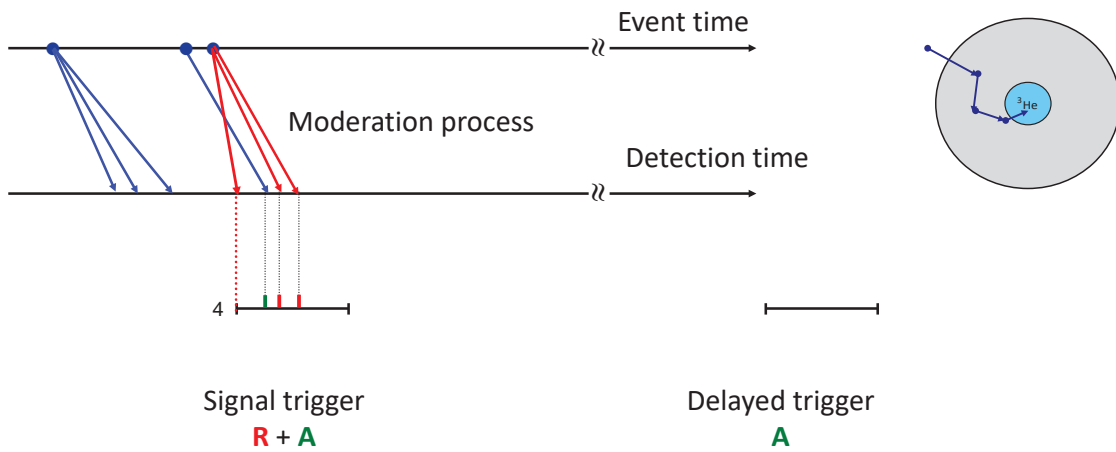
Delayed trigger  
**A**



**SHIFT – REGISTER: PRINCIPLE**

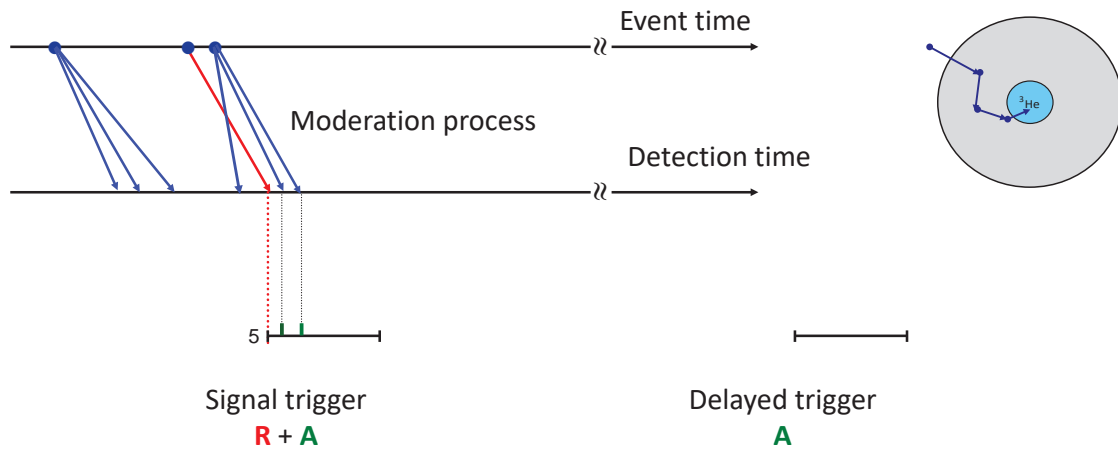


**SHIFT – REGISTER: PRINCIPLE**

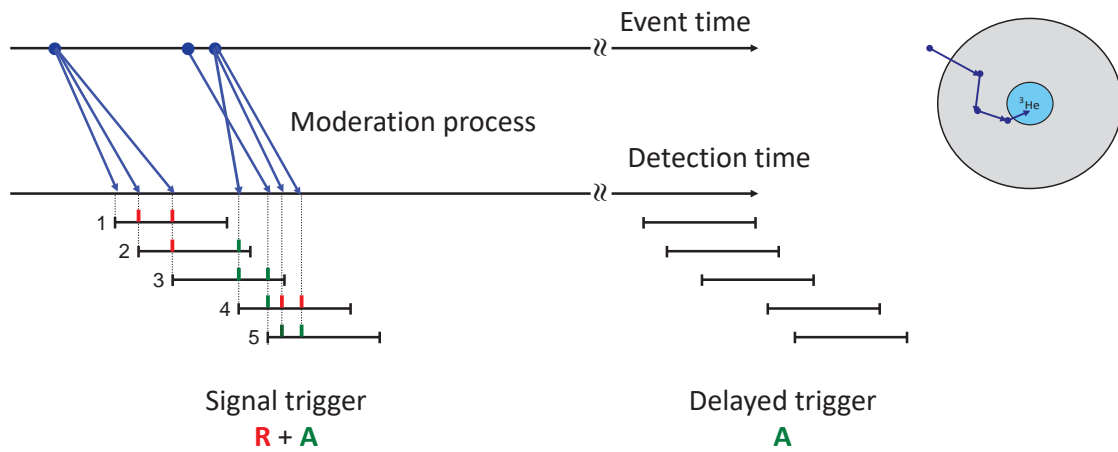




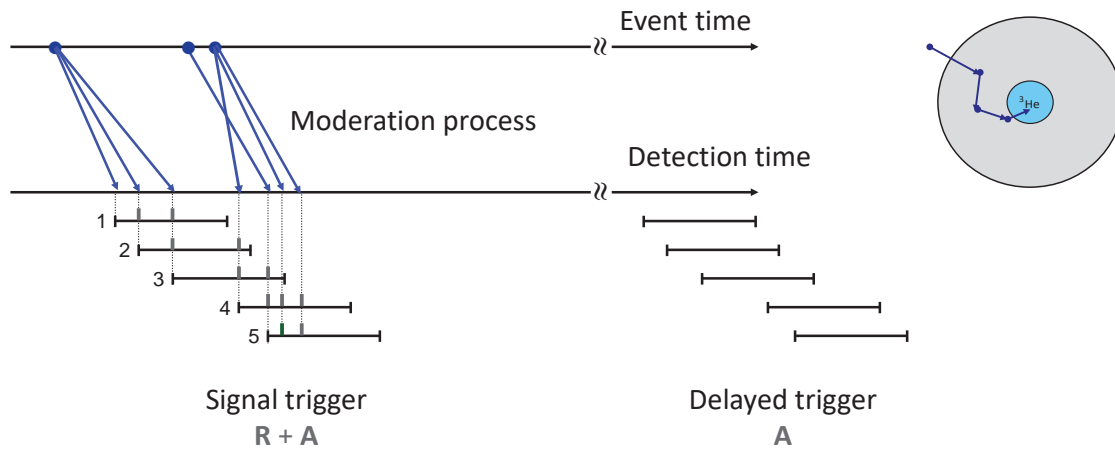
**SHIFT – REGISTER: PRINCIPLE**



**SHIFT – REGISTER: PRINCIPLE**



### SHIFT – REGISTER: PRINCIPLE



### DATA ANALYSIS: HAGE'S POINT MODEL

$$T = \epsilon_{sf} S_{sf} M [1 + \alpha]$$

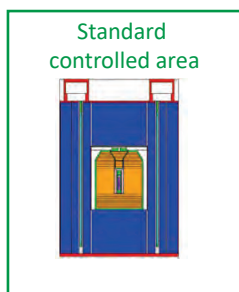
$$R = \epsilon_{sf}^2 f S_{sf} M^2 \left[ \frac{v_{sf(2)}}{v_{sf(1)}} + \frac{v_{(2)}}{v_{(1)} - 1} (M - 1)(1 + \alpha) \right]$$

- Experiment
  - T : total count rate corrected for dead time and background
  - R : reals count rate corrected for dead time and background
- Detector characteristics
  - $\epsilon_{sf}$  : detection efficiency
  - f : gate fraction
- Nuclear data
  - $v_{sf(1)}$  and  $v_{sf(2)}$  : 1<sup>st</sup> and 2<sup>nd</sup> order factorial moments of P(v) distribution for (sf)
  - $v_{sf(1)}$  and  $v_{sf(2)}$  : 1<sup>st</sup> and 2<sup>nd</sup> order factorial moments of P(v) distribution for (n,f)
- Sample properties
  - $S_{sf}$  : production rate for prompt fission neutrons by (sf)
  - $\alpha$  : ratio between neutron production rate by ( $\alpha, n$ ) and  $S_{sf}$
  - M : neutron leakage multiplication (derived by MC simulations,  $M \approx 1.006$ )

W. Hage and D.M. Cifarelli, NSE 89 (1985) 159 – 176  
 W. Hage and D.M. Cifarelli, NIMA 236 (1985) 165 – 177  
 D.M. Cifarelli and W. Hage, NIMA 251 (1986) 550 – 563



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

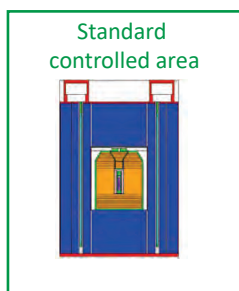


$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

$$\alpha = 0.039 (18)$$



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE



$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

$$\alpha = 0.039 (18)$$

#### Uncertainty evaluation and sensitivity analysis

Uncertainty component, $x_i$	$\frac{u_{x_j}}{x_j}$	$\frac{u_{S_{sf,j}}}{u_{S_{sf}}}$	$\frac{u_{\alpha,j}}{u_{\alpha}}$
Totals rate, T	0.0008	< 0.01	0.05
Reals rate, R	0.0027	0.15	0.17
Detection efficiency, $\epsilon_{sf}$	0.0055	0.60	0.35
Gate fraction, f	0.0071	0.40	0.45
First order factorial moment, $v_{sf(1)}$	0.0037	0.20	0.25
Second order factorial moment, $v_{sf(1)}$	0.0120	0.67	0.80
Multiplication, M	0.0020	0.01	< 0.01

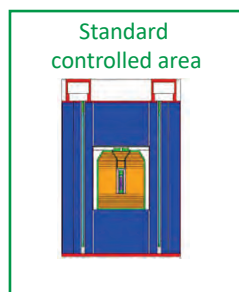
⇒ Improve

- detector characteristics
- nuclear data

Schillebeeckx et al., Frontiers in Energy Research 11 (2023) 1162367



## NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE



$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

$$S_{\alpha n} / S_{sf} = 0.039 (18)$$

Good agreement with:

Calculated from radiochemical analysis :

$$S_{sf} = 699 (28) \text{ s}^{-1} \text{ g}^{-1}$$

Note: uncertainty radiochemical analysis > 4% (> factor 2)



## NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

Code	Library	$S_{\text{calc}}/S_{\text{exp}}$
ALEPH2	JEFF-3.3	0.94
SCALE	ENDF/B-VII.0	0.96
Serpent2 (2.1.29)	ENDF/B-VII.0	1.01
	ENDF/B-VII.1	1.02
	ENDF/B-VIII.0	1.02
	JEFF-3.1.2	0.93
	JEFF-3.3	0.97
	JEFF-3.3 (1)	1.09
	JEFF-3.3 (2)	1.01
	JEFF-3.3 (3)	1.01
	JEFF-4T1	0.98
	JENDL-5.0	1.09

- (1)  $\sigma(n,\gamma) = 0$  for  $^{147}\text{Nd}$
- (2)  $\sigma(n,\gamma)$  for  $^{147}\text{Nd}$  from JENDL-4.0u
- (3)  $\sigma(n,\gamma)$  for  $^{147}\text{Nd}$  from JEFF-4T1



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

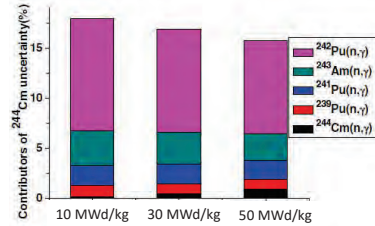
$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

Code	Library	$S_{calc}/S_{exp}$
ALEPH2	JEFF-3.3	0.94
SCALE	ENDF/B-VII.0	0.96
Serpent2 (2.1.29)	ENDF/B-VII.0	1.01
	ENDF/B-VII.1	1.02
	ENDF/B-VIII.0	1.02
	JEFF-3.1.2	0.93
	JEFF-3.3	0.97
	JEFF-3.3 (1)	1.09
	JEFF-3.3 (2)	1.01
	JEFF-3.3 (3)	1.01
	JEFF-4T1	0.98
	JENDL-5.0	1.09

Uncertainty theoretical estimation

Burnup	Relative uncertainty
10 MWd/kg	12.1 %
30 MWd/kg	11.1 %
50 MWd/kg	10.0 %

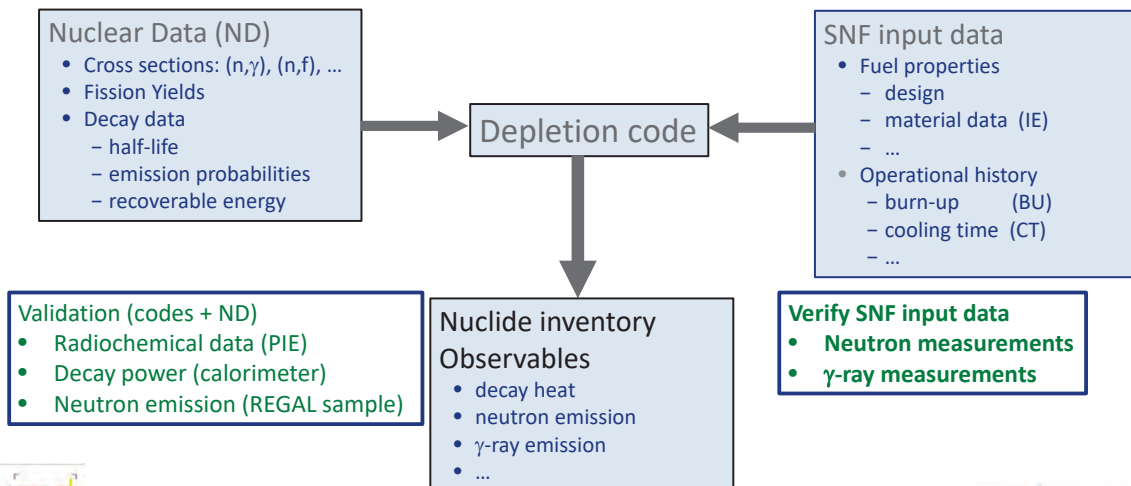
Contribution mainly from :  $^{242}\text{Pu}(n,\gamma)$  &  $^{243}\text{Am}(n,\gamma)$



Tiejun Zu et al., Annals of Nuclear Energy 94 (2016) 399



### TASK 2: PRODUCE VALIDATED DEPLETION CALCULATIONS WITH REALISTIC UNCERTAINTIES

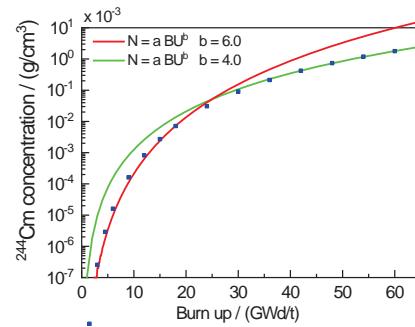


### NEUTRON EMISSION RATE

$N = aBU^b$   
 $b = 4$  for BU > 20 MWd/kg

$$\frac{\delta N}{N} = b \frac{\delta BU}{BU}$$

- ⇒ Total neutron emission extremely sensitive to BU
- ⇒ Good BU indicator



### <sup>137</sup>Cs

- Production : cumulative fission yields + burnup

$$N_k(t_0) \propto Y_c BU$$

- Decay power after cooling time t by <sup>137</sup>Cs

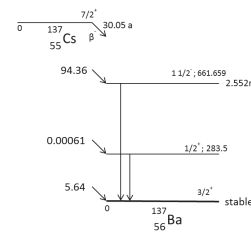
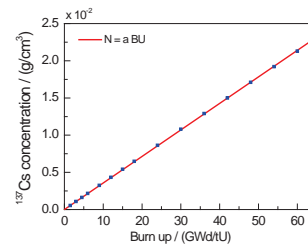
$$P_k(t) = p_k N_k(t_0) e^{-\lambda_k(t-t_0)}$$

⇒ Nuclear data

$$p_k = E_{dk} \lambda_k$$

- $Y_c$  : cumulative fission yields
- $\lambda_k$  : decay constant
- $E_{dk}$  : recoverable energy

⇒ Operational history : BU

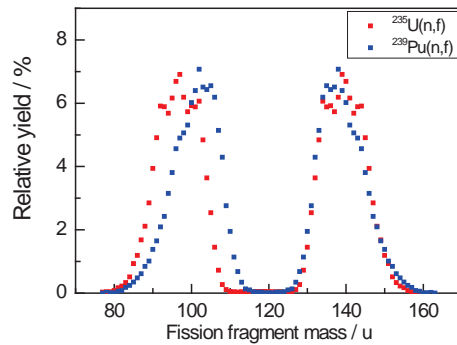


### **<sup>137</sup>Cs USED AS BURN-UP INDICATOR**

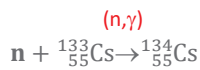
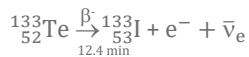
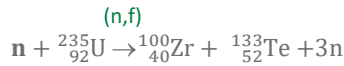
$$N_k(t) \approx Y_c \text{ BU}$$

- $N \propto \text{BU}$   
(long half-life, small  $\sigma_f$ )
- Not very sensitive to IE
- Cumulative fission yields (x 100)

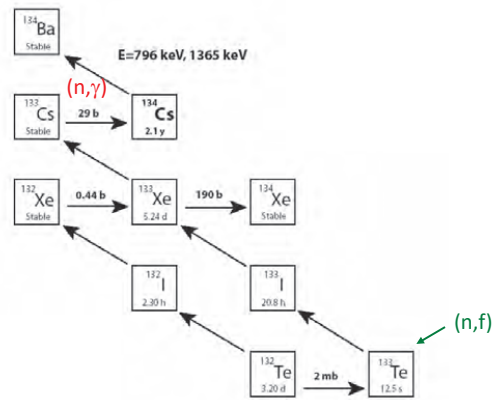
	<sup>235</sup> U(n,f)	<sup>239</sup> Pu(n,f)
<sup>106</sup> Ru	0.41 (1)	4.19 (9)
<sup>137</sup> Cs	6.22 (7)	6.59 (8)



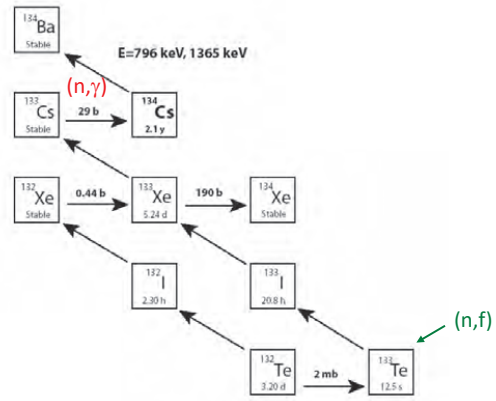
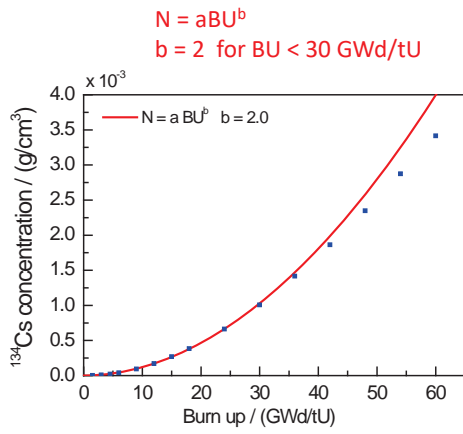
### **PRODUCTION OF <sup>134</sup>Cs**



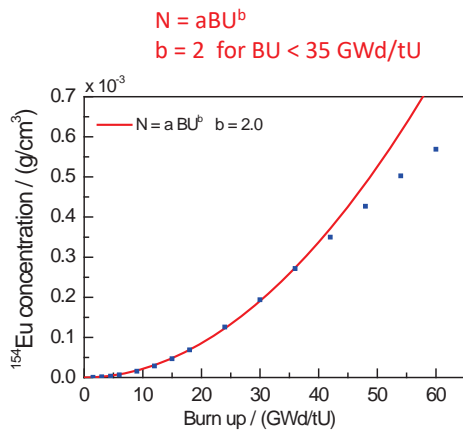
<sup>134</sup>Cs production:  
(n,f) followed by β<sup>-</sup> and (n,γ)



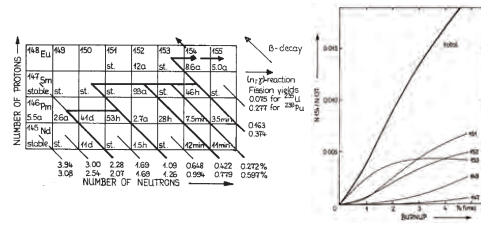
### PRODUCTION OF <sup>134</sup>Cs



### PRODUCTION OF <sup>154</sup>Eu



<sup>154</sup>Eu production: complex  
 (n,f), β<sup>-</sup> and (n,γ) from 5 mass chains



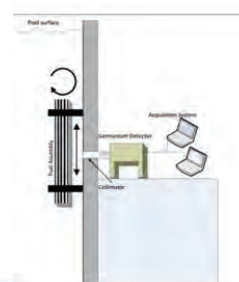
R. Berndt, Kernenergie 31 (1988) 59





## EXPERIMENTS AT CLAB

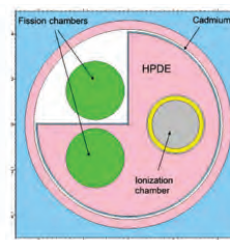
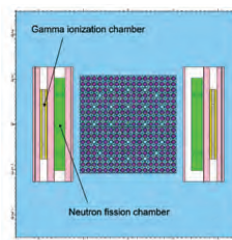
- FORK detector
  - Total neutron emission
  - Total  $\gamma$ -ray emission
- $\gamma$ -ray spectroscopy
  - HPGe detector
  - Axial scanning
- DDSI (Differential Die-away Self Interrogation)
  - MC-simulation
  - One experimental campaign (problems with device)



## NEUTRON AND $\gamma$ -RAY MEASUREMENTS: FORK DETECTOR

Passive NDA: detection of neutrons and  $\gamma$ -rays emitted by SNF assembly

- Neutron production
  - Primary neutrons: mainly prompt fission neutrons from  $^{244}\text{Cm}(\text{sf})$
  - Neutron multiplication: neutron induced fission after neutron moderation in the pool
- Neutron detection
  - $^{235}\text{U}$  fission chambers (FC)
  - Fission chamber with and without Cd
  - Total neutron count rate
- $\gamma$ -ray detection
  - Ionisation chamber (IC)
  - Total  $\gamma$ -ray dose rate measurement



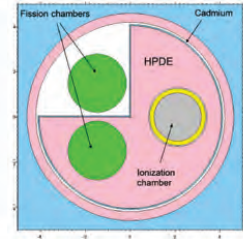
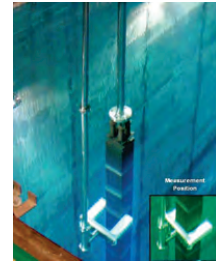
Vaccaro et al., NIMA 888 (2018) 202-217



## FORK DETECTORS: THEORETICAL CALCULATIONS

- Neutron and  $\gamma$ -ray emission spectra by ORIGEN
  - ENDF/B-VII.1
  - ORIGEN-ARP (covers a wide range of fuel types and irradiation conditions)
  - Neutron emission spectra: SOURCES 4C
- Neutron detection response
  - Energy dependent response functions by MCNP
  - Neutron multiplication, M
    - $k_{\infty}$  using macroscopic cross sections from ORIGEN
    - $(1 - L)$  by MCNP for each assembly lattice design
- $\gamma$ -ray detection response
  - Energy-dependent response function by MCNP
  - Correction for nonlinear behaviour of IC as a function of incident dose rate determined by comparison with calculated response

$$M = \frac{1}{1 - k_{\infty} (1 - L)}$$



Vaccaro et al., NIMA 888 (2018) 202-217



## FORK DETECTORS: RESPONSE FUNCTIONS

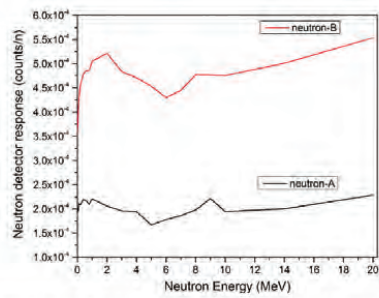


Fig. 5b. Energy-dependent response of the Fork detector neutron detectors and  $17 \times 17$  assembly calculated by MCNP and the measurement configuration in Fig. 4a. Neutron response is counts per emitted neutron in the fuel and includes neutron multiplication in the assembly. Neutron-A represents the bare fission chamber, while neutron-B is the cadmium-covered detector.

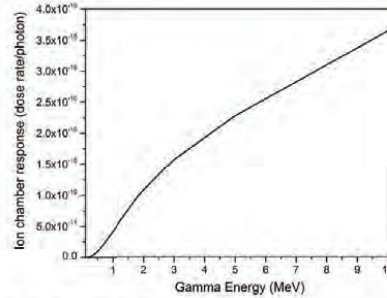
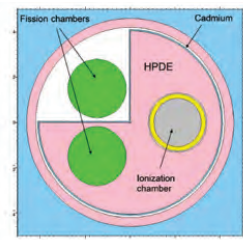


Fig. 5a. Energy-dependent response of the Fork detector gamma ionization chamber and  $17 \times 17$  assembly calculated by MCNP and the measurement configuration in Fig. 4a. Response is dose rate per photon emitted in the fuel.



Vaccaro et al., NIMA 888 (2018) 202-217



### FORK MEASUREMENTS AT CLAB

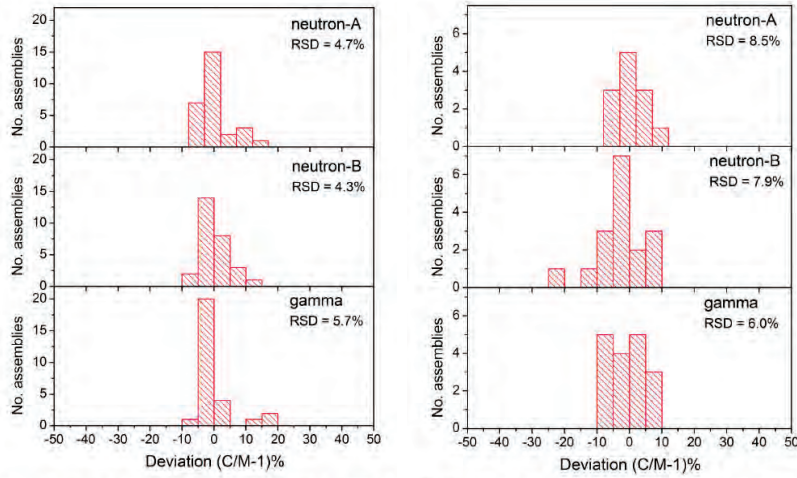
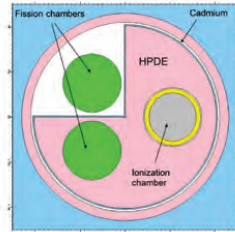
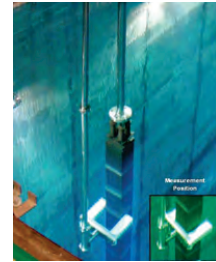


Fig. 10. Histogram distribution of the deviations between calculated (C) and measured (M) gamma, neutron-A, and neutron-B detector count rates for PWR assemblies measured at the Swedish Clab facility.

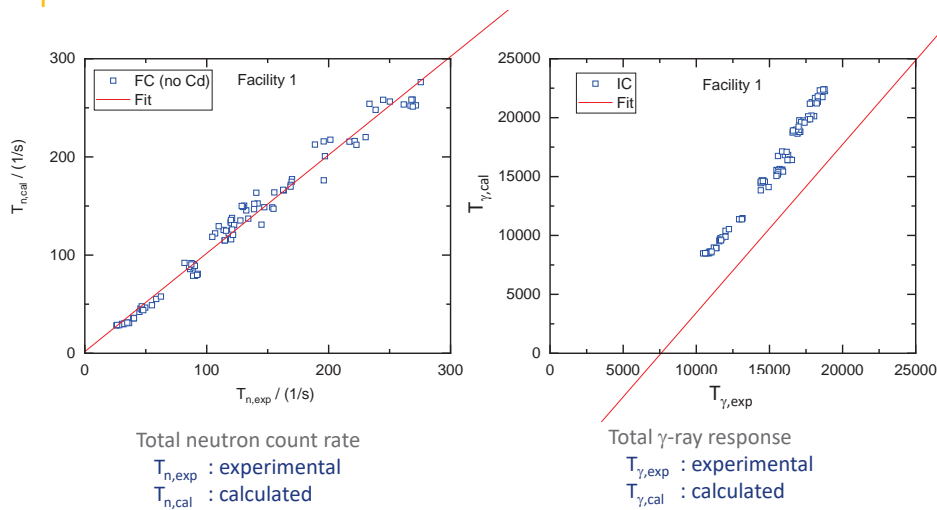
Fig. 11. Histogram distribution of the deviations between calculated (C) and measured (M) gamma, neutron-A, and neutron-B detector count rates for BWR assemblies measured at the Swedish Clab facility.



Vaccaro et al., NIMA 888 (2018) 202-217

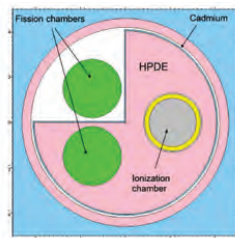


### FORK MEASUREMENTS: COMPARISON WITH CALCULATIONS



Total neutron count rate  
 $T_{n,exp}$  : experimental  
 $T_{n,cal}$  : calculated

Total  $\gamma$ -ray response  
 $T_{\gamma,exp}$  : experimental  
 $T_{\gamma,cal}$  : calculated

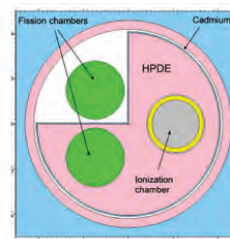
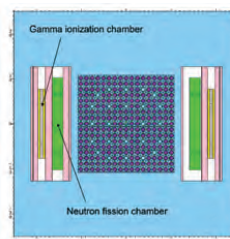


Mosconi, private communication



## FORK MEASUREMENTS

Detector	Facility 1	Facility 2	Facility 3
FC (no Cd)	9.0 %	12.0 %	2.2%
FC (Cd)	9.0 %	14.0 %	2.2 %
IC	4.2 %	11.0 %	1.8 %

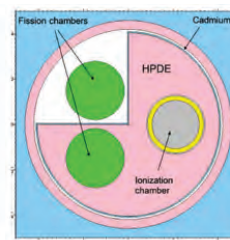
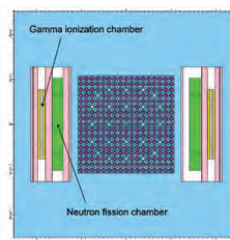


Mosconi, private communication



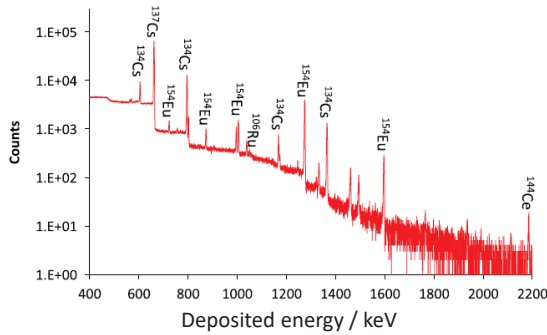
## TASK SHEET: IMPROVE THE VERIFICATION OF SPENT FUEL WITH FORK DETECTORS

- Determine detection efficiency
  - Design and construct a reference calibration set-up
  - Perform calibration measurements with radionuclide sources, i.e.  $^{244}\text{Cm}$
  - Perform measurements to validate MC-calculations
- MC simulations of detector response
  - MC simulations for the reference calibration set-up
  - Verify impact of  $^{10}\text{B}$  concentration in the pool
  - Define correction factors based on Cd/no-Cd ratio

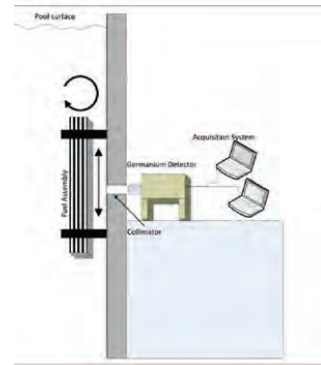
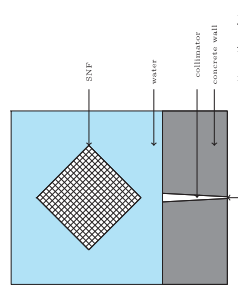


## γ-RAY SPECTROSCOPIC MEASUREMENTS

- HP Ge detector
- Axial scanning



<sup>137</sup>Cs: 662 keV  
<sup>134</sup>Cs: 605, 796, 1365 keV  
<sup>154</sup>Eu: 996, 1004, 1274, 1596 keV



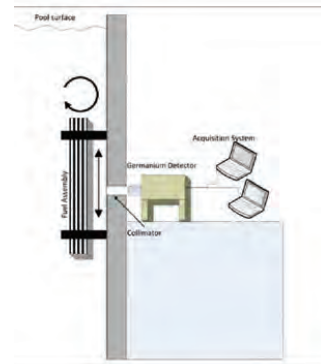
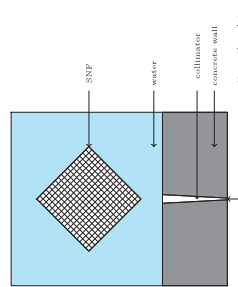
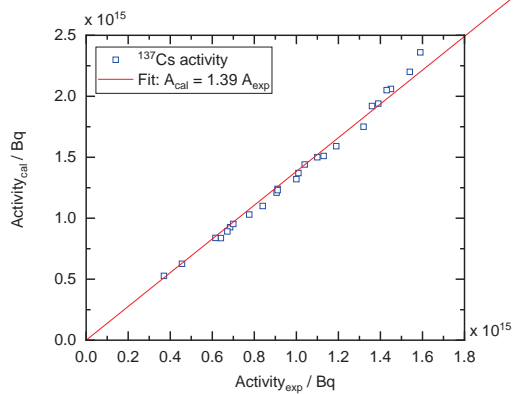
Solans et al., ANE 192 (2023) 109941  
 Bengtsson et al., Nucl. Techn. 208 (2022) 295  
 Vaccaro et al., NIMA A833 (2016) 208  
 Vo et al., NIMA 830 (2016) 325  
 Favalli et al., NIMA 820 (2016) 102



## <sup>137</sup>Cs ACTIVITY

$$\langle A_{cal}/A_{exp} \rangle = 1.39$$

$$\text{St. dev } A_{cal}/A_{exp} = 3.3\%$$

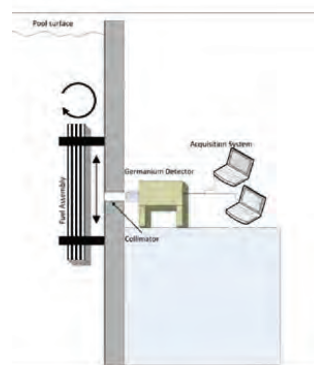
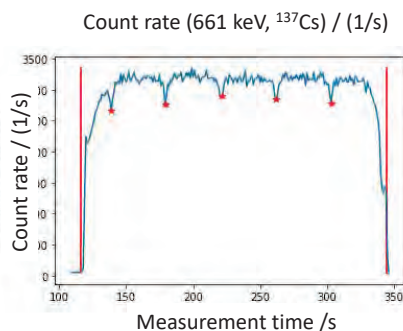
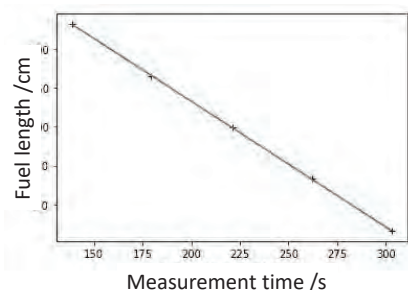


Bengtsson et al., Nucl. Techn. 208 (2022) 295





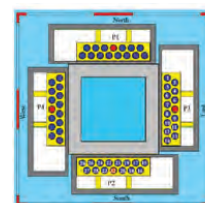
### AXIAL PROFILE <sup>137</sup>Cs ACTIVITY (BURNUP PROFILE)



### DIFFERENTIAL DIE-AWAY SELF-INTERROGATION (DDSI)

Passive NDA: detection of neutrons emitted by SNF assembly  
 Developed at LANL for nuclear safeguards applications

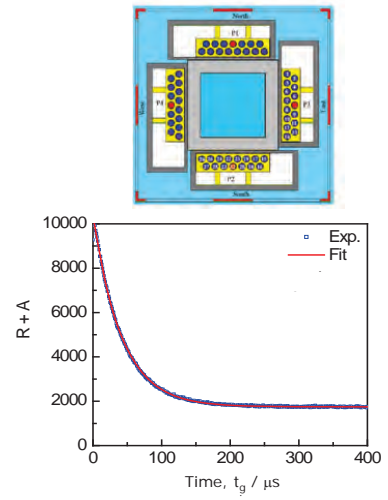
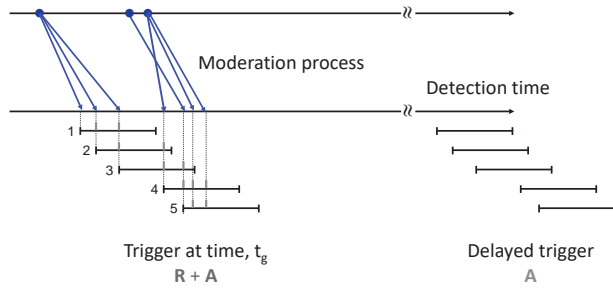
- Neutron production
  - Primary neutrons: mainly prompt fission neutrons from <sup>244</sup>Cm(sf)
  - Prompt fission neutrons from neutron induced fission in fuel mainly after neutron moderation in the water of the pool
- Detection principle
  - <sup>3</sup>He in moderator
  - Detection of **correlated neutrons**: construct **Rossi-alpha distribution**



Trahan et al., NIMA 955 (2020) 163329

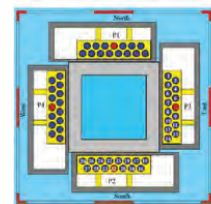
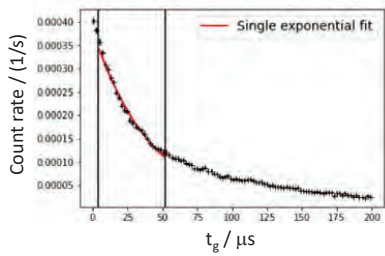


### DDSI: ROSSI-ALPHA DISTRIBUTION

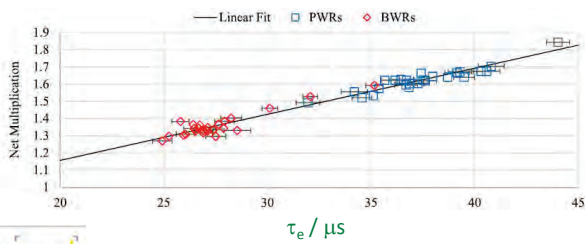


### DDSI: ROSSI-ALPHA DISTRIBUTION

$$R = R_0 e^{-\frac{t}{\tau_e}}$$

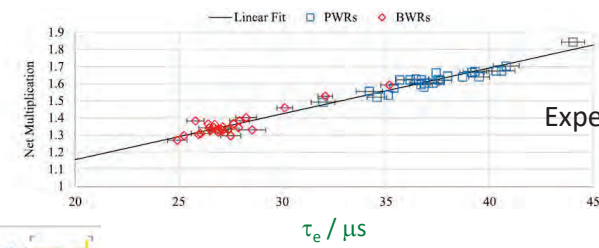
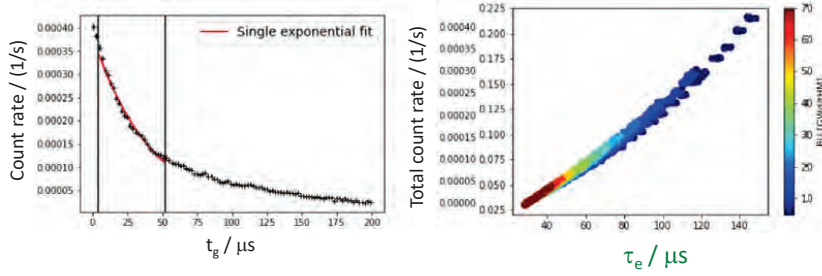


Trahan et al., NIMA 955 (2020) 163329

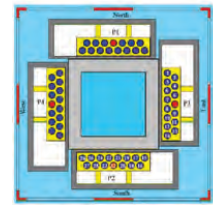


### DDSI: ROSSI-ALPHA DISTRIBUTION

$$R = R_0 e^{-\frac{t}{\tau_e}}$$



Experiments at CLAB



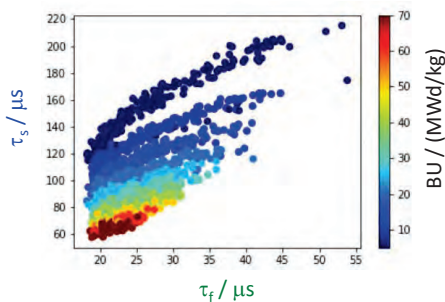
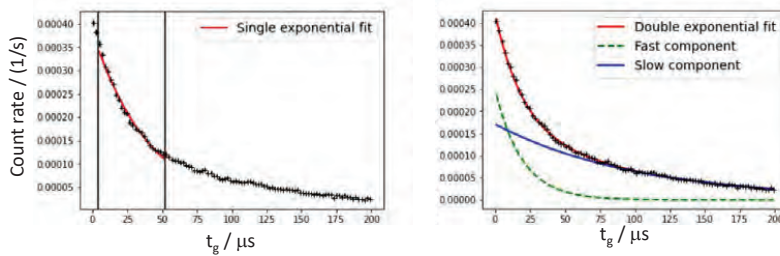
Trahan et al., NIMA 955 (2020) 163329



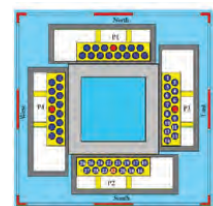
### DDSI: MC SIMULATIONS

$$R = R_0 e^{-\frac{t}{\tau_e}}$$

$$R = R_{01} e^{-\frac{t}{\tau_f}} + R_{02} e^{-\frac{t}{\tau_s}}$$



⇒ Additional information

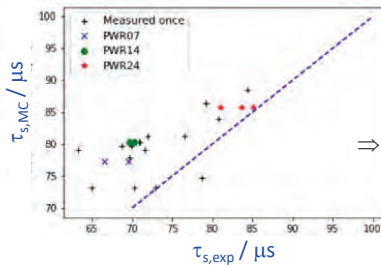
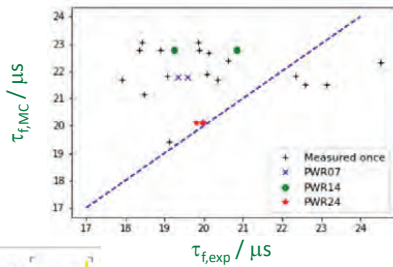
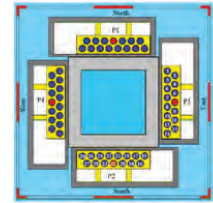
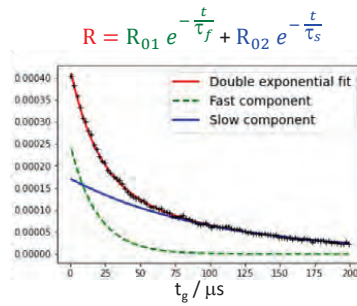
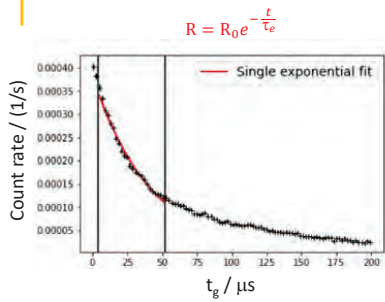


Solans et al., IAEA Symposium, November 2022  
IAEA-CN-303-137





**DDSI: EXPERIMENTS AT CLAB**



⇒ Not confirmed by experiment

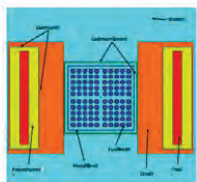
Solans et al., IAEA Symposium, November 2022  
IAEA-CN-303-137



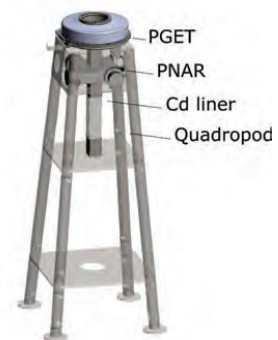
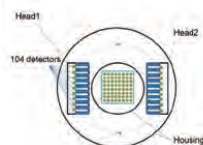
**FINLAND: ONKALO**

Marita Mosconi

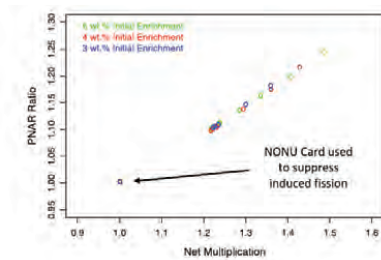
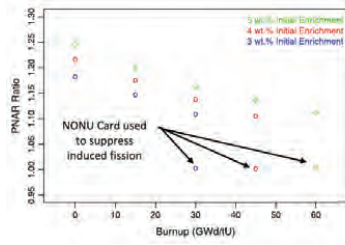
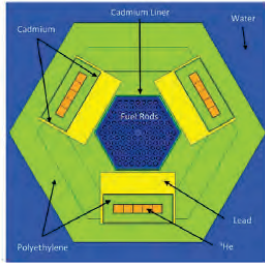
- Passive Neutron Albedo Reactivity (PNAR)  
LANL development, Tobin et al., NIMA 897 (2018) 32 - 37



- Passive Gamma Ray Emission Tomography (PGET)  
IAEA development, Honkamaa et al., Symp. Int. Safeguards, IAEA Vienna 2014



### PNAR CONCEPT: RESULTS FROM MC SIMULATIONS

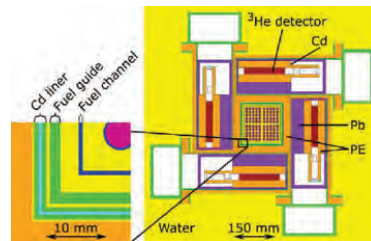
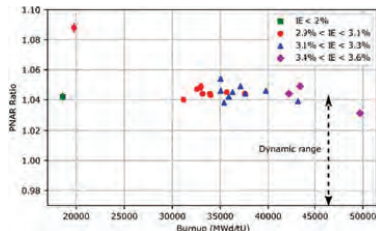


Tobin et al., NIMA 897 (2018) 32 - 37

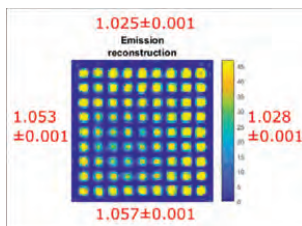


### PNAR + PGET AT ONKALO

PNAR



PGET



Tupasela et al., NIMA 986 (2021) 164707



## BIBLIOGRAPHY

Spent nuclear fuel observables and key nuclides

- Gauld et al., "Nuclide importance to criticality safety, decay heating and source terms related to transport and interim storage of high-burnup LWR fuel", Report NUREG/CR-6700, ORNL/TM-2000/284 (2001)
- Žerovnik et al., "Observables of interest for the characterisation of Spent Nuclear Fuel", EUR 29301 EN (2018), JRC112361
- Schillebeeckx et al., "Characterisation of spent nuclear fuel by theoretical calculations and non-destructive analysis", JRC114178 (2019)

Depletion codes

- Rearden and Jessee, "SCALE Code System", ORNL/TM-2005/39 Version 6.2, April 2016
- Gauld et al., "Isotopic depletion and decay methods and analysis capabilities in SCALE", Nuclear Technology 174 (2017) 169

Nuclear data

- Nuclear data libraries at JANIS NEA, [https://www.oecd-nea.org/jcms/pl\\_39910/janis](https://www.oecd-nea.org/jcms/pl_39910/janis)
- Decay data, <http://www.nucleide.org/DDEP.htm>
- Nichols et al., "Handbook of nuclear data for safeguards: database extensions, august 2008", INDC-2453, INDC(NDS) – 0534



## BIBLIOGRAPHY

Non-destructive assay

Calorimeter

- SKB, "Measurements of Decay Heat in Spent Nuclear Fuel at the Swedish Interim Storage Facility", Clab, SKB Report R-05-62, December 2006
- B.D. Murphy and I.C. Gauld, "Spent Fuel Decay Heat Measurements Performed at the Swedish Central Interim Storage Facility", Report ORNL/TM-2008/016, Oak Ridge National Laboratory, February 2010

Neutron

- Schillebeeckx et al., "An absolute measurements of the neutron production rate of a spent nuclear fuel sample used for depletion code validation", Frontiers in Energy Research 11 (2023) 1162367
- Schillebeeckx et al., "A non-destructive method to determine the neutron production rate of a sample of spent nuclear fuel under standard controlled area conditions", JRC Technical Report EUR 30379 EN, 2020
- Tupasela et al., "Passive neutron albedo reactivity measurements of spent fuel nuclear fuel", Nucl. Instr. Meth. A986 (2020) 164707
- Trahan et al., "Results of the Swedish spent fuel measurements field trials with the DDSI", Nucl. Instr. Meth. A955 (2020) 163329
- Tobin et al., "Measuring spent fuel assembly multiplication in borated water with a PNAR instrument", Nucl. Instr. Meth. A897 (2018) 32
- Vaccaro et al., "Advancing the FORK detector for quantitative spent nuclear fuel verification", Nucl. Instr. Meth. A888 (2018) 202

γ-ray

- Solans et al., "Spent nuclear fuel passive gamma analysis and reproducibility application to SKB-50 assemblies", Ann. Nucl. Energy 192 (2023) 109941
- Bengtsson et al., "Experimental method for the verification of calculated  $^{137}\text{Cs}$  content in nuclear fuel assemblies", Nucl. Techn. 208 (2022) 295
- Vaccaro et al., "PWR and BWR spent fuel assembly gamma spectra measurements", Nucl. Instr. Meth. A833 (2016) 208



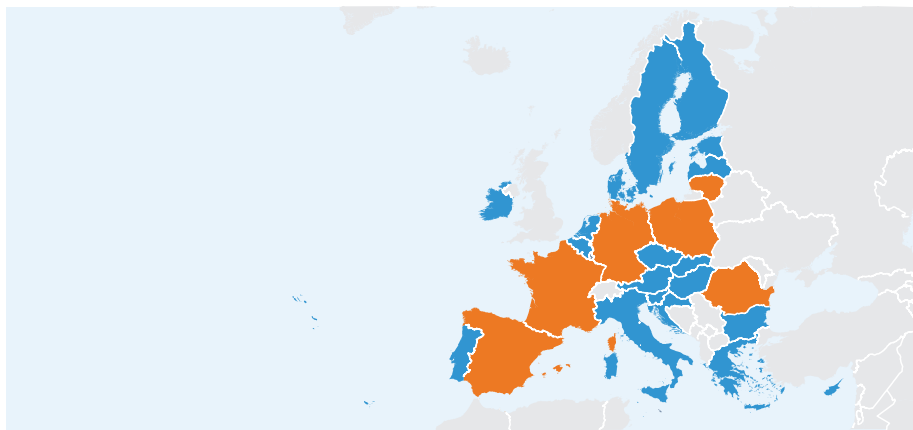
Thank you



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## EU countries



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## THEORETICAL CALCULATIONS OF THE NEUTRON EMISSION RATE

Code-to-code comparison (including nuclear data)

All calculations normalised to the  $^{147}\text{Nd}$  inventory

- Verify impact ND (use one code: Serpent2)
- Verify prediction of  $^{137}\text{Cs}$  inventory by different codes/ND libraries
- Verify prediction of BU derived from the codes/ND libraries



## CODE-TO-CODE COMPARISON: $^{137}\text{Cs}$ , $^{244}\text{Cm}$ AND BU

Code	Library	$^{137}\text{Cs}$	$^{137}\text{Cs}$	$^{244}\text{Cm}$	BU	$^{137}\text{Cs}$	$^{244}\text{Cm}$	BU
		$N_x/N_U \times 10^{-3}$	C/E	$N_x/N_U \times 10^{-5}$	MWd/kg			
ALEPH2	JEFF-3.3	2.225	0.982	6.290	53.25	<b>0.990</b>	0.981	<b>0.983</b>
SCALE	ENDF/B-VII.0	2.241	0.990	6.380	54.01	0.997	0.995	0.997
Serpent2	ENDF/B-VII.0	2.285	1.009	6.633	54.37	1.016	1.035	1.004
	ENDF/B-VII.1	2.274	1.004	6.710	54.39	1.012	1.047	1.004
	ENDF/B-VIII.0	2.274	1.004	6.701	54.38	1.012	1.045	1.004
	JEFF-3.1.2	2.248	0.993	6.110	54.18	1.000	<b>0.953</b>	1.000
	JEFF-3.3	2.225	0.982	6.354	53.37	<b>0.990</b>	0.991	0.985
	JEFF-3.3 (1)	2.290	1.011	7.149	55.24	1.019	1.115	<b>1.020</b>
	JEFF-3.3 (2)	2.249	0.993	6.644	54.21	1.000	1.037	1.001
	JEFF-3.3 (3)	2.246	0.992	6.599	54.12	0.999	1.029	0.999
	JEFF-4T1	2.248	0.993	6.410	54.16	1	1	1
	JENDL-4.0u	2.301	1.016	7.009	55.07	<b>1.024</b>	1.093	1.017
	JENDL-5.0	2.253	0.995	7.194	54.97	1.002	<b>1.122</b>	1.015

- (1)  $\sigma(n,\gamma) = 0$  for  $^{147}\text{Nd}$   
 (2)  $\sigma(n,\gamma)$  for  $^{147}\text{Nd}$  from JENDL-4.0u  
 (3)  $\sigma(n,\gamma)$  for  $^{147}\text{Nd}$  from JEFF-4T1



## NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

Code	Library	Ssf/ (1/sg)		C/E	
		LIB	REC	LIB	REC
ALEPH2	JEFF-3.3	640.1	642.4	0.944	0.947
SCALE	ENDF/B-VII.0	653	652.1	0.963	0.962
Serpent2	ENDF/B-VII.0	683.7	678.1	1.008	1.000
	ENDF/B-VII.1	689.4	685.3	1.017	1.011
	ENDF/B-VIII.0	688.5	684.3	1.015	1.009
	JEFF-3.1.2	632.5	623.8	0.933	0.920
	JEFF-3.3	656.8	648.9	0.969	0.957
	JEFF-3.3 (1)	739.4	730.5	1.091	1.077
	JEFF-3.3 (2)	686.8	678.6	1.013	1.001
	JEFF-3.3 (3)	682.2	673.9	1.006	0.994
	JEFF-4T1	662.6	654.6	0.977	0.965
	JEFF-4T2	676.4	668.3	0.998	0.986
JENDL-4.0u (4)			715.9		1.056
JENDL-5.0		738.4	733.9	1.089	1.082

$$S_{sf,exp} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

Overall good agreement

- (1)  $\sigma(n,\gamma) = 0$  for  $^{147}\text{Nd}$
- (2)  $\sigma(n,\gamma)$  for  $^{147}\text{Nd}$  from JENDL-4.0u
- (3)  $\sigma(n,\gamma)$  for  $^{147}\text{Nd}$  from JEFF-4T1
- (4) No data available to calculate  $S_{sf}$

**2.5 SNF characterisation by NDA; P. Schillebeeckx, JRC Geel;  
School on "Nuclear data for depletion calculations; 11/09 -  
15/09/2023**



**SANDA**  
Supplying Accurate Nuclear Data for  
energy and non-energy Applications

HORIZON2020

# SNF characterisation by NDA

Peter Schillebeeckx  
JRC Directorate G, Nuclear Safety and Security  
SANDA School, 11 – 15 September 2023, JRC Geel  
“Nuclear data for depletion calculations”

*The project leading to this application has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement n° 847593.*

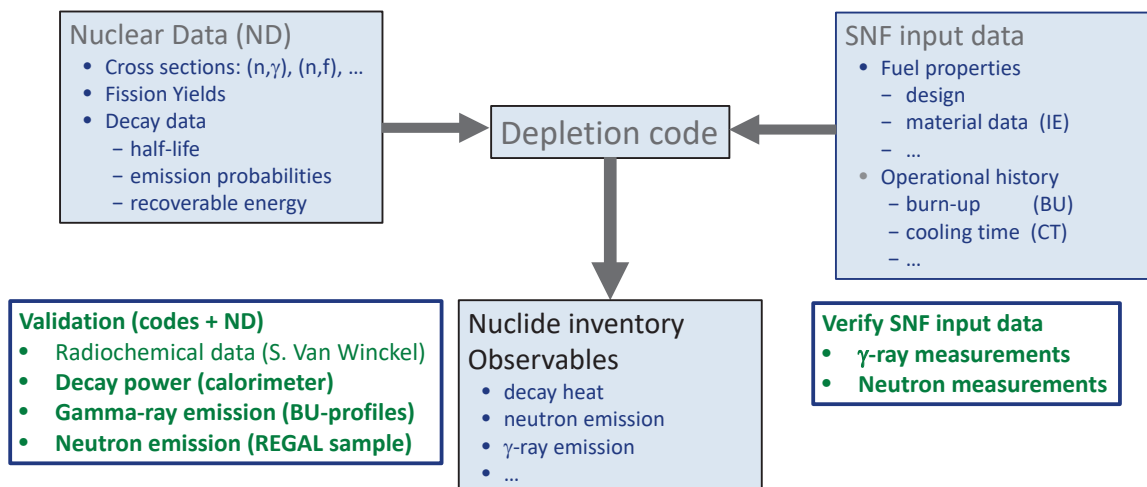


## CONTENTS

- Introduction
- NDA for code validation
  - CLAB Calorimeter
  - Neutron emission measurements
  - Gamma-ray measurements
- NDA for verification of assembly properties
  - Gamma-ray measurements
  - Neutron measurements



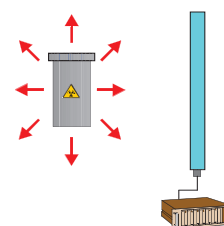
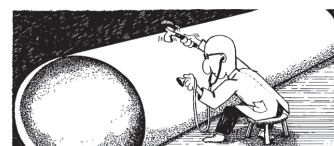
### SNF CHARACTERIZATION BY NON-DESTRUCTIVE ASSAY (NDA)



### NON-DESTRUCTIVE ASSAY (NDA)

Use radiation emitted by the sample as a fingerprint to determine the properties of nuclear material

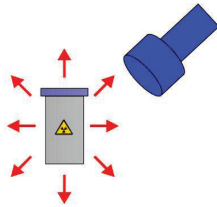
- Requirements
  - High penetration power
  - Detectable
- Radiation types
  - Charged particles (only for extreme thin samples)
  - Neutron
  - Gamma-ray
  - Heat



**NDA: PASSIVE - ACTIVE**

**Passive**

- Spontaneous emission
- Radioactive Decay

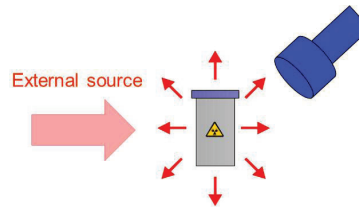


Source term: decay rate

$$S = \lambda N$$

**Active**

- Induced emission
- Nuclear reactions

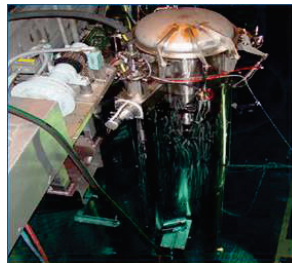


Source term : reaction yield

$$S_r = (1 - e^{-n \sigma_{tot}}) \frac{\sigma_r}{\sigma_{tot}} + \dots$$



**CLAB CALORIMETER: DECAY HEAT**



See presentations:

- G. Letnar
- O. Matuselanski
- A. Melic
- P. Romojaro

- Only operating calorimeter worldwide to determine decay power of SNF assemblies
- Extensively used to validate depletion codes, e.g.
  - Ilas and Burns, Nucl. Tech. 208 (2022) 403 SCALE 6.2.4
  - Shama et al., Ann. Nucl. Energy 165 (2022) 108758 ORIGE, CASMO5
  - Ebiwonjumi et al., Ann. Nucl. Energy 124 (2019) 80 STREAM
  - Yamamoto and Iwahashi J. Nucl. Sci. Technol. 53 (2016) 2108 ORIGEN2.2, CASMO5
  - Haeck and Ichou, EPJ Web of Conferences 146 (2017) 06012 VESTA
  - San-Felice et al., Nucl. Technol. 184 (2013) 217 DARWIN



### DATA FROM CLAB CALORIMETER: SOME RESULTS

Ref.	Year	Code	Library	PWR		BWR	
				<C/E>	St. dev	<C/E>	St. dev
Ilas and Gauld	2008	SCALE 5.1	ENDF/B-V	1.011	0.012	1.003	0.025
Ilas et al.	2014	SCALE 6.1.2	ENDF/B-VII.0	1.002	0.012	0.997	0.024
Ilas and Burns	2021	SCALE 6.2.4	ENDF/B-VII.0	1.013	0.013	1.002	0.012
	2021	SCALE 6.2.4	ENDF/B-VII.1	1.008	0.012	1.009	0.024
Ilas and Burns	2022	SCALE 6.3	ENDF/B-VIII.0	1.006	0.014	1.007	0.024
Shama et al.	2022	SCALE 6.2.3	ENDF/B-VII.1	1.019	0.012	1.003	0.025
		SCALE 6.2.3 (POLARIS)	ENDF/B-VII.1	1.015	0.012	1.010	0.026
Shama et al.	2022	CASMO5		1.009	0.013	1.008	0.025
Yamamoto	2016	CASMO5	JENDL-4.0	1.016	0.013	1.001	0.024
Haeck et al.	2022	VESTA 2.1	JEFF-3.1	0.978	0.012		
		VESTA 2.1	ENDF/B-VII.0	0.996	0.012		
Mills and Sutton	2009	FISPIN	JEF-2.2	0.995	0.013		
		FISPIN	JEFF-3.1.1	0.985	0.012		
San-Felice et al.	2012	DARWIN	JEFF-3.1.1	0.978	0.011		

Not blind!  
Adjustments not excluded

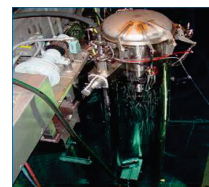


### BLIND TEST CLAB CALORIMETER: CODES + LIBRARIES

NUCLEAR SCIENCE AND ENGINEERING - VOLUME 196 - 1125-1145 - SEPTEMBER 2022  
 © 2022 The Author(s). Published with license by Taylor & Francis Group, LLC.  
 DOI: <https://doi.org/10.1080/00295639.2022.2053489>

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**Blind Benchmark Exercise for Spent Nuclear Fuel Decay Heat**



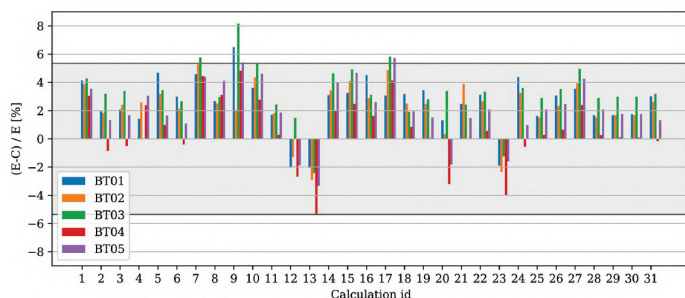
Code	Library	Appendix Section
ALEPH 2.7.2	ENDF/B-VII.1	A1A
APOLLO2.8/DARWIN2.3	JEFF-3.1.1	A1B
CASMO-4E + ORIGEN-S	JEF-2.2	A1C
CASMO-5 (2.03)	ENDF/B-VII.1	A1D
CASMO-5 (2.12.00) + SNF (1.07.02)	ENDF/B-VII.1	A1E
DRAGON 4.0.5	ENDF/B-VII.1	A1F
EVOLCODE (MCNP + ACAB)	JEFF-3.3	A1G
MCNP/CINDER + Nukleonika (2D)	ENDF/B-VII.1	A1H
Monteburns v3 + CINDER	ENDF/B-VII.1	A1I
MOTIVE (KENO-VI + VENTINA)	ENDF/B-VII.1	A1J
MOTIVE (OpenMC + VENTINA)	ENDF/B-VIII	A1K
MVP 3	ENDF/B-VII.1	A1L
MVP 3	JEFF-3.2	A1M
MVP 3	JENDL-4.0	A1N
OREST	JEF-2.2 + ENDF/B-VI	A1O
SCALE 6.0: ORIGEN-ARP	ENDF/B-V	A1P
SCALE 6.1.3: ORIGEN-ARP	ENDF/B-V	A1Q
SCALE 6.2.3: ORIGAMI	ENDF/B-VII.1	A1R
SCALE 6.2.3: Polaris	ENDF/B-VII.1	A1R
SCALE 6.2.3: ORIGEN	ENDF/B-VII.1	A1R
SCALE 6.2.3: TRITON/KENO	ENDF/B-VII.1	A1S
SCALE 6.2.3: TRITON/NEWT	ENDF/B-VII.1	A1T
SEADEP	JEFF-3.1.1	A1U
Serpent 2.1.29	ENDF/B-VII.1	A1V
Serpent 2.1.29	JEFF-3.1.1	A1W
Serpent 2.1.31	JEFF-3.2 + JEFF-3.1.1	A1X

Assembly ID	BU	CT	IE	Decay heat rate
BT01	53 MWd/kg	4.5 a	3.95 wt%	1662 W
BT02	55 MWd/kg	8.6 a	3.95 wt%	1068 W
BT03	50 MWd/kg	9.8 a	3.95 wt%	895 W
BT04	51 MWd/kg	13.5 a	3.70 wt%	768 W
BT05	50 MWd/kg	21.4 a	3.60 wt%	663 W



### BLIND TEST CLAB CALORIMETER: RESULTS

Assembly ID	P	CT	<C/E>	St. dev
BT01	1662 W	4.5 a	0.975	0.019
BT02	1068 W	8.6 a	0.977	0.018
BT03 (+ Gd)	895 W	9.8 a	0.967	0.019
BT04	768 W	13.5 a	0.994	0.023
BT05	663 W	21.4 a	0.979	0.021



### EPRI, PIRT, July 2020

Table 5-5  
Summary of Uncertainty in Calculated Decay Heat [17] for BWR Assembly at 37 GWd/MTU Burnup and 15.6 Years' Cooling Time

Perturbed Parameter Set	Relative Uncertainty (%)
Fuel design data	0.2
Operating history data	0.8
Nuclear cross-section data	0.9
Fission yield data	0.3
<b>Overall uncertainty</b>	<b>1.3</b>

Ilas et al., Nucl. Eng. Des. 319 (2017) 176

Table 5  
Decay heat uncertainty summary.

Data set	Data set	Uncertainty (1σ) (%)
Modeling data	Fuel design	0.20
	Operating data	0.85
	Total	0.87
Nuclear data	Cross sections	0.88
	Fission yields	0.26
	Total	0.92
Overall effect	Total	1.27

$u_p/P = 1.3\%$ , is this realistic?

### BLIND TEST CLAB CALORIMETER: QUOTED UNCERTAINTIES

Confidence Interval (CI): 68 %

- SKB Document R-05-62 (also used in EPRI, PRIT report)
  - PWR
    - 250 W 1.8 %
    - 900 W 1.0 %
  - BWR
    - 50 W 4.2 %
    - 350 W 0.9 %
- Blind test paper (Jansson et al., Nucl. Sci. Eng. 196 (2022) 1125)
  - 5% overall uncertainty

Only total (combined uncertainties) are given

No separation between

- Systematic and random effects
- Correlated and uncorrelated uncertainty components

⇒ Performance assessment and uncertainty evaluation of CLAB calorimeter is required

⇒ One of the main EURAD objectives of WP8 Task 2



**CLAB CALORIMETER: PRINCIPLE**

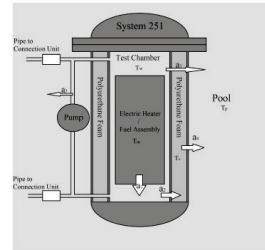
$$C \frac{\partial T_c}{\partial t} - k \frac{\partial^2 T_c}{\partial x^2} = [P - k(T_c - T_p)]$$

- P : power of heat source
- T<sub>c</sub> : calorimeter temperature
- T<sub>p</sub> : pool temperature
- C : heat capacity (calorimetric body)
- k : heat transfer coefficient
- t : time
- x : position

One component heat transfer model

Equilibrium water in calorimeter and heat source

- Calorimetric body at temperature T<sub>c</sub>
- Environment (pool) at a constant temperature T<sub>p</sub>



See e.g. Gunn, Nucl. Instr. Meth. 29 (1964) 1



**CLAB CALORIMETER: PRINCIPLE**

$$C \frac{\partial T_c}{\partial t} - k \frac{\partial^2 T_c}{\partial x^2} = [P - k(T_c \times T_p)]$$

- P : power of heat source
- T<sub>c</sub> : calorimeter temperature
- T<sub>p</sub> : pool temperature
- C : heat capacity (calorimetric body)
- k : heat transfer coefficient
- t : time
- x : position

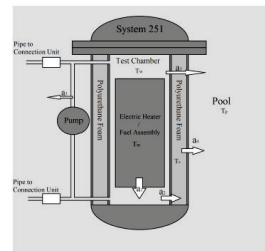
One component heat transfer model

Equilibrium water in calorimeter and heat source

- Calorimetric body at temperature T<sub>c</sub>
- Environment (pool) at a constant temperature T<sub>p</sub>

Conditions

- No spatial temperature distribution in calorimeter
- T<sub>c</sub> = T<sub>p</sub>



### CLAB CALORIMETER: PRINCIPLE

$$C \frac{\partial(T_c - T_p)}{\partial t} = P \quad \text{when } \Delta T = (T_c - T_p) = 0$$

- P : power of heat source
- T<sub>c</sub> : calorimeter temperature
- T<sub>p</sub> : pool temperature
- C : heat capacity (calorimetric body)
- k : heat transfer coefficient
- t : time
- x : position

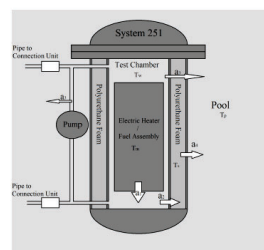
One component heat transfer model

Equilibrium water in calorimeter and heat source

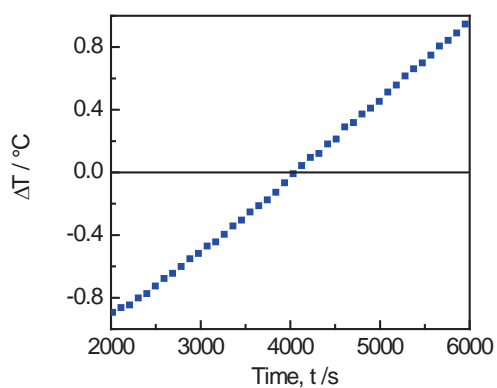
- Calorimetric body at temperature T<sub>c</sub>
- Environment (pool) at a constant temperature T<sub>p</sub>

Conditions

- No spatial temperature distribution in calorimeter
- T<sub>c</sub> = T<sub>p</sub>

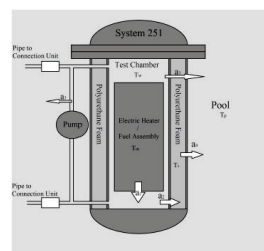


### CLAB CALORIMETER: PRINCIPLE

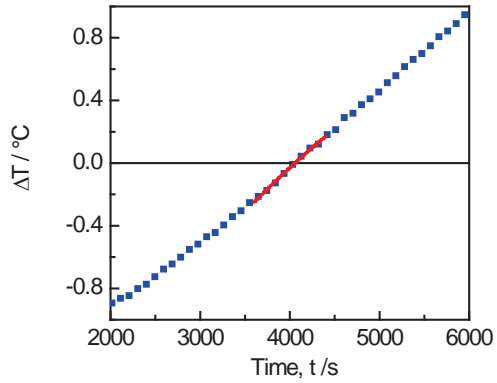


Measurement principle

- Cool down the water in calorimeter
- Stop cooling (continue circulation)
- Measure T<sub>c</sub> and T<sub>p</sub>
  - T<sub>c</sub> : temperature in calorimeter
  - T<sub>p</sub> : temperature in pool
- Determine ΔT = T<sub>c</sub> - T<sub>p</sub> vs time

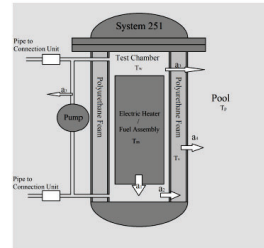


### CLAB CALORIMETER: PRINCIPLE

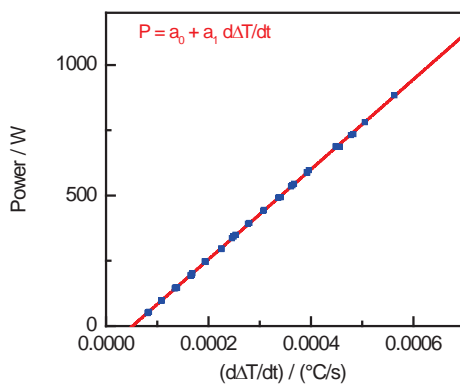


#### Measurement principle

- Cool down the water in calorimeter
- Stop cooling (continue circulation)
- Measure  $T_c$  and  $T_p$
- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$

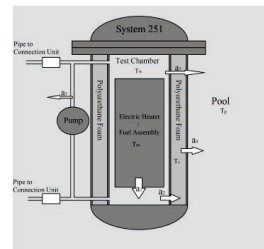


### CLAB CALORIMETER: PRINCIPLE



#### Calibration with an electrical heater

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$
- Fit to data:  $P = a_0 + a_1 d\Delta T/dt$



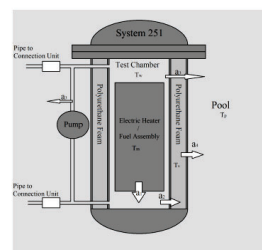
## CLAB CALORIMETER: PRINCIPLE

### Spent nuclear fuel assembly

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  when  $\Delta T = 0$
- $Q = a_0 + a_1 K d\Delta T/dt$
- $P = Q + P_\gamma$ 
  - $K$  : correction factor due to thermal capacity difference between electrical heater and fuel assembly
  - $P_\gamma$  : heat loss due to  $\gamma$ -rays escaping from the calorimeter

### Calibration with an electrical heater

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$
- Fit to data:  $P = a_0 + a_1 d\Delta T/dt$



## CLAB CALORIMETER: PRINCIPLE

### Spent nuclear fuel assembly

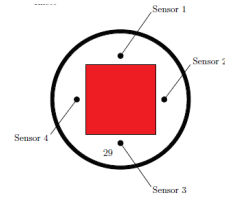
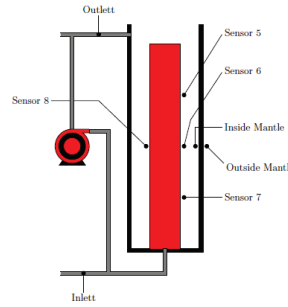
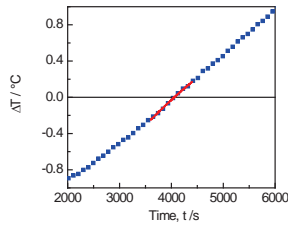
- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  when  $\Delta T = 0$
- $Q = a_0 + a_1 K d\Delta T/dt$
- $P = Q + P_\gamma$ 
  - $K$  : correction factor due to thermal capacity difference between electrical heater and fuel assembly
  - $P_\gamma$  : heat loss due to  $\gamma$ -rays escaping from the calorimeter

### Example

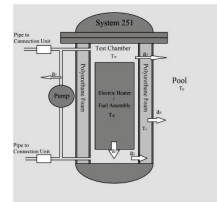
- BWR:  $P = 140$  W
  - $P_\gamma = 3.5$  W (2.5 %)
  - $K = 0.964$
- PWR:  $P = 450$  W
  - $P_\gamma = 13.5$  W (3.0 %)
  - $K = 0.915$



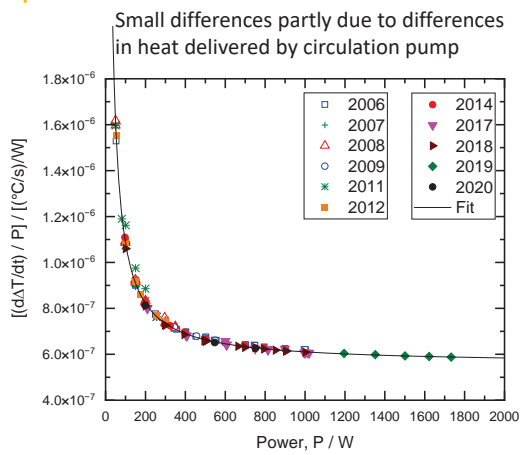
### CLAB CALORIMETER: ANALYSIS PROCEDURE



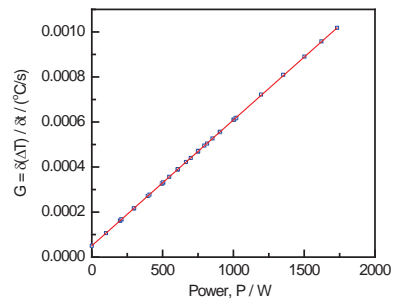
- Define temperature sensors to be used
  - Define analytical function to determine temperature gradient
  - Define optimum time region to fit
  - Define selection criteria for high quality data
- ⇒ Completely independent by JRC/JSI and SKB/Vattenfall



### CALIBRATION BY ELECTRICAL HEATER: RESULTS JRC/JSI



Calibration for blind test and SKB-50 data

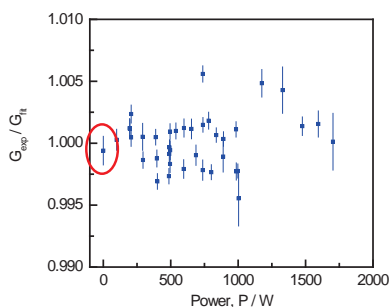


Perfect linear behaviour in whole range: from 0 W to 1800 W  
 No separation needed between low and high heat output as in R-05-62 report!  
 Offset due to heat produced by circulation pump

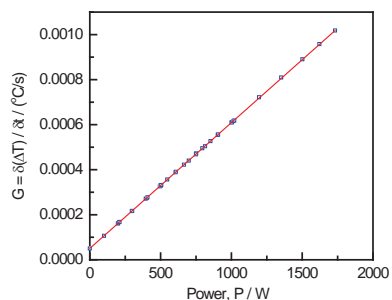


### CALIBRATION BY ELECTRICAL HEATER: RESULTS JRC/JSI

Data within 0.5% for 95% confidence limit



Calibration for blind test and SKB-50 data



Measurement without heater: fully consistent  
(heat delivered by circulation pump)



### BLIND TEST: DECAY HEAT DERIVED FROM CALORIMETER DATA

Correction for difference heater and assembly :  $K = 0.915$

Assembly ID	Decay heat derived from calorimeter measurements, P/ W			
	Blind test paper	JRC/JSI*	JRC/JSI	SKB/Vattenfall
		heater correction	not corrected	
BT01	1604	1584.0	1582.0	1580.0
BT02	1038	1022.6	1021.2	1019.3
BT03	874	859.6	858.5	857.0
BT04	753	740.8	739.8	738.8
BT05	651	640.2	639.3	638.5

Average ratio: 0.999

\*includes a small bias correction on the output of the electrical heater,  $P = 0.182W + 1.00114 P_h$



## BLIND TEST: CORRECTION FOR GAMMA-RAY ESCAPE

See presentations A. Mehic and G. Letnar

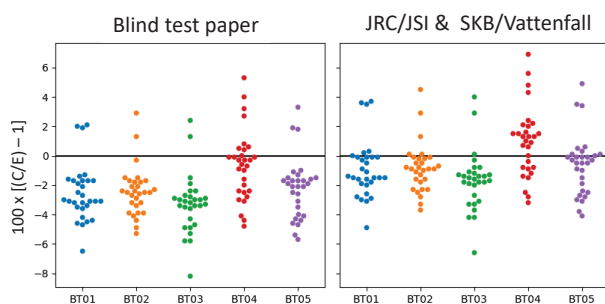
- Dose rate measurements combined with analytical geometry correction
  - Blind test paper
- Gamma-ray transport simulations combined with nuclide inventory
  - SKB/Vattenfall : MCNP + CASMO
  - JRC/JSI : SERPENT + SERPENT(inventory)/MCNP(Bremstrahlung)

Assembly ID	Escaping gamma-ray energy, $P_\gamma$ / W		
	Blind test paper	JRC/JSI	SKB/Vattenfall
BT01	58 (10)	49.4	49.2
BT02	30 (5)	25.3	24.7
BT03	21 (4)	20.6	20.3
BT04	15 (3)	15.0	13.8
BT05	12 (2)	12.8	11.5

Maximum difference 1.3 W



## BLIND TEST: COMPARISON EXPERIMENTAL DATA

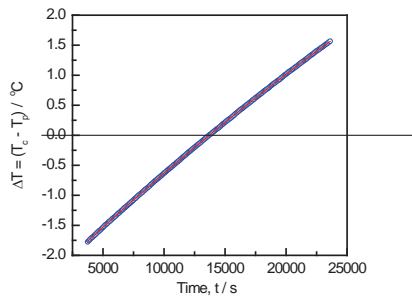


Assembly ID	CT	Average calculated	C/E	
			Blind test	JRC/JSI*
BT01	4.5 a	1620 W	0.975	0.992
BT02	8.6 a	1043 W	0.977	0.995
BT03 (+ Gd)	9.8 a	866 W	0.968	0.984
BT04	13.5 a	763 W	0.993	1.009
BT05	21.4 a	649 W	0.979	0.994

L. Fiorito



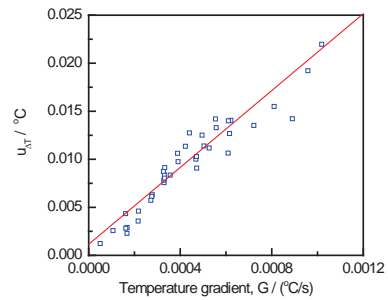
### UNCERTAINTY EVALUATION: RANDOM EFFECTS



Platinum resistance thermometers (PT-100 type), with a declared uncertainty of 0.01 °C.

The measured quantity is a temperature difference!

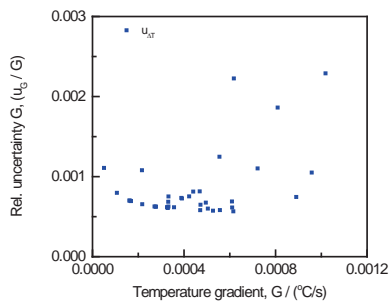
Variance analysis from calibration data ( $\chi^2/\nu = 1$ )



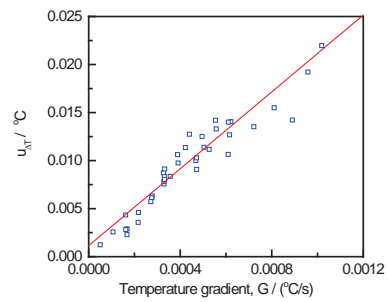
All data consistent with  $u_{\Delta T} = a_0 + a_1 G$   
 $a_0 = 0.0015 \text{ } ^\circ\text{C}$   
 $a_1 = 20 \text{ s}$



### UNCERTAINTY EVALUATION: RANDOM EFFECTS



Variance analysis from calibration data ( $\chi^2/\nu = 1$ )

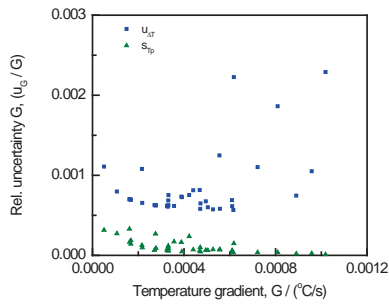


All data consistent with  $u_{\Delta T} = a_0 + a_1 G$   
 $a_0 = 0.0015 \text{ } ^\circ\text{C}$   
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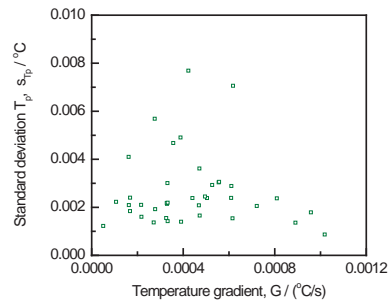


### UNCERTAINTY EVALUATION: RANDOM EFFECTS

$$C \frac{\partial T_c}{\partial t} = [P - k(T_c - T_p)]$$

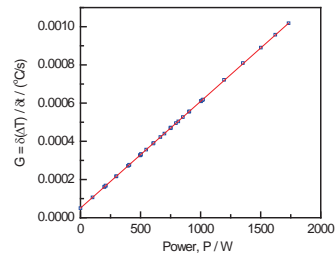
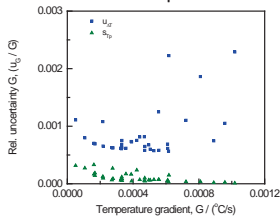


Pool temperature variations

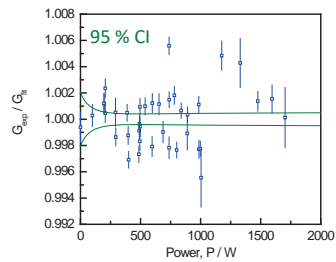
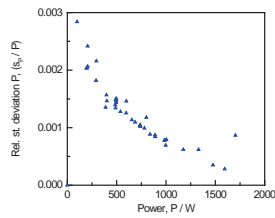


### UNCERTAINTY EVALUATION: RANDOM EFFECTS

Uncertainty on temperature difference  
Temperature variations in pool

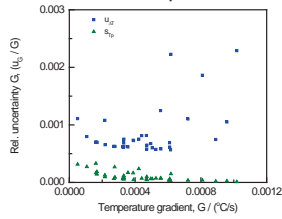


Variations in heater output

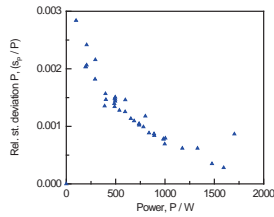


### UNCERTAINTY EVALUATION: RANDOM EFFECTS

Uncertainty on temperature difference  
Temperature variations in pool

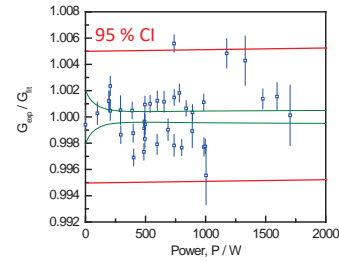


Variations in heater output



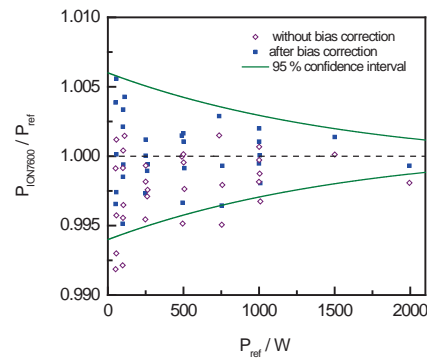
Scatter of data cannot be explained by propagating the uncertainty of random effects

⇒ All data suffer from a 0.25% (CI 68%) additional uncertainty due to hidden effect



### UNCERTAINTY EVALUATION: SYSTEMATIC EFFECTS (ELECTRICAL HEATER)

- Power meter (ION7600) of electrical heater is calibrated by an accredited service using an independent reference instrument
- Calibration data shows that the power  $P_h$  derived by the ION7600 suffers from a small bias effect  
⇒ correction:  $P = c_0 + c_1 P_h$  ( $c_0 = 0.182 \text{ W}$  and  $c_1 = 1.00114$ )
- 95% confidence interval after correction
  - 0.60 % at 0 W
  - 0.13 % at 2000 W



## UNCERTAINTY EVALUATION: SYSTEMATIC EFFECTS (ELECTRICAL HEATER)

- Loss of the power provided by the calibration unit due to cables outside the calorimeter  
The heat loss is estimated from the length and electrical resistance per unit length
  - Outside
    - Length: 2 x 20 m
    - Resistance per unit length: 0.012 Ω/m
  - Inside (heating cable in calorimeter)
    - Length: 261 m
    - Resistance per unit length: 0.10 Ω/m

⇒ Power loss fraction:  $26.1 / (26.1 + 0.48) = 0.982$
- No uncertainty data provided  
⇒ uncertainty evaluation based on least significant figure combined with rectangular distributions
- Probability distribution of correction factor can be approximated by a Gaussian distribution with
  - mean : 0.982
  - standard deviation : 0.00135



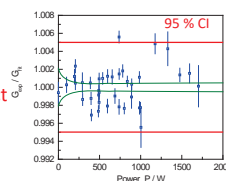
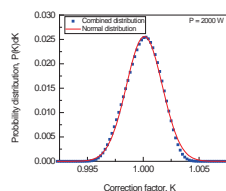
## UNCERTAINTY EVALUATION FUEL ELEMENT

- Systematic effects
  - Heat loss in cables
  - Bias on power meter of heater

Combined uncertainty

Power	$100 \times s_p/P$	95% CI
0	0.34	0.67
1000	0.20	0.40
2000	0.15	0.30

- Calibration constants (negligible)
- + 0.25% (1 st. dev) for hidden effect



- Random effects
  - Uncertainty temperature difference
  - Pool temperature variations

(negligible)



### CORRECTION FACTOR: HEATER - ASSEMBLY

Present correction factor: based on one component heat transfer model (for PWR  $K = 0.915$ ).  
 Verify by a three component heat transfer model

$$C_m \frac{dT_m}{dt} = -a_1(T_m - T_w) + Q_m$$

$$C_w \frac{dT_w}{dt} = a_1(T_m - T_w) - a_2(T_w - T_s) - a_3(T_w - T_p) + Q_w + a_c(T_w - T_c)$$

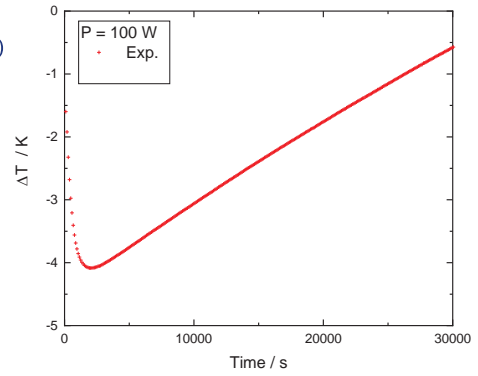
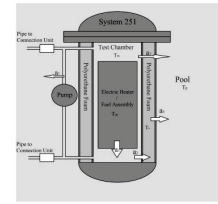
$$C_s \frac{dT_s}{dt} = a_2(T_w - T_s) - a_4(T_s - T_p)$$

Index:

- m : metal (heater or assembly)
- w : water
- s : structure
- p : pool

Parameters/variables

- T : temperature
- C : heat capacity
- a : heat transfer coefficient
- Q : heat source



### CORRECTION FACTOR: HEATER - ASSEMBLY

Present correction factor: based on one component heat transfer model (for PWR  $K = 0.915$ ).  
 Verify by a three component heat transfer model

$$C_m \frac{dT_m}{dt} = -a_1(T_m - T_w) + Q_m$$

$$C_w \frac{dT_w}{dt} = a_1(T_m - T_w) - a_2(T_w - T_s) - a_3(T_w - T_p) + Q_w + a_c(T_w - T_c)$$

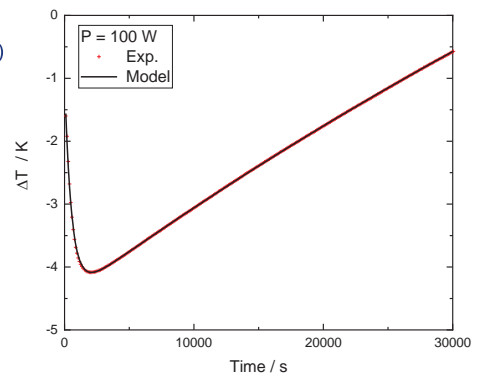
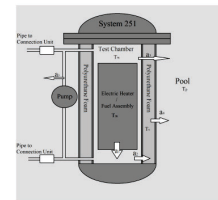
$$C_s \frac{dT_s}{dt} = a_2(T_w - T_s) - a_4(T_s - T_p)$$

Index:

- m : metal (heater or assembly)
- w : water
- s : structure
- p : pool

Parameters/variables

- T : temperature
- C : heat capacity
- a : heat transfer coefficient
- Q : heat source





### CORRECTION FACTOR: HEATER - ASSEMBLY

Present correction factor: based on one component heat transfer model  
 Verify by a three component heat transfer model

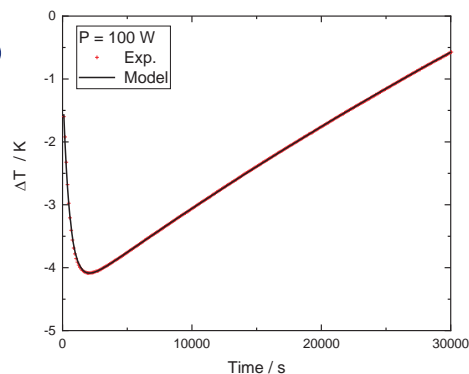
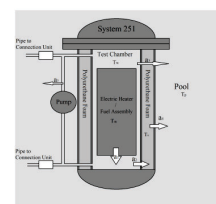
$$C_m \frac{dT_m}{dt} = -a_1(T_m - T_p) + Q_m$$

$$C_w \frac{dT_w}{dt} = a_1(T_m - T_w) - a_2(T_w - T_s) + Q_w + a_c(T_w - T_c)$$

$$C_s \frac{dT_s}{dt} = a_2(T_w - T_s) - a_4(T_s - T_p)$$

Work in progress

<p>Index:</p> <ul style="list-style-type: none"> <li>- m : metal (heater or assembly)</li> <li>- w : water</li> <li>- s : structure</li> <li>- p : pool</li> </ul>	<p>Parameters/variables</p> <ul style="list-style-type: none"> <li>- T : temperature</li> <li>- C : heat capacity</li> <li>- a : heat transfer coefficient</li> <li>- Q : heat source</li> </ul>
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### CLAB CALORIMETER: CONCLUSIONS

- Decay power from CLAB calorimeter are valuable (high quality) data for code validation
  - Measurement process and analysis procedures of CLAB calorimeter are well understood
  - Some previous results suffer from a bias effect
  - Uncertainty evaluation in progress
    - Preliminary estimation (95% confidence limit) : < 2%
    - **Main task: evaluate factor to correct for difference heater – assembly**
- Performance of present calorimeter can be improved:
  - Control characteristics of cables of the heater (length, resistivity, etc..)
  - Regular calibration of heater with reference instrument
  - Improved operational procedure, e.g.
    - Minimum cooling temperature
    - Perform long measurements to verify K based on steady-state condition



## NDA: GAMMA-RAY SPECTROSCOPY

Used as part of Radiochemical analysis of PIE data (see presentation S. Van Winckel)

### NDA: Direct measurements (no chemistry)

- Axial BU profile determination (presentation K. Govers, J. Kirkegaard)
  - e.g. Govers et al., Technical Report – BLG – 1142, April 2019, “Characterization of Belgian Spent Fuel Assemblies”
- Determination of nuclide inventory ratios
  - e.g. Caruso et al., ( $^{134}\text{Cs}/^{137}\text{Cs}$ ,  $^{134}\text{Cs}/^{154}\text{Eu}$  ratios (comparison with HPLC-MC-ICP-MS) (Nucl. Instr. Meth. A 589 (2008) 425)  
High-performance liquid chromatography coupled to inductively coupled plasma – Mass spectrometry
- Tomography: material properties
  - e.g. Caruso et al., J. Nucl. Sci. Techn. 45 (2008) 828
  - Holcombe et al., Nucl. Instr. Meth. A 837 (2016) 99

## NDA: GAMMA-RAY SPECTROSCOPY FOR CODE VALIDATION

### Axial BU profile determination

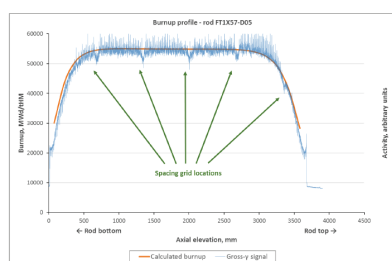


Figure 44 Calculated burnup axial profile for the same fuel rod as in Figure 43. The measured gross-gamma scan, dominated by the Cs-137 signal and, hence, roughly proportional to the burnup is superimposed. Spicing grid positions are easily identified on the activity signal, as they induce a local loss of power (loss of moderation).

### Spent nuclear fuel rod

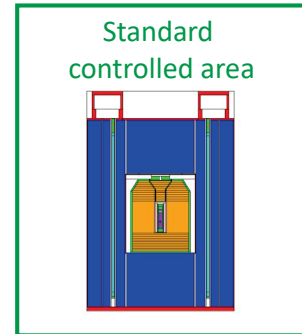
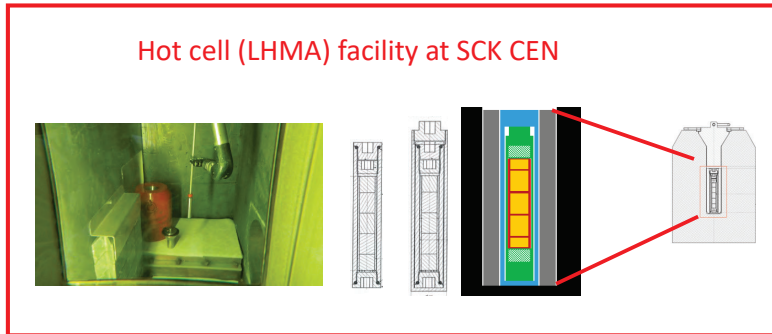
- rod D05 of FT1X57 (PWR)
- PWR Assembly (15 x 15):  
188  $\text{UO}_2$  rod (4.5 wt%  $^{235}\text{U}/\text{U}$ ) and 16  $(\text{U,Gd})\text{O}_2$  rods
- Irradiated at Tihange 1
- Rod used for other international project (First-Nuclides, REGAL, WETFUEL & AGAF, SF-ALE)

Govers et al., Technical Report – BLG – 1142, April 2019, “Characterization of Belgian Spent Fuel Assemblies”

## NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

**Non Destructive Assay method** to determine the neutron output of a **SNF** segment sample under **standard controlled area** conditions

Collaboration SCK CEN

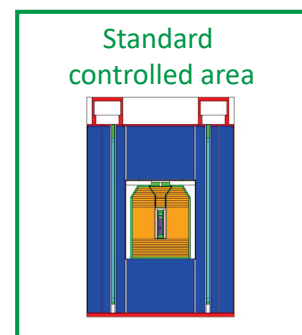
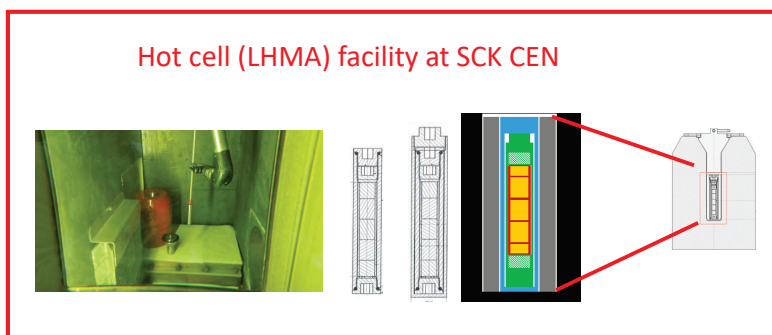


## NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

B. Bully (inv.)

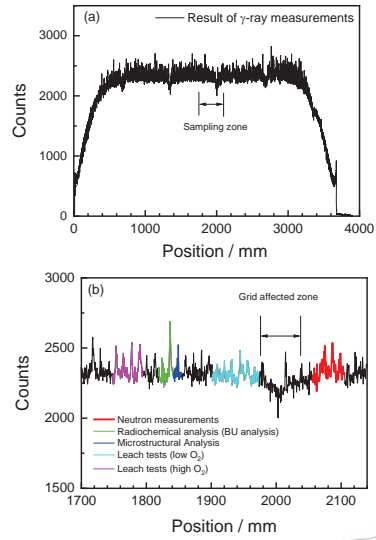
**Databook of flat burnup samples from rod D05 extracted from fuel assembly FT1X57, Tihange 1 NPP**

Data on fuel initial composition and irradiation history  
Authors: J. Speckers, M. Verwer  
Affiliates: MMS/RMA, SCK CEN



## EURAD: VALIDATION OF DEPLETION CODES USING THE REGAL SAMPLE

- **Irradiation history** of the SNF
  - Segment (~ 50 mm) from rod D05 of FT1X57 (PWR)
  - PWR Assembly (15 x 15):  
188 UO<sub>2</sub> rod (4.5 wt% <sup>235</sup>U/U) and 16 (U,Gd)O<sub>2</sub> rods
  - Irradiated at Tihange 1
  - Rod used for other international project (First-Nuclides, REGAL, WETFUEL & AGAF, SF-ALE)
- **SNF segment sample** by NDA
  - Part of a set of 4 samples (REGAL project)
    - Radiochemical analysis (BU)
    - Microstructural analysis
    - Leach tests (low O<sub>2</sub>)
    - Leach tests (high O<sub>2</sub>)



## NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

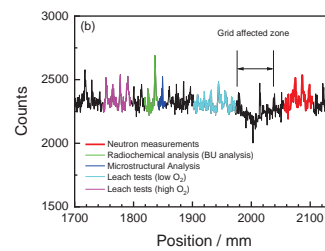
- Irradiation history burnup (REGAL project)

BU indicator	Analysis date	Nuclide Inventory N <sub>x</sub> /N <sub>0</sub>	BU MWd/kg
<sup>137</sup> Cs	21/10/2013	2.539 (55) × 10 <sup>-3</sup>	52.6 (11)
<sup>143+144</sup> Nd	05/02/2014	5.701 (60) × 10 <sup>-3</sup>	53.95 (56)
<sup>145+146</sup> Nd	05/02/2014	3.643 (38) × 10 <sup>-3</sup>	53.05 (56)
<sup>148</sup> Nd	05/02/2014	0.974 (21) × 10 <sup>-3</sup>	53.3 (12)
<sup>150</sup> Nd	05/02/2014	0.463 (21) × 10 <sup>-3</sup>	52.2 (23)
Average:			52.78 (37)

Govers et al., EPJ Nucl. S&T, 8 (2022) 18

- SNF segment sample: characteristics

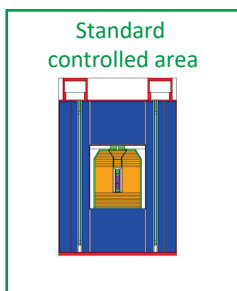
Parameter	Value
Segment length	52.01 (4) mm
Segment weight	42.616 (1) g
Cladding weight	6.71 (4) g
Net fuel weight	35.91 (4) g



⇒ Accurate information about design and operational history

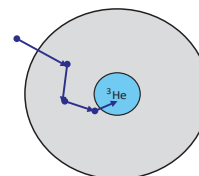


## NEUTRON EMISSION MEASUREMENT: CONVENTIONAL WELL COUNTER (AWCC)

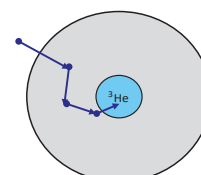
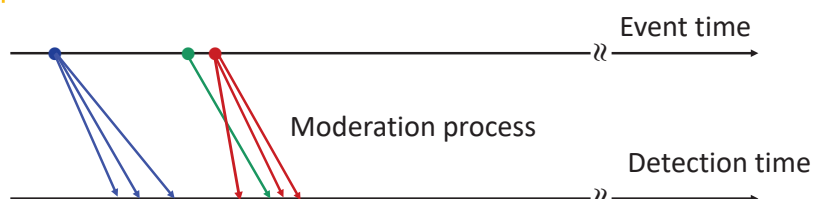


- Neutron detection
  - Modified AWCC (only internal cavity)
  - $^3\text{He}$  detectors in polyethylene
  - Detection efficiency for  $^{252}\text{Cf(sf)}$ :  $\epsilon = 0.28$
- Signal processing: shift register
  - Totals, reals and accidentals
- Data analysis: Hage's point model (JRC Ispra)

W. Hage and D.M. Cifarelli, NSE 89 (1985) 159 – 176  
 W. Hage and D.M. Cifarelli, NIMA 236 (1985) 165 – 177  
 D.M. Cifarelli and W. Hage, NIMA 251 (1986) 550 – 563



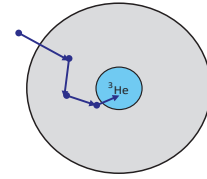
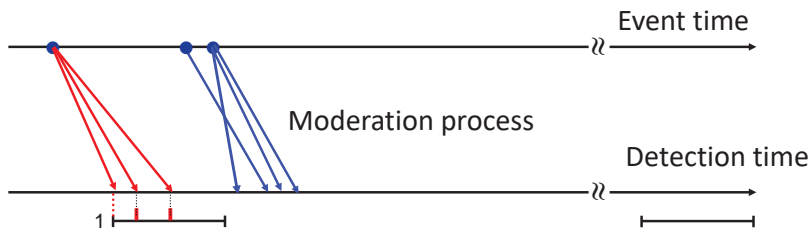
## SHIFT – REGISTER: PRINCIPLE



- Every detected neutron will trigger the opening of two gates
- Gate close to the signal (signal trigger)
  - Delayed gate



**SHIFT – REGISTER: PRINCIPLE**

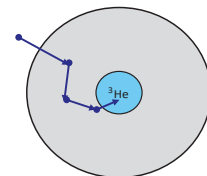
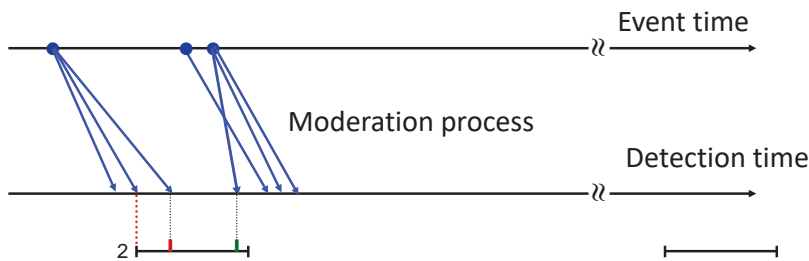


Signal trigger  
**R + A**

Delayed trigger  
**A**



**SHIFT – REGISTER: PRINCIPLE**

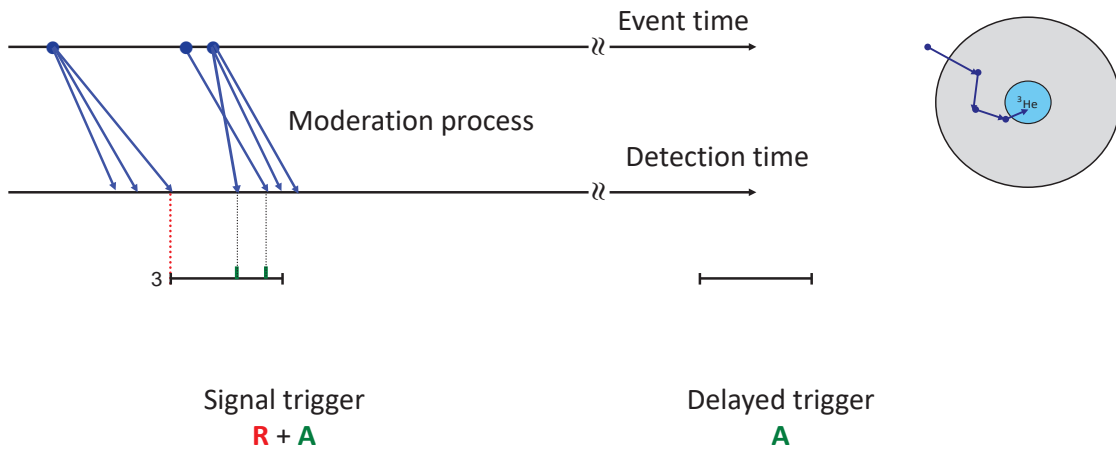


Signal trigger  
**R + A**

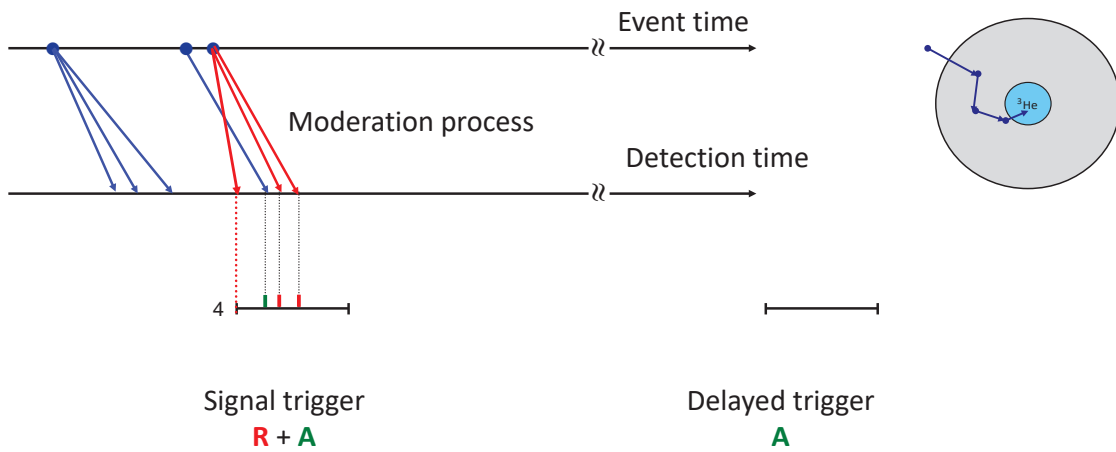
Delayed trigger  
**A**



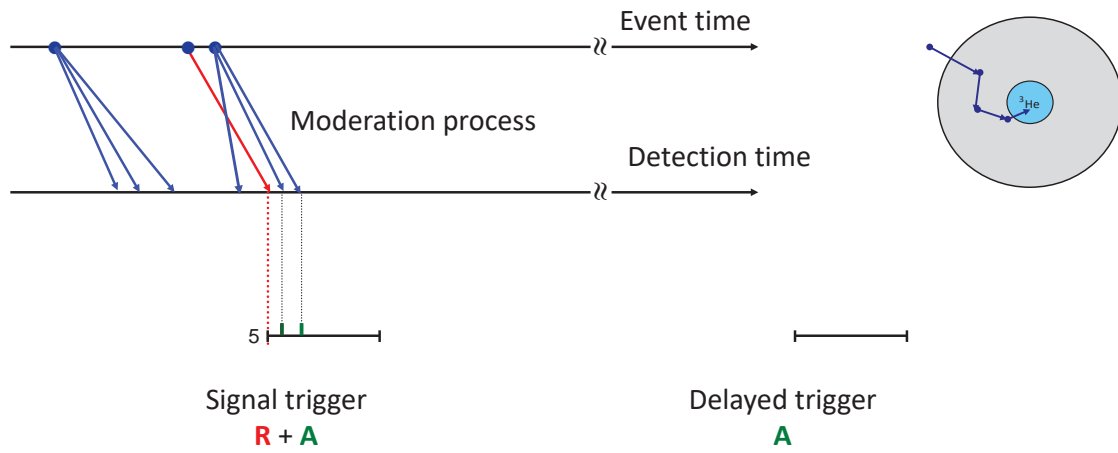
**SHIFT – REGISTER: PRINCIPLE**



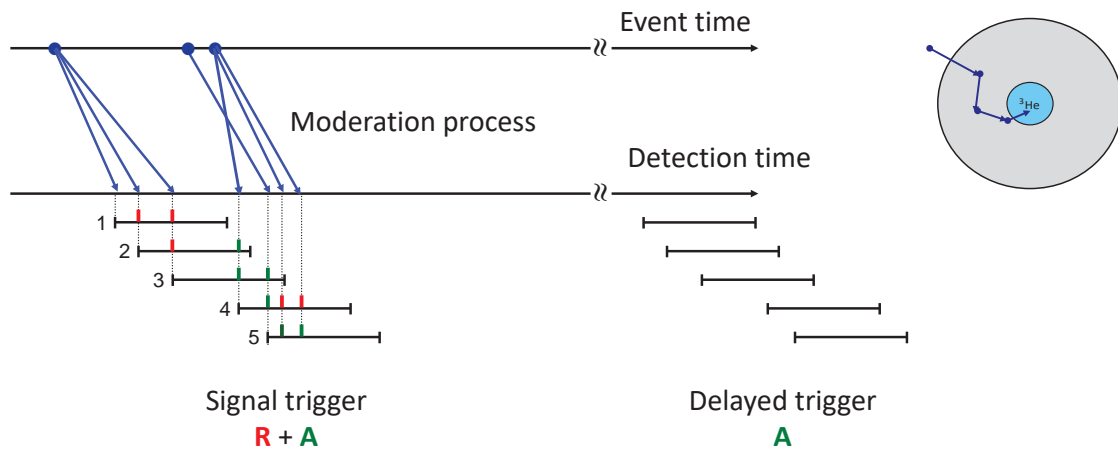
**SHIFT – REGISTER: PRINCIPLE**



**SHIFT – REGISTER: PRINCIPLE**

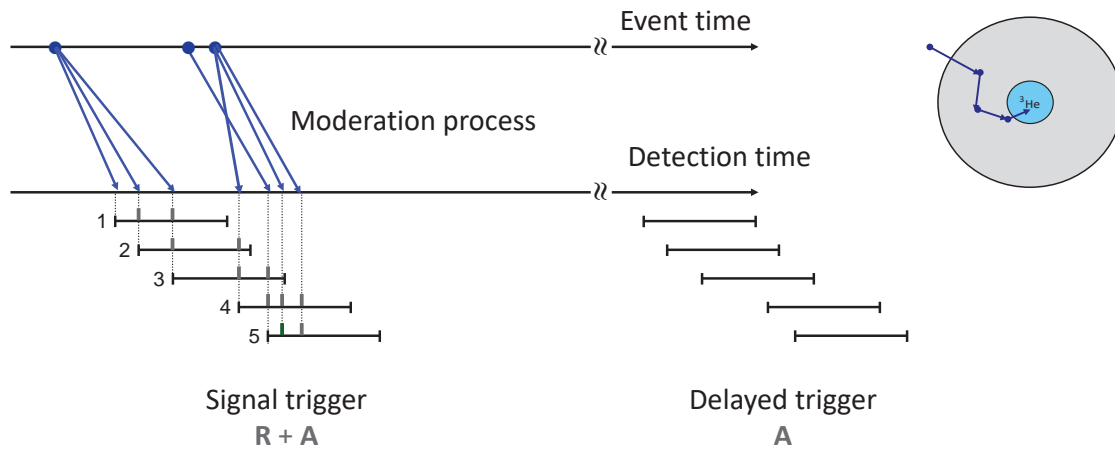


**SHIFT – REGISTER: PRINCIPLE**





### SHIFT – REGISTER: PRINCIPLE



### DATA ANALYSIS: HAGE'S POINT MODEL

$$T = \epsilon_{sf} S_{sf} M [1 + \alpha]$$

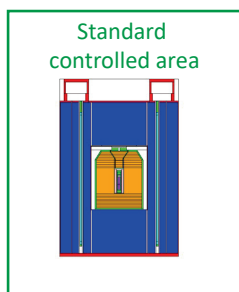
$$R = \epsilon_{sf}^2 f S_{sf} M^2 \left[ \frac{v_{sf(2)}}{v_{sf(1)}} + \frac{v_{(2)}}{v_{(1)} - 1} (M - 1)(1 + \alpha) \right]$$

- Experiment
  - T : total count rate corrected for dead time and background
  - R : reals count rate corrected for dead time and background
- Detector characteristics
  - $\epsilon_{sf}$  : detection efficiency
  - f : gate fraction
- Nuclear data
  - $v_{sf(1)}$  and  $v_{sf(2)}$  : 1<sup>st</sup> and 2<sup>nd</sup> order factorial moments of P(v) distribution for (sf)
  - $v_{sf(1)}$  and  $v_{sf(2)}$  : 1<sup>st</sup> and 2<sup>nd</sup> order factorial moments of P(v) distribution for (n,f)
- Sample properties
  - $S_{sf}$  : production rate for prompt fission neutrons by (sf)
  - $\alpha$  : ratio between neutron production rate by ( $\alpha, n$ ) and  $S_{sf}$
  - M : neutron leakage multiplication (derived by MC simulations,  $M \approx 1.006$ )

W. Hage and D.M. Cifarelli, NSE 89 (1985) 159 – 176  
 W. Hage and D.M. Cifarelli, NIMA 236 (1985) 165 – 177  
 D.M. Cifarelli and W. Hage, NIMA 251 (1986) 550 – 563



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE



- ⇒ Improve
- detector characteristics
  - nuclear data

$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

$$\alpha = 0.039 (18)$$

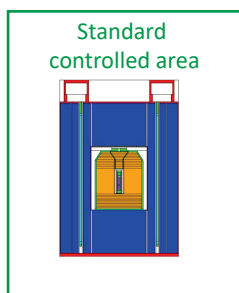
#### Uncertainty evaluation and sensitivity analysis

Uncertainty component, $x_j$	$\frac{u_{x_j}}{x_j}$	$\frac{u_{S_{sf,j}}}{u_{S_{sf}}}$	$\frac{u_{\alpha,j}}{u_{\alpha}}$
Totals rate, T	0.0008	< 0.01	0.05
Reals rate, R	0.0027	0.15	0.17
Detection efficiency, $\epsilon_{sf}$	0.0055	0.60	0.35
Gate fraction, f	0.0071	0.40	0.45
First order factorial moment, $v_{sf(1)}$	0.0037	0.20	0.25
Second order factorial moment, $v_{sf(2)}$	0.0120	0.67	0.80
Multiplication, M	0.0020	0.01	< 0.01

Schillebeeckx et al., Frontiers in Energy Research 11 (2023) 1162367



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE



$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

$$S_{\alpha,n} / S_{sf} = 0.039 (18)$$

Good agreement with:

Calculated from radiochemical analysis :

$$S_{sf} = 699 (28) \text{ s}^{-1} \text{ g}^{-1}$$

Note: uncertainty radiochemical analysis > 4% (> factor 2)



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

Code	Library	C/E LIB
ALEPH2	JEFF-3.3	0.944
SCALE	ENDF/B-VII.0	0.963
Serpent2 (2.1.29)	ENDF/B-VII.0	1.008
	ENDF/B-VII.0	1.017
	ENDF/B-VII.0	1.015
	JEFF-3.1.2	0.933
	JEFF-3.3	0.969
	JEFF-3.3 (1)	1.091
	JEFF-3.3 (2)	1.013
	JEFF-3.3 (3)	1.006
	JEFF-4T1	0.977
	JEFF-4T2	0.998
JENDL-4.0u (4)		
JENDL-5.0	1.089	

$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

All calculations normalised to produce the same <sup>148</sup>Nd inventory

Importance of normalization

- (1)  $\sigma(n,\gamma) = 0$  for <sup>147</sup>Nd
- (2)  $\sigma(n,\gamma)$  for <sup>147</sup>Nd from JENDL-4.0u
- (3)  $\sigma(n,\gamma)$  for <sup>147</sup>Nd from JEFF-4T1



### NEUTRON EMISSION: ABSOLUTE MEASUREMENTS OF SNF SEGMENT SAMPLE

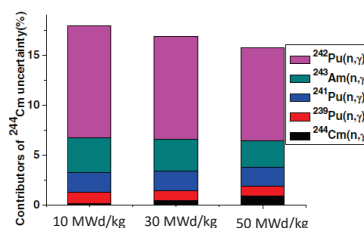
Code	Library	C/E LIB
ALEPH2	JEFF-3.3	0.944
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	ENDF/B-VII.0	1.017
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	JEFF-3.1.2	0.933
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	JEFF-3.3 (1)	1.091
	JEFF-3.3 (2)	1.013
	JEFF-3.3 (3)	1.006
	JEFF-4T1	0.977
	JEFF-4T2	0.998
JENDL-4.0u (4)		
JENDL-5.0	1.089	

$$S_{sf} = 678 (12) \text{ s}^{-1} \text{ g}^{-1}$$

Uncertainty theoretical estimation

Burnup	Relative uncertainty
10 MWd/kg	12.1 %
30 MWd/kg	11.1 %
50 MWd/kg	10.0 %

Contribution mainly from : <sup>242</sup>Pu(n,γ) & <sup>243</sup>Am(n,γ)



Tiejun Zu et al., Annals of Nuclear Energy 94 (2016) 399



## NEUTRON EMISSION: DECAY DATA AND NU-BAR

Code	Library	$S_{sf}/(1/gS)$		LIB/REC
		LIB	REC	
ALEPH2	JEFF-3.3	640.1	642.4	0.996
SCALE	ENDF/B-VII.0	653.0	652.1	1.001
Serpent2 (2.1.29)	ENDF/B-VII.0	683.7	678.1	1.008
	ENDF/B-VII.0	689.4	685.3	1.006
	ENDF/B-VII.0	688.5	684.3	1.006
	JEFF-3.1.2	632.5	623.8	1.014
	JEFF-3.3	656.8	648.9	1.012
	JEFF-3.3 (1)	739.4	730.5	1.012
	JEFF-3.3 (2)	686.8	678.6	1.012
	JEFF-3.3 (3)	682.2	673.9	1.012
	JEFF-4T1	662.6	654.6	1.012
	JEFF-4T2	676.4	668.3	1.012
JENDL-4.0u (4)		715.9		
JENDL-5.0		738.4	733.9	1.006

REC (recommended data)

Decay data : DDEP  
[http://www.lnhb.fr/ddep\\_wg/](http://www.lnhb.fr/ddep_wg/)

Neutron emission data: Santi and Muller  
 Nucl. Sci. Eng. 160 (2008) 199

## NEUTRON EMISSION: DECAY DATA AND NU-BAR

Nuclide	Decay constant, $\lambda$ / (1/s)		(sf) branching		nu-bar	
	ENDF/REC	JEFF/REC	ENDF/REC	JEFF/REC	ENDF/REC	JEFF/REC
<sup>238</sup> U	1.0000	1.0000	1.0018	1.0018	1.0101	1.0101
<sup>238</sup> Pu	1.0004	1.0005	1.0054	1.0054	1.0091	1.0091
<sup>240</sup> Pu	1.0000	0.9997	1.0000	1.0000	0.9986	0.9986
<sup>242</sup> Pu	0.9986	0.9986	1.0000	1.0000	0.9963	0.9963
<sup>242</sup> Cm	0.9995	0.9996	0.9591	0.9591	0.9953	0.9953
<sup>244</sup> Cm	0.9999	1.0061	1.0147	1.0147	0.9917	0.9917
<sup>246</sup> Cm	0.9921	0.9970	0.9996	0.9996	1.0061	1.0061

- Differences not only due to neutron emission
- Largest difference between (sf) branching values
- Compensation effect for neutron emission of <sup>244</sup>Cm(sf)

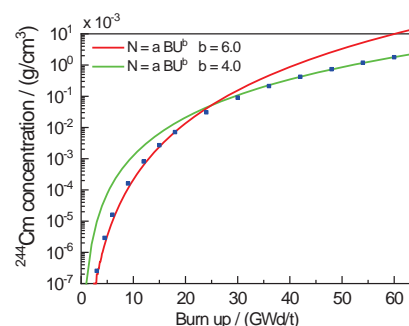
## NEUTRON EMISSION RATE

$$N = aBU^b$$

$$b = 4 \text{ for BU} > 20 \text{ MWd/kg}$$

$$\frac{\delta N}{N} = b \frac{\delta BU}{BU}$$

- ⇒ Total neutron emission extremely sensitive to BU
- ⇒ Good BU indicator



## NEUTRON MEASUREMENTS: CONCLUSIONS

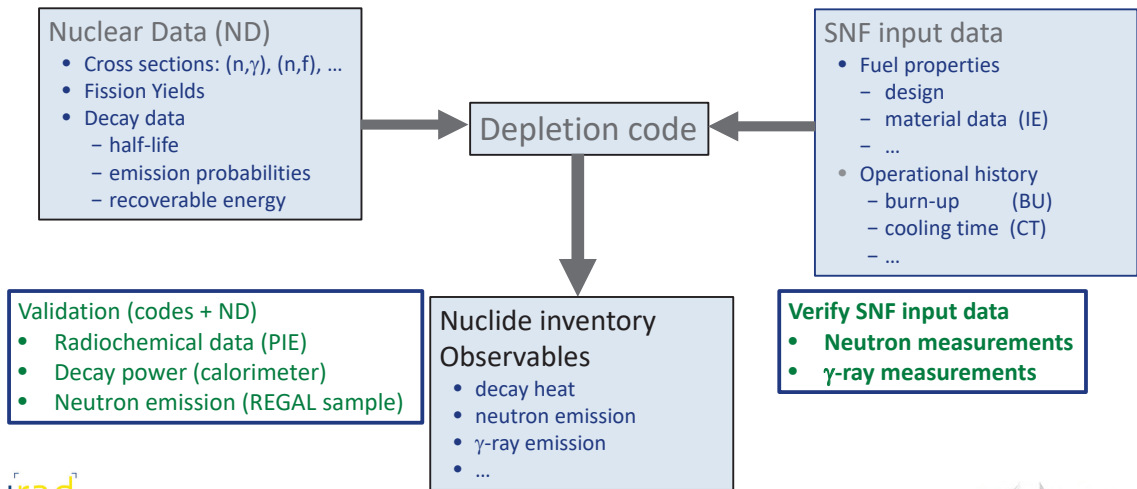
### Neutron emission (sensitive to BU)

- Neutron measurements presented in this work is a valuable method for code validation
- Neutron measurements can be used to verify the BU of an SNF assembly in industrial conditions

### Nuclear data:

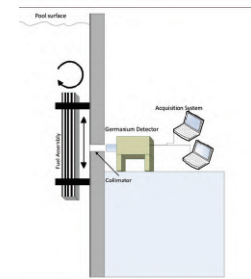
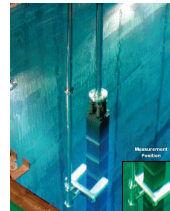
- Recommended decay and neutron emission data not always adopted in evaluated data libraries
- $^{241}\text{Pu}(n,\gamma)$  and  $^{243}\text{Am}(n,\gamma)$  cross sections require a re-evaluation (use of available experimental data)
- $P(v)$  of  $^{244}\text{Cm}(sf)$  needs to be improved
- $^{147}\text{Nd}(n,\gamma)$  cross section in JEFF-3.3 and ENDF/B-VIII.0 are too high (important for normalisation of PIE data)
- Fission yields for  $^{148}\text{Nd}$  in JENDL-5.0 are too low

**TASK 2: PRODUCE VALIDATED DEPLETION CALCULATIONS WITH REALISTIC UNCERTAINTIES**

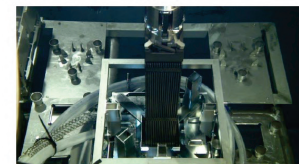


**NDA FOR CHARACTERISATION OF FUEL ASSEMBLIES**

- $\gamma$ -ray spectroscopy
  - HPGe detector
  - Axial scanning
- FORK detector
  - Total neutron emission
  - Total  $\gamma$ -ray emission

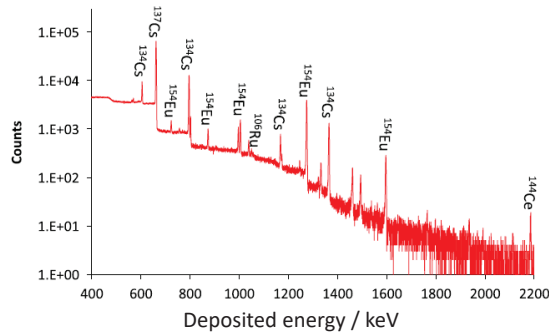


- DDSI (Differential Die-away Self Interrogation)
- PNAR (Passive Neutron Albedo Reactivity)

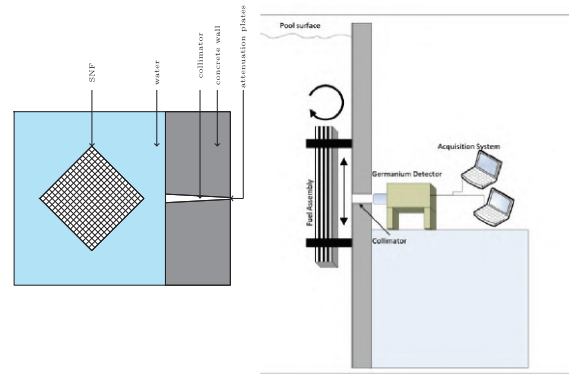


### γ-RAY SPECTROSCOPIC MEASUREMENTS

- HP Ge detector
- Axial scanning



<sup>137</sup>Cs: 662 keV  
<sup>134</sup>Cs: 605, 796, 1365 keV  
<sup>154</sup>Eu: 996, 1004, 1274, 1596 keV



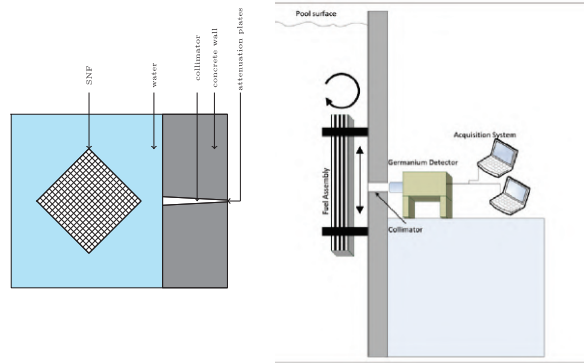
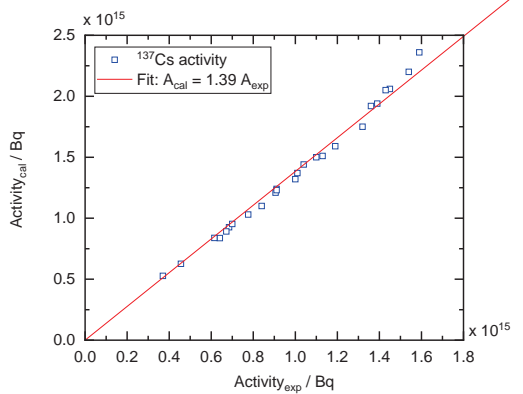
Solans et al., ANE 192 (2023) 109941  
 Bengtsson et al., Nucl. Techn. 208 (2022) 295  
 Vaccaro et al., NIMA A833 (2016) 208  
 Vo et al., NIMA 830 (2016) 325  
 Favalli et al., NIMA 820 (2016) 102



### <sup>137</sup>Cs ACTIVITY

$$\langle A_{cal}/A_{exp} \rangle = 1.39$$

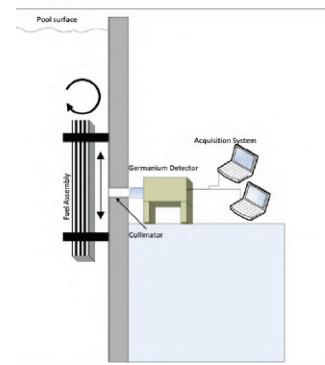
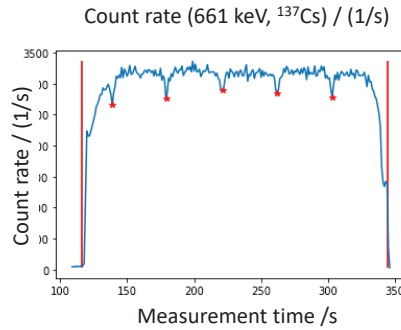
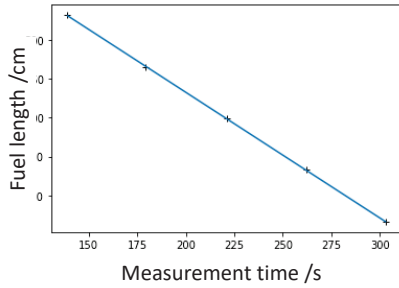
$$St. dev A_{cal}/A_{exp} = 3.3\%$$



Bengtsson et al., Nucl. Techn. 208 (2022) 295



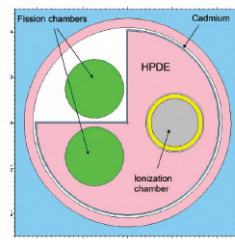
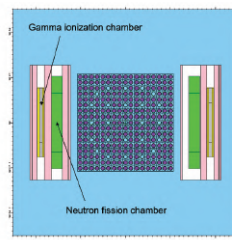
### AXIAL PROFILE <sup>137</sup>Cs ACTIVITY (BURNUP PROFILE)



### NEUTRON AND $\gamma$ -RAY MEASUREMENTS: FORK DETECTOR

Passive NDA: detection of neutrons and  $\gamma$ -rays emitted by SNF assembly

- Neutron detection
  - <sup>235</sup>U fission chambers (FC)
  - Fission chamber with and without Cd
  - Total neutron count rate
- $\gamma$ -ray detection
  - Ionisation chamber (IC)
  - Total  $\gamma$ -ray dose rate measurement



Vaccaro et al., NIMA 888 (2018) 202-217





### FORK MEASUREMENTS AT CLAB

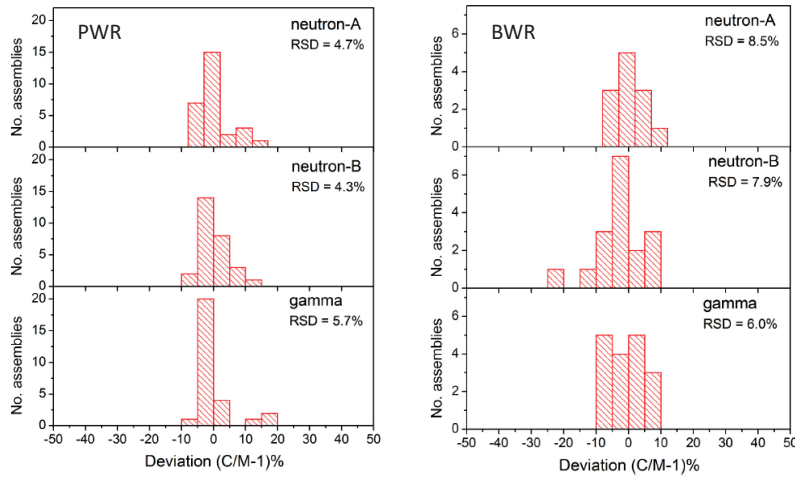
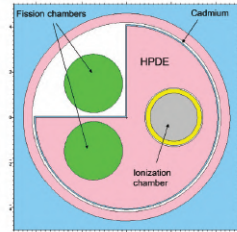
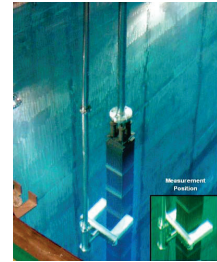


Fig. 10. Histogram distribution of the deviations between calculated (C) and measured (M) gamma, neutron-A, and neutron-B detector count rates for PWR assemblies measured at the Swedish Clab facility.

Fig. 11. Histogram distribution of the deviations between calculated (C) and measured (M) gamma, neutron-A, and neutron-B detector count rates for BWR assemblies measured at the Swedish Clab facility.



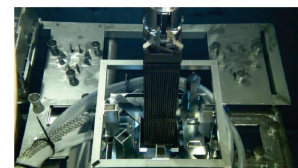
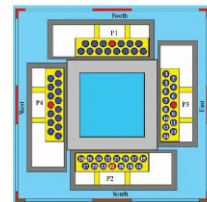
Vaccaro et al., NIMA 888 (2018) 202-217



### DIFFERENTIAL DIE-AWAY SELF-INTERROGATION (DDSI)

Passive NDA: detection of neutrons emitted by SNF assembly  
 Developed at LANL for nuclear safeguards applications

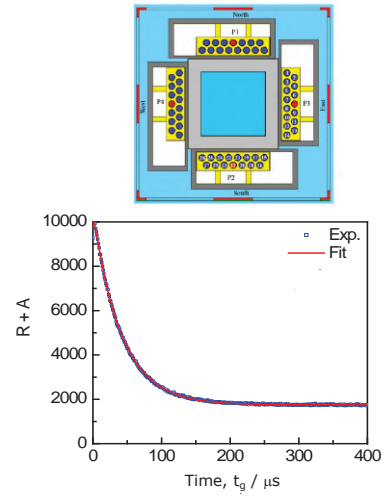
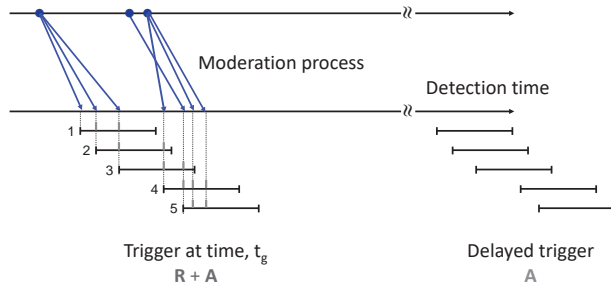
- Neutron production
  - Primary neutrons: mainly prompt fission neutrons from  $^{244}\text{Cm}(sf)$
  - Prompt fission neutrons from neutron induced fission in fuel mainly after neutron moderation in the water of the pool
- Detection principle
  - $^3\text{He}$  in moderator
  - Detection of **correlated neutrons**: construct **Rossi-alpha distribution**



Trahan et al., NIMA 955 (2020) 163329

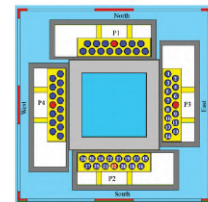
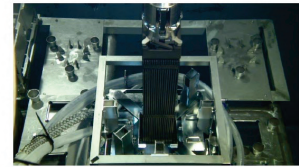
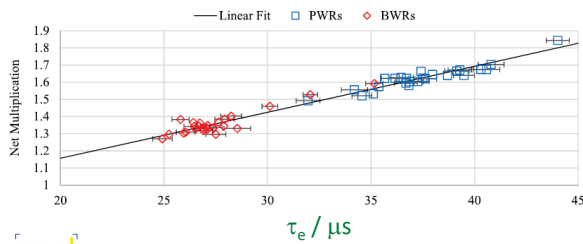
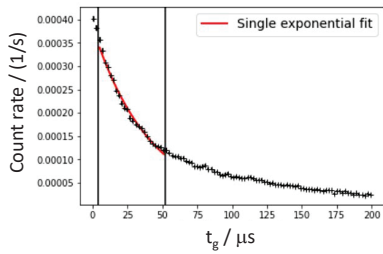


### DDSI: ROSSI-ALPHA DISTRIBUTION



### DDSI: ROSSI-ALPHA DISTRIBUTION

$$R = R_0 e^{-\frac{t}{\tau_e}}$$

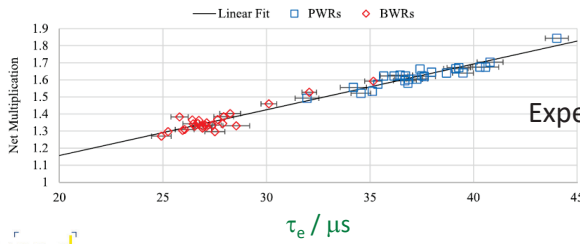
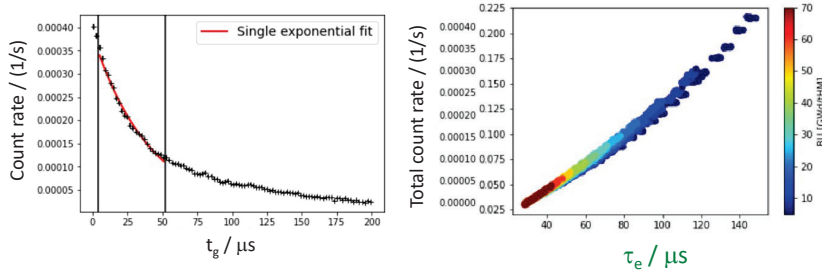


Trahan et al., NIMA 955 (2020) 163329

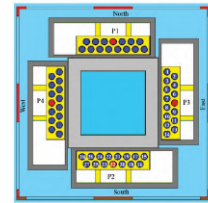
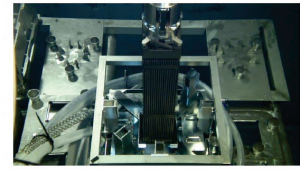


DDSI: ROSSI-ALPHA DISTRIBUTION

$$R = R_0 e^{-\frac{t}{\tau_e}}$$



Experiments at CLAB



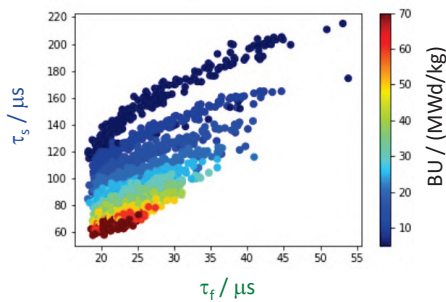
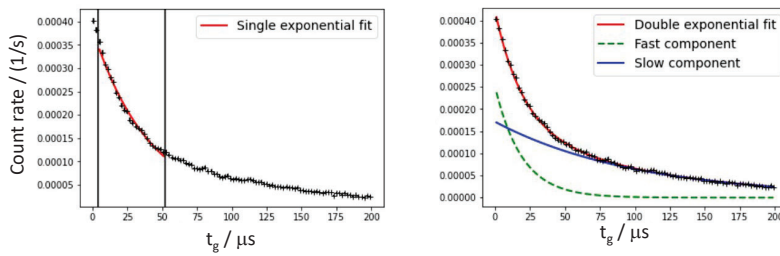
Trahan et al., NIMA 955 (2020) 163329



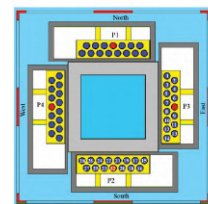
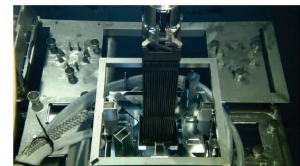
DDSI: MC SIMULATIONS

$$R = R_0 e^{-\frac{t}{\tau_e}}$$

$$R = R_{01} e^{-\frac{t}{\tau_f}} + R_{02} e^{-\frac{t}{\tau_s}}$$



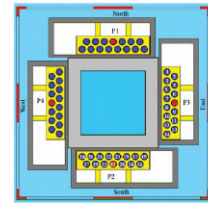
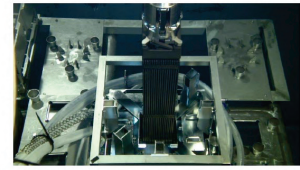
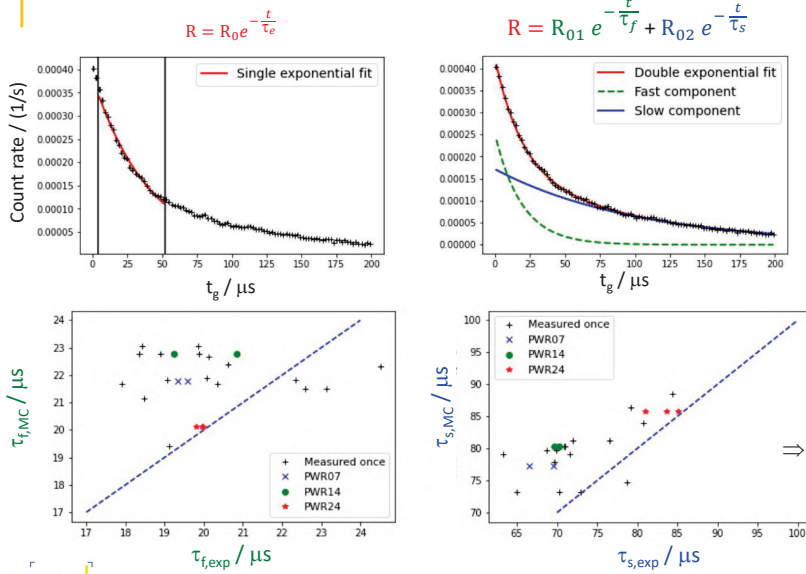
⇒ Additional information



Solans et al., IAEA Symposium, November 2022 IAEA-CN-303-137



**DDSI: EXPERIMENTS AT CLAB**



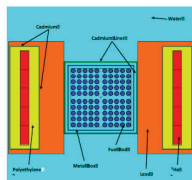
Solans et al., IAEA Symposium, November 2022  
IAEA-CN-303-137



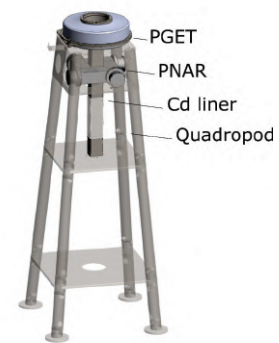
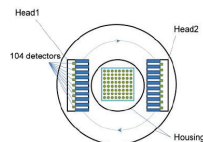
**FINLAND: ONKALO**

Marita Mosconi

- Passive Neutron Albedo Reactivity (PNAR)  
LANL development, Tobin et al., NIMA 897 (2018) 32 - 37



- Passive Gamma Ray Emission Tomography (PGET)  
IAEA development, Honkamaa et al., Symp. Int. Safeguards, IAEA Vienna 2014



## CONCLUSIONS

- NDA for code validation
  - Calorimeter at CLAB: ideal instrument to validate code performance for decay power prediction
  - Neutron correlation measurements is a valuable method to validate code performance for neutron emission prediction and an alternative to radiochemical methods to determine the  $^{244}\text{Cm}$  inventory
  - ND need to be improved to use neutron emission as BU indicator
- NDA of SNF assemblies
  - Methods based on neutron and gamma-ray emission detection require improvement



## CONTRIBUTORS

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S. Kopecky	(JRC Geel)
G. Letnar	(JSI)
A. Mehic	(SKB)
B. Pedersen	(JRC Ispra)
P. Romojaro	(SCK CEN)
V. Solans	(UU)
M. Verwerft	(SCK CEN)
G. Žerovnik	(JSI)



sck cen



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## BIBLIOGRAPHY

GUM: Guide to the expression of Uncertainty in Measurement

- Evaluation of measurements data (JCGM 100:2008(E))
- Supplement 1 – Propagation of distribution using a Monte Carlo method (JCGM 101:2008)
- Supplement 2 – Extension to any number of quantities (JCGM 102:2011)
- An introduction to the “GUM” and related documents (JCGM 104:2009)
- Guide to the expression of uncertainty in measurement Part 6: Developing and using measurement models (JCGM GUM-6:2020)

VIM: International Vocabulary of Metrology

- VIM – Basic and general concepts and associated terms (JCGM 200:2012)  
<https://www.bipm.org/en/committees/jc/jcgm/publications>

Spent nuclear fuel observables and key nuclides

- Gauld et al., “Nuclide importance to criticality safety, decay heating and source terms related to transport and interim storage of high-burnup LWR fuel”, Report NUREG/CR-6700, ORNL/TM-2000/284 (2001)
- Žerovnik et al. “Observables of interest for the characterisation of Spent Nuclear Fuel”, EUR 29301 EN (2018) , JRC112361
- Schillebeeckx et al., “Characterisation of spent nuclear fuel by theoretical calculations and non-destructive analysis”, JRC114178 (2019)

Nuclear data

- Nuclear data libraries at JANIS NEA, [https://www.oecd-nea.org/jcms/pl\\_39910/janis](https://www.oecd-nea.org/jcms/pl_39910/janis)
- Decay data, <http://www.nucleide.org/DDEP.htm>
- Nichols et al., “Handbook of nuclear data for safeguards: database extensions, august 2008”, INDC-2453, INDC(NDS) – 0534



## BIBLIOGRAPHY

Non-destructive assay of SNF

Calorimeter

- SKB, “Measurements of Decay Heat in Spent Nuclear Fuel at the Swedish Interim Storage Facility”, Clab, SKB Report R-05-62, December 2006
- B.D. Murphy and I.C. Gauld, “Spent Fuel Decay Heat Measurements Performed at the Swedish Central Interim Storage Facility”, Report ORNL/TM-2008/016, Oak Ridge National Laboratory, February 2010

Neutron

- Schillebeeckx et al., “An absolute measurements of the neutron production rate of a spent nuclear fuel sample used for depletion code validation”, Frontiers in Energy Research 11 (2023) 1162367
- Schillebeeckx et al., “A non-destructive method to determine the neutron production rate of a sample of spent nuclear fuel under standard controlled area conditions”, JRC Technical Report EUR 30379 EN, 2020
- Tupasela et al., “Passive neutron albedo reactivity measurements of spent fuel nuclear fuel”, Nucl. Instr. Meth. A986 (2020) 164707
- Trahan et al., “Results of the Swedish spent fuel measurements field trials with the DDSI”, Nucl. Instr. Meth. A955 (2020) 163329
- Tobin et al., “Measuring spent fuel assembly multiplication in borated water with a PNAR instrument”, Nucl. Instr. Meth. A897 (2018) 32
- Vaccaro et al., “Advancing the FORK detector for quantitative spent nuclear fuel verification”, Nucl. Instr. Meth. A888 (2018) 202

γ-ray

- Solans et al., “Spent nuclear fuel passive gamma analysis and reproducibility application to SKB-50 assemblies”, Ann. Nucl. Energy 192 (2023) 109941
- Bengtsson et al., “Experimental method for the verification of calculated <sup>137</sup>Cs content in nuclear fuel assemblies”, Nucl. Techn. 208 (2022) 295
- Vaccaro et al., “PWR and BWR spent fuel assembly gamma spectra measurements”, Nucl. Instr. Meth. A833 (2016) 208



# Thank you

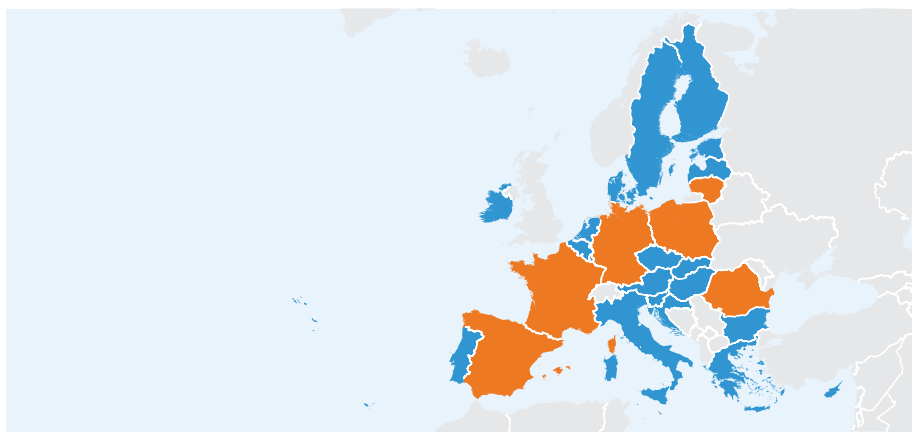
NRAS school: 13 – 17 May 2024  
ENEN2+



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**2.6 Observables of interest (in spent fuel); G. Žerovnik, JSI-;  
School on "Nuclear data for depletion calculations"11/09 -  
15/09/2023**





# SANDA

Supplying Accurate Nuclear Data for  
energy and non-energy Applications



HORIZON2020

## OBSERVABLES OF INTEREST (IN SPENT FUEL)

P. Schillebeeckx, [G. Žerovnik](#)



*The school has been funded by the Euratom Research and Training Programme 2014-2018 under Grant Agreement No. 847552 (SANDA).*

Training material

1



- Context: spent nuclear fuel management
- Characteristics of spent nuclear fuel (SNF)
  - Radionuclide inventory of SNF
  - Gamma-ray emission
  - Decay heat
  - Neutron emission
  - Key nuclides
- SNF depletion calculations
  - Principles
- Validation of depletion codes
  - Radiochemical data
  - Calorimeter at CLAB
  - Neutron measurements
- Summary and conclusions
- Material
  - Learning outcomes
  - Keywords
  - Additional bibliography and references



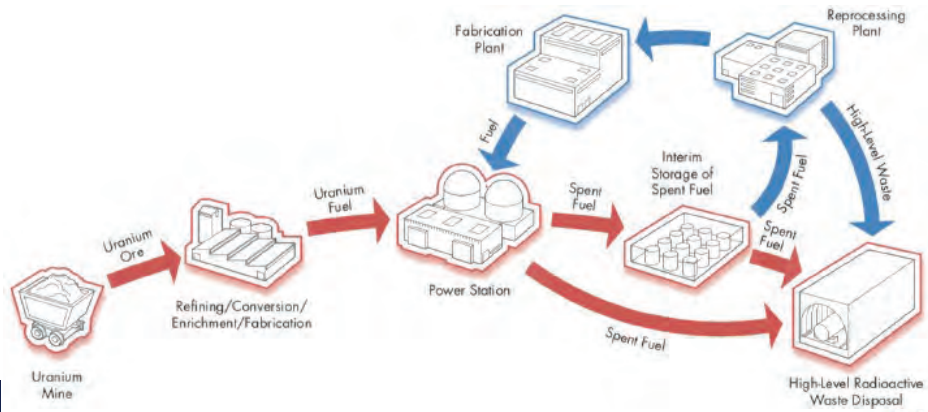
Training material





## NUCLEAR FUEL CYCLE

Nuclear fuel cycle  
(open or closed)  
produces waste



Training material



## SNF CHARACTERISATION

An accurate characterisation of **Spent Nuclear Fuel (SNF)** is required for a **safe, ecological and cost effective** operation of the facilities involved in **SNF management** (transport, storage, handling, reprocessing and disposal):

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ , Fission Products (BUC)
- Fissile material :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- Long-term safety : e.g.  $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$



- A reliable determination of these observables including **realistic uncertainties** requires a **good understanding** of the underlying physics process
- **Difficult** to be **measured** directly, in particular during **industrial operation**

Training material







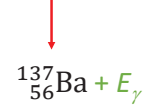
**$\beta^-$  - DECAY BY NEUTRON RICH NUCLIDES: e.g.  $^{137}\text{Cs}$**

- $T_{1/2} = 30.05 (8) \text{ a}$
- $Q_{\beta^-} = 1175.73 (17) \text{ keV}$

$$A = \lambda N = N \frac{\ln 2}{T_{1/2}}$$

$$P = \lambda N E_{rec}$$

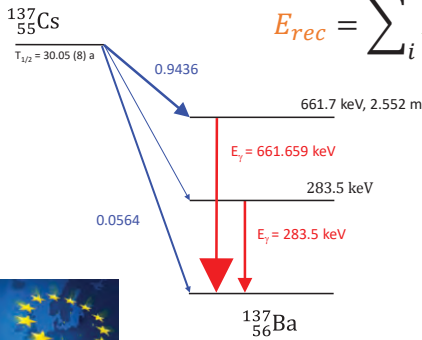
$$E_{rec} = \sum_i P_{\gamma i} E_{\gamma i} + \langle E_{e^-} \rangle < Q_{\beta^-}$$



Gamma-ray emission probability:  $P_{\gamma}$

$E_{\gamma}$	$P_{\gamma}$
661.7 keV	0.8499 (20)
283.5 keV	$5.8 (8) \times 10^{-6}$

[http://www.nucleide.org/DDEP\\_WG/Nuclides/Cs-137\\_tables.pdf](http://www.nucleide.org/DDEP_WG/Nuclides/Cs-137_tables.pdf)



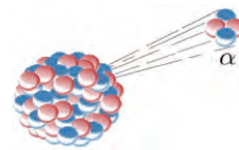
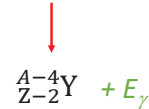
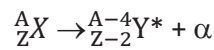
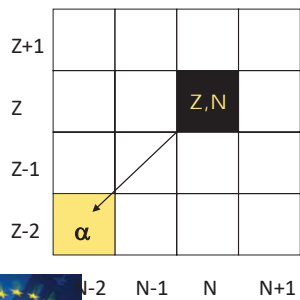
More in presentation by Mark Kellet

Training material



**$\alpha$  - DECAY**

Radioactive decay in which nucleus emits  $\alpha$ -particle ( $^4\text{He}$  nucleus) and transforms into nucleus with 4 less nucleons ( $2n, 2p$ )



in heavy nuclei

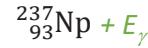
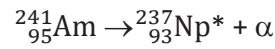
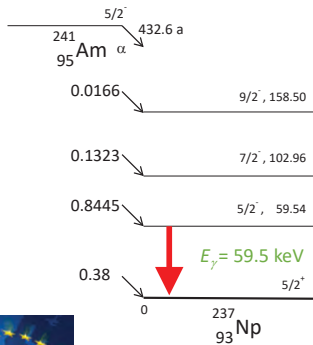
Training material





**α - DECAY BY ACTINIDES: e.g. <sup>241</sup>Am**

- $T_{1/2} = 432.6$  (6) a
- $Q_{\alpha} = 5637.82$  (12) keV



α -particle emission probability:

$E_{\alpha}$	$P_{\alpha}$
5388.3 keV	0.0166 (3)
5442.9 keV	0.1323 (10)
5485.6 keV	0.8445 (10)

[http://www.nucleide.org/DDEP\\_WG/Nuclides/Am-241\\_tables.pdf](http://www.nucleide.org/DDEP_WG/Nuclides/Am-241_tables.pdf)

$$E_{rec} = \sum_i P_{\gamma i} E_{\gamma i} + \sum_j P_{\alpha j} E_{\alpha j} = Q_{\alpha}$$

Training material

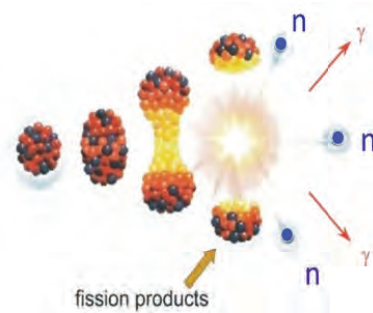


**SPONTANEOUS FISSION**

Fission: nucleus splits up into fission products (FP)

e.g. <sup>238,240,242</sup>Pu(sf), <sup>242,244,246</sup>Cm(sf), <sup>252</sup>Cf(sf)

- FP: acceleration due to Coulomb repulsion
- FP: strongly excited, emission of
  - Prompt fission neutrons (PFN)
  - Prompt fission γ-rays (PFG)



$$S_n = \lambda_{SF} N \langle \nu \rangle = \lambda x_{SF} N \langle \nu \rangle$$

$$P = \lambda_{SF} N E_{rec} = \lambda x_{SF} N E_{rec}$$

$$E_{rec} = \langle \nu \rangle \langle E_n \rangle + \langle \nu_{\gamma} \rangle \langle E_{\gamma} \rangle + \langle E_{rec,fp} \rangle$$

Prompt fission neutrons important for Non-Destructive Assay (NDA)

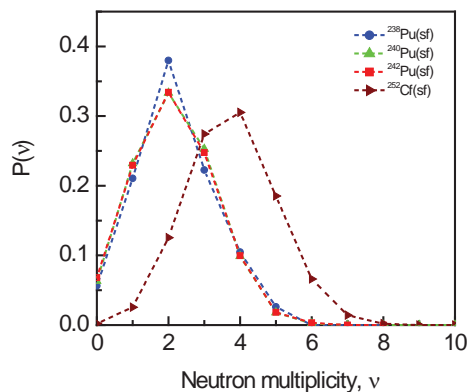


Training material



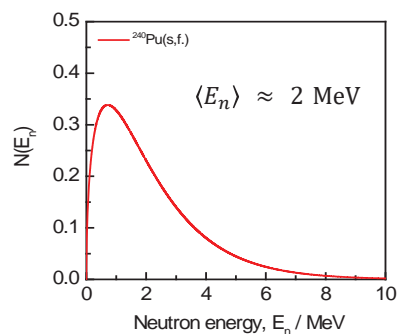


### PROMPT FISSION NEUTRONS: MULTIPLICITY AND ENERGY



Emission of prompt fission neutrons:

- statistical process
- $\langle v \rangle > 1$



Training material



### PROMPT FISSION NEUTRONS: EMISSION PROBABILITY

Nuclide	T <sub>1/2</sub> / a	Main decay mode	(sf) branch x 100	<v>	S <sub>n,sf</sub> (s <sup>-1</sup> g <sup>-1</sup> )
<sup>238</sup> U	4.468 10 <sup>9</sup>	α	5.45 10 <sup>-5</sup>	1.990	1.35 10 <sup>-2</sup>
<sup>238</sup> Pu	<b>87.74</b>	<b>α</b>	<b>1.85 10<sup>-7</sup></b>	<b>2.21</b>	<b>2592</b>
<sup>239</sup> Pu	24110	α	3.1 10 <sup>-10</sup>	2.219	2.18 10 <sup>-2</sup>
<sup>240</sup> Pu	<b>6561</b>	<b>α</b>	<b>5.7 10<sup>-6</sup></b>	<b>2.154</b>	<b>1023</b>
<sup>241</sup> Pu	14.29	β <sup>-</sup>	5.74 10 <sup>-13</sup>	2.27	4.5 10 <sup>-2</sup>
<sup>242</sup> Pu	<b>373500</b>	<b>α</b>	<b>5.49 10<sup>-4</sup></b>	<b>2.145</b>	<b>1725</b>
<sup>241</sup> Am	432.6	α	4.30 10 <sup>-10</sup>	2.46	1.3
<sup>242</sup> Cm	<b>0.446</b>	<b>α</b>	<b>6.36 10<sup>-4</sup></b>	<b>2.54</b>	<b>2.10 10<sup>7</sup></b>
<sup>244</sup> Cm	<b>18.1</b>	<b>α</b>	<b>1.37 10<sup>-4</sup></b>	<b>2.72</b>	<b>1.08 10<sup>7</sup></b>
<sup>252</sup> Cf	<b>2.645</b>	<b>α</b>	<b>3.10</b>	<b>3.757</b>	<b>2.31 10<sup>12</sup></b>



Training material



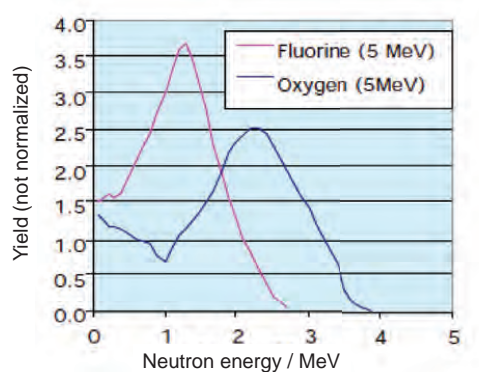


## NEUTRON PRODUCTION BY ( $\alpha,n$ ) REACTIONS

Additional neutron source,  $S_{n,\alpha}$

SNF:  $\alpha$  - decay of actinides followed by ( $\alpha,n$ ) reaction in light elements

- ( $\alpha,n$ ) reactions
  - $^{18}\text{O}(\alpha,n)^{21}\text{Ne}$
  - $^{17}\text{O}(\alpha,n)^{20}\text{Ne}$
  - $^{19}\text{F}(\alpha,n)^{22}\text{Na}$
- Neutron energy (emission)
  - $\text{O}(\alpha,n)$  :  $\langle E_n \rangle \sim 2$  MeV
  - $\text{F}(\alpha,n)$  :  $\langle E_n \rangle \sim 1$  MeV
- $\nu \equiv 1$   
used to separate prompt fission neutrons from ( $\alpha,n$ ) neutrons in neutron correlation counting (NDA)



Training material



## SPENT NUCLEAR FUEL: DEFINITIONS

- Initial enrichment (IE)
  - amount of  $^{235}\text{U}$  relative to the total amount of U (or actinides) in the fresh fuel
  - $^{235}\text{U}/\text{U}$  mostly expressed in wt. %
- Cooling time (CT)
  - Time period since the end of neutron irradiation
- Burnup (BU)
  - Measure of the total energy production
 
$$E_{tot} \approx E_{rec,f} \times N_f$$
    - $E_{tot}$  : total energy
    - $E_{rec,f}$  : energy per fission
    - $N_f$  : total number of fission events
  - Mostly defined as: total energy divided by total amount of actinides in initial fuel in MWd/kg (time integrated power/amount of initial fuel)



Training material





### NEUTRON EMISSION BY SPENT NUCLEAR FUEL

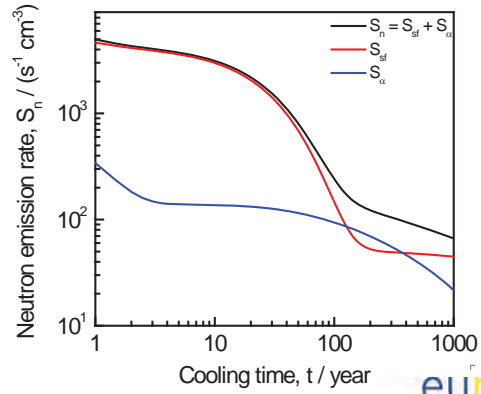
$$S_n(t) = \sum_k S_{n,k}(t)$$

- $S_{n,k}(t)$  : contribution of radionuclide k
- $S_{n,k}(t) = (s_{sf,k} + s_{\alpha,n,k}) N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $s_{sf,k}$  : specific neutron emission rate of nuclide k due to **spontaneous fission**
  - $s_{\alpha,k}$  : specific neutron emission rate of nuclide k due to **( $\alpha$ ,n) reactions**



Training material

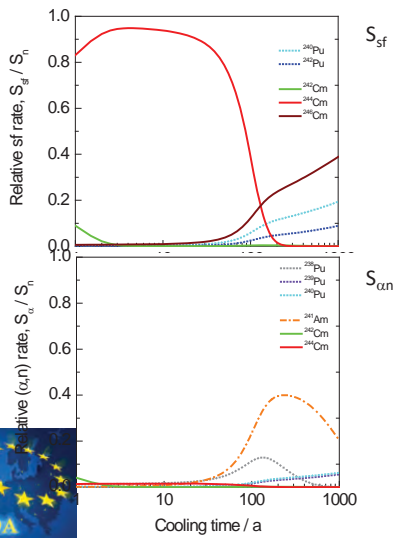
PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg



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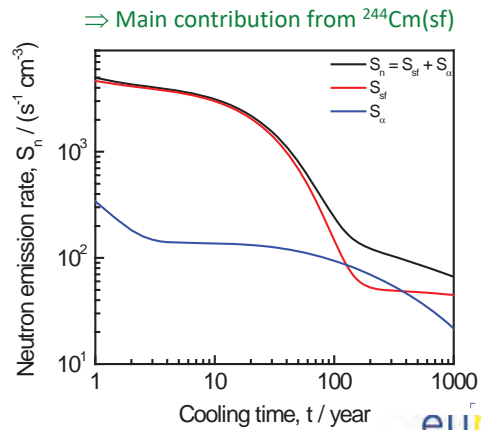


### NEUTRON EMISSION BY SPENT NUCLEAR FUEL



Training material

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg



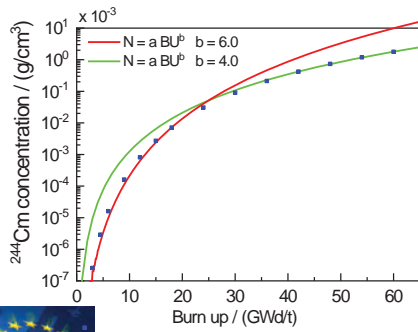
16





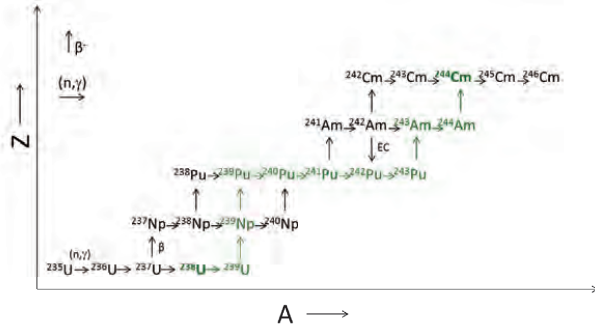
### <sup>244</sup>Cm PRODUCTION: A COMPLEX PROCESS

<sup>244</sup>Cm :  $N = aBU^b$   
 $b \approx 4$  for  $BU = 45$  MWd/kg       $\frac{\delta N}{N} = b \frac{\delta BU}{BU}$



$S_n = \frac{\ln 2}{T_{1/2}} x_{SF} \langle \nu \rangle = 4.5(1) \times 10^{-15} \text{ s}^{-1}$

- Sequence of
- (n,γ) reactions (6)
  - β<sup>-</sup> decays (4)



- $T_{1/2} = 18.11(3)$       Ref.: Nudat2; Singh and Browne, Nucl. Data Sheets 109 (2008) 2439
- $x_{SF} = 1.38(4) \times 10^{-6}$       Ref.: JEFF-3.3; Plompen et al., Eur. Phys. J. A 56 (2020) 181
- $\langle \nu \rangle = 2.6875$       Ref.: JEFF-3.3

Training material



17



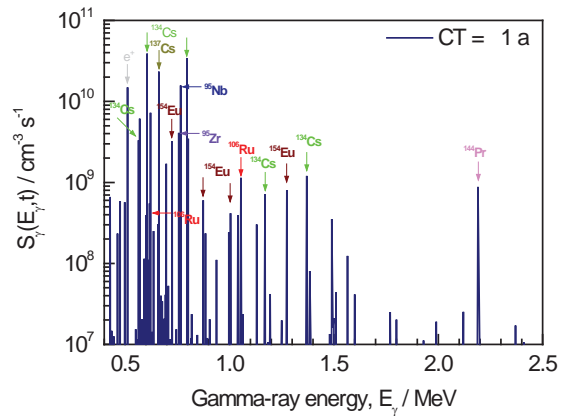
### GAMMA-RAY EMISSION BY SNF

$S_\gamma(t) = \sum_k S_{\gamma,k}(E_\gamma, t)$

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a



PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg



Training material



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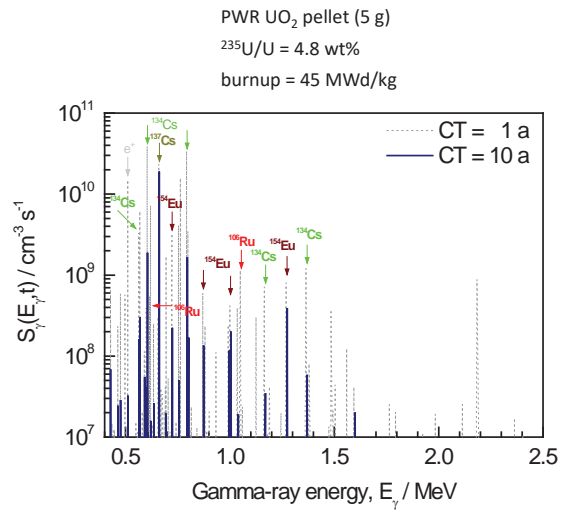
**GAMMA-RAY EMISSION BY SNF**

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

<sup>95</sup> Nb	35.0 d
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<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a



Training material



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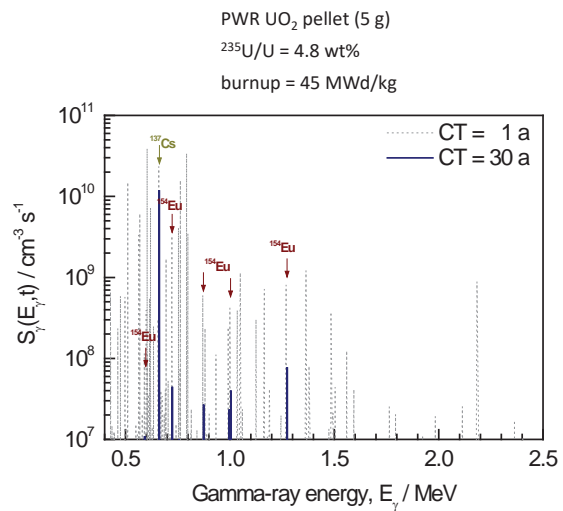
**GAMMA-RAY EMISSION BY SNF**

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

<sup>95</sup> Nb	35.0 d
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<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a



Training material



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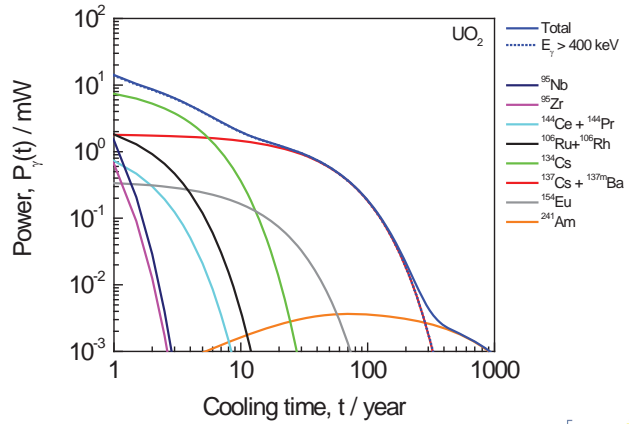


### GAMMA-RAY EMISSION: DECAY HEAT RATE (POWER)

$$P_\gamma(t) = \sum_k \lambda_k N_k(t) \int E_\gamma S_{\gamma,k}(E_\gamma, t) dE_\gamma$$

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a
<sup>241</sup> Am	432.6 a

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg



Training material

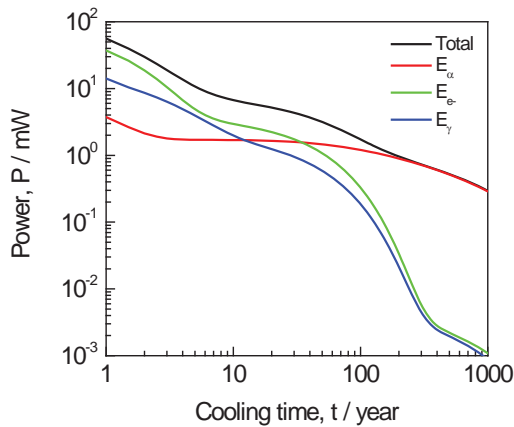


### DECAY POWER PRODUCED BY SNF

$$P(t) = \sum_k P_k(t)$$

- $P_k(t)$  : contribution of radionuclide k
- $P_k(t) = p_k N_k(t) = \lambda_k E_{rec,k} N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $p_k$  : specific decay heat rate of nuclide k

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg



Training material



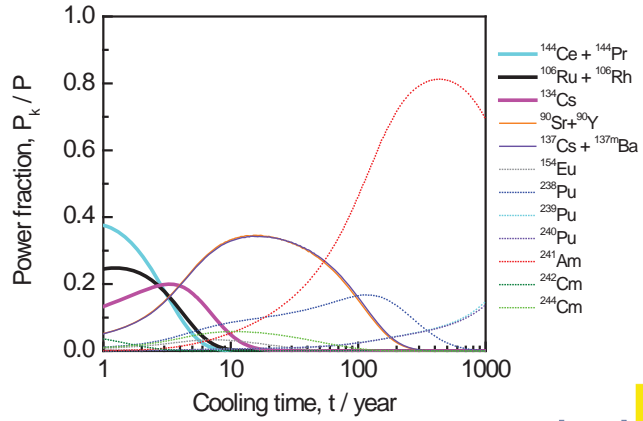


**DECAY POWER PRODUCED BY SNF**

- 1 a ≤ t ≤ 10 a
  - <sup>144</sup>Ce / <sup>144</sup>Pr
  - <sup>106</sup>Ru / <sup>106</sup>Rh
  - <sup>134</sup>Cs
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
- 10 a ≤ t ≤ 100 a
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
  - <sup>238</sup>Pu
  - <sup>241</sup>Am
  - <sup>244</sup>Cm
- 100 a ≤ t
  - <sup>241</sup>Am
  - <sup>238</sup>Pu
  - <sup>239,241</sup>Pu



PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg



Training material

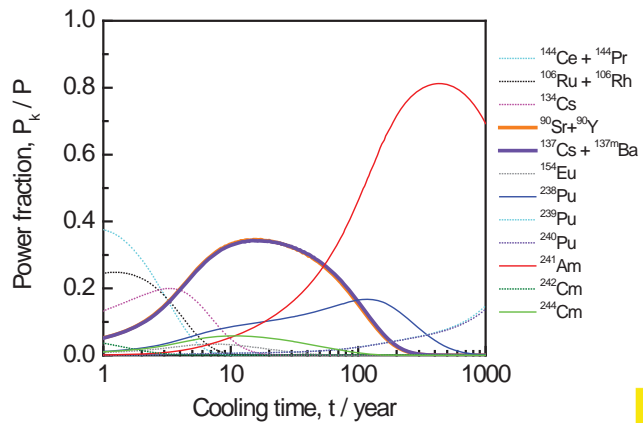


**DECAY POWER PRODUCED BY SNF**

- 1 a ≤ t ≤ 10 a
  - <sup>144</sup>Ce / <sup>144</sup>Pr
  - <sup>106</sup>Ru / <sup>106</sup>Rh
  - <sup>134</sup>Cs
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
- 10 a ≤ t ≤ 100 a
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
  - <sup>238</sup>Pu
  - <sup>241</sup>Am
  - <sup>244</sup>Cm
- 100 a ≤ t
  - <sup>241</sup>Am
  - <sup>238</sup>Pu
  - <sup>239,241</sup>Pu



PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg



Training material



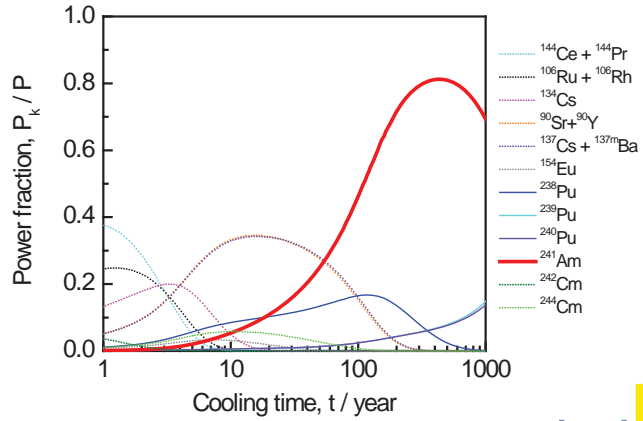


### DECAY POWER PRODUCED BY SNF

- 1 a ≤ t ≤ 10 a
  - <sup>144</sup>Ce / <sup>144</sup>Pr
  - <sup>106</sup>Ru / <sup>106</sup>Rh
  - <sup>134</sup>Cs
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
- 10 a ≤ t ≤ 100 a
  - <sup>90</sup>Sr / <sup>90</sup>Y
  - <sup>137</sup>Cs / <sup>137m</sup>Ba
  - <sup>238</sup>Pu
  - <sup>241</sup>Am
  - <sup>244</sup>Cm
- 100 a ≤ t
  - <sup>241</sup>Am
  - <sup>238</sup>Pu
  - <sup>239,241</sup>Pu



PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 wt%  
 burnup = 45 MWd/kg

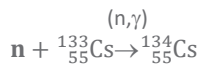
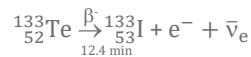


Training material

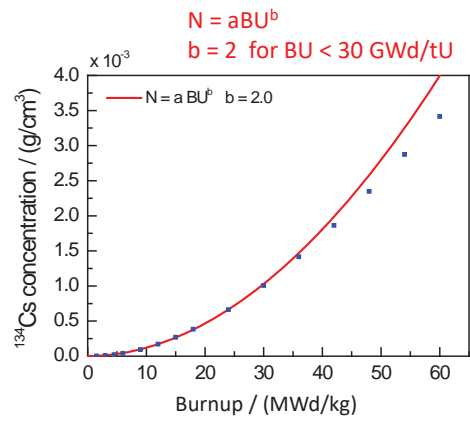


### <sup>134</sup>Cs: PRODUCTION

<sup>134</sup>Cs production:  
 (n,f) followed by β<sup>-</sup> and (n,γ)



More in presentation by  
 Daniel Cano Ott

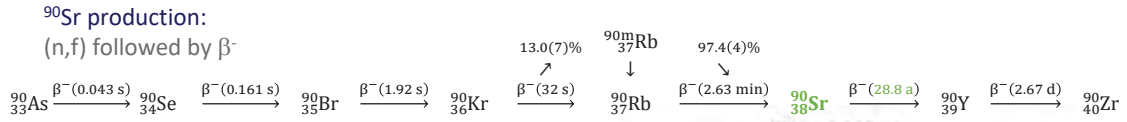


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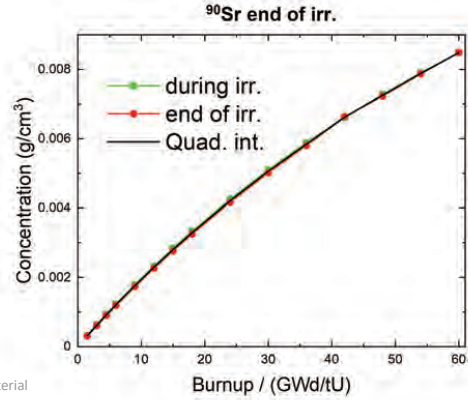


### <sup>90</sup>Sr: PRODUCTION



- Significantly different <sup>235</sup>U and <sup>239</sup>Pu fission yields:  
→ non-linearity vs. BU

	CFY (JEFF-3.3)
<sup>235</sup> U(n <sub>th</sub> ,f)	<b>0.0568(13)</b>
<sup>238</sup> U(n <sub>f</sub> ,f)	0.0320(14)
<sup>239</sup> Pu(n <sub>th</sub> ,f)	<b>0.0208(6)</b>
<sup>241</sup> Pu(n <sub>th</sub> ,f)	0.0146(4)



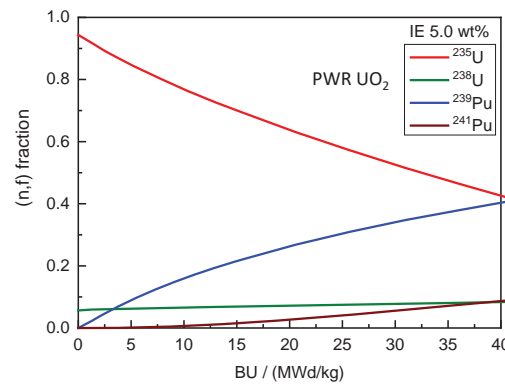
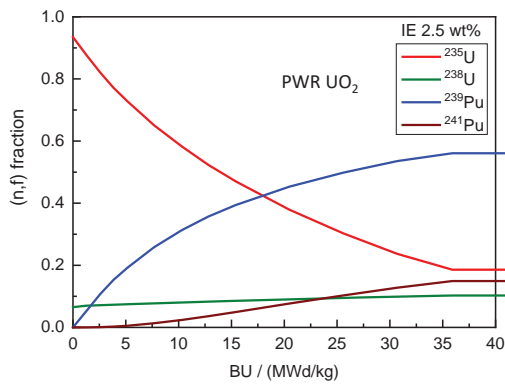
More in presentation by  
Olivier Serot

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### FISSION FRACTIONS OF <sup>235</sup>U, <sup>239</sup>Pu AND <sup>241</sup>Pu



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### SNF SOURCE TERMS: NUCLIDE INVENTORY

Nuclide	Source term	CT	Nuclide	Source term	CT
<sup>90</sup> Sr	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a	<sup>235</sup> U	R, S <sub>γ</sub>	10 <sup>5</sup> a ≤ t
<sup>106</sup> Ru	H	1 a ≤ t ≤ 10 a	<sup>238</sup> U	R, S <sub>γ</sub>	10 <sup>5</sup> a ≤ t
<sup>134</sup> Cs	H	1 a ≤ t ≤ 10 a	<sup>238</sup> Pu	H, S <sub>γ</sub>	10 a ≤ t
<sup>137</sup> Cs	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a	<sup>239</sup> Pu	R, S <sub>γ</sub>	100 a ≤ t ≤ 10 <sup>4</sup> a
<sup>144</sup> Ce	H	1 a ≤ t ≤ 10 a	<sup>240</sup> Pu	R, S <sub>γ</sub>	100 a ≤ t ≤ 10 <sup>4</sup> a
<sup>148</sup> Nd	Burn-up	stable	<sup>241</sup> Pu	H, S <sub>γ</sub>	10 a ≤ t ≤ 100 a
<sup>149</sup> Sm	Power	stable	<sup>241</sup> Am	H	10 a ≤ t
<sup>154</sup> Eu	H, S <sub>γ</sub>	1 a ≤ t ≤ 10 a	<sup>242</sup> Cm	H, S <sub>n</sub>	1 a ≤ t ≤ 10 a
			<sup>244</sup> Cm	H, S <sub>n</sub>	10 a ≤ t ≤ 100 a

H : thermal power or decay heat  
 S<sub>n</sub> : neutron emission  
 S<sub>γ</sub> : γ-ray emission  
 R : reactivity (criticality safety)

Criticality safety (Burn Up Credit, BUC):

<sup>95</sup>Mo, <sup>99</sup>Tc, <sup>101</sup>Ru, <sup>103</sup>Rh, <sup>109</sup>Ag, <sup>133</sup>Cs, <sup>143</sup>Nd, <sup>147,149,150,151,152</sup>Sm, <sup>155</sup>Gd

Long term safety:

<sup>14</sup>C, <sup>36</sup>Cl, <sup>79</sup>Se, <sup>94</sup>Nb, <sup>99</sup>Tc, <sup>129</sup>I, <sup>135</sup>Cs, <sup>226</sup>Ra, <sup>237</sup>Np

⇒ Requires complex nuclide inventory which can only be obtained by theoretical calculations



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### DEPLETION CALCULATIONS/CODES

Coupled neutron transport – nuclide depletion/creation

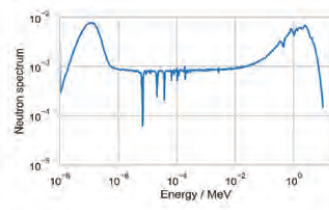
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

Update nuclide vector



- ALEPH2
- CASMO
- DARWIN
- EVOLCODE
- SERPENT
- SCALE
- STREAM
- VESTA
- ...

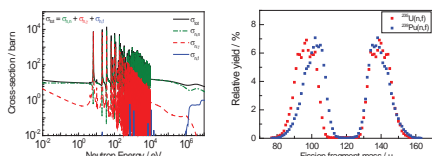
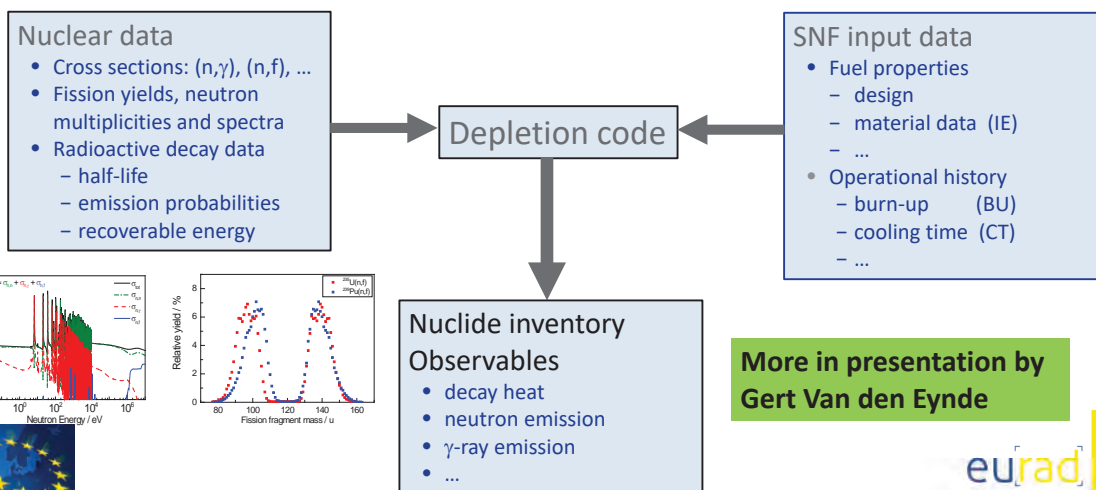


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### DEPLETION CODES: THEORETICAL CALCULATION OF SNF NUCLIDE INVENTORY AND OBSERVABLES



More in presentation by Gert Van den Eynde



Training material



### EXPERIMENTAL DATA TO VALIDATE DEPLETION CODES

- Results of analytical methods (destructive chemical and radiochemical analysis)
- Calorimetry data (assembly)
- Neutron emission measurements

In addition, an accurate knowledge of the design and operational history is required



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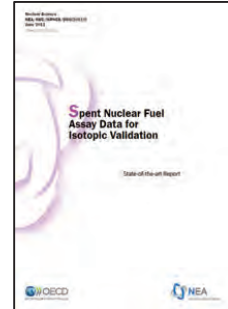
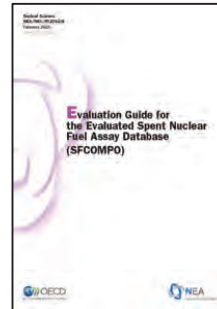




### ANALYTICAL METHODS FOR SNF ASSAY DATA

Post-Irradiation Experiments (PIE)  
 Complex process including different steps:

- Sampling and sample dissolution
  - Separation  
 linked to measurement technique, e.g. ICPMS)
  - Measurement
    - Radiometric ( $\alpha$ - and  $\gamma$ -spectrometry, Liquid Scintillation Counting ( $\alpha$ - and  $\beta$ -emitters))
    - Mass spectrometry
- ⇒ Data collected in SFCOMPO database



**More in presentations by:**

- Steven Van Winckel (experiment)
- Kevin Govers (use of ND)



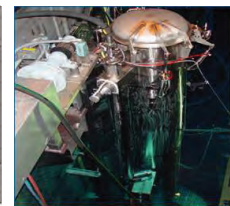
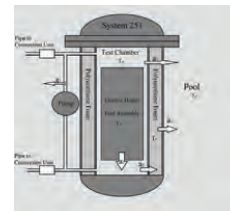
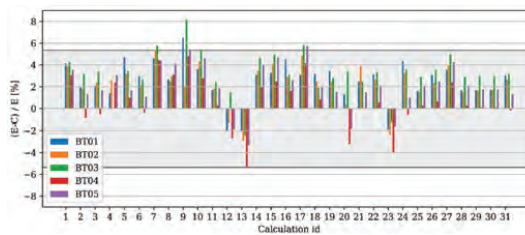
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### VALIDATION OF CALCULATIONS: CLAB CALORIMETER

- Only operating calorimeter worldwide to determine decay power of SNF assemblies
- Extensively used to validate depletion codes, e.g.
- Blind Test on decay heat:

Assembly ID	P	CT	<C/E>	St. dev
BT01	1662 W	4.5 a	0.975	0.019
BT02	1068 W	8.6 a	0.977	0.018
BT03 (+ Gd)	895 W	9.8 a	0.967	0.019
BT04	768 W	13.5 a	0.994	0.023
BT05	663 W	21.4 a	0.979	0.021



**More in presentations by:**

- Peter Schillebeeckx (experiment)
- Pablo Romojaro (use of ND)



Training material



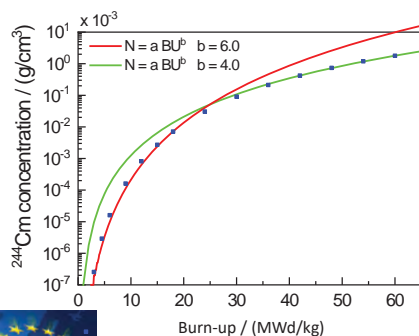


## IMPORTANCE OF NEUTRON EMISSION ESTIMATION FOR SNF MANAGEMENT

$$^{244}\text{Cm} : N = a\text{BU}^b$$

$$b \approx 4 \text{ for BU} = 45 \text{ MWd/kg}$$

$$\frac{\delta N}{N} = b \frac{\delta \text{BU}}{\text{BU}}$$



- Use neutron emission as a BU indicator to improve the operational input for depletion calculations
- For nuclear safeguards authorities using neutron emission as a signature for the fissile material
- Neutron dose

More in presentation by  
Peter Schillebeeckx

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## SUMMARY AND CONCLUSIONS

- The main observables of interest for a safe handling, transport, storage and disposal of SNF were identified and discussed
- A characterisation of SNF for these observables requires the inventory of some key nuclides with different characteristics
- The inventory of some key nuclides can only be obtained by theoretical calculations using depletion codes
- The quality of the theoretical calculations strongly depends on the quality of the nuclear data and design and operational history of the SNF
- Some key nuclear data such as cumulative fission yields and neutron induced capture cross sections need to be improved to allow a more accurate estimation of the main observables of interest



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## LEARNING OUTCOMES

After the completion of this training lesson, the participants should be able to

- identify the observables that are important for the transport, handling, storage and disposal of spent nuclear fuel
- identify key nuclides determining these observables
- identify the different components involved in the theoretical calculations of the observables
- understand the importance of nuclear data and design characteristics and operational history of the fuel for an accurate theoretical estimation of the observables
- realise the need of accurate experimental data to validate theoretical calculations



Training material



## KEY WORDS

- Actinides
- Alpha-decay
- Bateman equation
- Beta-decay
- Burnup
- Cooling time
- Cross section
- Decay heat
- Decay power
- Depletion codes
- Disposal
- Fission product
- Fission yields
- Gamma-ray emission
- Initial enrichment
- Irradiation history
- Light water reactor
- Neutron emission
- Neutron reactions
- Neutron induced capture reaction
- Neutron induced fission reaction
- Neutron transport
- Nuclear data
- Pressurised water reactor
- Recoverable energy
- Spent nuclear fuel
- Spontaneous fission



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## ADDITIONAL BIBLIOGRAPHY AND REFERENCES

### Spent nuclear fuel observables and key nuclides

- Broadhead et al., "Investigation of nuclide importance to functional requirements related to transport and long-term storage of LWR spent fuel", Report ORNL/TM-12742 (1995)
- Gauld et al., "Nuclide importance to criticality safety, decay heating and source terms related to transport and interim storage of high-burnup LWR fuel", Report NUREG/CR-6700, ORNL/TM-2000/284 (2001)
- Žerovnik et al., "Observables of interest for the characterisation of Spent Nuclear Fuel", EUR 29301 EN (2018) , JRC112361
- Schillebeeckx et al., "Characterisation of spent nuclear fuel by theoretical calculations and non-destructive analysis", see JRC114178 (2019)

### Depletion codes

- Stankovskiy and Van den Eynde, "Advanced method for calculations of core burn-up, activation of structural materials and spallation products accumulation in accelerator driven system", Science and Technology of Nuclear Installations 2012 (2012) 545103
- Álvarez-Velarde, "Validation of the burn-up code EVOLCODE 2.0 with PWR experimental data and with a Sensitivity/Uncertainty analysis", Annals of Nuclear Energy 73 (2014) 175
- Leppänen et al., "The Serpent Monte Carlo code: status, development and applications in 2013", Annals of Nuclear Energy 82 (2015) 142
- Kashima et al., "Validation of burnup calculation code SWAT4 by evaluation of isotopic composition data of mixed oxide fuel irradiated in pressurized water reactor", Energy Procedia 71 (2015) 159
- Rearden and Jessee, "SCALE Code System", ORNL/TM-2005/39 Version 6.2, April 2016
- Gauld et al., "Isotopic depletion and decay methods and analysis capabilities in SCALE", Nuclear Technology 174 (2017) 169
- Ebiwonjumi et al., "Verification and validation of radiation source term capabilities in STREAM", Annals of Nuclear Energy 124 (2019) 80



Training material



## ADDITIONAL BIBLIOGRAPHY AND REFERENCES

### Radiochemical analysis and validation of depletion codes

- DE Scatena-Wachsel, "Radiochemical analysis methodology for uranium depletion measurements", Report LM-06K140, January 2007
- Gauld et al., "Uncertainties in Predicted Isotopic Compositions for High Burnup PWR Spent Nuclear Fuel", Report NUREG/CR-7012, ORNL/TM-2010/41, January 2011
- OECD/NEA, "Spent Nuclear Fuel Assay Data for Isotopic Validation, State-of-the-art Report", Nuclear Science, NEA/NSC/WPNC/DOC(2011)5, June 2011
- OECD/NEA, "Evaluation Guide for the Evaluated Spent Nuclear Fuel Assay Database (SFCOMPO)", Nuclear Science, NEA/NSC/R(2015)8, February 2016. Ilas, "Review of Experimental Assay Data for PWR Spent Fuel", Report ORNL/SPR-2019/1143, April 2019

### Non-destructive assay

- SKB, "Measurements of Decay Heat in Spent Nuclear Fuel at the Swedish Interim Storage Facility", Clab, SKB Report R-05-62, December 2006
- B.D. Murphy and I.C. Gauld, "Spent Fuel Decay Heat Measurements Performed at the Swedish Central Interim Storage Facility", Report ORNL/TM-2008/016, Oak Ridge National Laboratory, February 2010
- Schillebeeckx et al., "A non-destructive method to determine the neutron production rate of a sample of spent nuclear fuel under standard controlled area conditions", JRC Technical Report EUR 30379 EN, 2020

### Nuclear data

- Nuclear data libraries at JANIS NEA, [https://www.oecd-nea.org/jcms/pl\\_39910/janis](https://www.oecd-nea.org/jcms/pl_39910/janis)
- Decay data, <http://www.nucleide.org/DDEP.htm>
- Nichols et al., "Handbook of nuclear data for safeguards: database extensions, august 2008", INDC-2453, INDC(NDS) – 0534



Training material




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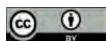
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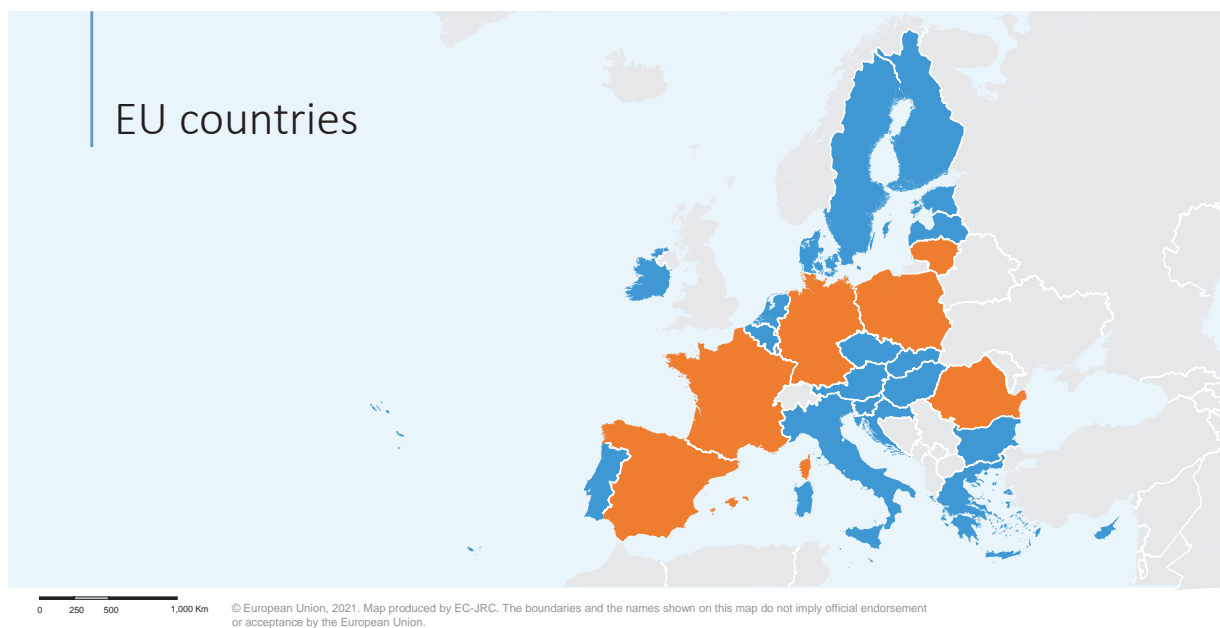
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# Thank you



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### 3. Internal meeting

- Dry Storage Accidents; IDOM; SFC Annual Meeting 2022; 20/09/2022
- Spectroscopic investigation of fission and activation products in irradiated light water reactor fuels; T. König, R. Dagan, K. Dardenne, M. Herm, V. Metz, T. Pruessmann, J. Rothe, D. Schild, A. Walschburger, H. Geckeis; WP8 SFC Annual Meeting 2023; 11/01/2023

### **3.1 Dry Storage Accidents; IDOM; SFC Annual Meeting 2022; 20/09/2022**





## EURAD SFC

### IDOM - Dry Storage Accidents, Risk Assessment Methodology

Carlos Pérez – 20 September 2022



*This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement N°847593*

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## INDEX

- BACKGROUND
- OVERALL OBJECTIVE
- APPROACH
- METHODOLOGY
- DEVELOPMENT OF THE WORK
  - STAGE 1
  - STAGE 2
  - SUMMARY
  - CONCLUSIONS TO DATE
- NEXT STEPS

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## BACKGROUND

IDOM is a Spanish firm providing Consulting, Engineering and Architecture professional services for clients including NPPs, WMOs, and TSOs like CIEMAT. It takes part in EURAD WP8 Task 4 as a LTP of CIEMAT.

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## OVERALL OBJECTIVE

The overall objective of IDOMs work is to establish the influence of the SNF parameters or the degradation phenomena that may be present in it during accidents of Dry Storage Systems.

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## APPROACH

To meet the proposed objective, an initial methodology has been established, which could be applicable later to particular cases.

In addition, the initial methodology has been extended and made more specific to the national case through the Spanish perspective. This is, from the Spanish regulatory point of view and the fuel types and Dry Storage Systems available in Spain.

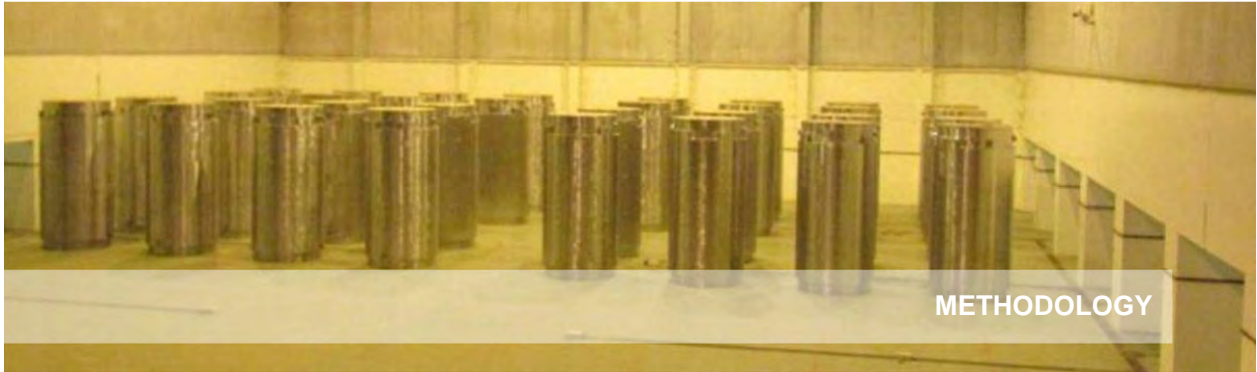
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IIT-004  
Risk Assessment Methodology  
November 2020.



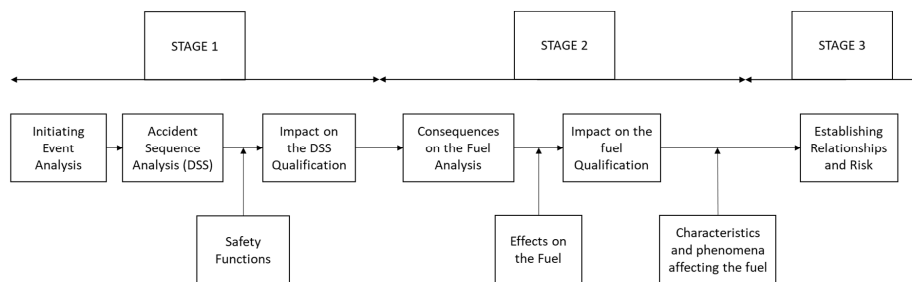


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## METHODOLOGY



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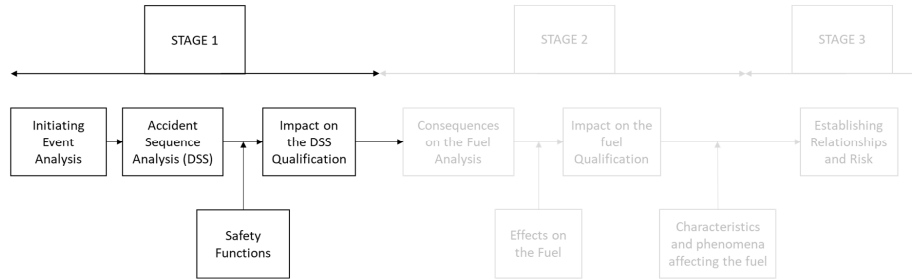
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## METHODOLOGY

### STAGE 1 – Dry Storage System Analysis



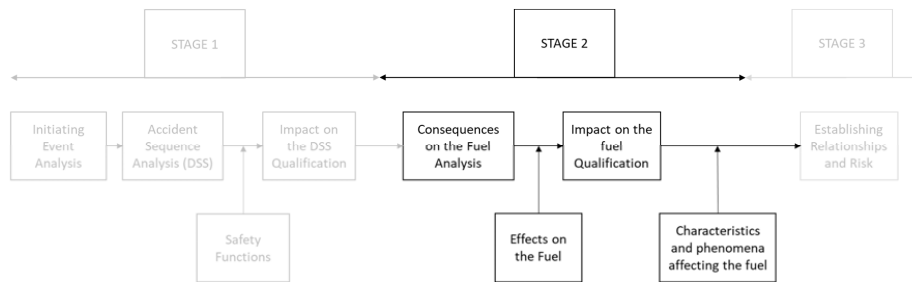
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## METHODOLOGY

### STAGE 2 – Spent Nuclear Fuel



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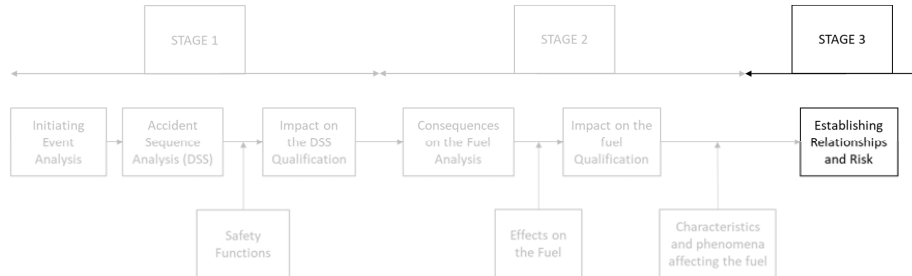
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## METHODOLOGY

### STAGE 3 – Establishing Relationships



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DEVELOPMENT OF THE WORK

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**DEVELOPMENT OF THE WORK**

**STAGE 1 – Storage System Analysis**

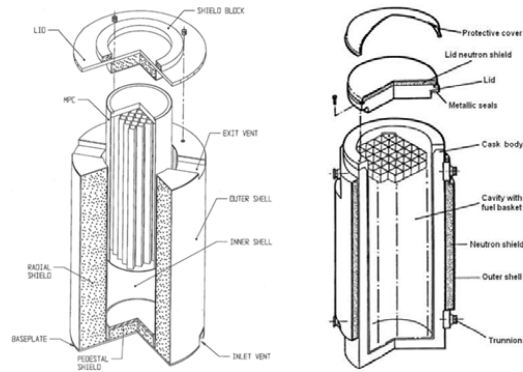
**Scoping**

Fuel Types in the scope:

- **BWR**
- **PWR**

Dry Storage Systems in the scope:

- **Canister + Overpack**
- **Dual Purpose Cask**



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**DEVELOPMENT OF THE WORK**

**STAGE 1 – Storage System Analysis**

What can be found in references by DSS designers and regulators?

- Tip over
- Drop
- Flood
- Fire
- Explosion
- Lightning
- Earthquake
- Loss of Shielding
- Adiabatic Heatup
- Tornado
- Missiles generated by natural phenomena
- ...

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## DEVELOPMENT OF THE WORK

### STAGE 1 – Storage System Analysis

#### Accident Sequence Analysis

Initiating Events	Accident	Consequences to de DSS
Earthquake	Tip over	Loss of Shielding
Handling device failure	Drop	Lid ovalization
Damm breach / Tsunami	Flood	
Transfer vehicicle fire	Fire	Adiabatic Heatup
On / off-site explosion	Explosion	
Electrical storm	Lightning	
Tornado	Missiles generated by natural phenomena	Loss of Shielding

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## DEVELOPMENT OF THE WORK

### STAGE 1 – Storage System Analysis

#### Accident Sequence Analysis – Cask Tip-Over Example

Initiating Events	Accident	Consequences to de DSS
<ul style="list-style-type: none"> <li>• Tornado / hurricane winds</li> <li>• Missiles generated by natural phenomena</li> <li>• Flooding (water drag)</li> <li>• Earthquake</li> <li>• Lifting device failure</li> </ul>	Tip-Over	<ul style="list-style-type: none"> <li>• Overstress and deformation of certain structural components (e.g., shell, lids, bolting, support channels, etc.).</li> <li>• Overstress and deformation of basket plates.</li> <li>• Localized decrease in shielding material thickness.</li> <li>• General temperature increase due to horizontal reorientation.</li> <li>• CRUD detachment.</li> </ul>

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## DEVELOPMENT OF THE WORK

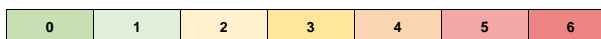
### STAGE 1 – Storage System Analysis

How do we evaluate the severity of an accident from the DSS point of view?

#### SAFETY FUNCTIONS

- Criticality Control (CC)
- Structural Support (SS)
- Heat Transfer (HT)
- Confinement (CF)
- Radiation Shielding (RS)
- Retrievability (RT)

Severity from the DSS point of view is established as the sum of the number of compromised Safety Functions. (0 to 6)



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## DEVELOPMENT OF THE WORK

### STAGE 1 – Storage System Analysis

#### Accident Sequence Analysis – Cask Tip-Over Example

##### Consequences to de DSS

- Overstress and deformation of certain structural components (e.g., shell, lids, bolting, support channels, etc.).  
**(CF, SS, RT, HT)**
- Overstress and deformation of basket plates.  
**(CC, SS, HT, RT)**
- Localized decrease in shielding material thickness.  
**(RS)**
- General temperature increase due to horizontal reorientation.  
**(HT)**
- CRUD detachment.  
**(No consequences to the DSS)**

**Total number of compromised Safety Functions:**

(CF, SS, RT, HT, RS, CC) -> 6

**SEVERITY FROM THE DSS POINT OF VIEW:**



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## DEVELOPMENT OF THE WORK

### STAGE 1 – Storage System Analysis

#### Accident Sequence Analysis – Lightning Example

##### Consequences to de DSS

- Local temperature increase in the point of impact under allowable limits.

(No consequences to the DSS)

**Total number of compromised Safety Functions:**

(None) -> 0

**SEVERITY FROM THE DSS POINT OF VIEW:**

0

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## DEVELOPMENT OF THE WORK

### STAGE 2 – Consequences in the Spent Fuel Analysis

How does an accident affect the fuel?

- Normally, DSS documentation does not go into detail regarding the effects of an accident in the fuel.
- Consequences in the container can be seen as the initiating events for the effects in the fuel.

##### Examples:

- Accelerations in the container -> Accelerations in the fuel -> Induced buckling or flexion
- Fire in the container -> Loss of heat transfer -> Cladding temperature increase
- Flooding in the container -> Change in moderation conditions

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**DEVELOPMENT OF THE WORK**      **STAGE 2 – Consequences in the Spent Fuel Analysis**

**Consequences in the Fuel - Cask Tip-Over Example**

- The fuel might suffer deformations and damages due to the accelerations induced on it, grid-to-rod fretting, or it might be crushed and hit by violent contact with the components of the DSS (basket plates) or other fuel assemblies.
- Rearrangement of the fuel assemblies within the storage system basket, both from the DSS horizontal reorientation and the deformation of the basket plates.
- CRUD detachment.

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**DEVELOPMENT OF THE WORK**      **STAGE 2 – Consequences in the Spent Fuel Analysis**

How do we evaluate the severity of an accident from the SNF point of view?

- **Mechanical Effects (ME):**
  - Cladding failure, either with breached (punctured) or damaged rods
  - Rod / assembly deformation without cladding failure
  - Changes to the assembly axial alignment without cladding failure
- **Thermal Effects (TE):**
  - Heating of the cladding
  - Repeated heating and cooling cycles
- **Criticality Effects (CE):**
  - Any effect that will result in a variation of the effective neutron multiplication factor  $k_{eff}$

Severity from the SNF point of view is established as the sum of the number of Effects on the fuel. (0 to 3)

0	1	2	3
---	---	---	---

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**DEVELOPMENT OF THE WORK**

**STAGE 2 – Consequences in the Spent Fuel Analysis**

**Consequences in the Fuel - Cask Tip-Over Example**

- The fuel might suffer deformations and damages due to the accelerations induced on it, grid-to-rod fretting, or it might be crushed and hit by violent contact with the components of the DSS (basket plates) or other fuel assemblies.  
**(ME, TE, CE)**
- Rearrangement of the fuel assemblies within the storage system basket, both from the DSS horizontal reorientation and the deformation of the basket plates.  
**(TE, CE)**
- CRUD detachment.  
**(No effects from the Safety Point of view)**

**Total number of Effects:**  
(ME, TE, CE) -> 3

**SEVERITY FROM THE SNF POINT OF VIEW:**

3

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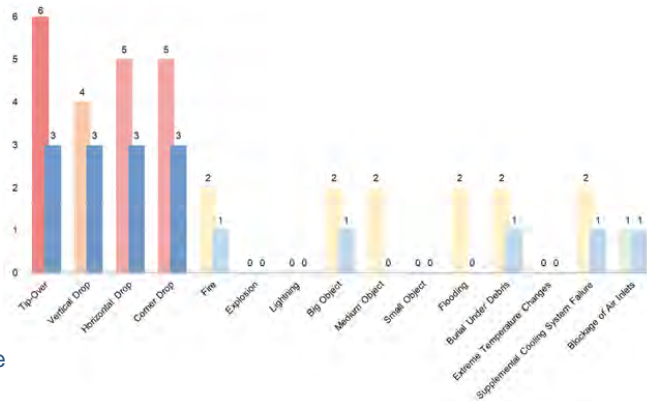


**DEVELOPMENT OF THE WORK**

**Summary of Results**

- Tip-Over
- Drop
- Fire
- Explosion
- Lightning
- Object Impact
- Flooding
- Burial Under Debris
- Extreme Temperature Changes
- Supplemental Cooling System Failure
- Blockage of Air Inlets

Accident Severity from the DSS and the SNF points of view



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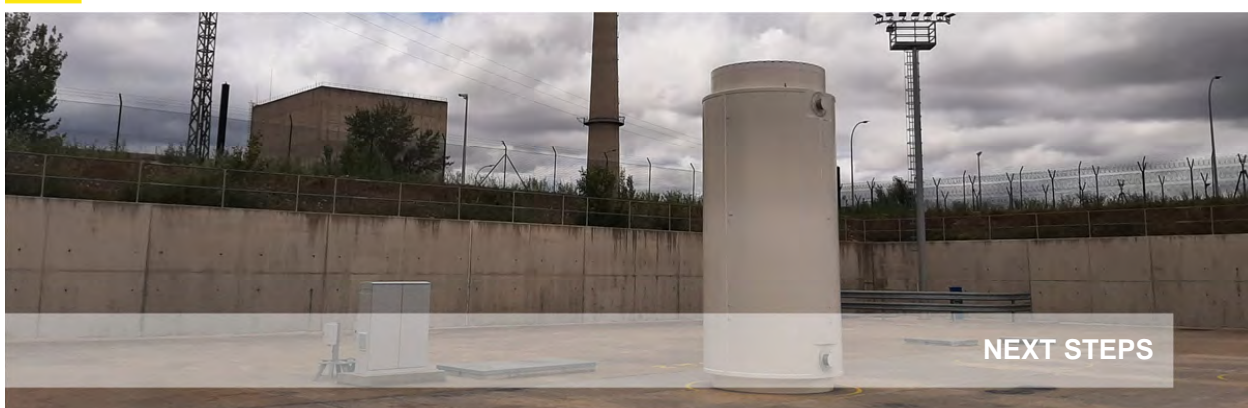
## DEVELOPMENT OF THE WORK

### Accident Severity Evaluation Conclusions

- The severity of an accident in the DSS is not necessarily related to the severity in the SNF, as it can be seen in the case of flooding or medium object impact.
- Accidents involving movement of the DSS (Tip-Over and Drop) can have the greatest effect on the fuel, which confirm the prioritisation of their analyses.
- A number of analyses that are not of great relevance from the DSS nor SNF damage point of view are identified (explosion, lightning, small object or extreme temperature changes).

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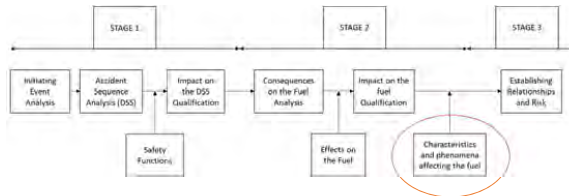


## NEXT STEPS

### STAGE 2 (Continuation)

Review of documentation and references applicable to LWR fuel, identifying the most common degradation mechanisms, classifying them and establishing their applicability or likelihood of occurrence based on operating parameters, e.g.:

- Burnup (+- 45 Gwd/MTU)
- Cooling time in spent fuel pool
- Dry Storage time (extended 20+ years)
- Temperatures during the loading of the Dry Storage System



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Thank you!

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**3.2 Spectroscopic investigation of fission and activation products in irradiated light water reactor fuels; T. König, R. Dagan, K. Dardenne, M. Herm, V. Metz, T. Pruessmann, J. Rothe, D. Schild, A. Walschburger, H. Geckeis; WP8 SFC Annual Meeting 2023; 11/01/2023**



## Spectroscopic investigation of fission and activation products in irradiated light water reactor fuels

EURAD SFC Annual Meeting 2023, Wettingen

T. König, R. Dagan, K. Dardenne, M. Herm, V. Metz, T. Pruessmann, J. Rothe, D. Schild, A. Walschburger and H. Geckeis  
 Karlsruhe Institute of Technology (KIT), Institute for Nuclear Waste Disposal (INE), P.O. Box 3640, 76021 Karlsruhe Germany



This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement N°847593

01.11.2023

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\*koenig.tobias@kit.edu



## Outline

- **Introduction:**
- **Experimental:**
  - Examined fuel types – *High burn-up UO<sub>x</sub> and mixed oxide (MOX) fuel*
  - Spectroscopic analysis – *Interaction layer between fuel and cladding*
    - SEM-EDX and XPS analysis
    - XAS analysis
- **Summary**

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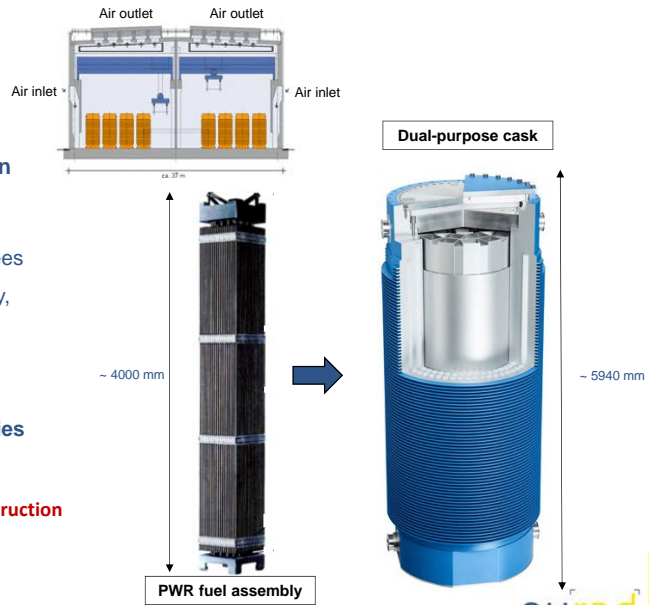


## Dry interim storage

- Interim dry storage of used fuel assemblies in dual-purpose casks:

- Dual-purpose cask (e.g. CASTOR®) guarantees **shielding of radiation**, as well as a temporary, **safe enclosure of radionuclides**.
- **Decay heat** dissipated by air circulation.
- **However, final repositories in many countries not operational yet.**

➔ **Necessity of prolonged interim storage until construction and commissioning of a final repository site!**



Sources: GNS, CASTOR® V/19, Nuclear Engineering International (2003), EnBW Kraftwerk AG

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## Dry interim storage

- Interim dry storage of used fuel assemblies in dual-purpose casks:

- Dual-purpose cask guarantees **shielding of radiation**, as well as a temporary, **safe enclosure of radionuclides**.
- Interim storage of irradiated fuel assemblies is licensed for only **40 years**.
- **Final repository not available until at least 2050 and emplacement of the last fuel assemblies decades later!**

- Several phenomena affect the cladding integrity during interim storage:

- **Increase in pressure** due to swelling of the pellet and ongoing  $\alpha$ -decays.
- **Irradiation damage of cladding** via  $\alpha$ -decays.
- Cracking due to **hydride re-orientation**.  
$$\text{Zr} + 2 \text{H}_2\text{O} \rightarrow \text{ZrO}_2 + 2 \text{H}_2$$
- **Corrosion of cladding induced by fission and activation products.**

➔ **Formation of agglomerates on the inner side of the cladding due to thermal gradient in SNF and possibility of halogen induced stress corrosion cracking.**

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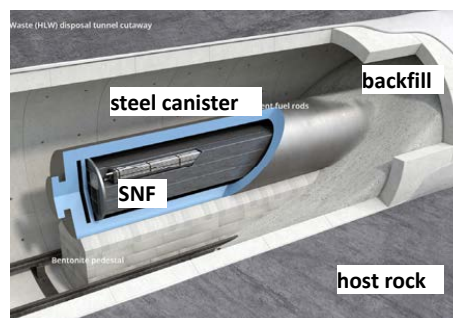
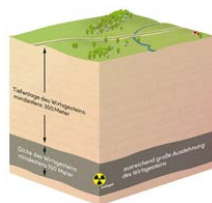




## Final disposal

### • Deep geological disposal:

- Multibarrier concept: technical (e.g. waste matrix, cladding), geo-technical (e.g. buffer, backfill) and geological barriers (e.g. host rock, overburden).
- Oxygen trapped in deep geological repository after its closure will be consumed e.g. by bacteria, reducing minerals and aerobic corrosion of outer layers of waste canisters.
- Subsequently, ground water in contact with metallic canisters leads to anaerobic corrosion of metals, mainly corrosion of iron.
- H<sub>2</sub> pressure build-up ≥ 50 bar in repository.



➔ **Safety analyses require profound knowledge on the occurrence and chemical behaviour of long-lived and dose relevant radionuclides (e.g. <sup>36</sup>Cl, <sup>129</sup>I, <sup>135</sup>Cs).**

<https://www.grimsel.com/gts-information/waste-disposal-overview/the-engineered-barrier-system> (02.11.2021).  
[https://www.einblicke.de/fileadmin/images/magazin/Einblicke\\_6/Kriterien\\_zur\\_Endlagersuche.jpg](https://www.einblicke.de/fileadmin/images/magazin/Einblicke_6/Kriterien_zur_Endlagersuche.jpg) (04.04.2022).

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## Open questions

- In which condition is the fuel-cladding interface during interim storage and will it impact the integrity of the cladding?
- In which chemical speciation are possible cladding degrading elements such as chlorine or iodine present in SNF and cladding?

➔ **Reducing uncertainties on degradation processes.**



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## SNF specimens

### Fuel rod segment N0204, irradiated in the pressurised water reactor Gösgen (CH):

- Fuel type: **UO<sub>x</sub>**, initial 3.8% <sup>235</sup>U enrichment (NIKUSI).
- Cladding alloy: **Zircaloy-4**.
- Full power days: 1226 days in 4 cycles.
- Average linear power: 260 W/cm.
- Average burn-up: **50.4 GWd/t<sub>HM</sub>**.
- Decay time: ~ 32 years.



### Fuel rod 5810, irradiated in the pressurised water reactor Obrigheim (DE):

- Fuel type: **MOX**, initial 3.2% Pu<sub>fiss</sub> enrichment (OCOM).
- Cladding alloy: **Zircaloy-4**.
- Full power days: 1157 days in 4 cycles.
- Average linear power: 200 W/cm.
- Average burn-up: **38.0 GWd/t<sub>HM</sub>**.
- Decay time: ~ 36 years.



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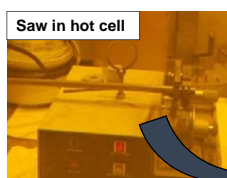


## Preparation of the SNF specimens

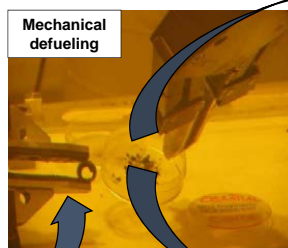
- Segmentation of the SNF specimens in specially equipped laboratories (hot cells).
- Use of a cutting machine Isomet® Low Speed Saw (11-1180, Buehler Ltd).
- Equipped with a diamond wafering blade Isomet® (11-4254 Buehler Ltd).
- Mechanical defueling of SNF specimens:
  - Fuel fragments.
  - Zircaloy cladding segments.



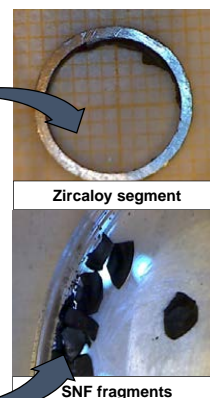
Hot cells of INE



Saw in hot cell



Mechanical defueling



Zircaloy segment

SNF fragments

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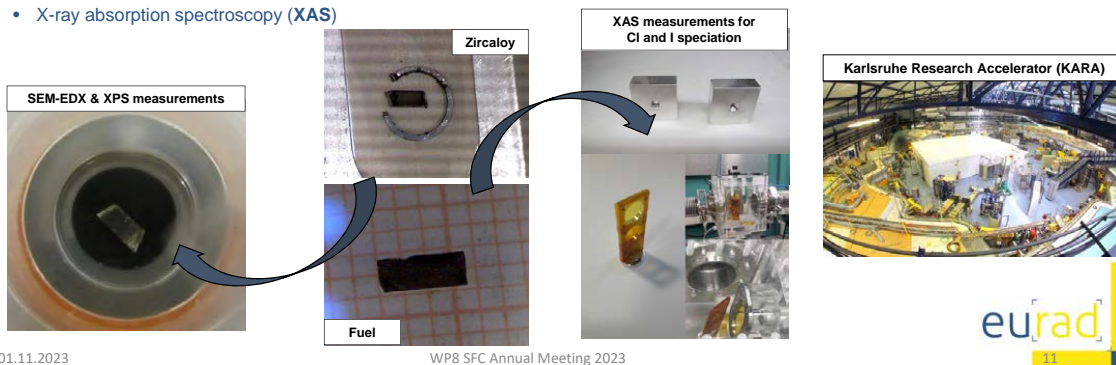
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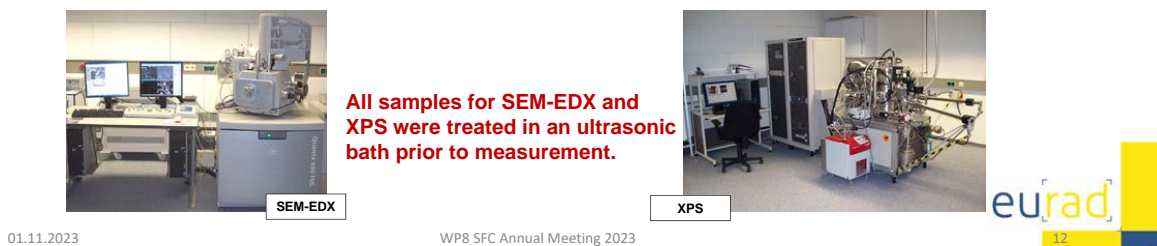
## Spectroscopic measurements

- Preparation of fuel fragments and Zircaloy segments for spectroscopic analyses:
  - Scanning electron microscopy coupled with energy dispersive X-ray spectroscopy (**SEM-EDX**)
  - X-ray Photoelectron spectroscopy (**XPS**)
  - X-ray absorption spectroscopy (**XAS**)



## Spectroscopic measurements: SEM-EDX and XPS

- **SEM-EDX:**
  - Measurements were performed by use of a Quanta 650 FEG.
  - Accelerating voltage: 15 kV; beam current: 1 nA
  - **Information depth in range of few  $\mu\text{m}$ .**
- **XPS:**
  - Measurements performed on an ULVAC-PHI VersaProbe II spectrometer.
  - Mg K $\alpha$  (E = 1253.6 eV) and Al K $\alpha$  (E = 1486.7 eV) radiation sources.
  - **Information depth in range of few nm.**





## INE-Beamline and CAT-ACT station at the KIT light source

- **INE-Beamline** fully operational since October 2005 (2nd dedicated beamline for radioactive materials in Europe).
- **CAT-ACT station** fully operational since fall 2016.
- Energy range 2.1 – 55 keV, bending magnet (INE-Beamline) or superconductin wiggler source (CAT-ACT).

Both stations are licensed for working with 10<sup>6</sup> the exemption limit and up to 200 mg of fissile <sup>235</sup>U and <sup>239</sup>Pu within a double containment.



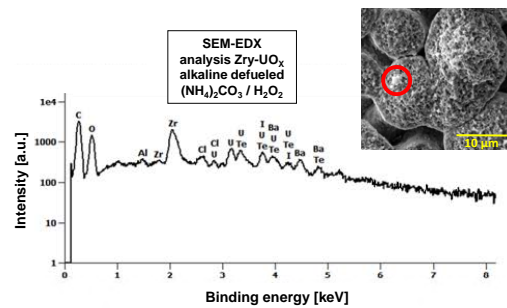
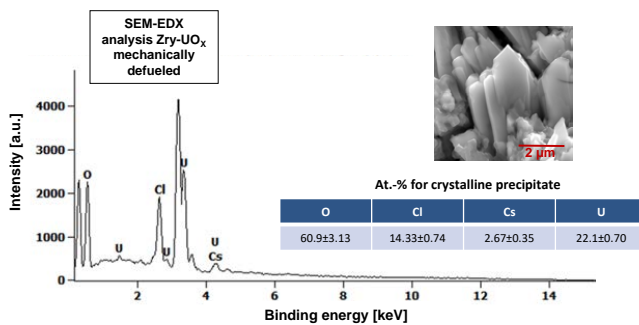
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## Spectroscopic analysis – SEM-EDX

- Zircaloy in contact with spent UO<sub>x</sub> / MOX fuel:
  - **SEM-EDX: Cl, Te, I, Cs, Fe, Zr, Ba, U.**



At.-% for agglomerates on alkaline defueled cladding								
C	O	Al	Cl	Zr	Te	I	Ba	U
51.1±1.1	34.4±1.4	0.4±0.1	0.8±0.2	6.0±0.2	2.7±0.5	1.9±0.5	1.2±0.2	1.4±0.1

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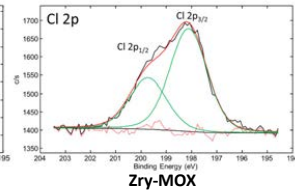
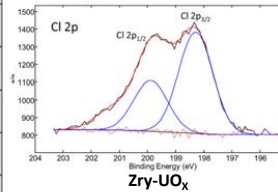
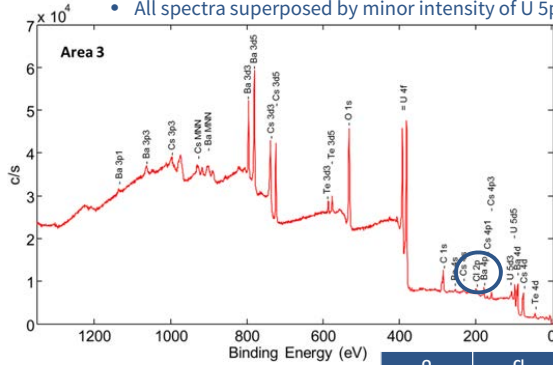
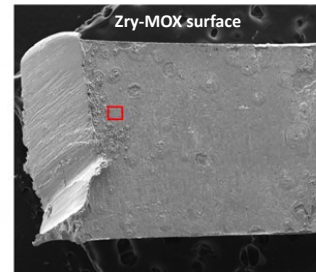




## Spectroscopic analysis – XPS

- XPS analysis confirms Chlorine in oxidation state -I as Chloride (Cl<sup>-</sup>):

- Binding energy Cl<sub>p<sub>3/2</sub></sub> for metal chlorides: ~198.5 – 199 eV.
- All spectra superposed by minor intensity of U 5p<sub>3/2</sub>.



At.-% for analysed Zry-MOX area

O	Cl	Cd	Te	Cs	Ba	U
79.7±12.0	1.8±0.3	0.2±0.1	1.0±0.2	4.3±0.6	5.7±0.9	7.3±1.1

XPS survey, Al K<sub>α</sub> mono. X-ray excitation (1486.7 eV)

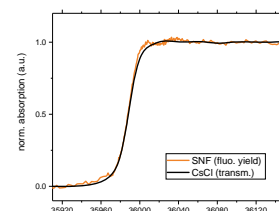
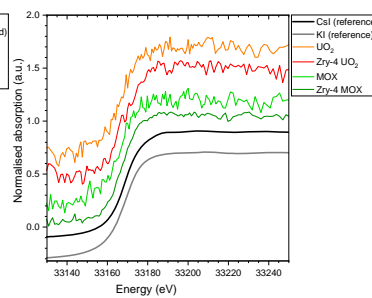
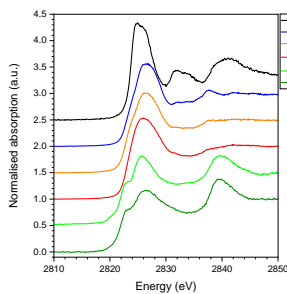
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## Spectroscopic analysis – XAS

- Knowledge on the chlorine (and iodine) inventory and speciation in fuel and Zircaloy afflicted with large uncertainties.
- Initial maximum impurity assumptions of up to 25 ppm Cl in the fuel and 20 ppm Cl in Zircaloy-4 cladding [HÄK19].
- First ever XAS measurements for chlorine (and iodine) speciation in fuel and cladding. ➡ **Complex mixed phases in case of chlorine.**



[HÄK19] S. Häkkinen, *Impurities in LWR fuel and structural materials*, VTT, Finland (2019).

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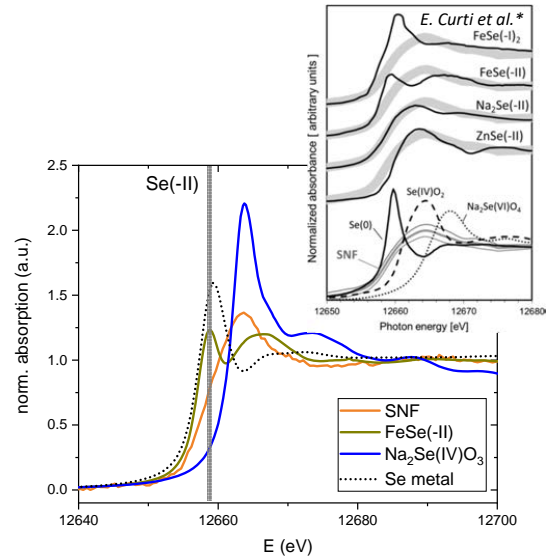
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## Spectroscopic analysis – XAS

- Initial analysis confirms results obtained by E. Curti et al.\* (PSI, SNF bulk sample obtained by FIB): Se is present as Se(-II) in  $UO_2$  lattice replacing oxygen.
- Se K-EXAFS point to U in the first Se coordination sphere.
- Selenium (same as tellurium) are reacting strongly with zirconium-based cladding tubes.
- However**, in presence of caesium, formation of Cs-selenides / Cs-tellurides is thermodynamically preferred, reducing reactions with the cladding.



\* E. Curti et al., *Environ. Sci.: Processes Impacts* 17, 2015, E. Curti et al., *Journal of Nuclear Materials* 453, 2014

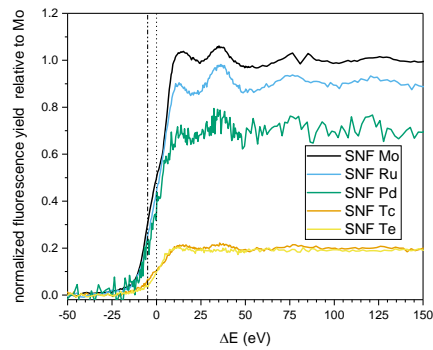
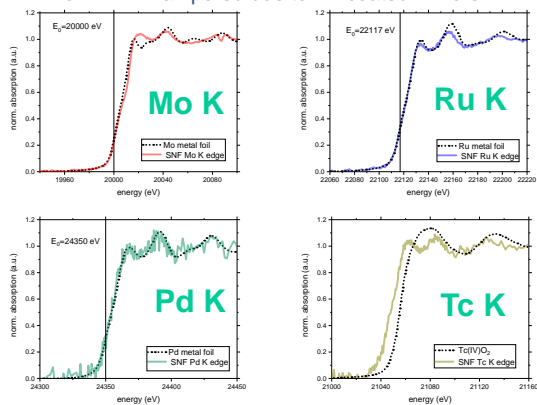
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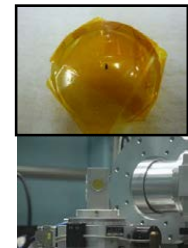


## Spectroscopic analysis – XAS

- Measurements in UOX fuel: Mo K, Ru K, Pd K, Tc K, Te K – Rh hampered due to Rh coated mirrors!



Measurements on MOX (38.0 GWd/t<sub>HM</sub>) were performed. Data analysis ongoing.



element	at%	calc.
Mo	0.324	0.324
Ru	0.223	0.203
Pd	0.135	0.114
Tc	0.056	0.072
Te	0.017	0.040

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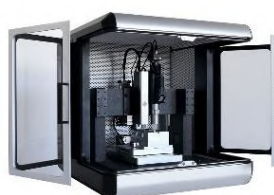






## Summary

- **First ever measurements of Cl K- and I K-edge** in high active waste specimens (SNF and Zircaloy).
- Agglomerates in interaction layer consist, amongst others, of halogen-rich mixed phases (**Cl and I**), as well as Cs, Te, Ba, U and Pu.
- However: **For profound statement on cladding integrity**, experiments for mechanical stability (e.g. nanoindentation) are necessary.



Femto-Indenter FT-104  
Soon to be established in controlled  
area of KIT-INE

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- E. González-Robles (IdISBa)
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- K. Hardock (KIT-INE)
- Beamline-Staff (KIT-IBPT)



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**Thank you for your kind attention**

#### 4. Participation to a Conference

- Verification and validation of MCNP/CINDER burnup capabilities; S. Panizo, CIEMAT; 46th Annual Meeting of the Spanish Nuclear Society; 06 - 08/10/2021
- Evaluating Peak Area Uncertainties in Connection to Passive Gamma Measurements of Spent Nuclear Fuel; V. Solans, UU; TopFuel conference, Santander, Spain; 24 -28/10/2021
- Spent Fuel Characterization to Support NPP Krško Spent Fuel Dry Storage Project; M. Kromar, JSI; 13th International Conference of the Croatian Nuclear Society; 05 - 08/06/2022
- Passive neutron and gamma technique for spent nuclear fuel characterisation; V. Solans, UU; IAEA CRP spent fuel characterization ; 22 – 23/09/2022
- Recent Spent Fuel Research at VTT; S. Häkkinen, P. Juutilainen, L. Vaara, R. Tuominen; Nuclear Science and Technology Symposium 2022 (SYP2022); 27/05/2021
- Rossi-Alpha distribution analysis of DDSI data for spent nuclear fuel investigation ; V. Solans, UU; Symposium on International Safeguards: Reflecting on the Past and Anticipating the Future; 31/10-04/11/2022

**4.1 Verification and validation of MCNP/CINDER burnup capabilities; S. Panizo, CIEMAT; 46th Annual Meeting of the Spanish Nuclear Society; 06 - 08/10/2021**

# Verification and validation of MCNP/CINDER burnup capabilities

Impact evaluation of the nuclear data library *cinder.dat*

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CIEMAT – Unidad de Innovación Nuclear.

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## Introduction

- The **characterization of spent nuclear waste** is essential for its safe management given that it is the source of decay heat, neutron emission and gamma emission, coming from unstable isotopes.
- The EU **EURAD** (European Joint Programme on Radioactive Waste Management) project includes a Work Package devoted to Spent Fuel Characterization and Evolution Until Disposal, where this work is framed.
- **Burn-up calculations** are needed for this characterization. They are based on the coupling of codes for neutronics and isotopic evolution with the irradiation. Tools dedicated to burn-up are usually validated using the SFCOMPO database (available at the OECD/NEA).
- This work includes the validation of two burn-up codes, **EVOLCODE** and **MCNP/CINDER**, with light water reactor experimental data from the SFCOMPO database, and their verification when both use the same basic neutron library.

## MCNP/CINDER & EVOLCODE

- **MCNP**: general-purpose Monte Carlo N-Particle code that simulates neutron, photon and electron transport.
- **CINDER**: burnup code that calculates the isotopic inventory evolution of irradiated materials. It uses a self-contained library file, `cinder.dat`, that includes fission yields, decay data and cross-sections distributed among 63 energy groups.
- **EVOLCODE**: burnup code developed at CIEMAT that incorporates neutron transport and depletion evolution, by means respectively of **MCNP** and **ORIGEN** or **ACAB** codes. It also incorporates a predictor/corrector method.

$$\frac{dN}{dt} = -N_m(t)\beta_m + Y_m + \sum N_k(t)P_{k \rightarrow m}$$

$N_m(t)$ : atomic density of isotope "m"  
 $\beta_m$ : transmutation probability of isotope "m"  
 $Y_m$ : production rate of isotope "m"  
 $P_{k \rightarrow m}$ : transmutation probability of isotope "k" to "m"

$$\vec{\nabla} \cdot \vec{j}(\vec{r}) + \Sigma_a(\vec{r})\phi(\vec{r}) = s'''(\vec{r}) + \nu\Sigma_f(\vec{r})\phi(\vec{r})$$

$\vec{\nabla} \cdot \vec{j}(\vec{r}) dV$ : neutrons in dV that escape without interaction  
 $\Sigma_a(\vec{r})\phi(\vec{r})dV$ : captured neutrons in dV  
 $s'''(\vec{r})dV$ : neutrons from external source in dV  
 $\nu\Sigma_f(\vec{r})\phi(\vec{r})dV$ : neutrons produced by fission in dV

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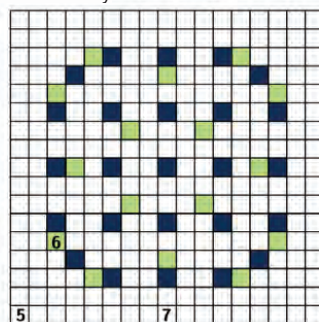
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## Takahama-3

- **Takahama-3**. Japanese light water reactor (LWR) operated by Kansai Electric Power Company (KEPCO).
- Three fuel rods of the assembly **NT3G23** from Takahama-3 which are referred to as **SF95**, SF96 and SF97, were reproduced in both codes, MCNP and EVOLCODE.
- **SF95-5** fuel pin selected – EURAD. Single model includes cladding and moderator.

Fuel assembly **NT3G23** from Takahama-3.



□  $UO_2$  fuel  
 ■  $UO_2 - Gd_2O_3$  fuel  
 ■ Water

Operating history of **SF95** fuel rod in Takahama-3.

Beginning	Ending	Days	Status
26/01/199	15/02/199	385	Burnup
0	1		
15/02/199	14/05/199	88	Cool
1	1		
14/05/199	19/06/199	402	Burnup
1	2		

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## Results - actinides

	C/E	
	MCNP/CINDER	EVOLCODE
U-234	0.91	0.91
U-235	1.03	1.04
U-236	1.01	0.99
U-238	1	1
Pu-238	1.12	1.15
Pu-239	1.12	1.14
Pu-240	1.07	1.07
Pu-241	1.07	1.09
Pu-242	1	1
Am-241	1.12	1.09
Am-242m	-	1.29
Am-243	1.04	1.09
Cm-242	1.03	1.04
Cm-243	1.01	1.05
Cm-244	1.17	1.24
Cm-245	1.4	1.52
Cm-246	1.73	1.86

The (C/E) values show a good agreement between calculations and experimental values for the **actinides**.

- For the uranium isotopes: 3-4% difference for  $^{235}\text{U}$  and even better agreement for  $^{236}\text{U}$  and  $^{238}\text{U}$ .
- Largest discrepancies between the simulations and the experimental data:  $^{244,245,246}\text{Cm}$ .
- Relevant discrepancies for  $^{238}\text{Pu}$  and  $^{239}\text{Pu}$ .

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## Results - fission products

The **fission products** also show a good agreement except for  $^{125}\text{Sb}$  and  $^{154}\text{Eu}$ .

	C/E	
	MCNP/CINDE R	EVOLCODE
Cs-137	0.97	0.96
Cs-134	0.98	0.98
Eu-154	1.13	1.25
Ce-144	0.97	0.96
Sb-125	2.07	2.26
Ru-106	1.09	1.13
Nd-142	0.88	0.91
Nd-143	0.97	0.98
Nd-144	0.96	0.95
Nd-145	0.97	0.98
Nd-146	1	1.01
Nd-148	1	0.99
Nd-150	0.99	1

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Results -  $^{154}\text{Eu}$ 

The discrepancy in this isotope comes from the thermal  $^{239}\text{Pu}$  cumulative fission product yields for  $^{153}\text{Eu}$  between JEFF-3.3 and ENDF/B-VI:

FY (cumulative)	ENDF/B-VI	JEFF-3.3
<b>Pu-239</b>	$3.61 \cdot 10^{-3}$	$5.90 \cdot 10^{-3}$

$^{154}\text{Tb}$	$^{155}\text{Tb}$	$^{156}\text{Tb}$	$^{157}\text{Tb}$	$^{158}\text{Tb}$
$^{153}\text{Gd}$	$^{154}\text{Gd}$	$^{155}\text{Gd}$	$^{156}\text{Gd}$	$^{157}\text{Gd}$
$^{152}\text{Eu}$	$^{153}\text{Eu}$	$^{154}\text{Eu}$	$^{155}\text{Eu}$	$^{156}\text{Eu}$
$^{151}\text{Sm}$	$^{152}\text{Sm}$	$^{153}\text{Sm}$	$^{154}\text{Sm}$	$^{155}\text{Sm}$
$^{150}\text{Pm}$	$^{151}\text{Pm}$	$^{152}\text{Pm}$	$^{153}\text{Pm}$	$^{154}\text{Pm}$

■ Stable  
 ■ EC +  $\beta^+$   
 ■  $\beta^-$

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Library *cinder.dat* in MCNP

**MCNP** supersedes all the **cross-section** data in *cinder.dat* for those isotopes and reactions with transport information.

No information about **fission yields** is updated from the transport data file.

This has been verified using the SF95-5 model with a single burn-up step of 120 days to ease the subsequent analysis.

To this end, three calculations have been performed, replacing in *cinder.dat* information from the JEFF-3.3 data:

- **XS**: Only the cross-sections are replaced.
- **XS+FY**: The cross-sections and the fission product yields are replaced.
- **XS+FY+HL**: Cross-sections, fission product yields and half-life data are replaced.

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Isotope	XS	XS + FY	XS + FY + HL
U-233	-1.50 %	-0.50 %	-0.50 %
U-234	0.00 %	0.00 %	0.00 %
U-235	0.00 %	0.00 %	0.00 %
U-236	0.00 %	0.00 %	0.00 %
U-238	0.00 %	0.00 %	0.00 %
Np-237	-0.10 %	-0.10 %	-0.10 %
Pu-238	-0.10 %	-0.20 %	-0.10 %
Pu-239	0.00 %	0.00 %	0.00 %
Pu-240	0.00 %	-0.10 %	-0.10 %
Pu-241	0.00 %	-0.20 %	-0.20 %
Pu-242	0.00 %	-0.20 %	-0.30 %
Sr-88	0.00 %	0.20 %	0.20 %
Sr-90	0.10 %	-2.00 %	-2.00 %
Mo-95	0.00 %	0.00 %	-0.10 %
Tc-99	0.10 %	0.20 %	0.20 %
Ru-101	0.00 %	0.20 %	0.20 %
Ru-106	0.00 %	2.70 %	2.70 %
Rh-103	0.00 %	1.90 %	1.90 %
<b>Ag-109</b>	0.10 %	<b>-21.80 %</b>	<b>-21.80 %</b>
<b>Sb-125</b>	0.00 %	<b>-18.80 %</b>	<b>-18.80 %</b>
<b>I-129</b>	0.00 %	<b>27.80 %</b>	<b>27.80 %</b>
Cs-133	0.10 %	-0.60 %	-0.60 %
Cs-134	-1.10 %	-1.90 %	-1.90 %
Cs-137	0.00 %	-1.70 %	-1.70 %
Ce-144	0.10 %	-7.20 %	-7.20 %

Isotope	XS	XS + FY	XS + FY + HL
Nd-142	-0.10 %	0.00 %	0.00 %
Nd-143	0.10 %	-0.20 %	-0.20 %
Nd-144	0.00 %	-6.80 %	-6.80 %
Nd-145	0.10 %	0.70 %	-
Nd-146	0.10 %	0.30 %	-0.20 %
Nd-148	0.00 %	2.50 %	2.50 %
Nd-150	0.00 %	0.70 %	0.70 %
Pm-147	0.00 %	0.20 %	0.10 %
Sm-147	0.00 %	0.20 %	0.10 %
<b>Sm-148</b>	<b>34.60 %</b>	<b>34.70 %</b>	<b>34.60 %</b>
Sm-149	-0.60 %	-5.50 %	-5.50 %
Sm-150	-0.20 %	-4.90 %	-4.90 %
Sm-151	0.10 %	1.90 %	2.00 %
Sm-152	0.00 %	-2.30 %	-2.30 %
Sm-153	0.10 %	-7.20 %	-7.20 %
Eu-151	0.10 %	2.00 %	-3.10 %
Eu-153	0.00 %	-7.70 %	-7.70 %
<b>Eu-154</b>	<b>-0.70 %</b>	<b>-12.10 %</b>	<b>-7.30 %</b>
Eu-155	0.00 %	-1.80 %	-1.80 %
Gd-154	-2.10 %	-11.10 %	-7.40 %
Gd-155	0.00 %	-1.90 %	-3.50 %
Gd-156	0.00 %	-8.40 %	-8.30 %
Gd-157	0.00 %	-7.90 %	-7.90 %
<b>Gd-158</b>	<b>0.00 %</b>	<b>-16.90 %</b>	<b>-16.90 %</b>

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## Results - <sup>148</sup>Sm

There is a **lack of cross-section** data in JEFF-3.3 for **capture in <sup>147</sup>Pm** leading to <sup>148</sup>MPm, one of the parents of <sup>148</sup>Sm (with a half-life of 41.3 d, larger than the ground <sup>148</sup>Pm, with 5.37 d), allowing an extra accumulation of <sup>148</sup>Sm with JEFF-3.3.

Isotope	XS	XS + FY	XS + FY + HL
<b>Sm-148</b>	<b>34.60 %</b>	34.70 %	34.60 %

<sup>148</sup> Gd	<sup>149</sup> Gd	<sup>150</sup> Gd	<sup>151</sup> Gd	<sup>152</sup> Gd
<sup>147</sup> Eu	<sup>148</sup> Eu	<sup>149</sup> Eu	<sup>150</sup> Eu	<sup>151</sup> Eu
<sup>146</sup> Sm	<sup>147</sup> Sm	<sup>148</sup> Sm	<sup>149</sup> Sm	<sup>150</sup> Sm
<sup>145</sup> Pm	<sup>146</sup> Pm	<sup>147</sup> Pm	<sup>148</sup> Pm	<sup>149</sup> Pm
<sup>144</sup> Nd	<sup>145</sup> Nd	<sup>146</sup> Nd	<sup>147</sup> Nd	<sup>148</sup> Nd

■ Stable ■ EC + β<sup>+</sup> ■ β<sup>-</sup> ■ α

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## Results - <sup>109</sup>Ag

The discrepancy in this isotope comes from the cumulative fission product yields in JEFF-3.3, which are smaller than in ENDF/B-VI for the most relevant tables. <sup>239</sup>Pu is the largest contributor.

FY (cumulative)	ENDF/B-VI	JEFF-3.3
U-235	$3.12 \cdot 10^{-4}$	$2.85 \cdot 10^{-4}$
U-238	$2.52 \cdot 10^{-3}$	$1.62 \cdot 10^{-3}$
Pu-239	$1.48 \cdot 10^{-2}$	$1.11 \cdot 10^{-2}$

Isotope	XS	XS + FY	XS + FY + HL
Ag-109	0.10 %	-21.80 %	-21.80 %

<sup>109</sup> In	<sup>110</sup> In	<sup>111</sup> In	<sup>112</sup> In	<sup>113</sup> In
<sup>108</sup> Cd 2E	<sup>109</sup> Cd	<sup>110</sup> Cd	<sup>111</sup> Cd	<sup>112</sup> Cd
<sup>107</sup> Ag	<sup>108</sup> Ag	<sup>109</sup> Ag	<sup>110</sup> Ag	<sup>111</sup> Ag
<sup>106</sup> Pd	<sup>107</sup> Pd	<sup>108</sup> Pd	<sup>109</sup> Pd	<sup>110</sup> Pd
<sup>105</sup> Rh	<sup>106</sup> Rh	<sup>107</sup> Rh	<sup>108</sup> Rh	<sup>109</sup> Rh

■ Stable ■ EC + β<sup>+</sup> ■ β<sup>-</sup>

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## Results - <sup>129</sup>I

The discrepancy in this isotope comes from the cumulative fission product yields in JEFF-3.3, which are smaller than in ENDF/B-VI for the most relevant tables. <sup>235</sup>U is responsible for the 90% production.

FY (cumulative)	ENDF/B-VI	JEFF-3.3
U-235	$5.43 \cdot 10^{-3}$	$8.14 \cdot 10^{-3}$

Isotope	XS	XS + FY	XS + FY + HL
I-129	0.00 %	27.80 %	27.80 %

<sup>129</sup> Cs	<sup>130</sup> Cs	<sup>131</sup> Cs	<sup>132</sup> Cs	<sup>133</sup> Cs
<sup>128</sup> Xe	<sup>129</sup> Xe	<sup>130</sup> Xe	<sup>131</sup> Xe	<sup>132</sup> Xe
<sup>127</sup> I	<sup>128</sup> I	<sup>129</sup> I	<sup>130</sup> I	<sup>131</sup> I
<sup>126</sup> Te	<sup>127</sup> Te	<sup>128</sup> Te	<sup>129</sup> Te	<sup>130</sup> Te
<sup>125</sup> Sb	<sup>126</sup> Sb	<sup>127</sup> Sb	<sup>128</sup> Sb	<sup>129</sup> Sb

■ Stable ■ EC + β<sup>+</sup> ■ β<sup>-</sup>

7<sup>th</sup> October 2021

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## Results - <sup>125</sup>Sb

Again, the discrepancy in this isotope comes from the cumulative fission product yields. The 80% of its mass appears as cumulative fission yield from the <sup>238</sup>U fast fission table.

FY (cumulative)	ENDF/B-VI	JEFF-3.3
U-238	$4.85 \cdot 10^{-4}$	$2.10 \cdot 10^{-4}$

Isotope	XS	XS + FY	XS + FY + HL
Sb-125	0.00 %	-18.80 %	-18.80 %

<sup>125</sup> I	<sup>126</sup> I	<sup>127</sup> I	<sup>128</sup> I	<sup>129</sup> I
<sup>124</sup> Te	<sup>125</sup> Te	<sup>126</sup> Te	<sup>127</sup> Te	<sup>128</sup> Te
<sup>123</sup> Sb	<sup>124</sup> Sb	<sup>125</sup> Sb	<sup>126</sup> Sb	<sup>127</sup> Sb
<sup>122</sup> Sn	<sup>123</sup> Sn	<sup>124</sup> Sn	<sup>125</sup> Sn	<sup>126</sup> Sn
<sup>121</sup> In	<sup>122</sup> In	<sup>123</sup> In	<sup>124</sup> In	<sup>125</sup> In

■ Stable ■ EC + β<sup>+</sup> ■ β<sup>-</sup>

7<sup>th</sup> October 2021

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## Results - <sup>158</sup>Gd

The discrepancy comes from two different sources.

- Discrepancy ~7000 b between ENDF and JEFF in capture cross-section of <sup>157</sup>Gd (sufficiently small).
- Formation of <sup>158</sup>Gd as fission product and again discrepancies come from the cumulative fission product yields.

FY (cumulative)	ENDF/B-VI	JEFF-3.3
U-238	$3.29 \cdot 10^{-5}$	$1.96 \cdot 10^{-5}$

Isotope	XS	XS + FY	XS + FY + HL
Gd-158	0.00 %	-16.90 %	-16.90 %

<sup>158</sup> Dy	<sup>159</sup> Dy	<sup>160</sup> Dy	<sup>161</sup> Dy	<sup>162</sup> Dy
<sup>157</sup> Tb	<sup>158</sup> Tb	<sup>159</sup> Tb	<sup>160</sup> Tb	<sup>161</sup> Tb
<sup>156</sup> Gd	<sup>157</sup> Gd	<sup>158</sup> Gd	<sup>159</sup> Gd	<sup>160</sup> Gd
<sup>155</sup> Eu	<sup>156</sup> Eu	<sup>157</sup> Eu	<sup>158</sup> Eu	<sup>159</sup> Eu
<sup>154</sup> Sm	<sup>155</sup> Sm	<sup>156</sup> Sm	<sup>157</sup> Sm	<sup>158</sup> Sm

■ Stable ■ EC + β<sup>+</sup> ■ β<sup>-</sup>

7<sup>th</sup> October 2021

46<sup>a</sup> Reunión Anual SNE

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## Conclusions

- General **good agreement** between calculations with EVOLCODE and MCNP/CINDER and experimental values have been obtained for a simple model of the Takahama-3 benchmark.
- Some severe discrepancies in the fission products between codes led to a more in-depth study of the MCNP and CINDER coupling.
  - Identification of an **inconsistent use of cinder.dat** in MCNP.
- The replacement of data from JEFF-3.3 in cinder.dat has a substantial impact is for some of the fission products, especially in the case of the **fission yield data substitution**.
- It is necessary to create a **new version** of the **cinder.dat** library replacing all the data by JEFF-3.3 data if coherent estimations are desired.

**4.2 Evaluating Peak Area Uncertainties in Connection to Passive Gamma Measurements of Spent Nuclear Fuel; V. Solans, UU; TopFuel conference, Santander, Spain; 24 -28/10/2021**



UPPSALA  
UNIVERSITET

# EVALUATING PEAK AREA UNCERTAINTIES IN CONNECTION TO PASSIVE GAMMA MEASUREMENTS OF SPENT NUCLEAR FUEL

V. SOLANS<sup>1</sup>, H. SJÖSTRAND<sup>1</sup>, P. JANSSON<sup>1</sup>, S. GRAPE<sup>1</sup>, P. SCHILLEBEECKX<sup>2</sup>, A. SJÖLAND<sup>3,4</sup>

<sup>1</sup> Uppsala University, <sup>2</sup> JRC-Geel, <sup>3</sup> Swedish Nuclear Fuel and Waste Management Company <sup>4</sup> Lund University

## Objective

In this study, the objective is to estimate the uncertainty in the peak area determination of those radionuclides from the SNFs using results of passive gamma-ray measurements. In particular the uncertainty coming from the parameters of the models will be investigated, and compared for the different models.

## Fitted models

The signal part of the full-energy peak is here proposed to be described using a Gaussian function and a tailing function.

**Gaussian function**

$$P(x) = a_1 \cdot \exp(-(x - \mu)^2/\sigma^2) \quad (1)$$

**Tailing function**

$$T(x) = a_3 \cdot (\exp(B(x - \mu))) \cdot (1 - \exp(-1/\sigma^2)(x - \mu)^2) \cdot \delta \quad (2)$$

**Background function**

$$B(x) = a_2 \cdot \operatorname{erfc}(x - \mu)/\sigma + \text{constant} \quad (3)$$

where  $a_1$ ,  $a_2$  and  $a_3$  are scale parameters,  $\mu$  is the mean value of the Gaussian peak, and  $\sigma$  is related to the width of the peak.  $\delta$  takes the value 1 when  $x < \mu$  and 0 when  $x$  is above  $\mu$ .  $x$  are the channels of the spectrum (proportional to the energy deposited).

## Numerical integration

**Numerical integration using best fitted model,  $NI_{BFM}$**

For this method the background is simultaneously fitted together with the peak. I.e., the background level is determined from the best fitted model (the model that fits the data the best between the one with or without the tailing term).

**Numerical integration fitting background using only edge channels,  $NI_E$**

In this method, a sequential fit of the peak and the background is performed. First the full spectrum is fitted. Subsequently, the parameters defining the full energy peak are fixed. Finally, the background parameters (*erfc* function and constant value) are fitted using only the edge channels. By first defining the peak and subsequently fitting the background in a region where the spectrum is dominated by the background, a better fit to the background can be obtained. Since the *NI* (Numerical Integration) methods only need a good method to define the background level, this method is considered to be best practise and is the reference method for the paper.



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## Conclusion

On average, the numerical integration gives higher uncertainties than the other methods tested in this study on the full-energy peak area after subtraction of the background. However other methods such as the fitted models has uncertainties that cannot be trusted for  $\chi^2 \gg 1$ . Therefore this method (integration using only the edges,  $NI_E$ ) should be used in similar cases.

## Peak area evaluation and uncertainty

$$\text{Area uncertainty} = \sqrt{J_{\text{Area}} * J_{\text{Parameters}} * \text{Cov} * J_{\text{Parameters}}^T * J_{\text{Area}}^T} \quad (4)$$

where *Cov* is the covariance matrix of the parameters of the fit given by the "fit" function of the lmfit package in Python.  $J_{\text{Parameters}}$  is the Jacobian of the fitted model with respect to the parameters of the fit.  $J_{\text{Area}}$  is the Jacobian of the function that described the peak area, with respect to the predicted count per channel. This is one of the methods that can be used to account for a non-perfect parameterisation of the data.

To compute the uncertainty for the numerical integration methods, it was decided to use again Eq. 4, and the square root of the total area:

$$\text{Area uncertainty} = \sqrt{(\sqrt{\text{total area}})^2 + (\text{uncertainty from Eq.4})^2} \quad (5)$$

For the numerical method  $NI_E$ , the ratio between the  $\sqrt{\text{total area}}$  and the uncertainty from Eq.5 is compared. In average, the  $\sqrt{\text{total area}}$  is 1.43 higher than the uncertainty from Eq.4. The minimum ratio in the 166 spectra measured on 42 assemblies at Clab, is 1.08, and the maximum ratio is 1.63. Therefore in all the spectrum the  $\sqrt{\text{total area}}$  component of the uncertainty is the bigger.

## Results

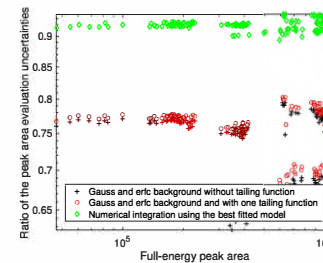


Fig. 1: Ratio of the full-energy peak area uncertainty for all models with respect to numerical integration using only the edges ( $NI_E$ ).

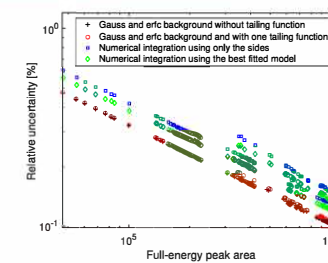


Fig. 2: Relative uncertainty of the full-energy peak area uncertainty for all models

The relative uncertainty decreases when the full-energy peak area, because the counting statistics improves (mainly the term  $\sqrt{\text{total area}}$ ). At maximum the uncertainty is 0.6% for the reference model, and 0.2% in average. The relative uncertainty can be fitted to an exponential relation depending on the full-energy peak area which is:  $\text{Relative uncertainty [\%]} = (\text{Full-energy peak area})^{-0.4844} \cdot 112.1$ .

## Acknowledgement

The project leading to this paper has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 847593.

**4.3 Spent Fuel Characterization to Support NPP Krško Spent Fuel  
Dry Storage Project; M. Kromar, JSI; 13th International  
Conference of the Croatian Nuclear Society; 05 - 08/06/2022**

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# Spent Fuel Characterization to Support NPP Krško Spent Fuel Dry Storage Project

Marjan Kromar, Jan Malec  
“Jožef Stefan” Institute  
Andrej Kavčič  
Nuclear Power Plant Krško



13<sup>th</sup> International Conference of the Croatian Nuclear Society  
Zadar, Croatia, June 5-8, 2022

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## OUTLINE

- Introduction
- Fuel manufacturing and irradiation data
- Determination of the suitable calculation tools and models
- Sensitivity analysis
- Fuel segmentation
- Conclusions

## Introduction

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- Currently, all spent fuel in the NPP Krško (NEK) is stored in the spent fuel pool located in the fuel handling building of the plant.
- NEK decided to implement inherently safer dry storage solution.
- Spent Fuel Dry Storage (SFDS) project - the building with Holtec International HI-STORM FW casks.
- Jožef Stefan Institute (JSI) is supporting NPP Krško SFDS project together with the Faculty of Electrical Engineering and Computing (FER), University of Zagreb.
- JSI is providing independent spent fuel characterization data together with validated procedures and calculation tools.

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## Fuel manufacturing and irradiation data

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- NEK database maintained by FAR code - "as built" fuel manufacturing data (provided by the fuel manufacturer Westinghouse Electric Company) and measurements performed at the plant.
- JSI database maintained by calculation performed by CORD-2 system - "as built" data periodically sent from NEK to JSI.
- Harmonization of both databases - the following FA parameters were compared:
  - mass,
  - enrichment,
  - number of BPRs,
  - number of IFBA rods,
  - burnup.

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## Fuel manufacturing and irradiation data

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- All FAs inserted into the core up to the cycle 31 were considered. Burnup comparison was performed for the first 30 cycles.
- Comparison has shown a few minor differences, which were resolved by inspection of original documents from NEK archive.
- Final FAs burnup reported in the FAR (obtained from INCORE measurements) and FASLIB (obtained from CORD-2 calculations) agree well. All values are within 3.5 %.

## Determination of the fuel parameter space

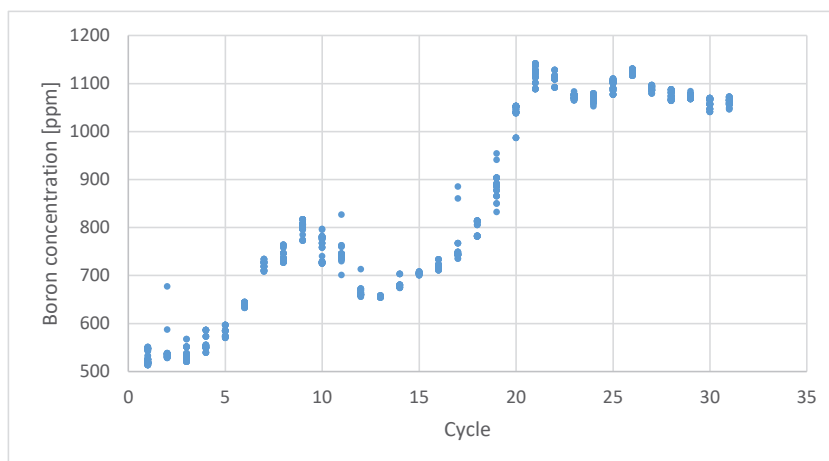
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- Determination of the suitable fuel parameters range covering entire spent fuel variations is needed to define valid parameter space.
- FASLIB database was used, since it contains calculated data required for the sensitivity analysis such as burnup distribution, various temperatures, moderator density, specific power, soluble boron concentrations etc.
- Data are listed for 10 axial layers with relative thicknesses (1, 1, 2, 4, 4, 4, 4, 2, 1, 1), where the unit is 15.24 cm (6 inch). Special attention is needed for the first and last axial periphery region, where masses and enrichments differ significantly (axial blankets) compared to the central regions for the Vantage5 fuel.

## Determination of the fuel parameter space

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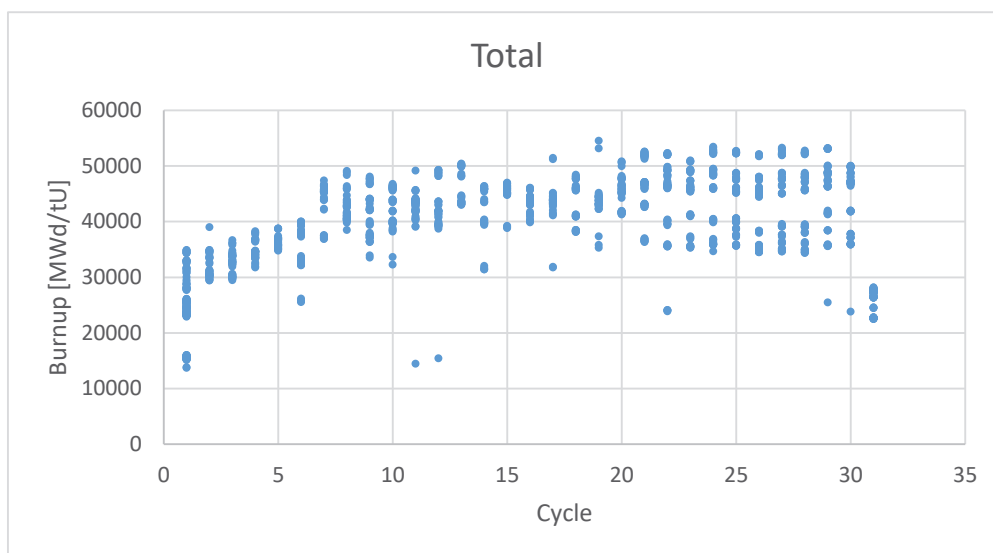
- Relative large parameter variations occurred during the plant operation of almost 40 years.



Average soluble boron concentration

## Determination of the fuel parameter space

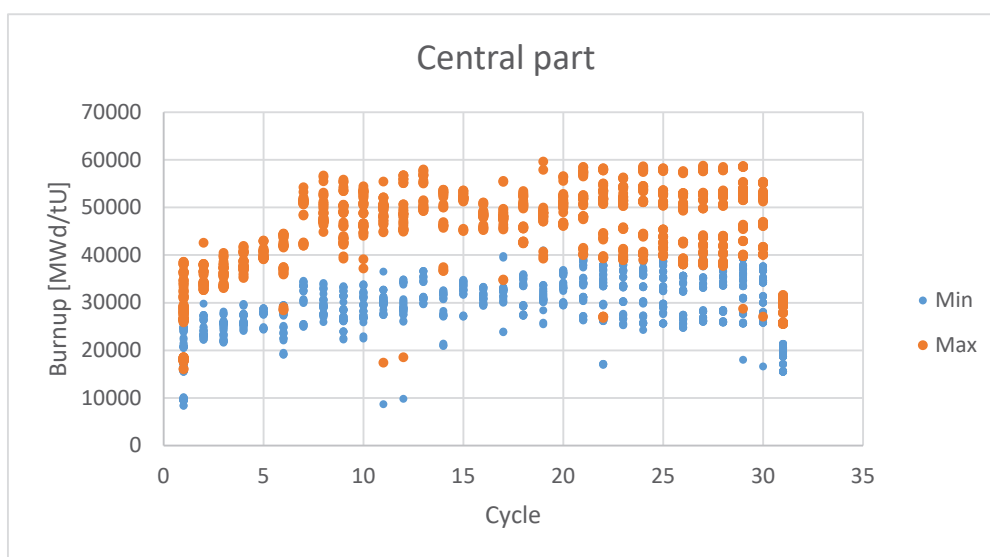
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Total fuel assembly burnup

## Determination of the fuel parameter space

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Minimal and maximal burnup values of central regions

## Determination of the fuel parameter space

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### Fuel parameters range

Parameter	Range
Fuel enrichment	0.7 % - 5 %
Maximal burnup, max. difference	60000 MWd/tU, 24000 MWd/tU
Burnup range	36000 MWd/tU - 60000 MWd/tU
Fuel temperature	600 K – 1100 K
Moderator density	0.655 g/cm <sup>3</sup> (601.91 K)-0.755 g/cm <sup>3</sup> (558.56 K)
Boron concentration	500 ppm -1200 ppm
Specific power	15 W/gU - 65 W/gU
Number of rods in BPR absorbers	0 - 16
Number of IFBA rods	0 - 116

## Determination of the suitable calculation tools and models

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- SCALE code system has been selected for the spent fuel characterization, while the Serpent2 code served as an independent supplementary tool to validate prepared SCALE models. Both code systems are widely used and are thoroughly validated.
- The TRITON/NEWT module from the SCALE package has been used in the analysis, since for now more contemporary POLARIS is not capable to provide ORIGEN binary one-group reaction coefficients library files (.f33). SCALE version 6.2.4 with internal 56 energy group library v7-56 based on the ENDF/B-VII.1 evaluated nuclear data files has been applied.
- Version 2.1.29 of the Monte Carlo code Serpent2 and the continuous energy cross section library in ACE format, based also on the ENDF/B-VII.1 evaluated nuclear data files has been used for the validation.

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## NPP Krško fuel model validation

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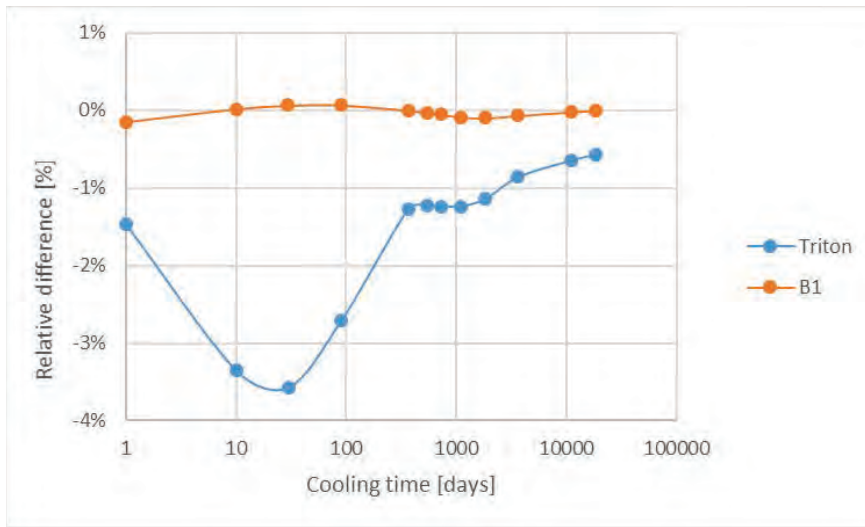
- A typical FA with 4.95 % enrichment and no IFBA rods was selected as a test case. A reference 2-D case scenario (infinite in axial direction) with periodic boundary conditions in lateral direction consists of the following reactor operational parameters:
  1. Fuel temperature 900 K,
  2. Moderator temperature 580.46 K with density 0.70871 g/cm<sup>3</sup>,
  3. Soluble boron concentration of 1000 ppm.
- Parameters are close to the average operational parameters applied in the last NPP Krško cycles.
- Decay heat, fuel activity, photon and neutron source term after burnup of 60000 MWd/tU were examined.

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NPP Krško fuel model validation

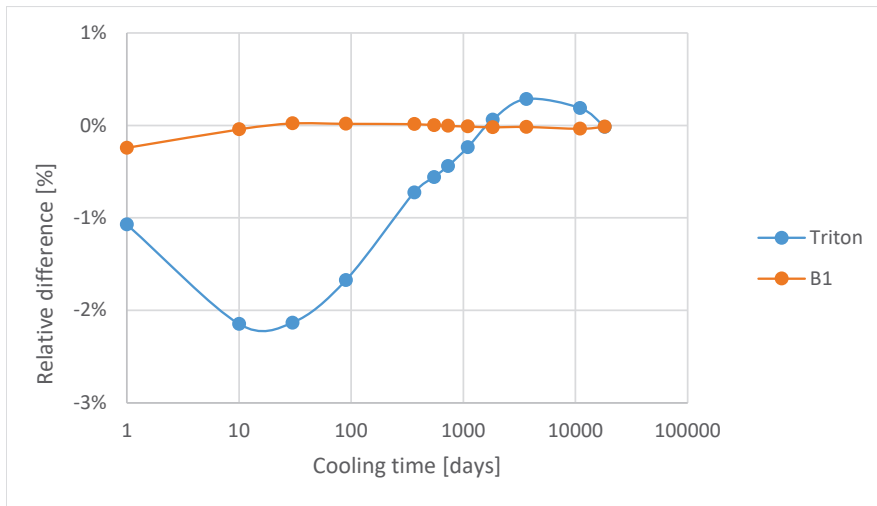
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Relative differences of the decay heat – DH; Triton:  $(DH_{SCALE} - DH_{Serpent}) / DH_{Serpent}$ , B1:  $(DH_{B1} - DH_{SCALE}) / DH_{SCALE}$

NPP Krško fuel model validation

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Relative differences of the activity – A; Triton:  $(A_{SCALE} - A_{Serpent}) / A_{Serpent}$ , B1:  $(A_{B1} - A_{SCALE}) / A_{SCALE}$

## Origami model validation

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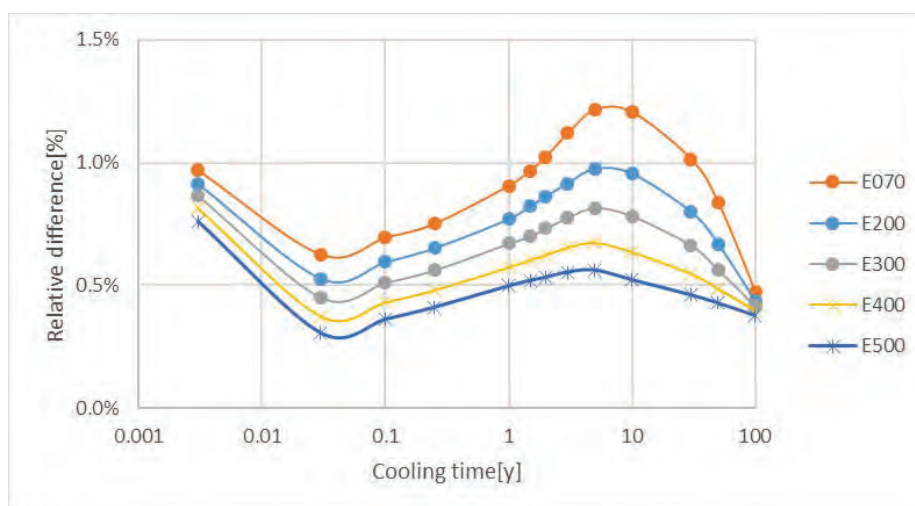
- The use of the TRITON/NEWT sequence for the characterization of the more than 1400 considered FAs would be impractical, since a single depletion run takes around 2 hours on the PC with the Intel I7 processor.
- Fortunately, the TRITON/NEWT module is capable to provide ORIGEN binary one-group reaction coefficients library .f33 files. These library files are sufficient to determine isotopic composition during the fuel irradiation (solution of Bateman equations) avoiding the need of time-consuming neutron transport calculation.
- However, the calculation sequence has to be validated.

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## Origami model validation

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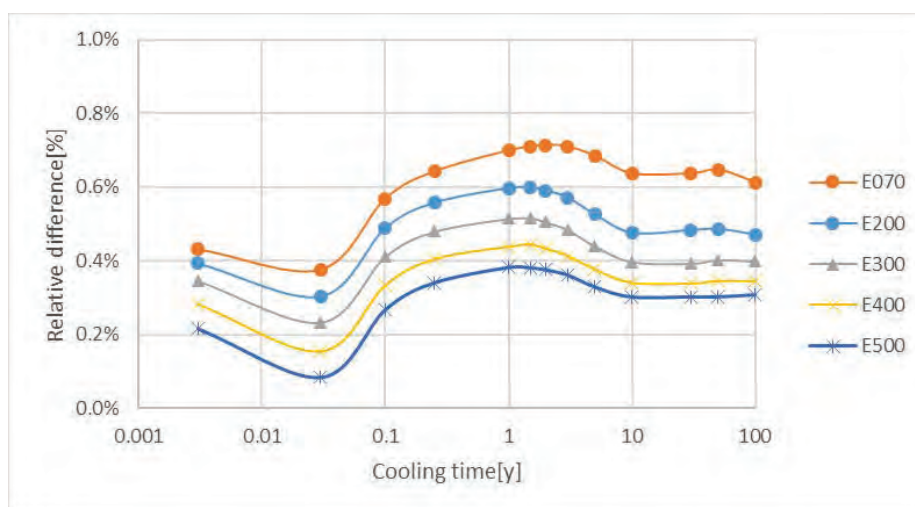
Relative differences of the ORIGAMI decay heat compared to the TRITON/NEWT results

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## Origami model validation

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Relative differences of the ORIGAMI activities compared to the TRITON/NEWT results

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## Origami model validation

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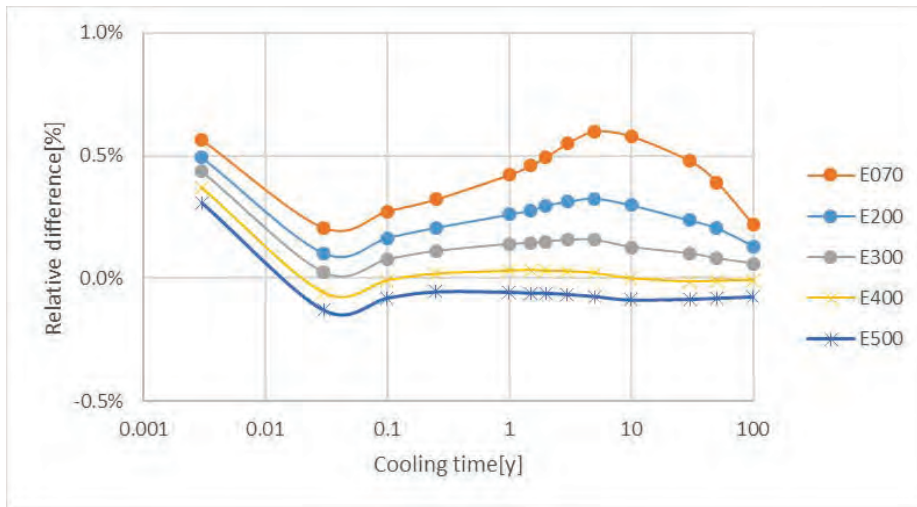
- Closer examination has revealed that the observed differences are due to the neutron capture reactions.
- Namely, in the FA non-fuel materials (e.g., structural materials) are also present. These materials contribute to the overall power production due to the energy produced by the neutron capture. For a given value of the total assembly power, this reduces the power from the fuel mass and thus slightly alter the fuel burnup and isotopics.
- The problem is that this contribution is case dependant and varies with enrichment, burnup, etc. The factor of the energy contributed to the fuel itself varies from 0.986 (enrichment 0.7 %) to the 0.997 (enrichment 5 %) for the presented cases.

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## Origami model validation

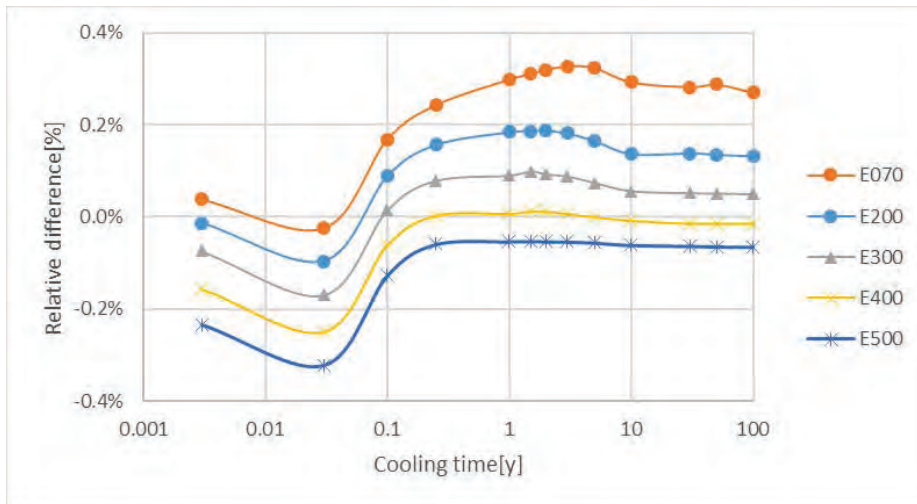
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Relative differences of the ORIGAMI decay heat compared to the TRITON/NEWT results, neutron capture correction factor 0.996

## Origami model validation

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Relative differences of the ORIGAMI activities compared to the TRITON/NEWT results, neutron capture correction factor 0.996



## Sensitivity analysis

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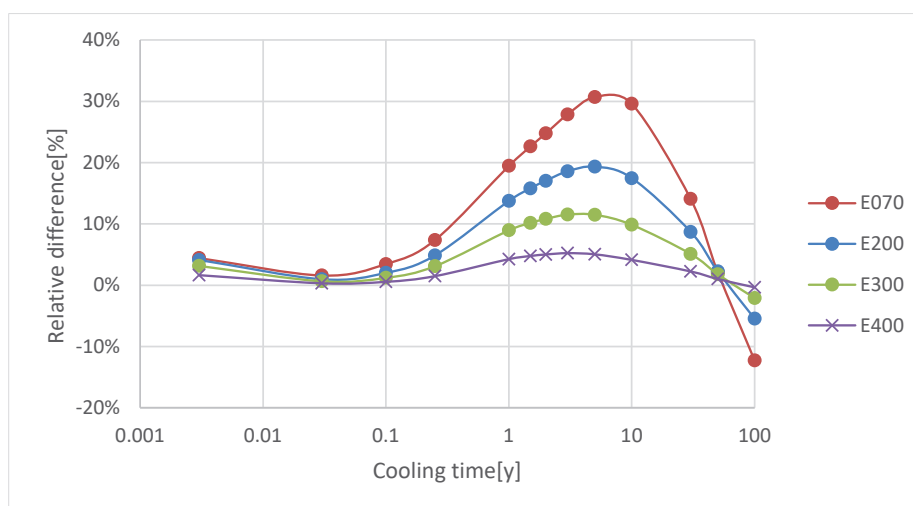
- Sensitivity analysis defines response of the parameter variation on the observables and can be used to determine conservative approach, when explicit parameter consideration in the characterization process is not reasonable or viable, and define basic uncertainties due to propagation of uncertainties in each parameter and selected process.
- In the evaluation of the averaging process, non-linearity of the sensitivity coefficients should be examined also. Namely, calculations are usually performed at some averaged parameters value. It is not self-evident that such averaging process would yield also an averaged result.

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## Sensitivity analysis

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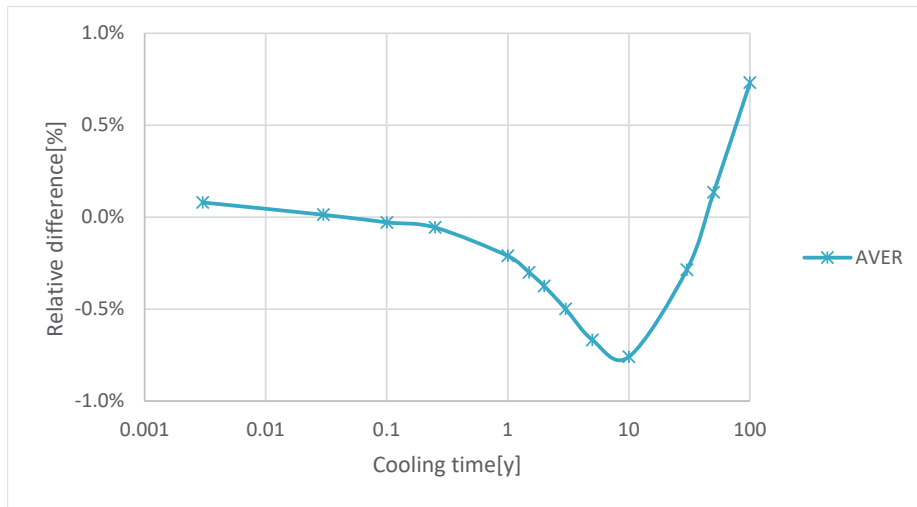
### Impact of the fuel enrichment on the decay heat

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### Sensitivity analysis

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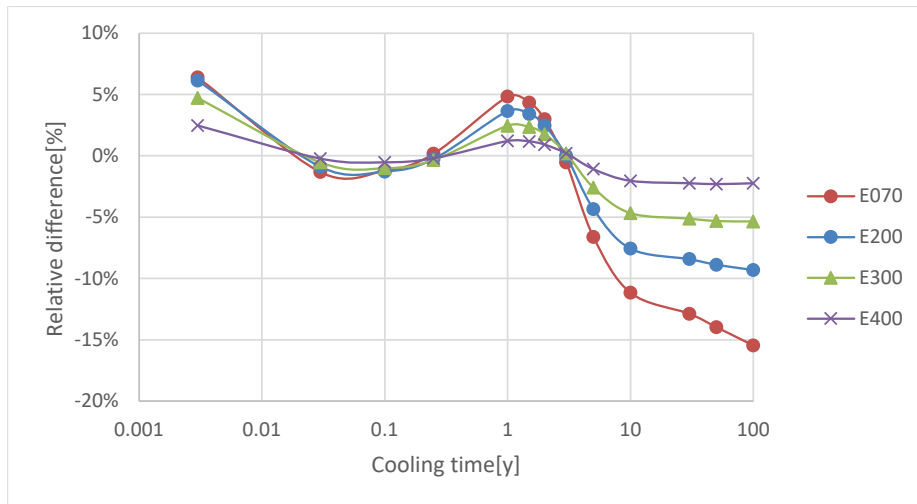
### Impact of the ±1 % enrichment averaging on the decay heat

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### Sensitivity analysis

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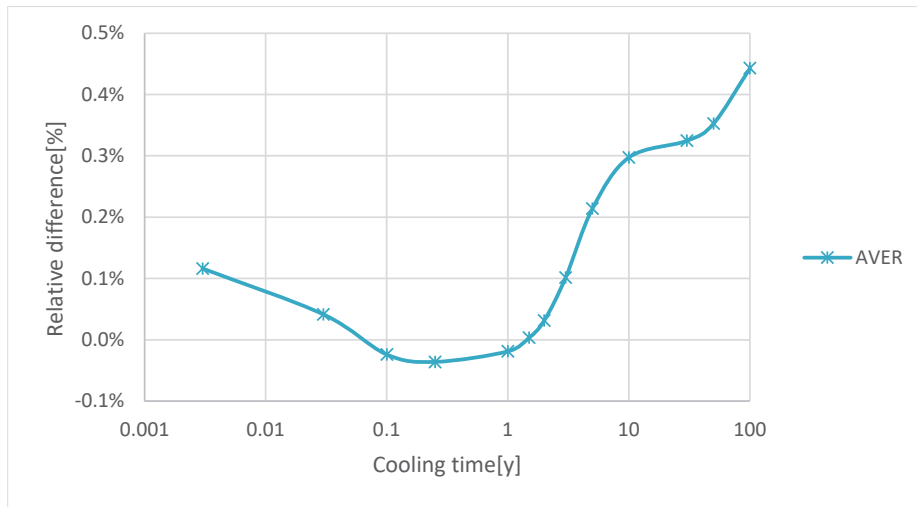
### Impact of the fuel enrichment on the activity

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### Sensitivity analysis

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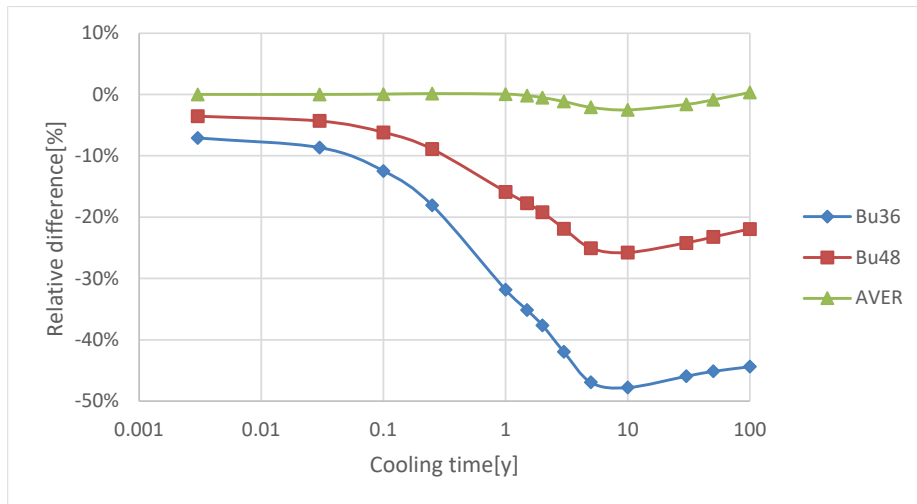
#### Impact of the ±1 % enrichment averaging on the activity

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### Sensitivity analysis

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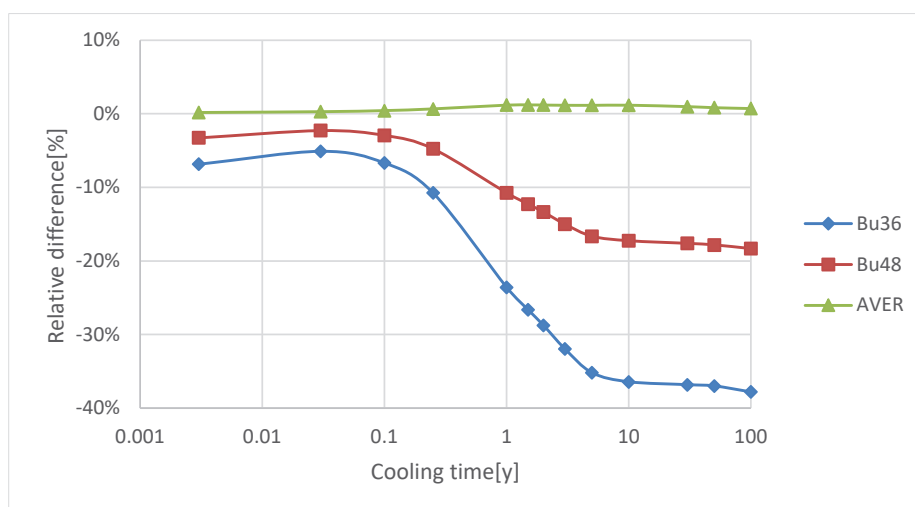
#### Impact of the fuel burnup on the decay heat

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## Sensitivity analysis

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### Impact of the fuel burnup on activity

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## Sensitivity analysis

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- Impact of all other parameters has been evaluated in the project.
- Due to programming and execution time constraints in ORIGAMI, only limited number of variables can be explicitly taken into account in the interpolation of the .f33 files.
- All others will have to be covered in some conservative manner. The final decision has yet to be made.

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## Fuel segmentation

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- Performed sensitivity analysis has determined impact of individual parameters on the specific spent fuel observable.
- Unfortunately, averaging process yields to over prediction in some cases and under prediction in others, with possible opposite trends in different observables.
- It is very hard to identify the most important ones for all cases. The final result is a mixture of individual contributions.
- The most accurate approach would be to take all 10 axial regions explicitly. However, such approach is time consuming. It would take more than 3 years of the CPU time to calculate 1400 FAs with the TRITON/NEWT sequence. Even ORIGAMI would require several days of calculation.
- Some kind of homogenization is therefore necessary.

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## Fuel segmentation

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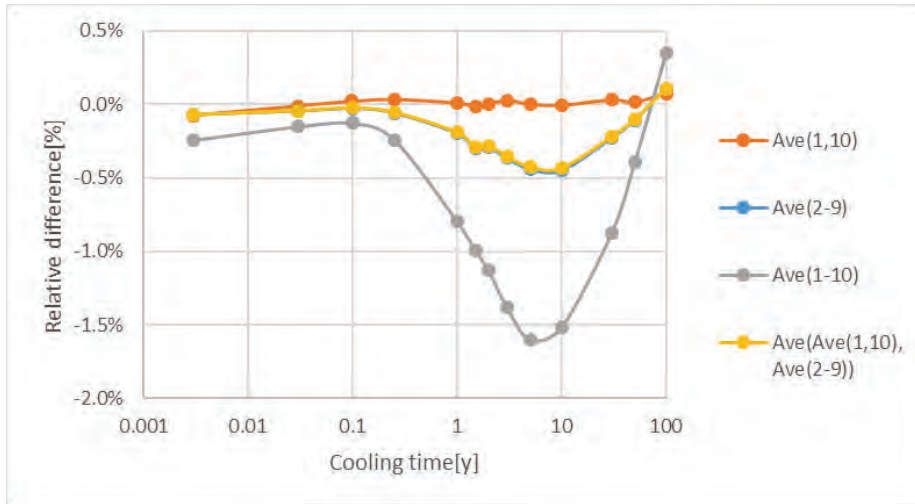
- It seems natural to explore axial blankets, since there are large material heterogeneities present.
- To get a proper feeling, a few typical cases have been evaluated:
  - A – standard FA without axial blankets (cycles 1-7)
  - B – FA with natural uranium axial blankets (cycles 7-16)
  - C – FA with annular axial blankets (from cycle 16 onward)

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## Fuel segmentation

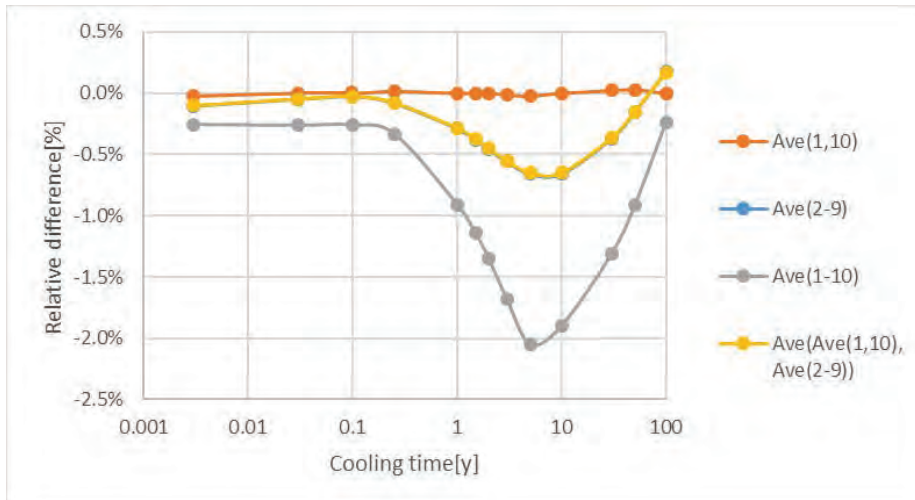
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Impact of the homogenization on decay heat – case A

## Fuel segmentation

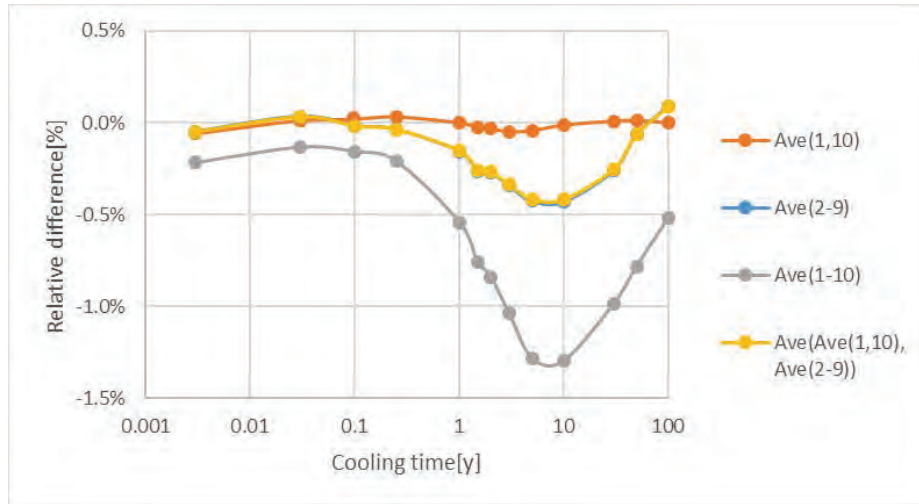
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Impact of the homogenization on decay heat – case B

Fuel segmentation

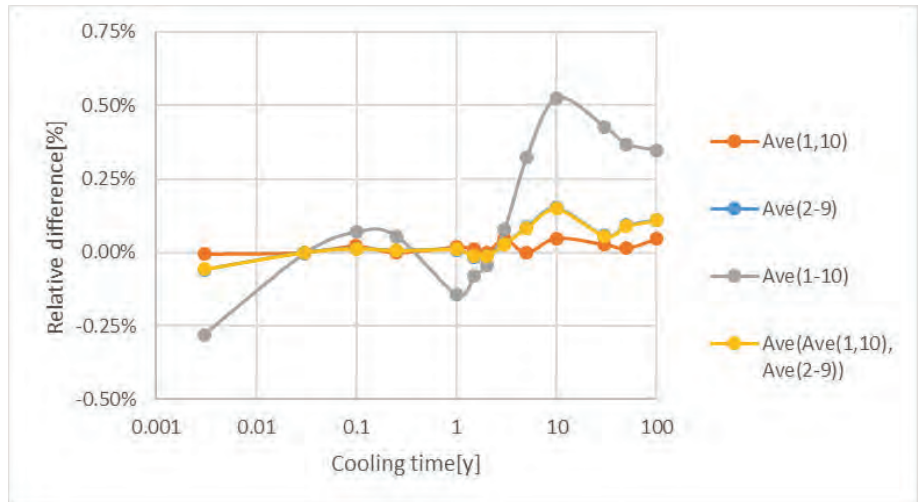
33/40



Impact of the homogenization on decay heat – case C

Fuel segmentation

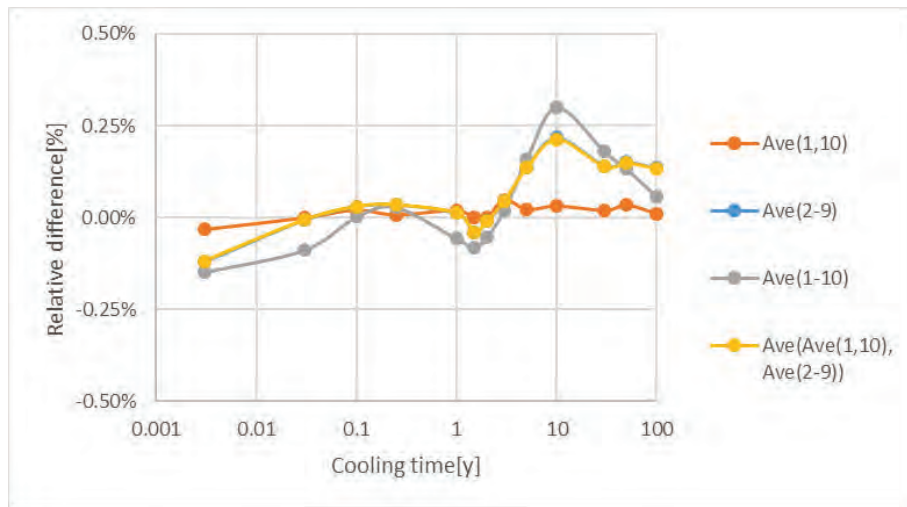
34/40



Impact of the homogenization on activity – case A

## Fuel segmentation

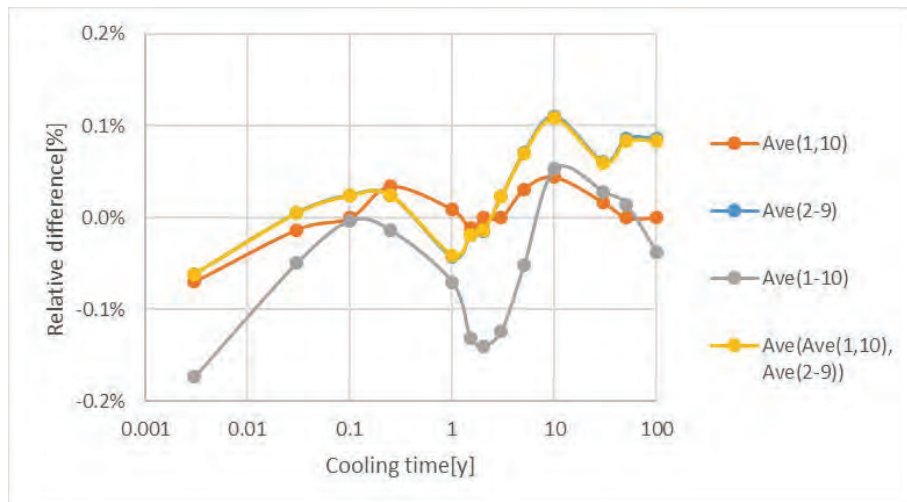
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Impact of the homogenization on activity – case B

## Fuel segmentation

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Impact of the homogenization on activity – case C



## Conclusion

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- Activities performed at JSI to support NPP Krško Spent Fuel Dry Storage project are presented in this report.
- In the initial phase of the project, FAR and FASLIB fuel assembly databases have been harmonized. Validated data from the FASLIB database served to analyse fuel manufacturing and irradiation data.
- TRITON/NEWT calculation model has been validated by the comparison of the predictions obtained from the stochastic neutron transport code Serpent2.
- Results obtained by both codes are in good agreement. For the time period of 1 year – 50 years decay heat differences are less than 1.3 %, in activity 1 %, while neutron and photon emissions are inside 5 % and 2 % respectively.

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## Conclusion

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- ORIGAMI model running on the TRITON/NEWT binary one-group reaction coefficients library (.f33 files) has been validated. The importance of the energy produced by the neutron capture has been stressed to reduced observed differences.
- NPP Krško spent fuel sensitivity study has been accomplished based on the developed TRITON/NEWT model and fuel predetermined parameters range.
- It seems that fuel burnup and enrichment are the most influential parameters in the calculation of observables.

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## Conclusion

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- In the evaluation of the averaging process, non-linearity of the sensitivity coefficients was examined also.
- The effect is mainly noticeable for the enrichment and burnup, where the decay heat prediction might be several % too low, if unsuitable segmentation is performed.
- A few FA cases based on the real data have been analyzed to demonstrate reasonable axial discretization.
- Planned activities are gradually coming to successful conclusion contributing to the safe and economical spent fuel dry storage on the NPP Krško site.

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**Thank you for your attention!**

**Questions?**

**4.4 Passive neutron and gamma technique for spent nuclear fuel characterisation; V. Solans, UU; IAEA CRP spent fuel characterization; 22 – 23/09/2022**



## PASSIVE NEUTRON AND GAMMA TECHNIQUE FOR SPENT NUCLEAR FUEL CHARACTERISATION

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Henrik Sjöstrand, Sophie Grape, Erik Branger (UU)

Alessandro Borella, Riccardo Rossa (SCK CEN)

Peter Schillebeeckx (IRC), Anders Sjöland (SKB)



*This project has received funding from the European Union's Horizon 2020 research and innovation programme 2014-2018 under grant agreement N°847593*

September 2022

IAEA CRP

1



**UPPSALA UNIVERSITY**

• **Spent nuclear characterization for the geological repository (EURAD)**

• **Safeguards**

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• **Fuel performance modelling**

• [henrik.sjostrand@physics.uu.se](mailto:henrik.sjostrand@physics.uu.se)

• **Gamma tomography**

• [peter.andersson@physics.uu.se](mailto:peter.andersson@physics.uu.se)





## EURAD GOALS

• **In deep geological repositories, spent nuclear fuel needs to be characterized:**

- Reactivity
- Decay heat
- Gamma's and neutron's dose
- Safeguards parameters

• **Before encapsulation, need to verify (update), the fuel parameters calculated by the state of the art codes.**

• **Experimental measurements:**

- Calorimetric measurements
- **Gamma-ray scans**
- **Neutron measurements**



## SUMMARY

• **Gamma measurements**

- Reproducibility measurement
- Intrinsic self-calibration

• **Neutron measurements**

- Fit Rossi-alpha distribution with double exponential fit
- Predict BU and IE





### SKB50

- Set of 25 BWR and 25 PWR assemblies
- Used in Swedish reactors
- Various burnup, initial enrichment, cooling time, manufacturers
- Gamma scans
- Calorimetric measurements
- Neutron measurements
- Chosen around 2013-2014



Image reference: Andersson, J., Skagius, K., Winberg, A. et al. Site-descriptive modelling for a final repository for spent nuclear fuel in Sweden. *Environ Earth Sci* 69, 1045–1060 (2013). <https://doi.org/10.1007/s12665-013-2226-1>



### DIFFERENT CAMPAIGNS

#### • Campaign 1

- Done in 2014
- Static measurement

#### • Campaign 2

- Done in 2014
- Axial measurement

#### • Campaign 3

- Done in 2016-2019
- Axial measurement

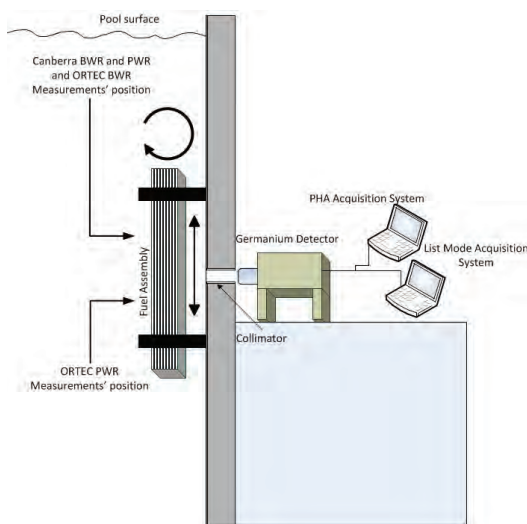
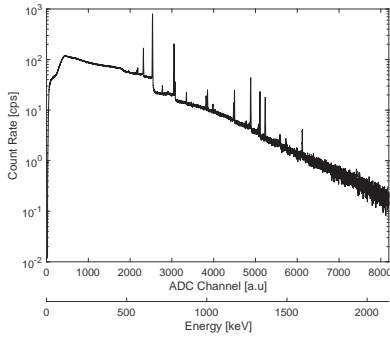


Image reference: S. Vaccaro, et al., PWR and BWR spent fuel assembly gamma spectra measurement using nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, Volume 833, 2016





## SPECTRUM



V. Solans, et Al. evaluating peak area uncertainties in connection to passive gamma measurements of spent nuclear fuel, TopFuel Conference 2021

From SNF's spectrum it is possible to extract the count rate (by numerical integration):

Cs-137, 662 keV	$T_{1/2} = 30y$
Cs-134, 996 keV	$T_{1/2} = 2.1y$
1004 keV	
1274 keV	
1596 keV	
Eu-154, 605 keV	$T_{1/2} = 8.6y$
796 keV	
1365 keV	



## COUNT RATE

Comparing count rate between different campaigns have several challenges :

- Attenuation plates
- Detector efficiency
- Position of the fuel with respect to the detector
- ...

Use of the intrinsic self calibration method

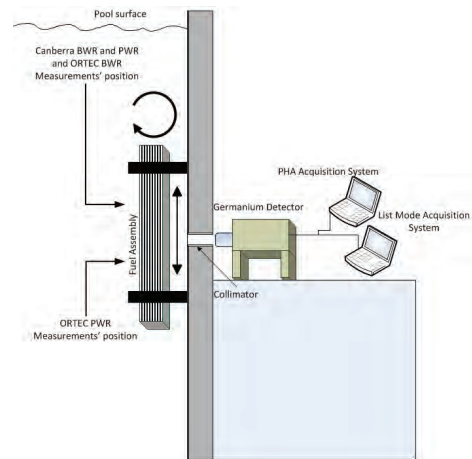
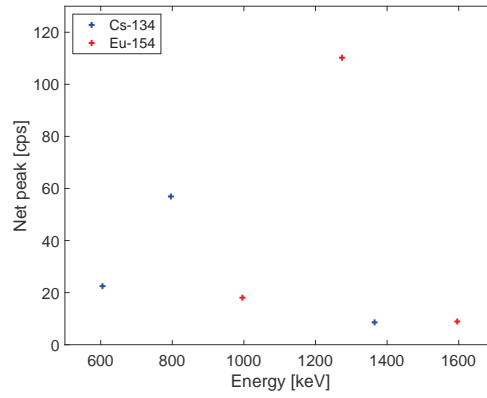


Image reference: S. Vaccaro, et AL, PWR and BWR spent fuel assembly gamma spectra measurements, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, Volume 833, 2016

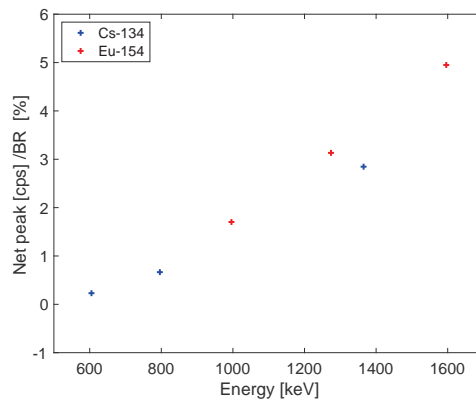




**INTRINSIC SELF-CALIBRATION**



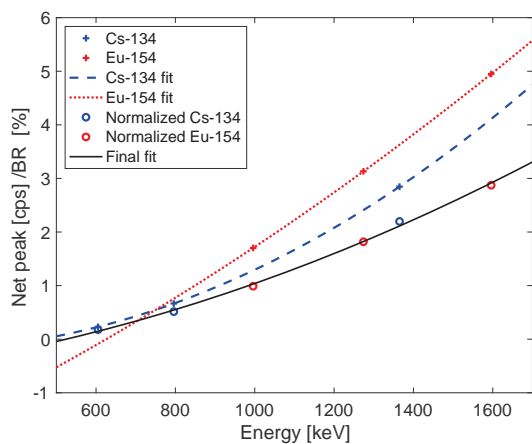
**INTRINSIC SELF-CALIBRATION**







## INTRINSIC SELF-CALIBRATION



Multiple peaks for a singles/multiple radionuclides:

- Self calibration possible
- Remove dependence on the detector and geometry
- Cs-134/Cs 137 and Eu-154/Cs-137 can be determined independently of knowledge of the campaign details



## RESULTS – SELF CALIBRATION

• Even if the measurement conditions were different between the campaigns, mean deviation between campaigns obtained were:

• With self-calibration

- 1.4% for Cs-137
- 2.3% for Eu-154/Cs-137
- 1.9% for Cs-134/Cs-137

• Without self-calibration

- 1.4% for Cs-137
- 8.1% for Eu-154/Cs-137
- 4.0% for Cs-134/Cs-137





## RESULTS - REPRODUCIBILITY

### Standard deviation of the best determined peak:

The standard deviation in the inter-campaign reproducibility for the best-determined gamma peaks is between 2 and 3%.



## DIFFERENTIAL DIE-AWAY SELF INTERROGATION INSTRUMENT (DDSI)

- Passive instrument developed and built in LANL
- Use neutron from Cm244 to interrogate the assembly
- Detect neutrons in coincidence (Rossi-alpha distribution)
- 56  $^3\text{He}$  tubes detect thermal neutrons
- Polyethylene to slow down neutrons
- Lead to reduce gamma-ray dose rate

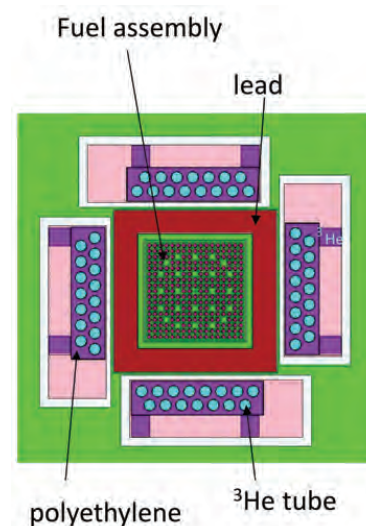
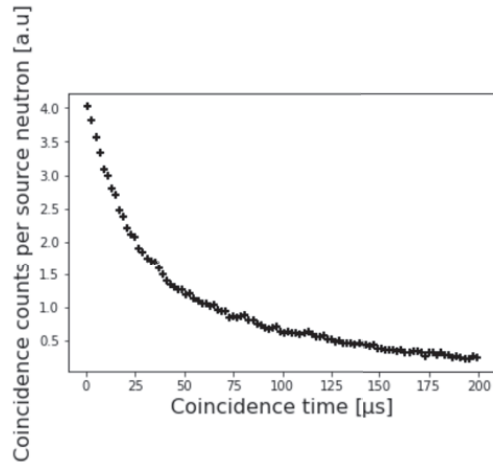


Image courtesy of Li Balkestahl





### ROSSI-ALPHA DISTRIBUTION (RAD)



• Rossi-alpha distribution (RAD)

• Time correlation for coincident neutrons

• Each neutron as start

• Total number of neutrons detected is also an outcome of the DDSI



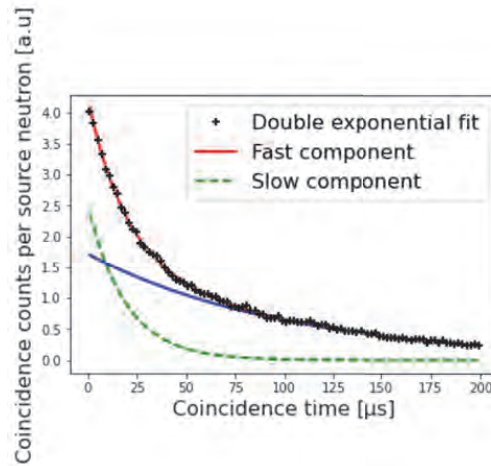
### DOUBLE EXPONENTIAL

• A fast and a slow component

• Fast is not only direct detection or fast multiplication

• Slow is neutrons that have time to thermalized before fission

$$RAD_{double}(t) = A_{fast} \cdot \exp(-\tau_{fast} t) + A_{slow} \cdot \exp(-\tau_{slow} t)$$

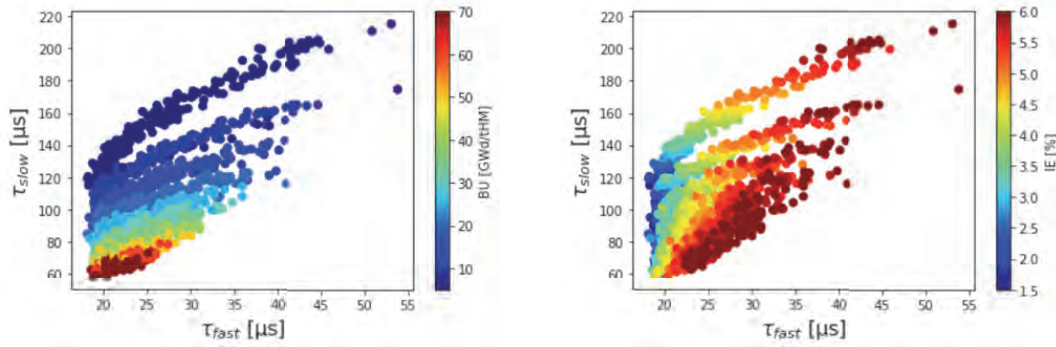


Increase in absorbers will decrease the fission chain therefore will lead to a smaller slow component





### TAU FAST VERSUS TAU SLOW



Indication that there is more information

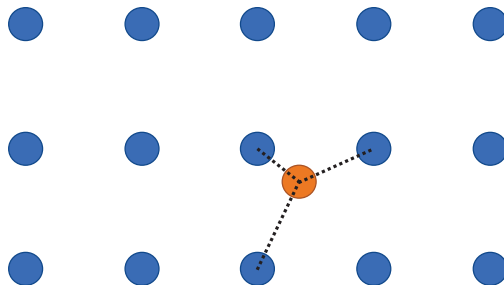
Same data point with different colouring indicating BU or IE



### MODEL

#### Use a KNN model

- Trained on the simulated dataset
- Tested on the simulated dataset and the experimental data



Average of the 3 closet neighbours





## DATASETS

### Simulated dataset

- 2536 samples (from a pincell model)
- 17x17 PWR fuel
- BU ranges from 5 to 70 GWd/tHM
- IE from 1.5% to 6% (alternating 0.3% and 0.2% steps)
- CT from 0 to 70 y (with intermediate CTs at 2.5, 5, 7.5, 10, 12.5, 15, 20, 30, 40, 55 y)

### Experimental data

- SKB 50 PWR 17x17 SNFs ranges from 19 to 48 GWd/tHM, and IE goes from 2.1 to 3.94%. The cooling time at the time of the measurement of the SNFs was between 6.3 and 30.4 years.



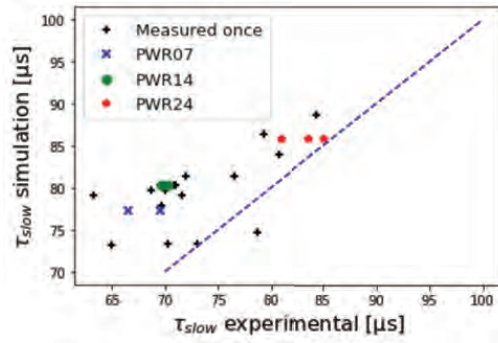
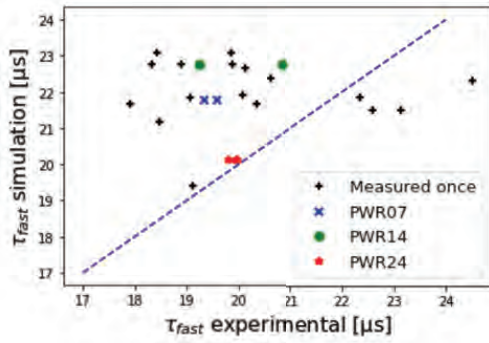
## RESULTS

RMSE	BU [GWd/tHM]	IE [%]
Test set simulation	4.51	0.284
Experimental After KNN	11.85	0.963





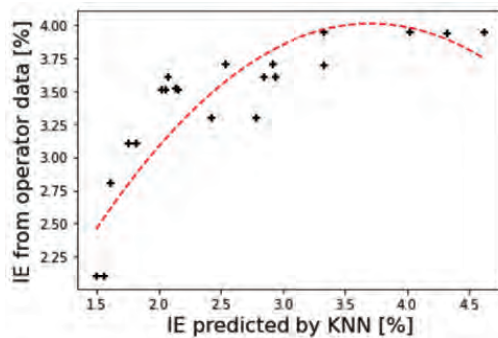
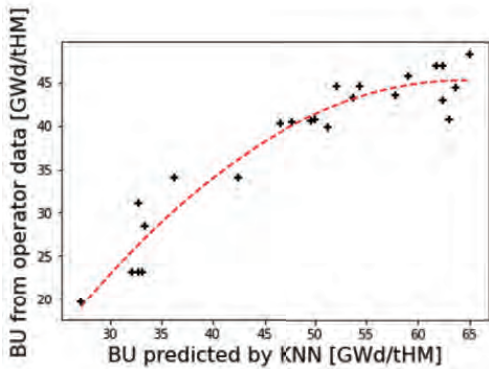
### EXPERIMENTAL RESULTS



Dotted line is the unity line



### RESULTS





## RESULTS

RMSE	BU [GWd/tHM]	IE [%]
Test set simulation	4.51	0.284
Experimental After KNN	11.85	0.963
Experimental After fit	2.65	0.324
Simulated set after fit	2.45	0.640




## CONCLUSION

### Gamma measurement:

- Reproducibility of the SKB50 measurement campaigns has been investigated between 1.4 to 2.3 %
- Intrinsic self calibration for the experimental gamma measurements applied to the SKB-50

### Neutron measurement:

- Predict BU and IE using KNN enabled by the double exponential fit
- Improve the prediction capability using polynomial fit

**For the future, focus on predicting decay heat using gamma and neutron measurements**



**4.5 Recent Spent Fuel Research at VTT; S. Häkkinen, P. Juutilainen, L. Vaara, R. Tuominen; Nuclear Science and Technology Symposium 2022 (SYP2022); 27/05/2021**





**VTT**

## Recent spent fuel research at VTT

Silja Häkkinen, Pauli Juutilainen, Lauri Vaara, Riku Tuominen  
SYP 1.-2.11.2022


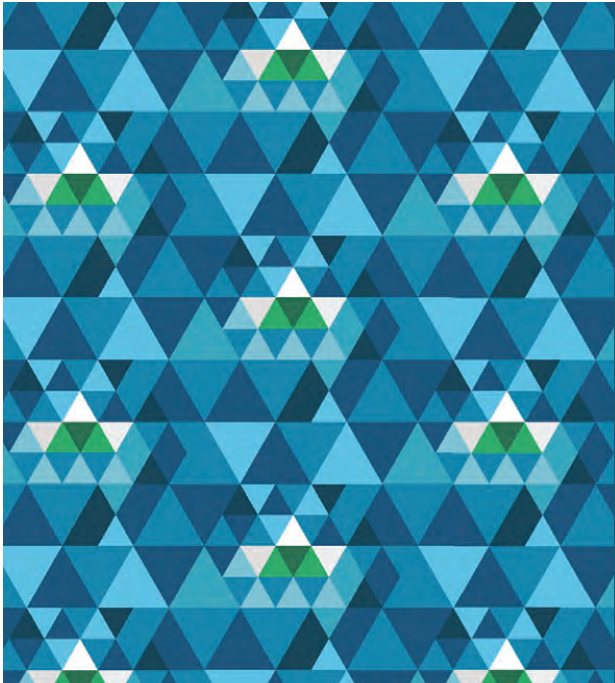
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**VTT**

## Outline

- Motivation and overview
- Results in selected topics
- Nuclear data uncertainty propagation
- Key take aways and future work



# Motivation and overview

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## Motivation

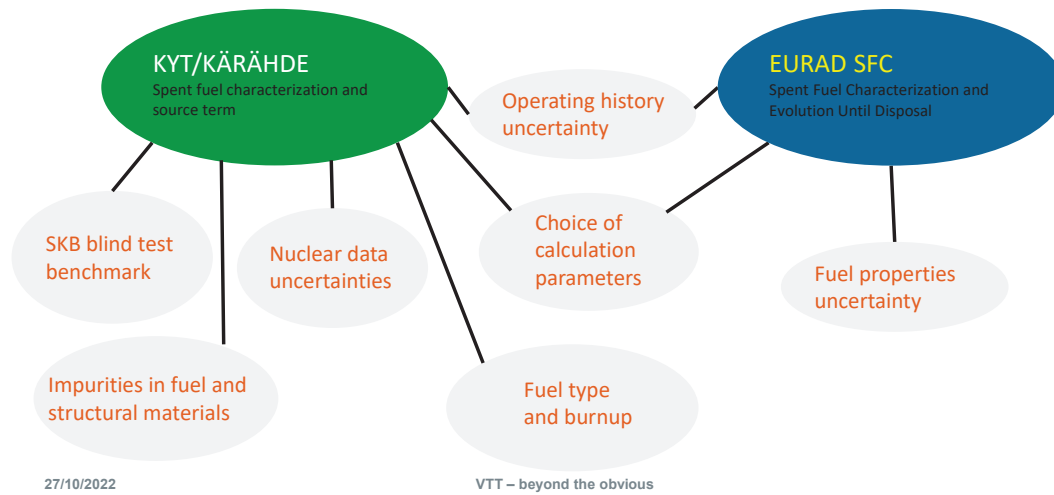
- Knowledge of spent fuel (SNF) properties is important for safe handling and final disposal
  - Decay heat and reactivity → volume of repository space
  - Nuclide inventories → radiation protection, dose estimates
- Computational determination of decay heat involves several uncertainty sources
- SNF properties are also dependent on fuel type, enrichment and burnup
- At VTT, these uncertainties have been studied using the Monte Carlo reactor physics code Serpent 2 [1]



[1] Leppänen, J., et al. (2015) "The Serpent Monte Carlo code: Status, development and applications in 2013." *Ann. Nucl. Energy*, 82 (2015) 142-150.



## Recent spent fuel studies at VTT

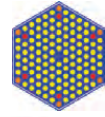


VTT

# Results in selected topics

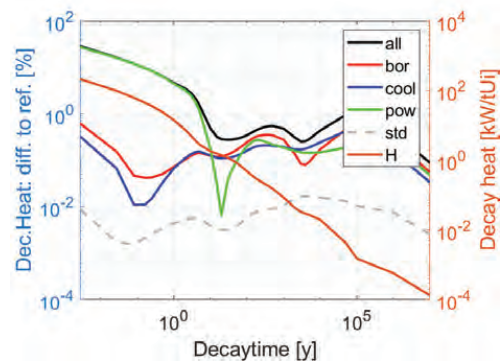
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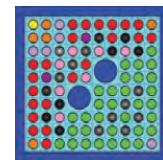
## Simplifications in operating history

- Boron concentration, assembly power and coolant temperature and density were averaged over three cycles.
- Averaging assembly power overestimates activity, decay heat and photon emission rate 64 – 78 % right after irradiation.
- After 10 years the effect is < 1 %
- Effect on spontaneous fission rate and the studied nuclides (C-14, Cl-36, Mo-93, Ag-108m, I-129, U-233, U-235, Pu-239, Pu-241) is mostly below 1.5 %



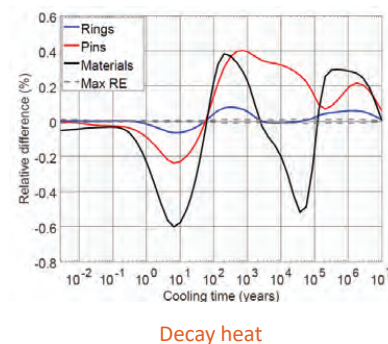
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## Choice of calculation parameters

- Studied calculation parameters:
  - Depletion zone division
  - Depletion step length
  - Doppler-broadening rejection correction (DBRC)
  - Unresolved resonance probability table sampling
  - Energy-dependent branching ratios
- Maximum effects (depletion zone division)
  - Decay heat 0.6 % at 7 y
  - Photon emission rate 1.1 % at ~7000 y
  - Spontaneous fission rate 8 % at ~400 y
- Neglecting DBRC
  - non-negligible effect on some heavier nuclides
  - Maximum effect on DH and PE ~0.5 %

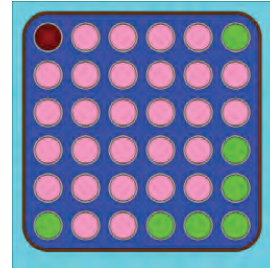


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## Uncertainty analysis of one sample in a 6x6 BWR assembly

Parameter	Average	RSD [%]
Moderator density	0.759 g/cm <sup>3</sup>	2
Power density	18.84 W/gU	1.7
Fuel temperature	923 K	2
Water temperature	549 K	1
Void <sub>1</sub>	50 %	6.7 (Δvoid = ±10 %)
Void <sub>2</sub>	50 %	1.3 (Δvoid = ±2 %)
Fuel density	10.5 g/cm <sup>3</sup>	0.3
Fuel radius	0.612 cm	0.01
<sup>234</sup> U enrichment (in <sup>235</sup> U)	0.65	0.1 (Δ <sup>234</sup> U = ±0.25 %)
<sup>235</sup> U enrichment	2.53	0.7 (Δ <sup>235</sup> U = ±0.05 %)
<sup>238</sup> U content	85.92	0.7
Burnup (assembly)	22.627	2



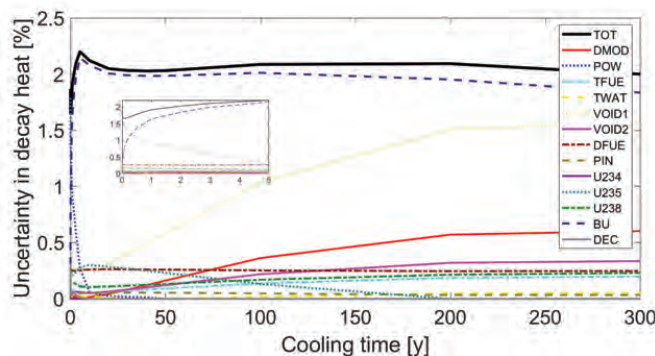
$$\sigma_{calc,i}^2 = \sigma_i^2 + \sigma_{MC}^2$$

$$\sigma_{tot}^2 = \sum_{i=1}^n \sigma_i^2$$

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## Decay heat uncertainty of the BWR sample



- TOT – Total uncertainty (void<sub>2</sub> = ±2 %)
- DMOD – Moderator density
- POW – Power density
- TFUE – Fuel temperature
- TWAT – Water temperature
- VOID1 – Void<sub>1</sub> = ±10 %
- VOID2 – Void<sub>2</sub> = ±2 %
- DFUE – Fuel density
- PIN – Fuel radius
- U234 – <sup>234</sup>U enrichment
- U235 – <sup>235</sup>U enrichment
- U238 – <sup>238</sup>U content
- BU – Burnup
- DEC – Decay data

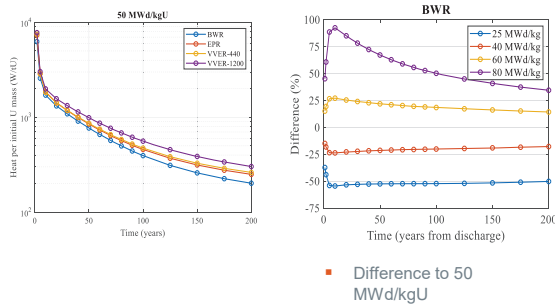
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# Impact of fuel type and burnup on decay heat

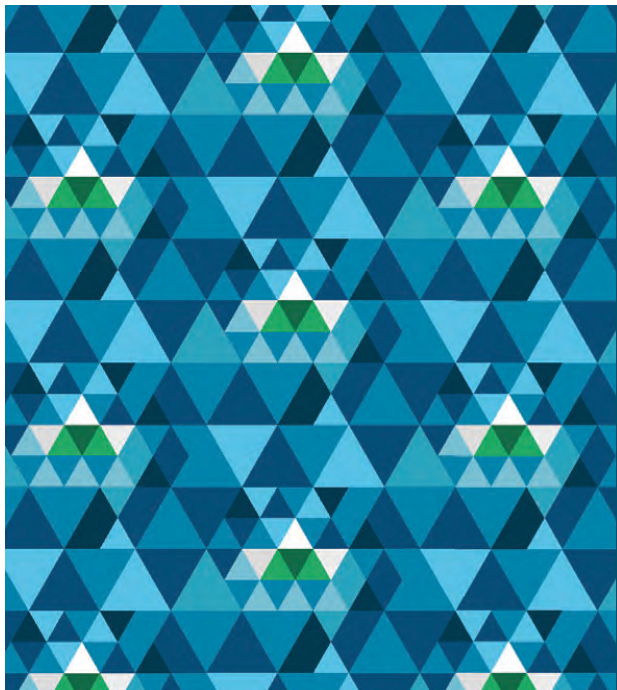


Top decay heat contributors 5 y (top) and 100 y (below) after irradiation

BWR	%	EPR	%	VVER-440	%	VVER-1200	%
Y90	27.7	Cs134	27.2	Cs134	27.9	Cs134	25.4
Ba137m	27.2	Ba137m	24.5	Y90	25.2	Y90	24.2
Cs134	24.9	Y90	23.2	Ba137m	25.1	Ba137m	23.2
Cm244	10.2	Cm244	13.7	Rh106	11.4	Pu238	16.9
Rh106	10.0	Rh106	11.4	Cm244	10.3	Rh106	10.4

Nuclides	% (BWR)	% (EPR)	% (VVER-440)	% (VVER-1200)
Am241	40.0	44.8	46.4	39.1
Pu238	22.8	23.6	22.6	34.8
Ba137m	16.3	14.1	13.6	11.4
Y90	15.0	12.1	12.4	10.7
Pu240	5.9	5.4	5.0	4.0

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# Nuclear data uncertainty propagation

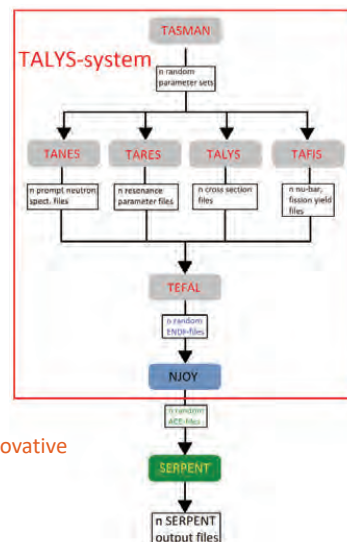
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## Key Idea

- Create hundreds of randomized nuclear data files for many nuclides
  - New nuclear data is produced from nuclear models and experimental data: No need to resort to covariance data.
  - The data is produced with TALYS and a few satellite programs = T6 [2]
- Assign a random combination of the random data files for a Serpent run
  - Repeat hundreds of times and compile uncertainty in the output with an appropriate statistic

[2] A.J. Koning et al. (2019) "TENDL: Complete Nuclear Data Library for innovative Nuclear Science and Technology". In: Nuclear Data Sheets 155, 1-55.

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## Current state

- 500 files for 88 nuclides have been produced for 0 K, 300 K, 600K, 900 K and 1200 K temperatures
- Random fission yield files have been included
  - Adopted from TENDL – website
- Scripts for file processing, TALYS/Serpent environment initialization, data visualization etc. have been set up.
- It is now straightforward to propagate data uncertainties through Serpent, although computationally expensive.

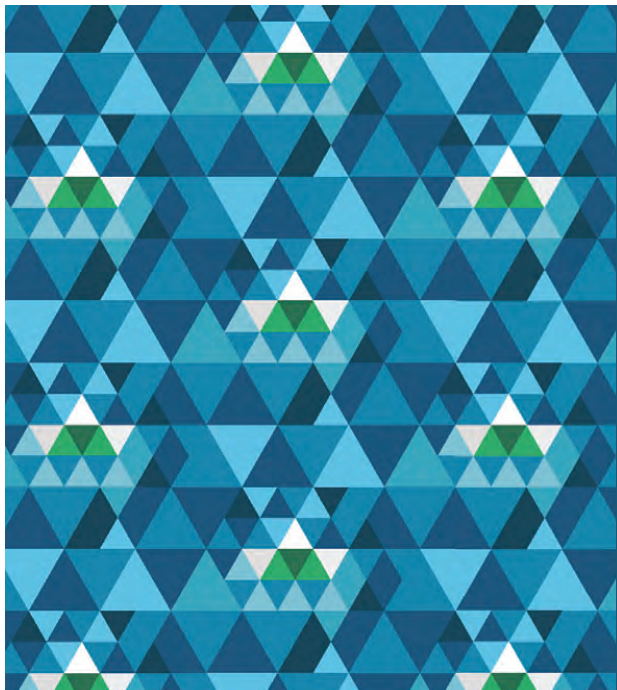
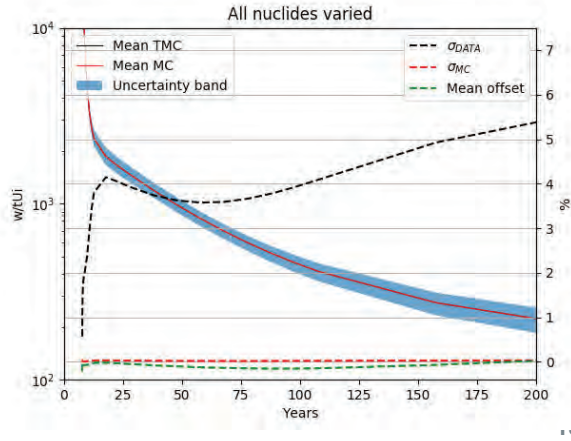
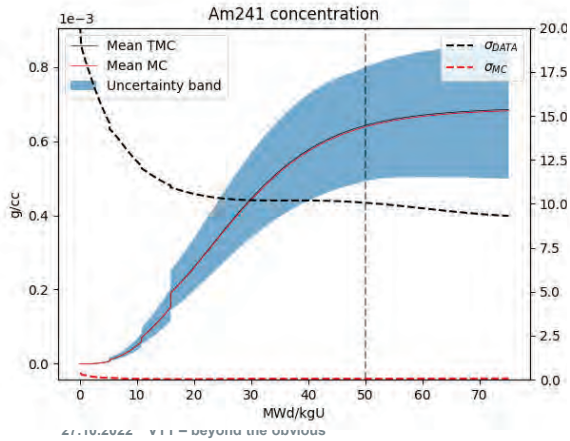
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# Significant Uncertainties in Actinide Concentrations

Uncertainty in decay heat > 3.5 % due to nuclear data when cooling time >15 y



## Key take aways and future work



## Key take aways

- Approximations in power density should be avoided, when dealing with "fresh" SNF (cooling time < 10 y).
- Pin-wise depletion zone division should be used in burnup calculations and Gd pins should be further divided in radial rings.
- DBRC should not be neglected. Use on U isotopes and  $^{239}\text{Pu}$  and  $^{240}\text{Pu}$  is mainly sufficient.
- Significant sources of uncertainty for BWR assembly calculations
  - Nuclear data
  - Burnup
  - (Void fraction and moderator density)
- Using recycled uranium significantly increases decay heat from SNF

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## Future work

- Full libraries and random nuclear data files with T6
- Expanding from 2D assembly calculations to 3D full core
  - Serpent – Ants sequence (Kraken computational framework [3])
- Participation in activities of NEA subgroup on decay heat

[3] Leppänen, J., et al. (2022) "Current Status and On-Going Development of VTT's Kraken Core Physics Computational Framework" *Energies*, 15, 876, <https://doi.org/10.3390/en15030876>.

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## Selected publications

- International Journal publications
  1. Tuominen R., Vallavirta V. (2022). "The Effect of Serpent 2 Calculation Parameters on Evaluated Spent Nuclear Fuel Source Term", Journal of Nuclear Engineering and Radiation Science, 8(4), [044503]. <https://doi.org/10.1115/1.4051444>.
  2. Häkkinen S. (2022). "Impact of Approximations in Operating History Data on Spent Fuel Properties with Serpent 2", Journal of Nuclear Engineering and Radiation Science, 8(4), 041901. [NERS-21-1015]. <https://doi.org/10.1115/1.4051444>.
  3. Jansson P., et al. (2022). "Blind Benchmark Exercise for Spent Nuclear Fuel Decay Heat", Nuclear Science and Engineering, 196, pp.1125-1145. <https://doi.org/10.1080/00295639.2022.2053489>.
  4. Rochman D., et al., "On the estimation of nuclide inventory and decay heat: a review from the EURAD European project", Frontiers in Energy Research. (submitted in 2022).
- Conference articles
  1. Rintala A., "Evaluating the Effect of Decay and Fission Yield Data Uncertainty on Spent Nuclear Fuel Source Term Using Serpent 2", In Proc. 28th International Conference Nuclear Energy for New Europe, Paper No. 602, Portorož, Slovenia, 2019.
  2. Juutilainen P., Häkkinen S., "Impact of Fuel Type and Discharge Burnup on Source Term", In Proc. 28th International Conference Nuclear Energy for New Europe, Paper No. 906, Portorož, Slovenia, 2019.
  3. Rintala A., "Evaluating the Effect of Decay and Fission Yield Data Uncertainty on BWR Spent Nuclear Fuel Source Term", In Proc. 29th International Conference Nuclear Energy for New Europe, Paper No. 1506, Portorož, Slovenia, 2020.
  4. Tuominen R., Vallavirta V., "The Effect of Serpent 2 Calculation Parameters on Evaluated Spent Nuclear Fuel Source Term", In Proc. 29th International Conference Nuclear Energy for New Europe, Paper No. 1503, Portorož, Slovenia, 2020.
  5. Häkkinen S., "Impact of Approximations in Operating History Data on Spent Fuel Properties with Serpent 2", In Proc. 29th International Conference Nuclear Energy for New Europe, Paper No. 1505, Portorož, Slovenia, 2020.
- Research reports
  1. Rintala A., "Evaluating the effect of decay and fission yield data uncertainty on spent nuclear fuel source term using Serpent 2 – continued study", VTT Research Report, VTT-R-00209-20, 2020.
  2. Rintala A., "Separate effect of decay and fission yield data uncertainty on spent nuclear fuel source term", VTT Research Report, VTT-R-00106-21, 2021.
  3. Juutilainen P., "Effect of burnable absorber rods and U-235 enrichment on EPR UO<sub>2</sub> fuel assembly source term with Serpent 2", VTT-R-00242-21, 2021.
  4. Häkkinen S., "Gundremmingen-A assembly B23 sample I2680 depletion calculation with Serpent 2", VTT Research Report, VTT-R-00631-21, 2021.
  5. Häkkinen S., "Sensitivity and uncertainty analysis of Gundremmingen-A assembly B23 sample I2680 depletion calculation with Serpent 2", VTT Research Report, VTT-R-00632-21, 2021.
- Thesis
  1. Vaara L., "Nuclear Data Uncertainty Propagation in Total Monte-Carlo Method", M.Sc. Thesis, Aalto University, 2022.
  2. Vaara L., "Impurly-generated impact on the characteristics of spent nuclear fuel", Special Assignment, Aalto University, 2020.

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## Acknowledgements

- This work has received funding from the Finnish Research Programme on Nuclear Waste Management KYT2022.
- This work has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement N°847593.

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# bey<sup>o</sup>nd

## the obvious

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27/10/2022

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**4.6 Rossi-Alpha distribution analysis of DDSI data for spent nuclear fuel investigation; V. Solans, UU; Symposium on International Safeguards: Reflecting on the Past and Anticipating the Future; 31/10-04/11/2022**

**ABSTRACT**

- Aim: Predict burnup (BU) and initial enrichment (IE) from differential die-away self-interrogation (DDSI) instrument response
- Fit a double exponential fit to the Rossi-alpha distribution (RAD), describing neutrons detected in coincidence, for both simulated and experimental data
- Enhance prediction using a polynomial fit between predicted values and operator data

**INTRODUCTION**

- Safety, operational and safeguards parameters need to be verified with NDA measurements.
- The differential die-away self-interrogation (DDSI) instrument is a passive neutron measurement technique
- Investigate if a double exponential fit to the RAD (Fig 1) can provide additional information about the fuel compared to a single exponential fit

$$RAD_{double}(t) = A_{fast} \cdot \exp(-\tau_{fast} t) + A_{slow} \cdot \exp(-\tau_{slow} t)$$

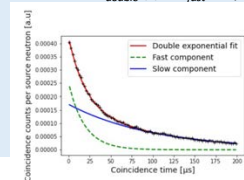


Fig 1. RAD for a simulated PWR SNF having BU= 10 Gwd/tHM, IE= 1.5% and CT= 50 y

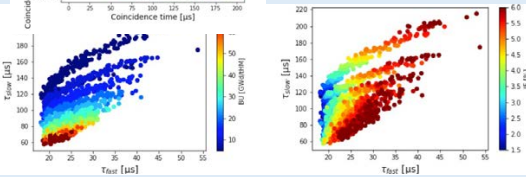


Fig 2.  $\tau_{fast}$  and  $\tau_{slow}$  depending on the BU (left) and IE (right) for the simulated dataset.

# Rossi-Alpha distribution analysis of DDSI data for spent nuclear fuel investigation

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 virginie.solans@physics.uu.se  
 S. Grape (UU), H. Sjöstrand (UU), E. Branger (UU), P. Schillebeeckx (JRC), A. Borella (SCK CEN), R. Rossa (SCK CEN), A. Sjöland (SKB)

**DESCRIPTION OF THE DATA**

**SIMULATED DATASET**

- 2536 samples of 17x17 PWR fuel, obtained with Serpent 2 and MCNP BU: (5 to 70 Gwd/tHM), IE: (1.5% to 6%), CT: (0 to 70 y)

**EXPERIMENTAL DATASET**

- 20 PWR 17x17 SNFs from the SKB-50 fuel set, irradiated in Swedish reactors
- BU: (19 to 48 Gwd/tHM), IE: (2.1 % to 3.94%), CT: (6.3 to 30.4 y).

**COMPARING DATASETS**

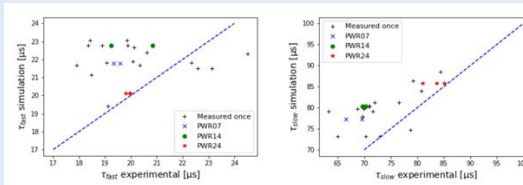


Fig 3.  $\tau_{fast}$  (left) and  $\tau_{slow}$  (right) calculated from the simulated and experimental data. The dashed line is the unity line.

**RESULTS**

**PREDICTING MODEL**

- kNN trained on simulated data, tested on simulated and experimental data using 10-fold cross validation
- Correcting for bias in experimental predictions (which is due to the fuels being fully depleted) using a calibration (Fig. 4) improves the prediction capability.

RMSE for predictions with	BU [Gwd/tHM]	IE [%]
Simulated data	4.51	0.284
Experimental data	11.86	0.963
Experimental data and calibration	2.65	0.324
Simulated data and calibration	2.69	0.104

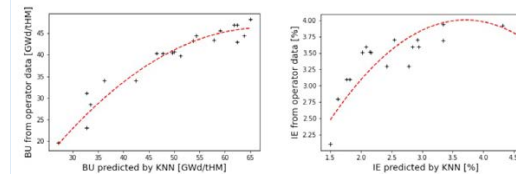


Fig 4. Operator declared BU (left) and IE (right) versus kNN predicted quantities. The red curve is a polynomial fit of degree 2.

**CONCLUSION**

- It is possible to predict BU and IE using a double exponential fit on the Rossi-alpha distribution.

**ACKNOWLEDGEMENTS**

The project leading to this poster presentation has received funding from the European Union's Horizon 2020 research and innovation program under grant agreement No 847593.



## 5. Participation to a Workshop

- Fuel properties characterisation and related uncertainty analysis (EURAD/SFC/Task 2); P. Schillebeeckx, JRC Geel; Spent Fuel Workshop 2019, Ghent, Belgium; 15/11/2019
- Fuel properties characterisation and related uncertainty analysis; P. Schillebeeckx, JRC Geel; ESARDA Final Disposal Working Group Meeting, SCK CEN, Mol; 06 - 07/02/2020
- Predicting the Bias in Calculations of Spent Nuclear Fuel Characteristics; A. Shama, NAGRA; Workshop on Machine Learning in Nuclear Science and Technology, Madrid, Spain (online); 27/05/2021
- Chemical and spectroscopic investigations on the distribution of radionuclides in fuel-cladding interfaces of irradiated high burn-up UOX and MOX fuels; R. Dagan, T. König et al., KIT; Safety of Extended Dry Storage; 01 – 03/06/2022
- Experimentelle und numerische Bestimmungen des Radionuklidinventars von abgebrannten Kernbrennstoffen als eine Grundlage für die vorläufige Sicherheitsuntersuchung (vSU); R. Dagan, T. König et al., KIT; Tage der Standortauswahl; 08 - 10/06/2022
- Passive gamma and neutron measurements for characterization of spent nuclear fuel; V. Solans, UU; 31th Spent Fuel Workshop; 19 – 21/10/2022
- Characterisation of spent nuclear fuel for a typical PWR; G. Žerovnik, JSI; 31th Spent Fuel Workshop; 19 – 21/10/2022
- Impact of Some 3-D Modelling Effects on the Spent Fuel Characterization; ; 31th Spent Fuel Workshop; 19 – 21/10/2022
- Burnup credit application in CONSTOR SNF cask criticality analysis for RBMK-1500 fuel; R.Plukiene, FTMC; 31th Spent Fuel Workshop; 19 – 21/10/2022

**5.1 Fuel properties characterisation and related uncertainty analysis (EURAD/SFC/Task 2); P. Schillebeeckx, JRC Geel; Spent Fuel Workshop 2019, Ghent, Belgium; 15/11/2019**



## Task 2: Fuel properties characterisation and related uncertainty analysis

Volker Metz	KIT
Dimitri Rochman	PSI
Peter Schillebeeckx	JRC Geel
Marcus Seidl	PEL
Marc Verwerft	SCK•CEN

### Participants:

CIEMAT, CPST, CTU (SURAO), ENRESA, ENUSA, JRC, JSI, KIT, LEI, NAGRA, PEL, PSI, SCK•CEN, SKB, SSTC, NRS, TUS, VTT, UU

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## SFC: Spent Fuel Characterization and Evolution Until Disposal

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- Task 1: S/T coordination, state-of-the-art and training material
- **Task 2: Fuel properties characterisation and related uncertainty analysis**
- Task 3: Behaviour of nuclear fuel and cladding after discharge
- Task 4: Accident scenario and consequence analysis
- Task 5: Civil Society interaction

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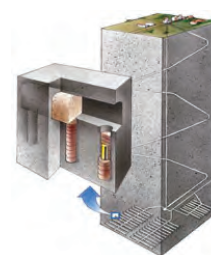
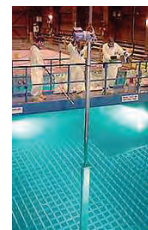




## Spent Nuclear Fuel (SNF) intermediate storage or final disposal

A **safe, secure, ecological** and **economic** transport, storage and final disposal requires that **SNF is characterised** for the main source terms of interest:

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity : R
- Fissile material : Nuclear Safeguards  
i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- Specific nuclides : Long term safety  
e.g.  $^{14}\text{C}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$

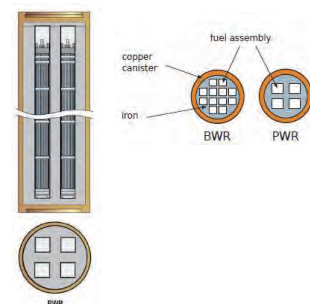


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## Characterisation of SNF

Main **source terms** of interest:

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ , Fission Products (BUC)
- Fissile material :  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- Long-term safety : e.g.  $^{14}\text{C}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$



difficult to be measured directly, in particular during industrial operation

- Decay heat by calorimetry at CLAB: accurate but long measurement times
- Criticality safety analysis: calculations required to account for burn-up credit (MA, FP)

⇒ **Determined/estimated by theoretical calculations** using a burnup code  
Neutron transport + depletion/creation code (see L. Fiorito)



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### e.g. decay heat of SNF

Decay heat rate:  $H(t) = \sum_j H_j(t)$

- $H_j(t)$  : contribution of radionuclide j

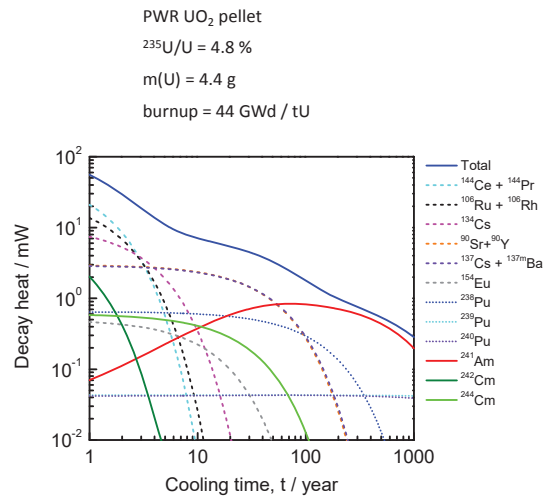
$H_j(t) = h_j N_j(t)$

- $h_j$  : specific decay heat rate of nuclide j
- $N_j(t)$  : number of nuclei of nuclide j at time t

- $N_j(t = t_0)$  known at  $t = t_0$  (after irradiation)

- $N_j(t > t_0)$  can be predicted accurately
- $N_j(t) = N_j(t_0) e^{-\lambda_j (t-t_0)}$

⇒ accurate nuclide vector  $N_j(t_0)$  at  $t_0$  is required from burn-up codes



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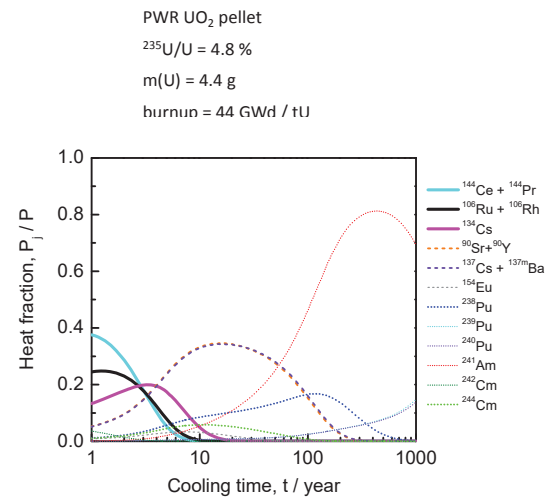
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## Task 2: Fuel properties characterisation and related uncertainty analysis

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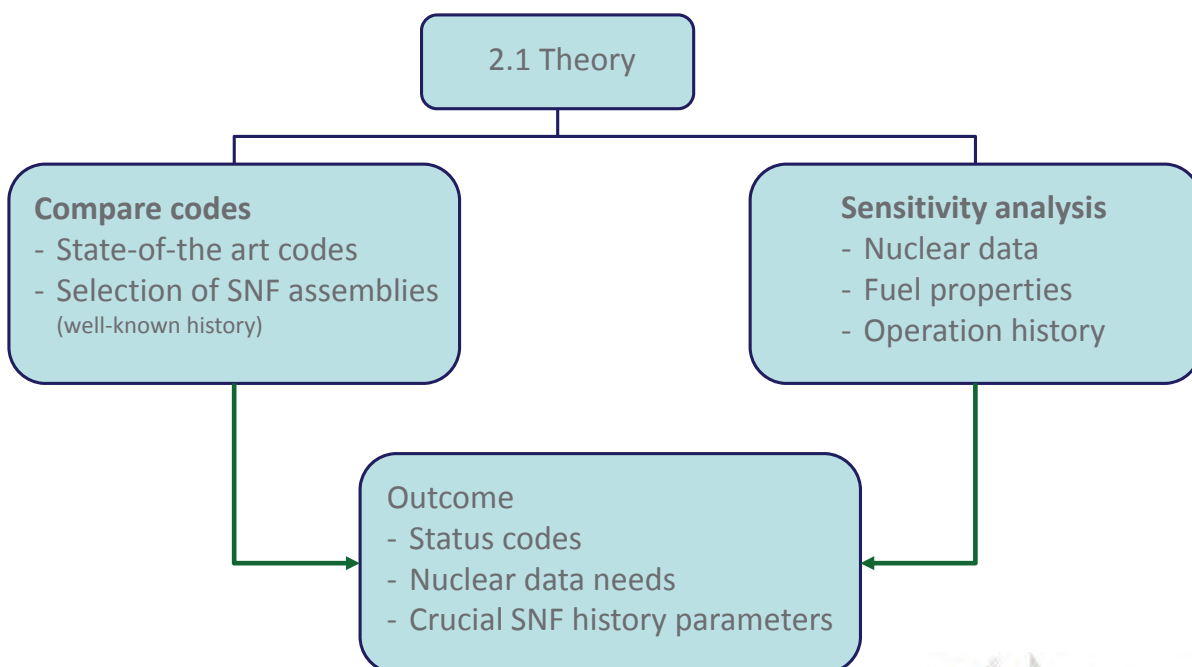
- **Subtask 2.1 (Theory)** co-ordinator PSI  
Theoretical study of SNF source terms (assess and improve performance)
- **Subtask 2.2 (NDA)** co-ordinator SCK•CEN  
Develop, improve and demonstrate NDA methods/systems for SNF characterisation
- **Subtask 2.3 (Cladding)** co-ordinator KIT  
Calculate and determine experimentally the inventory of activation and fission products in cladding material
- **Subtask 2.4 (Final procedures)** co-ordinator KIT (PEL)  
Define and verify procedures to determine the source terms of SNF with realistic confidence limits

SNF-Task 2, SKB (07/08/2019)



### Subtask 2.1: Theoretical study of SNF source term

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## Subtask 2.1 – Code comparison

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- NAGRA : SCALE
- JSI : SCALE, DRAGON, (MCNP/FISPACT)
- PSI : CASMO
- VTT : SERPENT
- JRC Geel : SERPENT
- CIEMAT : MCNP/ACAB
- SCK•CEN : MCNP/ALEPH-2

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## Subtask 2.1 – SNF assemblies for code comparison

---

- **3 PWR assemblies**
  - SF95-5 from the Takahama-3 reactor (UO<sub>2</sub> assembly, 30 MWd/kgU, 2 cycles, 4.1 %). Details in **SFCOMPO**
  - BM1 from the ARIANE campaign (MOX assembly, 45-47 MWd/kgU, 5 cycles, 4.2 % fissile). Details in **ARIANE** public report
  - GU1 from the ARIANE campaign (UO<sub>2</sub> assembly, 60 MWd/kgU, 4 cycles, 3.5 %). Details in **ARIANE** public report
- **2 BWR assemblies**
  - KLU1 from the MALIBU campaign (UO<sub>2</sub> assembly, 60 MWd/kgU, 7 cycles, 3.9 %). Details **publicly available** 01/2020
  - Gundremmingen-7 sample (UO<sub>2</sub>, 25 MWd/kgU, 4 cycles, 2.5 %). Details in **SFCOMPO**
- **Subtask 2.2**
  - ENRESA (BWR)
  - **SKB-50** campaign + blind test SKB: 2 PWR assemblies
  - **Reference pellet (REGAL)** (PWR UO<sub>2</sub>, 4.25 %, 50 MWd / kgU)

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## Subtask 2.1: Sensitivity and covariance analysis

- **Nuclear data**
  - Cross sections
  - Fission yields
  - Decay data (emission probabilities, recoverable energy per reaction/decay)
- **Fuel properties: geometry and material data**
  - Initial enrichment
  - ...
- **Operational history**
  - Burn-up
  - Cooling time
  - Influence of neighbouring assemblies
  - Albedo boundary conditions
  - ...
- **Computational**
  - Method (stochastic/deterministic)
  - Model (2D/3D, boundary conditions, etc.)
  - Numerical approximations (depletion time steps, depletion zones, etc.)

⇒ Recommendations for improvement and realistic uncertainty limits

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## Sensitivity analysis: e.g. <sup>242</sup>, <sup>244</sup>Cm production in MOX

- MOX, Borella et al. MC 2017, Jeju, Korea

- PWR: 17 x 17
- Single pin model

$$S_{N\sigma} = \frac{\partial N/N}{\partial \sigma/\sigma}$$

- Production :  $\sigma(n,\gamma)$

- <sup>242</sup>Cm : 2.5 %      <sup>241</sup>Am(n,γ), <sup>242m</sup>Am(n,γ)
- <sup>244</sup>Cm : 10 %      <sup>242</sup>Pu(n,γ), <sup>243</sup>Am(n,γ)

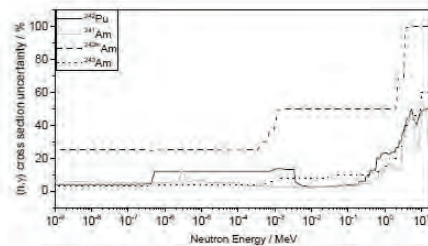
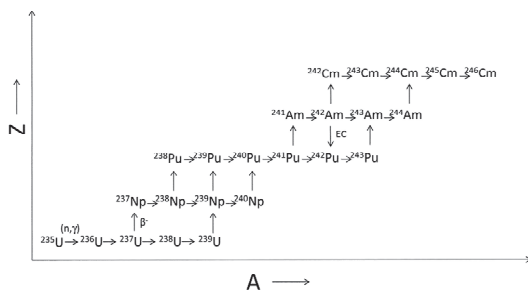


Fig. 4. Relative uncertainties of some of the considered radiative capture cross sections.

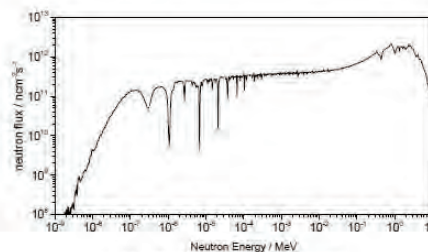
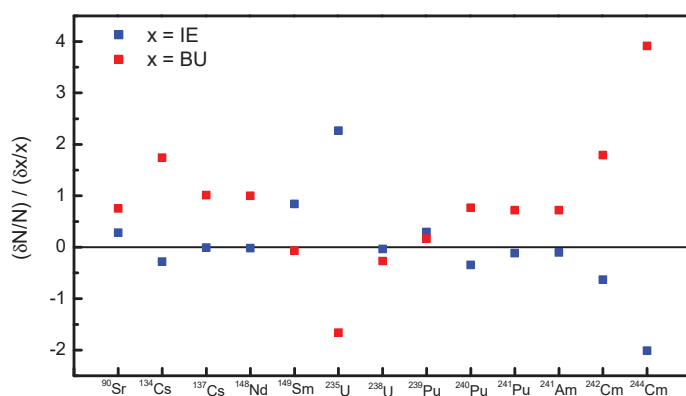


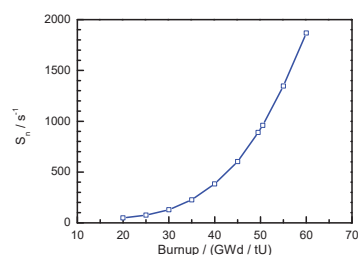
Fig. 5. Neutron flux spectrum in the studied model.



## Sensitivity analysis: initial enrichment and burnup

PWR UO<sub>2</sub><sup>235</sup>U/U = 4.8 %

burnup = 50 MWd/kgU



### Subtask 2.2: NDA methods/systems for SNF characterisation

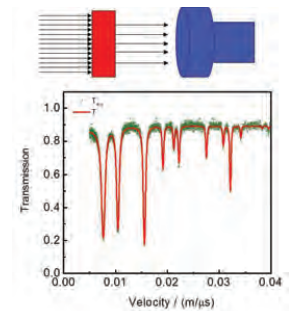
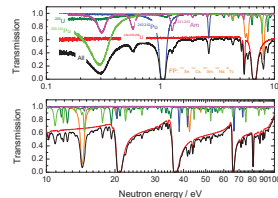
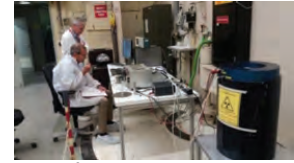
- **Innovative NDA** methods to characterise **small samples**
  - Validate codes (alternative to radiochemical analysis)
  - Production of a reference pellet
- **NDA** methods to characterise **fuel assemblies** (SKB-50)
  - Validate codes
  - Improve theoretical predictions during industrial routine operation
- Study new detectors
  - CLYC, CVD
- *Radiochemical analysis of BWR samples*

⇒ input to 2.1 and 2.4



## NDA methods to characterise small samples

- **Neutron emission rate of a SNF pellet**
  - Non-destructive method to determine  $^{244}\text{Cm}$  content
  - Measurements in conventional controlled area conditions
  - First measurements at SCK•CEN Mol using an existing neutron counter developed and calibrated at JRC finalised
  - Improved/optimised neutron counter under development at JRC Ispra (optimised to apply Hage's point model)
- **Nuclide vector of SNF pellet by NRTA**
  - Non-destructive; no chemical analysis
  - Absolute measurement
  - Measurements at GELINA facility of JRC Geel

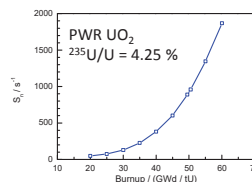
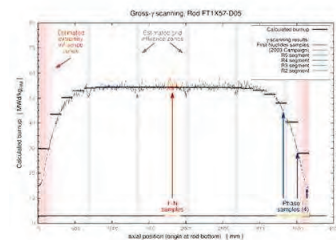
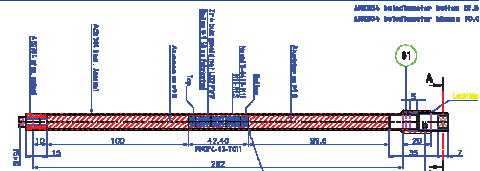


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## Reference spent nuclear fuel pellet

- **Material: REGAL project**
  - Well-known production and irradiation history
  - $\gamma$ -ray scan of fuel pin
  - Neighbouring pellets: analysed by radio-chemistry
- **NDA measurements on reference SNF pellet**
  - $\gamma$ -ray spectroscopy
  - **Neutron emission rate**
  - **NRTA: nuclide inventory (GELINA)**



PWR  $\text{UO}_2$   
 $^{235}\text{U}/\text{U} = 4.25\%$   
 burnup = 50 Gwd / tU

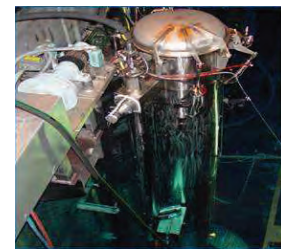
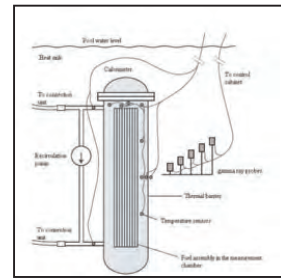
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## Fuel assemblies: calorimeter at CLAB

### Improve and assess performance of calorimeter

- Performance assessment
    - Understand measurement method (analytic model)
    - Dedicated experiments to apply ANOVA and MLE
      - ANOVA : Analysis Of Variance
      - MLE : Maximum Likelihood Estimate (Bayesian approach)
  - Calibration
    - Difference electrical heater  $\leftrightarrow$  nuclear fuel
    - Heat losses due to escaping  $\gamma$ -rays
- $\Rightarrow$  **Reference instrument** for code validation  
(SKB-50 input for 2.1 and 2.4)



$\Rightarrow$  **Objective: decay heat  $\sim$  2%**

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## Fuel assemblies: DDSI and DDA (LANL development, NGS)

### Improve/extend data analysis of DDA and DDSI (part of the SKB-50 project)

- Differential Die Away Self-Interrogation (DDSI, passive) *A.C. Trahan, LA-UR\_16\_20026*

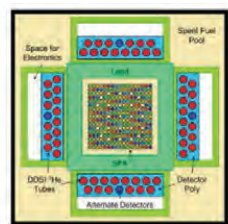
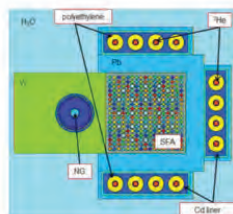


Fig. 1. Cross-sectional view of the simulated DDSI instrument.

- Differential Die Away (DDA, active) *V. Henzl, LANL-UR-123025*



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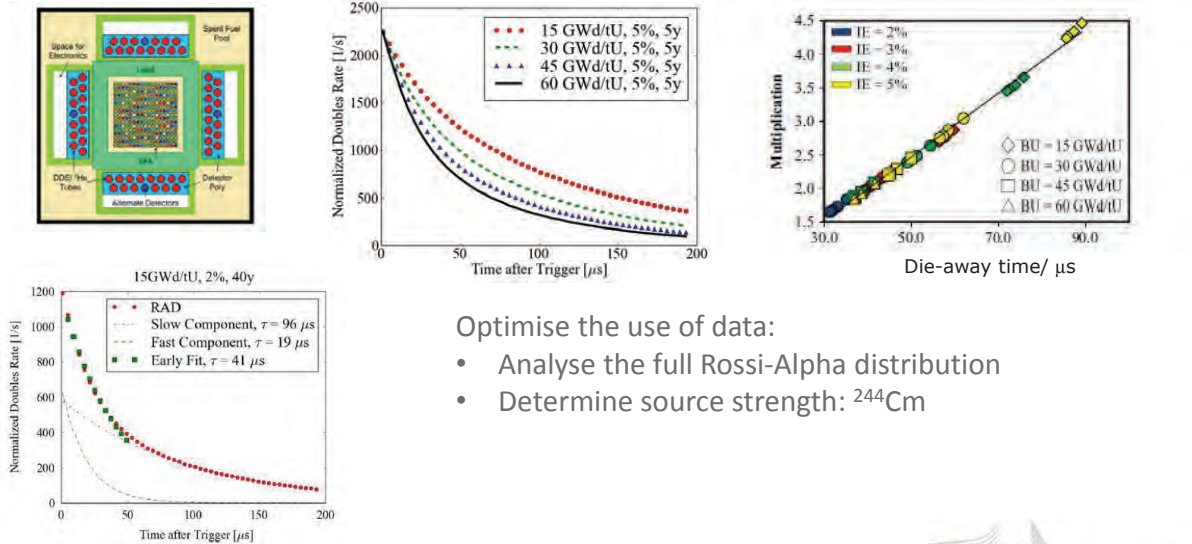




## Fuel assemblies: DDSI and DDA (LANL development)

Improve/extend data analysis of DDA and DDSI

- Differential Die Away Self-Interrogation (DDSI, passive) *A.C. Trahan, LA-UR\_16\_20026*



Optimise the use of data:

- Analyse the full Rossi-Alpha distribution
- Determine source strength:  $^{244}\text{Cm}$

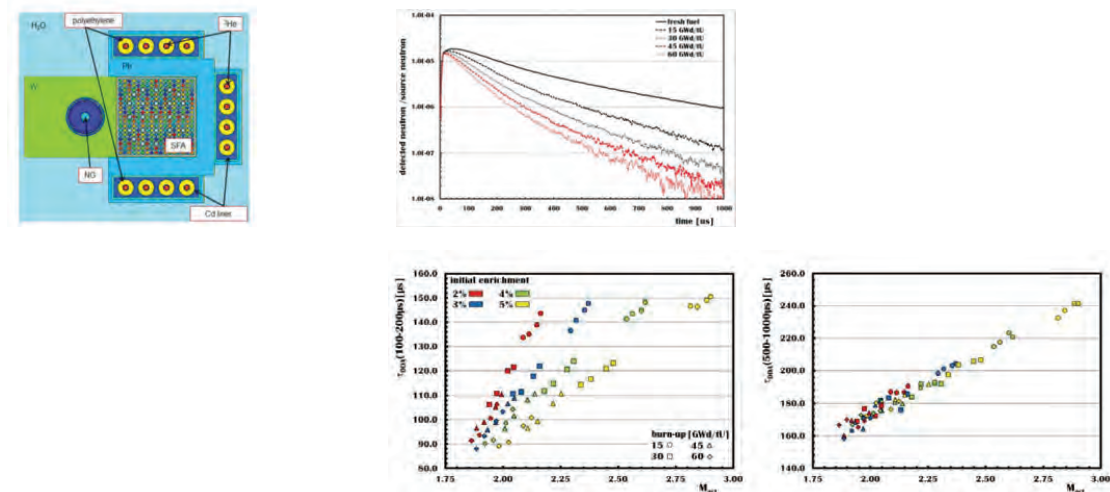
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## Fuel assemblies: DDSI and DDA (LANL development)

Improve/extend data analysis of DDA and DDSI

- Differential Die Away (DDA, active) *V. Henzl, LANL-UR-123025*

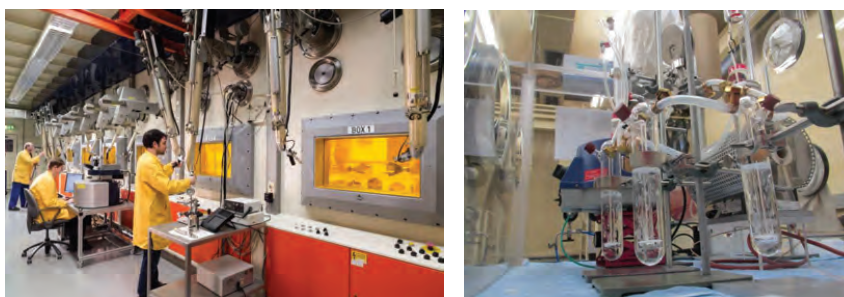


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## Subtask 2.3 – Inventory of activation products and FP in cladding

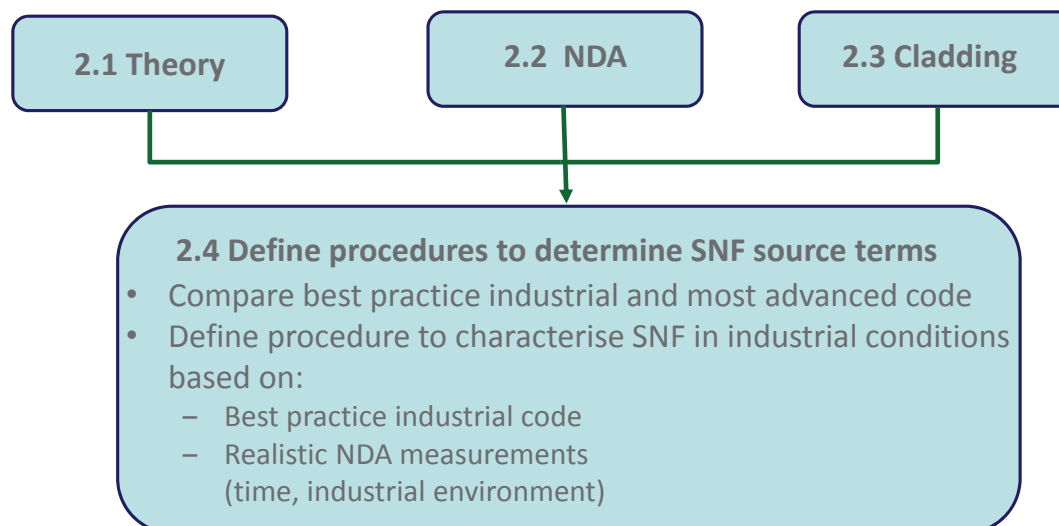
- Preparation of three irradiated samples for further analysis ( 2 types)
  - Cladded pellets of  $\text{UO}_2$  (50 GWd/ $t_{\text{HM}}$ ) and MOX (38 GWd/ $t_{\text{HM}}$ ) irradiated in a PWR
  - Plenum cladding from a  $\text{UO}_2$  (50 GWd/ $t_{\text{HM}}$ ) rod segment irradiated in a PWR
- Experimental determination of nuclide inventory: radiochemical analysis
  - FP +  $^{14}\text{C}$  and  $^{36}\text{Cl}$
- Validate and improve theoretical calculations of nuclide inventory



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## Subtask 2.4: Final objective



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## Thank you for the attention

- EURAD project (SNF characterisation)
  - PhD position at Uppsala University  
<https://www.uu.se/en/about-uu/join-us/details/?positionId=300024>
  - NUGENIA  
<http://nugenia.org/call-for-mobility-grants-open/>



**5.2 Fuel properties characterisation and related uncertainty analysis; P. Schillebeeckx, JRC Geel; ESARDA Final Disposal Working Group Meeting, SCK CEN, Mol; 06 - 07/02/2020**



## Task 2: Fuel properties characterisation and related uncertainty analysis

Ron Dagan	KIT
Dimitri Rochman	PSI
Peter Schillebeeckx	<b>JRC Geel (co-ordinator)</b>
Marcus Seidl	PEL
Marc Verwerft	SCK•CEN

### Partners:

CIEMAT, CPST, CTU (SURAO), ENRESA, ENUSA, JRC, JSI, KIT, LEI, NAGRA, PEL, PSI, SCK•CEN, SKB, SSTC NRS, TUS, VTT, UU

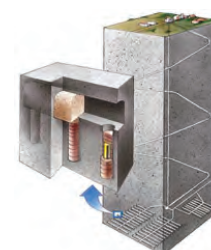
ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



## Spent Nuclear Fuel (SNF) intermediate storage or final disposal

A **safe, secure, economic** and **ecological** transport, storage and final disposal requires that **SNF is characterised** for the main source terms of interest:

- Decay heat
- Neutron emission
- $\gamma$ -ray emission
- **Reactivity** (burnup credit)  
nuclides with high neutron absorption cross section)
- **Fissile material (Safeguards)**  
i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- **Specific long-lived radionuclides (Long term safety)**  
e.g.  $^{14}\text{C}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

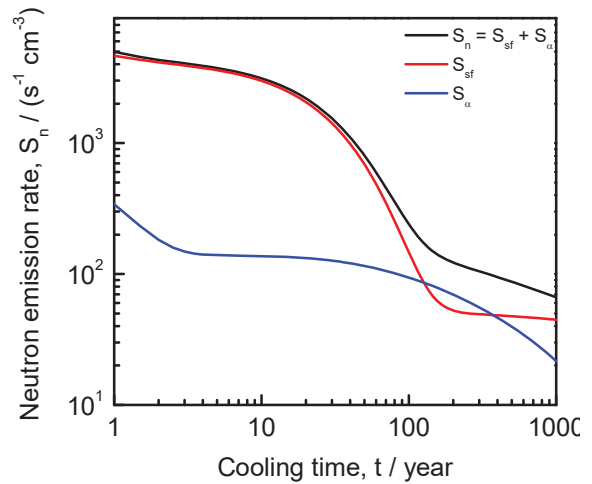


## Neutron emission by SNF

$$S_n(t) = \sum_k S_{n,k}(t)$$

- $S_{n,k}(t)$  : contribution of radionuclide k
- $S_{n,k}(t) = (s_{sf,k} + s_{\alpha n,k}) N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $s_{sf,k}$  : specific neutron emission rate of nuclide k due to sf
  - $s_{\alpha,k}$  : specific neutron emission rate of nuclide k due to  $(\alpha,n)$  reactions

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/t



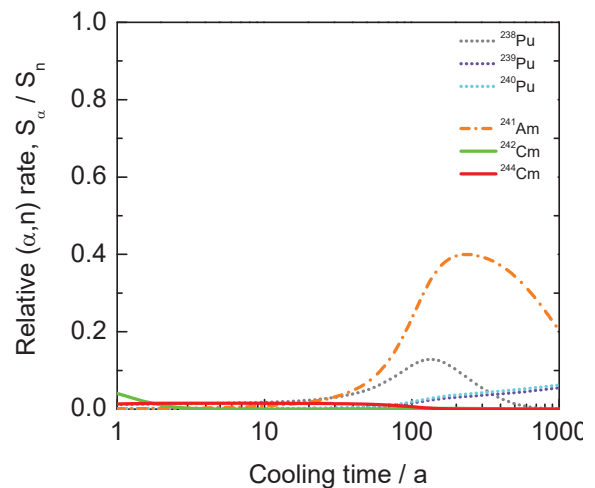
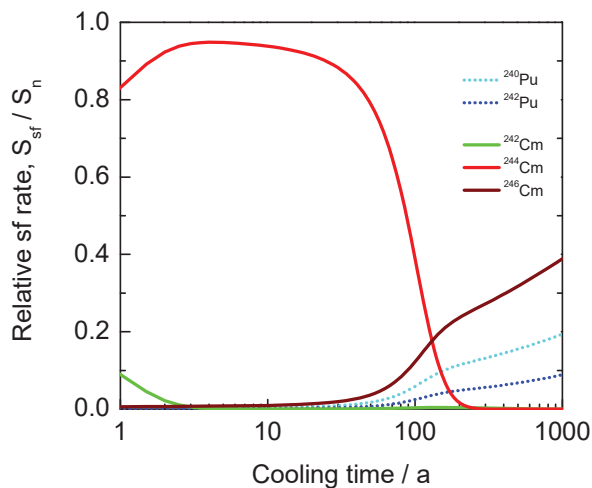
ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



## Neutron emission by SNF

$$S_n(t) = \sum_k (s_{sf,k} + s_{\alpha n,k}) N_k(t)$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/t



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

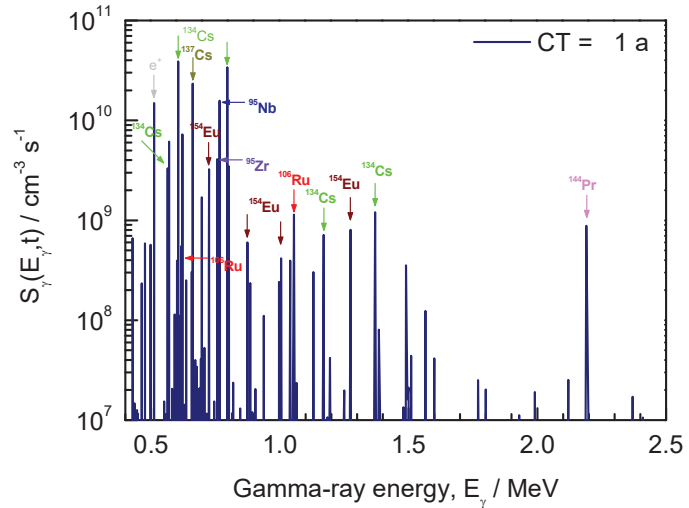


## Gamma-ray emission by SNF

$$S_\gamma(t) = \sum_k S_{\gamma,k}(E_\gamma, t)$$

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/t



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

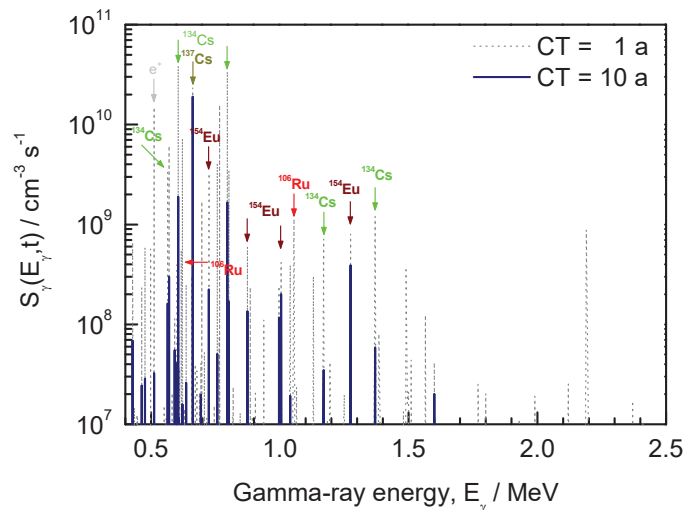


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ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



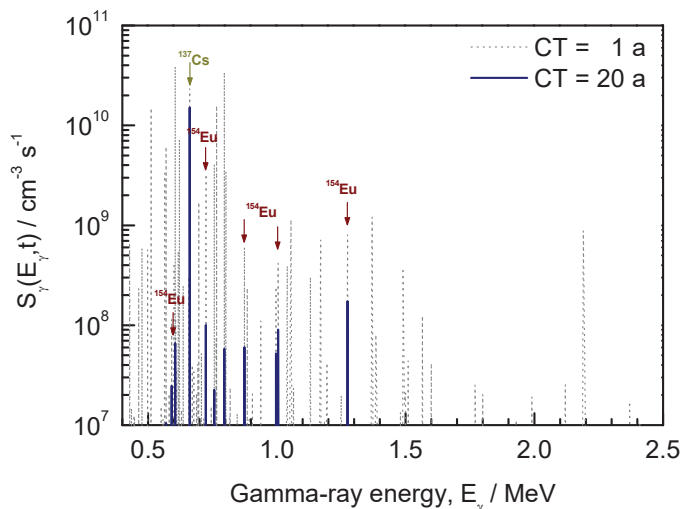


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 burnup = 44 GWd/t



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

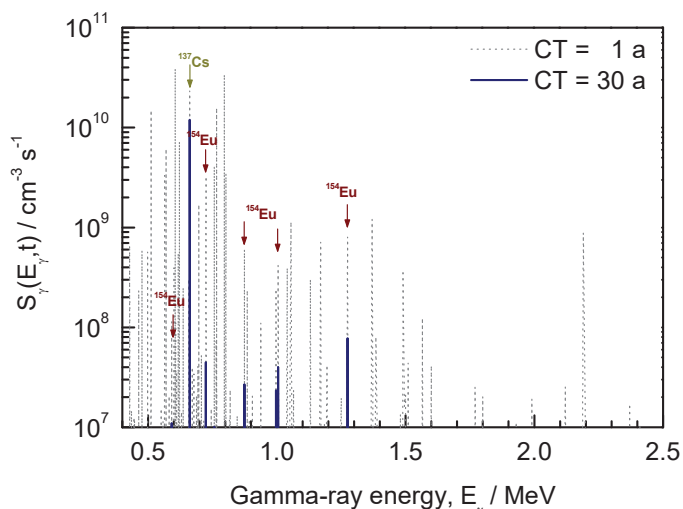


### Gamma-ray emission by SNF

$$S_{\gamma}(t) = \sum_k S_{\gamma,k}(E_{\gamma}, t)$$

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	<b>8.8 a</b>
<sup>137</sup> Cs/ <sup>137m</sup> Ba	<b>30.0 a</b>

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/t



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

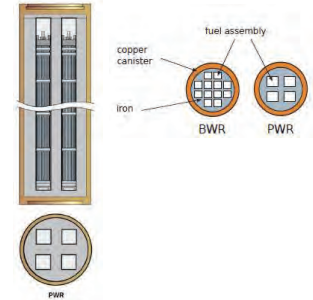




## Characterisation of SNF

### Main source terms of interest:

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity :  $^{235}\text{U}, ^{239}\text{Pu}, ^{241}\text{Am}, \text{Fission Products (BUC)}$
- Fissile material :  $^{235}\text{U}, ^{239}\text{Pu}$
- Long-term safety : e.g.  $^{14}\text{C}, ^{79}\text{Se}, ^{94}\text{Nb}, ^{99}\text{Tc}, ^{129}\text{I}, ^{226}\text{Ra}$



### Contributions of nuclides with different characteristics

Difficult to be measured directly, in particular during industrial operation

e.g. decay heat by calorimetry at CLAB: accurate but long measurement times

⇒ Estimated by **theoretical calculations** using a burnup code

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$(N_k(t_0), k = 1, \dots, n)$ : by theoretical calculations

### Coupled neutron transport – nuclide depletion/creation calculation

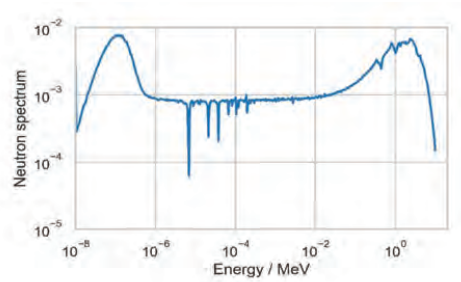
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

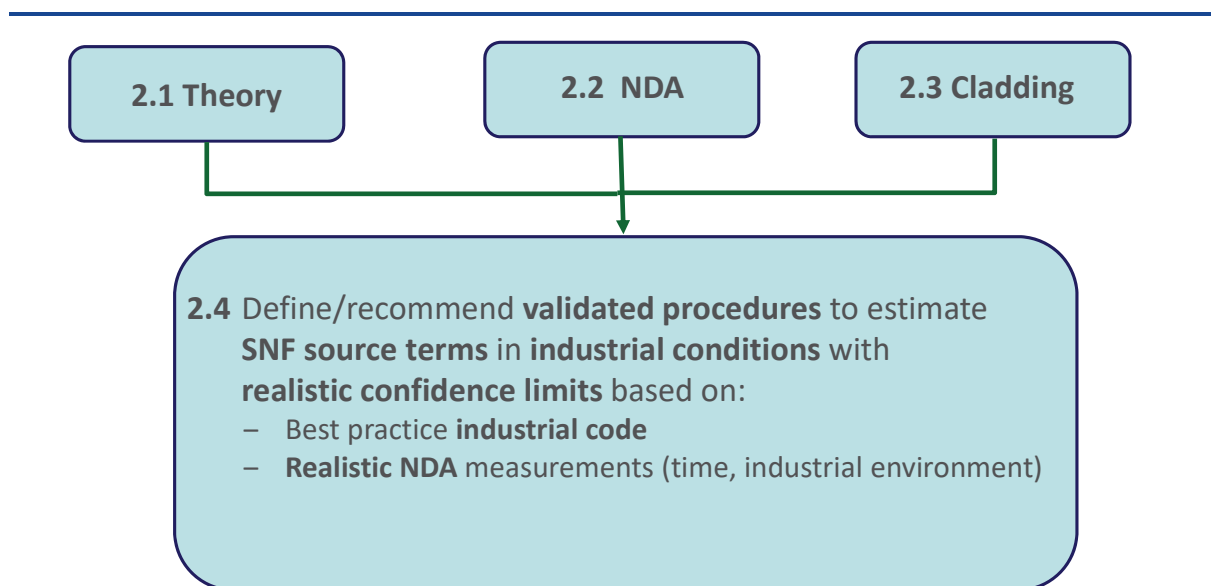
Update nuclide vector



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## SFC – Task 2 (structure)



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



## SFC- Task 2: Code comparison

- CIEMAT : EVOLCODE (MCNP)
- JRC Geel : SERPENT, SCALE
- JSI : SCALE, DRAGON
- KIT : MCNP-CINDER
- NAGRA : SCALE
- PSI : CASMO
- SCK CEN : ALEPH-2 (MCNP)
- VTT : SERPENT

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## Sensitivity and Uncertainty (S/U) analysis

• Input data:

– Nuclear Data (ND)

- Cross sections (neutron interactions)
- Fission yields
- Neutron emission probabilities
- Decay data

– Fuel History (FH)

- Fuel properties (design, composition) e.g. Initial enrichment (IE)
- Reactor operation and irradiation conditions e.g. Burnup (BU)
- Cooling time (CT)

BurnUp (BU):  
 time integrated power per mass of initial fuel (MWd/kg)  
 $\propto$  total number of fission  $\times$  energy per fission event

• Computational

- Method: stochastic/deterministic
- Model (2D/3D, boundary conditions, ...)
- Numerical approximations (depletion time steps, depletion zones, ...)

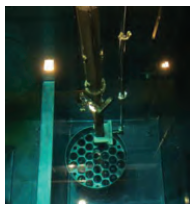
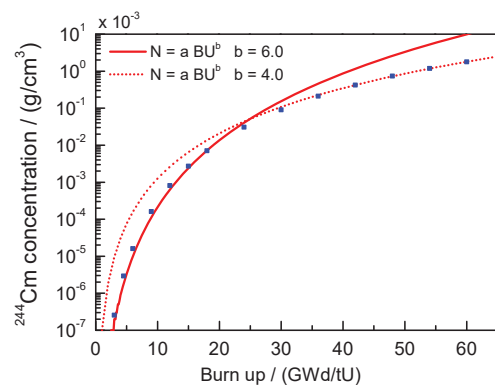
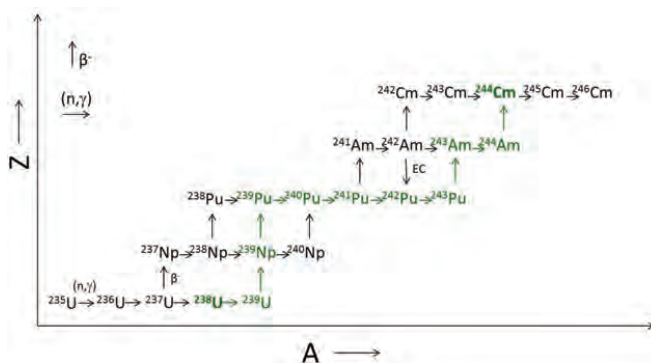
ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



### S/U analysis: <sup>244</sup>Cm production

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

$N = aBU^b$   
 $b = 6$  for BU < 20 GWd/t



$\Rightarrow$  <sup>244</sup>Cm : burnup indicator  
 $\Rightarrow$  Neutron emission rate : burnup indicator

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## S/U analysis: estimation of <sup>244</sup>Cm inventory

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

Ref.	Library	Reactor	Fuel	BU Gwd/t	IE wt%	<sup>244</sup> Cm
Rochman	ENDF/B-VII.0	PWR	UO <sub>2</sub>	10	4.1	18.7 %
	ENDF/B-VII.0	PWR	UO <sub>2</sub>	20	4.1	16.9 %
	ENDF/B-VII.0	PWR	UO <sub>2</sub>	30	4.1	15.5 %
	ENDF/B-VII.0	PWR	UO <sub>2</sub>	40	4.1	14.1 %
Zwermann	SCALE-6.1	PWR	UO <sub>2</sub>	40	4.1	8.5 %
Leary	ENDF/B-VII.1	PWR	UO <sub>2</sub>	54	3.4	9.6 %
Rochman	ENDF/B-VII.1	PWR	UO <sub>2</sub>	54	3.4	9.1 %
Rochman	ENDF/B-VII.1	PWR	UO <sub>2</sub>	40	4.1	9.7 %

<sup>244</sup>Cm inventory prediction production

- uncertainty due to nuclear data : ~10%
- due to <sup>242</sup>Pu(n,γ), <sup>243</sup>Am(n,γ)

⇒ Systematic study for key nuclides

⇒ Improve nuclear data

- Input HPRL NEA/OECD

- Input to SANDA (DG-RTD)

<https://cordis.europa.eu/project/id/847552>  
Supplying Accurate Nuclear Data for energy and non-energy Applications

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## Innovative NDA methods/systems for SNF characterisation

- **Innovative NDA methods to characterise pin segments**
  - **Validate codes** (alternative to radiochemical analysis)
  - Production of a reference pellet
- **NDA methods to characterise fuel assemblies (SKB-50)**
  - Improve theoretical source term predictions during industrial routine operation
  - Improve fuel history data:** e.g. BU
  - Validate codes
- **Study new detectors**
  - CLYC, CVD

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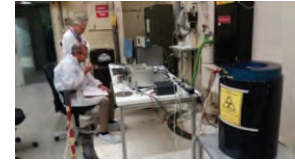


## NDA methods to characterise pin segments

- **Neutron emission rate** of a SNF pin segment

(collaboration SCK CEN – JRC Geel, Ispra)

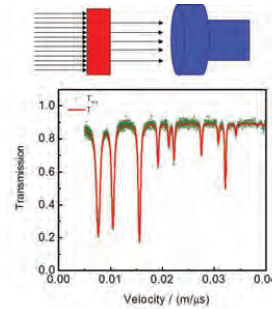
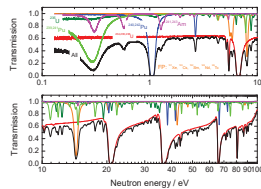
- Non-destructive method to determine  $^{244}\text{Cm}$  content
  - Measurements in conventional controlled area conditions
- Hage's point model, JRC Ispra (B. Pedersen)



- **Nuclide vector** of SNF pin segment by **NRTA**

(collaboration SCK CEN – JRC Geel)

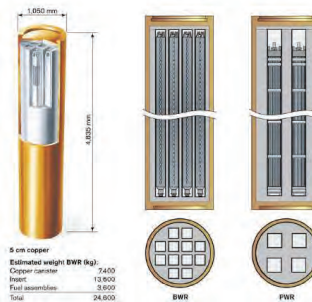
- **Non-destructive**; no chemical analysis
- **Absolute** measurement (no calibration)
- Measurements at **GELINA** facility of JRC Geel



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## Experiments at CLAB: SKB-50



### Installed systems

- Calorimeter
- Gamma-ray spectroscopic scanner

### Testing of advanced systems (LANL)

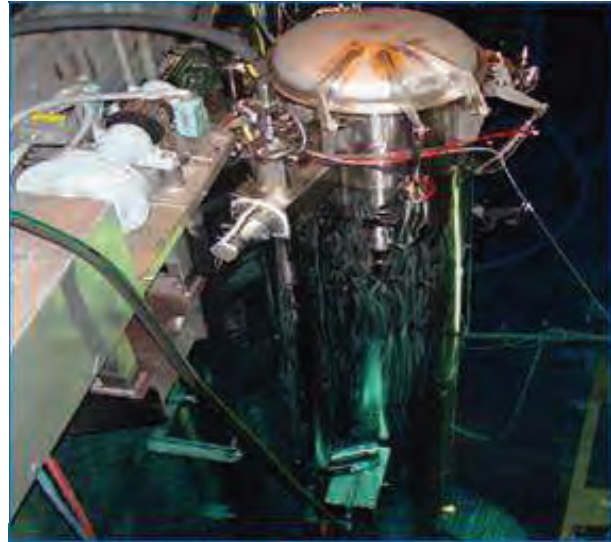
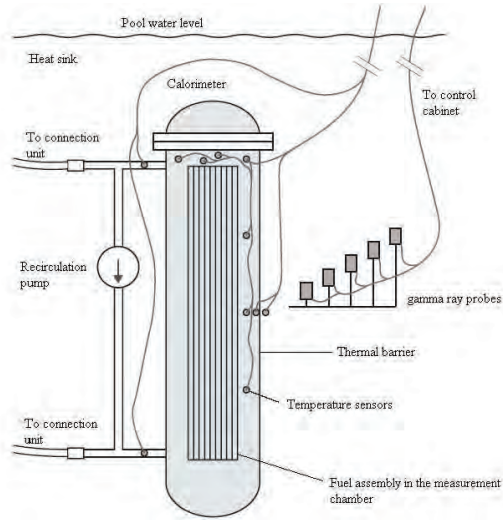
- Differential Die-Away Self-Interrogation (DDSI)
- Differential Die-Away (DDA)



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### Calorimeter at CLAB

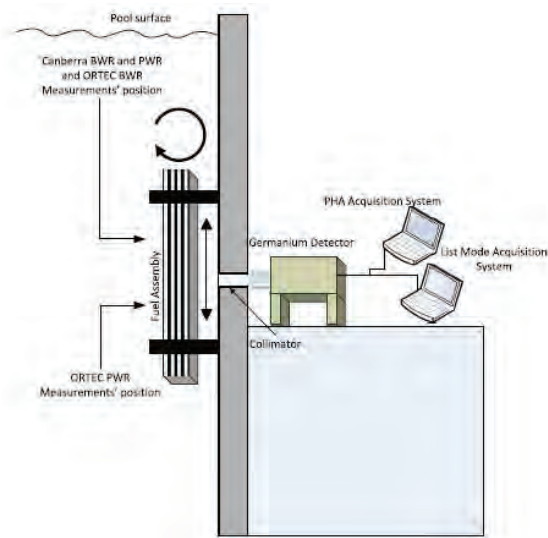


- ⇒ Target value uncertainty  $\leq 2\%$
- ⇒ Reference instrument for decay heat of SNF

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### Gamma-ray spectroscopic scanning system at CLAB



Vaccaro et al. NIMA 830 (2016) 325  $^{134}\text{Cs}$ ,  $^{137}\text{Cs}$ ,  $^{154}\text{Eu}$

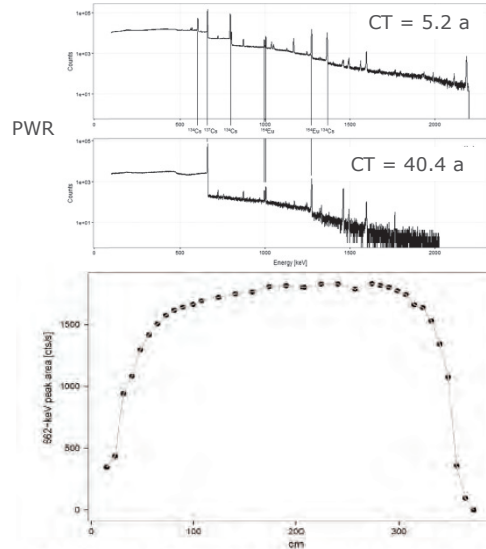


Fig. 8. Count rate for the 662-keV  $^{137}\text{Cs}$  net peak area as a function of axial location along BWRs. These data were measured with the ORTEC GMX detector and Canberra Lynx MCA from the 45° corner. The axial location is specified as downward along the uranium containing portion of the fuel (The indicated absolute positions are accurate to  $\pm 10$  cm, the error bars are much smaller than the data points).

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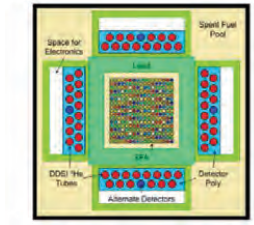




## Fuel assemblies: DDSI and DDA at CLAB (LANL development, NGSi)

- **Differential Die Away Self-Interrogation (DDSI, passive)**

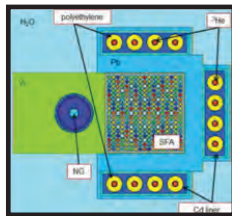
A.C. Trahan, LA-UR\_16\_20026 Kaplan et al., NIMA 764 (2014) 347 - 351



⇒ Optimise data analysis procedures for source term determination (not only safeguards)

- **Differential Die Away (DDA, active)**

V. Henzl, LANL-UR-123025



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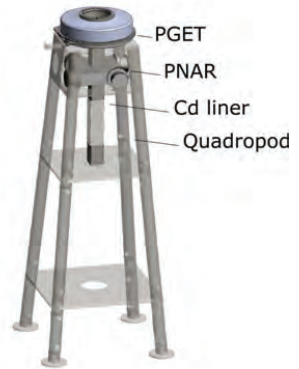
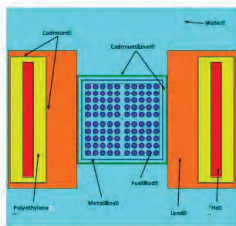


## Fuel assemblies: Finland

- **Passive Neutron Albedo Reactivity (PNAR, NGSi)**

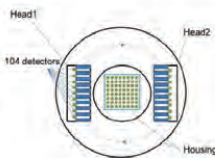
LANL development, Tobin et al., NIMA 897 (2018) 32 - 37

Tobin et al., ESARDA bulletin 56 (2018) 12 - 18



- **Passive Gamma Ray Emission Tomography (PGET)**

IAEA development, Honkamaa et al., Symp. Int. Safeguards, IAEA Vienna 2014



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## EURAD-SFC (4 years project)

---

Define/recommend **validated procedures** to estimate **SNF source terms** (including fissile material) in **industrial conditions** with **realistic confidence limits** based on:

- Best practice **industrial code**
- **Realistic NDA** measurements (time, industrial environment)

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- 
- EURAD project (SNF characterisation)
    - <https://www.ejp-urad.eu/about-urad>
    - NUGENIA, <http://nugenia.org/call-for-mobility-grants-open/>
  - ARIEL  
support for open access, scientific visits, training early researchers, ...
    - [www.ariel-h2020.eu](http://www.ariel-h2020.eu)
  - JRC Geel open access
    - <https://ec.europa.eu/jrc/en/research-facility/open-access>

ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)





**5.3 Predicting the Bias in Calculations of Spent Nuclear Fuel Characteristics; A. Shama, NAGRA; Workshop on Machine Learning in Nuclear Science and Technology, Madrid, Spain (online); 27/05/2021**



Ahmed Shama :: PhD Student (EPFL/LRS, PSI/LRT)

## Predicting the Bias in Calculations of Spent Nuclear Fuel Characteristics

27 May 2021

Workshop on ML in Nuclear Science and Technology Applications



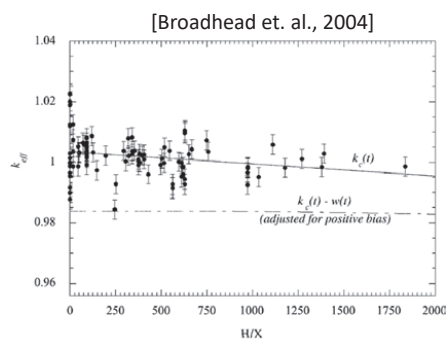
### Background and Motivation

- SNF characterization relies on calculations (measurements are extremely expensive, difficult)
- A question arises: How can we be sure about these calculations?
- Validation is required *a priori*, modelling benchmarks which have their characteristics measured, and comparing calculations to measurements (e.g.,  $C - E$  or  $C/E$ )
  - Limited measurements (e.g., ~300 SNF decay heat measurement worldwide) and actual SNF are ~13,000 SNF in Switzerland alone
  - Benchmarks cover ranges of SNF properties, area-of-applicability (AOA), and realistic SNF calculations usually have different properties
- We need to predict the bias (i.e., predictive modeling), by comparison with validation benchmarks

In criticality safety, methods are established

**ANS-8.17:** Criticality Safety Criteria for the Handling, Storage, and Transportation of LWR Fuel Outside Reactors

**ANS-8.24:** Validation of neutron transport methods for nuclear criticality safety calculations



Seite 2



## Overview of this work

### Research Questions:

- Could the bias be predicted for SNF properties (**decay heat** and **nuclide concentration**) given a set of validation benchmarks?
- What properties would be informative into these predictions?
- What are the assumptions of these predictions?

$$C - E = f(X) + \varepsilon$$

### Hypotheses:

- Bias prediction is based on neutronically similar benchmarks → [Neighborhood-based schemes](#)
- Integral SNF properties, such as spectral index, burnup, and correlations could be informative toward the bias prediction

Seite 3



## Research Steps

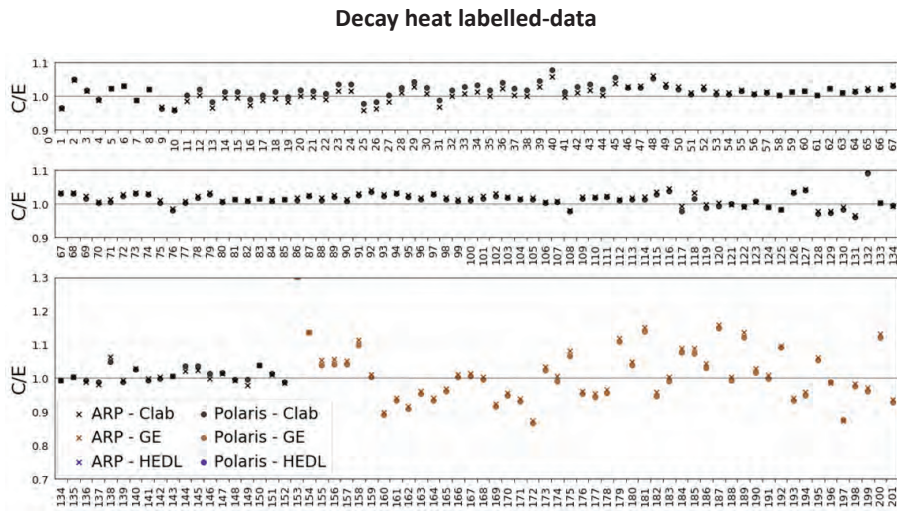
- 1. Collecting data:** SNF validation benchmarks (calculations and measurements)
- 2. Extracting features:** sensitivity analysis and uncertainty propagation
- 3. Application of data-driven techniques (novelty of this work):** Machine Learning models and algorithms

Seite 4



## Research Steps

1. Collecting data: SNF validation benchmarks (calculations and measurements)

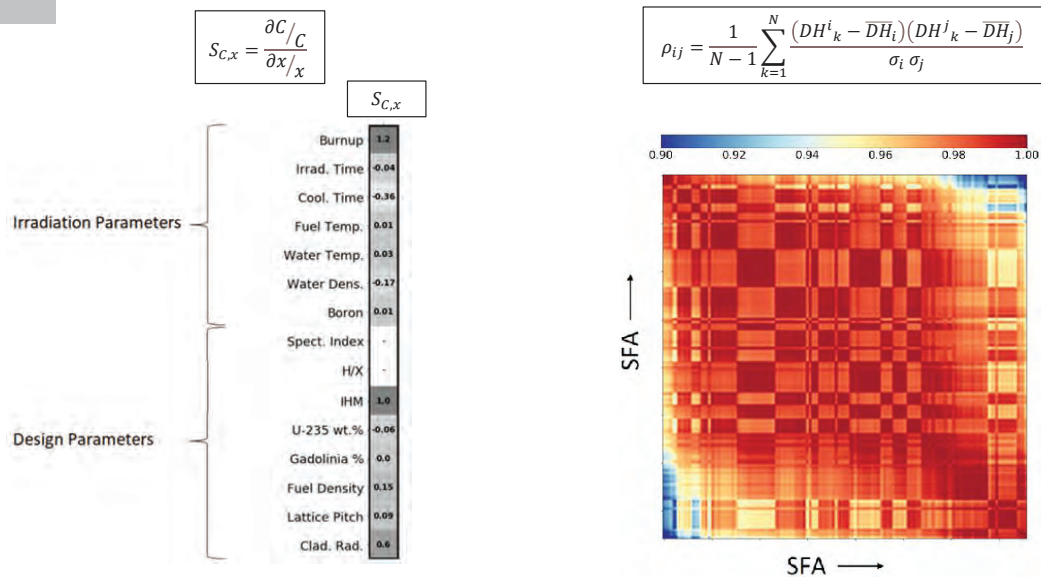


Seite 5



## Research Steps

1. Collecting data: SNF validation benchmarks (calculations and measurements)
2. Extracting features: sensitivity analysis and uncertainty propagation

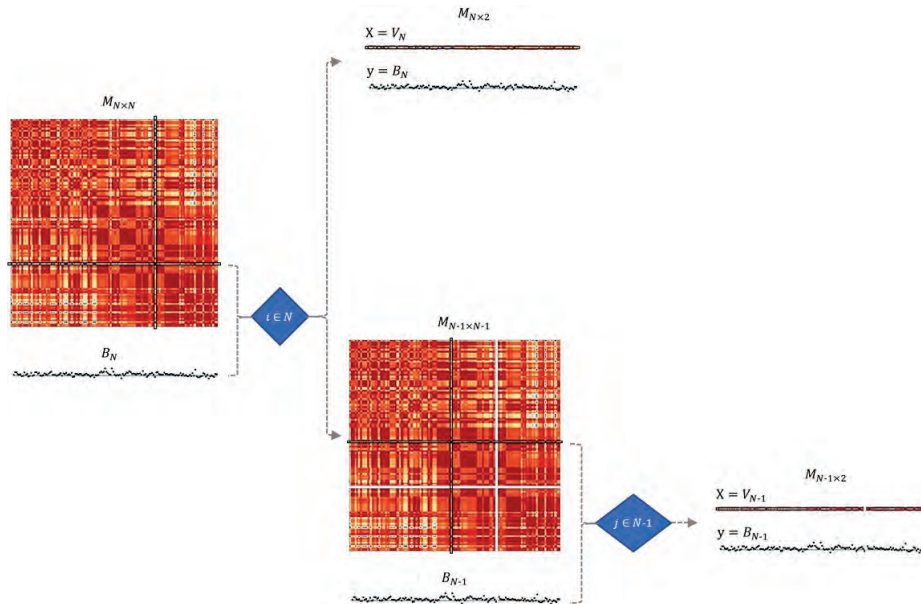


Seite 6



## Research Steps

1. **Collecting data:** SNF validation benchmarks (calculations and measurements)
2. **Extracting features:** sensitivity analysis and uncertainty propagation



Seite 7



## Research Steps

1. **Collecting data:** SNF validation benchmarks (calculations and measurements)
2. **Extracting features:** sensitivity analysis and uncertainty propagation
3. **Application of data-driven techniques (novelty of this work):** Machine Learning models and algorithms

$$C - E = f(X) + \varepsilon$$

### Hypotheses

- Bias prediction is based on neutronically similar benchmarks
- Integral SNF properties, such as spectral index ( $S_I$ ) correlations between benchmarks, could be informative toward the bias predictions

### Linear Model (~ criticality safety)

*LM with cutoffs:*  $B_{(\rho=1)} = I_{\rho > c_0}(\rho)\beta\rho$

### Neighborhood-based Schemes

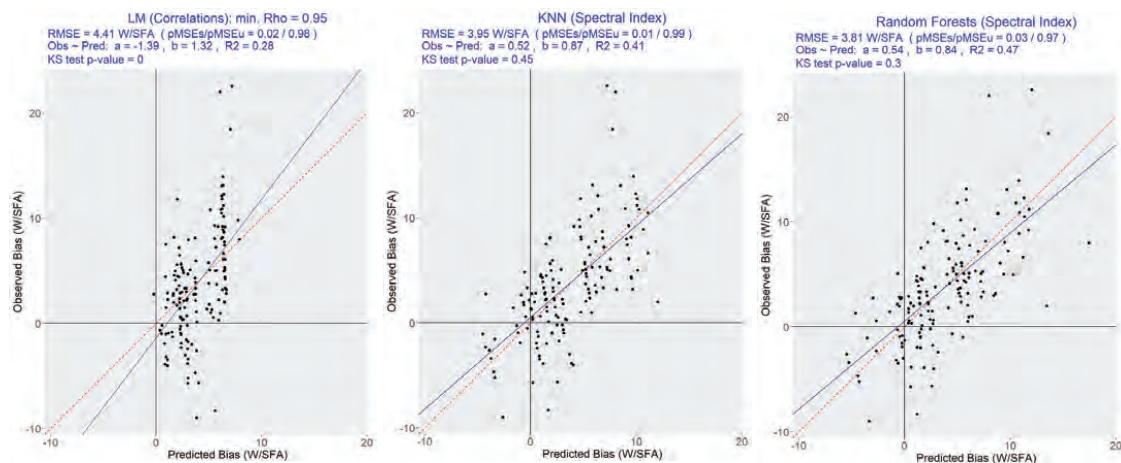
*KKNN:*  $B_{(\rho=1)} = \sum_{k=1}^K w_k B_k$

*RF:*  $B_{(\rho=1)} = \frac{1}{N} \sum_{n=1}^N \left( \sum_{\rho \in [c/0, 1]} w_n B_\rho \right)$

Seite 8

## Results : Decay Heat

- Comparing predictions to observations (Features: SI or Correlations)
- Statistical testing, Kolmogorov–Smirnov test, testing whether model-predicted biases originate from the same distribution as observed ones at  $p$ -value = 0.05



Seite 9

## Summary

- SNF calculations are being validated (i.e., decay heat and nuclide concentration)
- Machine Learning models are being analyzed for their predictive performance, comparing bias model predictions to observed ones
- **We have shown that the bias could be predicted from validation data (benchmarks), meaning we could support activities such as license applications, and decisions on safety margins**
- Neighborhood based schemes (neutronically similar benchmarks) predict biases statistically similar to observed ones
- The models rely only on few SNF features, namely:
  - Spectral index (neutron flux)
  - Correlation between benchmarks
- **Ongoing work:** bias prediction for other quantities, i.e., actinides conc. (U-235 and Pu-239) and a fission product (Cs-137), using also neighborhood-based schemes and SNF features measuring similarities

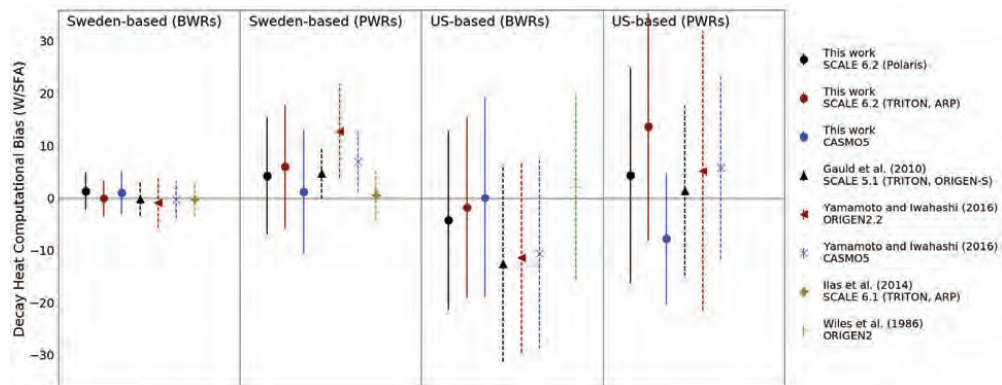
Seite 10





Thanks everyone – do you have questions?

## Appendix : Validation

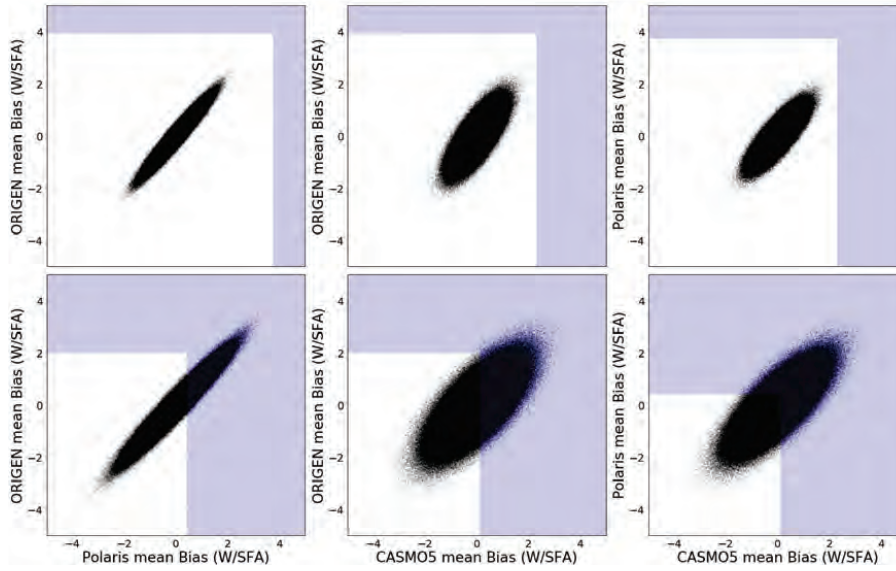




## Appendix : Selecting Benchmarks

$$H_0: C_p \text{ or } C_o \text{ or } C_c = E$$

$$H_a: C_p \text{ and } C_o \text{ and } C_c \neq E$$



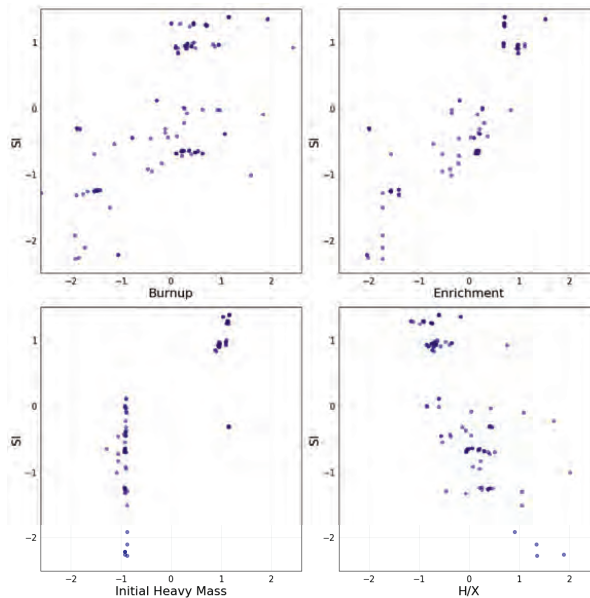
Seite 13



## Appendix : Spectral Index

$$SI_i = \frac{\phi_{E>0.625 \text{ eV}}}{\phi_{total}}$$

$$SI = \frac{\sum_1^n (BU_i \times SI_i)}{\sum_1^n (BU_i)}$$



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## Appendix : Final Models

Table. Test errors of the applied models along with fractions of the explained variances.

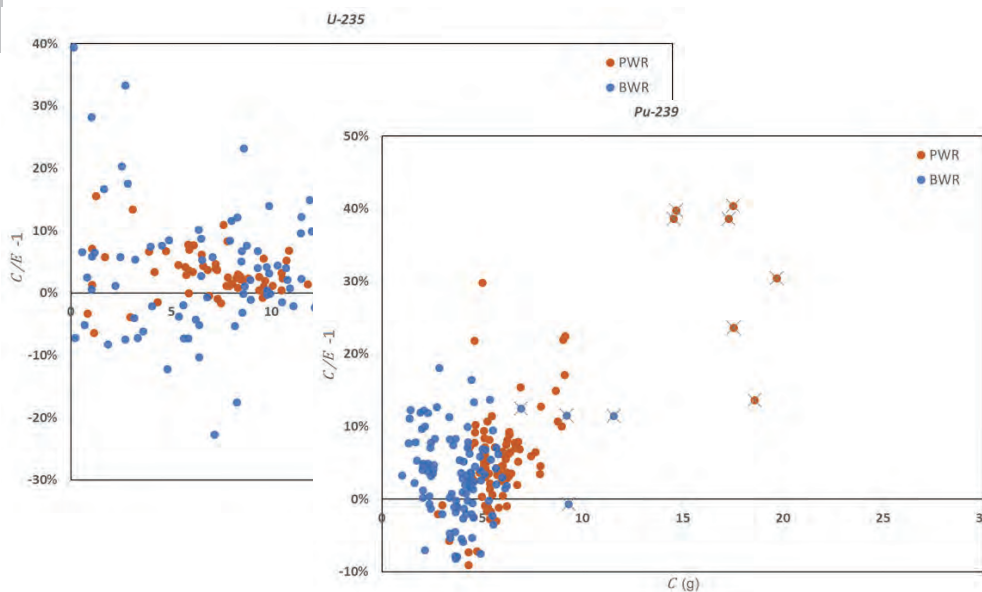
Design Matrix	Model	MAE $\pm 1\sigma$ (W/SFA)	R <sup>2</sup>
Spectral Index	RF	2.94 $\pm$ 2.42	0.47
	KNN	3.01 $\pm$ 2.56	0.41
	KKNN	2.97 $\pm$ 2.40	0.46
Correlation	RF	2.99 $\pm$ 2.67	0.44
	KNN	3.35 $\pm$ 2.69	0.32
	KKNN	3.49 $\pm$ 2.60	0.30

Seite 15



## Appendix : Ongoing Activities

Bias prediction for other quantities, i.e., concentration of actinides (U-235 and Pu-239) and a fission product (Cs-137), using neighborhood-based schemes and SNF features measuring similarities



Seite 16

**5.4 Chemical and spectroscopic investigations on the distribution of radionuclides in fuel-cladding interfaces of irradiated high burn-up UOX and MOX fuels; R. Dagan, T. König et al., KIT; Safety of Extended Dry Storage; 01 – 03/06/2022**



## Chemical and spectroscopic investigations on the distribution and enrichment of radionuclides in fuel-cladding interfaces of irradiated high burn-up $UO_x$ and MOX fuels

T. König, R. Dagan, K. Dardenne, M. Herm, V. Metz, T. Pruessmann, J. Rothe, D. Schild, A. Walschburger and H. Geckeis

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## Outline



### ■ Introduction:


- Nuclear fuel – *From cradle to grave*

### ■ Experimental:

- Examined fuel types – *High burn-up  $UO_x$  and MOX fuel*
- Radionuclide analysis – *Inventory determination of spent nuclear fuel*
- Spectroscopic analysis – *Interaction layer between fuel and cladding*
- Model systems – *Experiments on the formation of agglomerates and corrosion of the reaction layer*

### ■ Summary

From cradle to grave | Materials and methods | Radionuclide analysis | Spectroscopic analysis | Summary

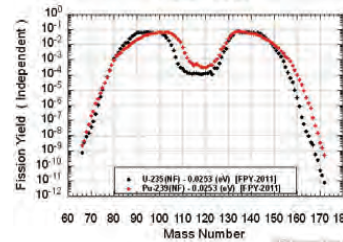
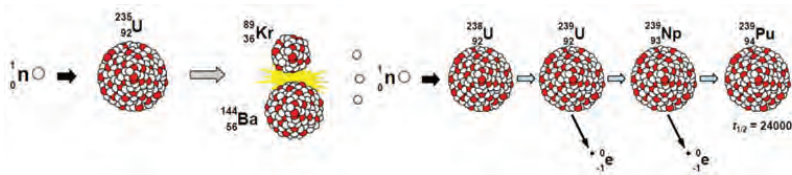


## Nuclear fission in Light Water Reactors

- **Neutron induced fission of fissile material ( $^{235}\text{U}$ ,  $^{239}\text{Pu}$ , etc.):**
  - Generation of neutrons → **Maintaining the chain reaction.**
  - Built-up of fission products → **2 – 3 fragments per fission.**
  - Neutron capture reactions → **Built-up of transuranic isotopes (Np, Pu, etc.) & activation products ( $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ).**

■ **Burn-up as definition of fuel utilisation:**

→ **Produced energy per mass initial heavy metal atom [GWd/t<sub>HM</sub>].**



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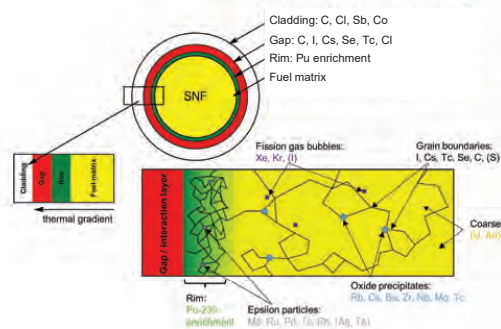
From cradle to grave | Materials and methods | Radionuclide analysis | Spectroscopic analysis | Summary



## Spent Nuclear Fuel (SNF)

■ **Composition of SNF (4.0%  $^{235}\text{U}$ , 52 GWd/t<sub>HM</sub>) utilised in a light water reactor (LWR) for ~ 4 years:**

- **93.4%  $\text{UO}_2$  matrix:**
  - 92%  $^{238}\text{U}$ , < 1%  $^{235}\text{U}$ , < 0.5%  $^{236}\text{U}$
- **1.2% transuranium isotopes / actinides:**
  - 1%  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{241}\text{Pu}$ ,  $^{237}\text{Np}$  >  $^{244}\text{Cm}$  >  $^{241}\text{Am}$ , etc.
- **5.4% fission products:**
  - 1.7%  $^{90}\text{Sr}$ ,  $^{135}$ ,  $^{137}\text{Cs}$ ,  $^{129}\text{I}$ , etc.
  - 1.6% lanthanides
  - 1.3%  $\epsilon$ -phases ( $^{99}\text{Tc}$ ,  $^{109}\text{Pd}$ , etc.)
  - 0.8% fission gases (krypton, xenon)
- **Activation products:**
  - e.g.  $^{14}\text{C}$ ,  $^{93}\text{Zr}$ ,  $^{36}\text{Cl}$  →  $^{35}\text{Cl} (n,\gamma) ^{36}\text{Cl}$



→ **Heterogenous distribution of radionuclides.**

Source: Hippler, Reaktorchemie, Leibniz Universität Hannover

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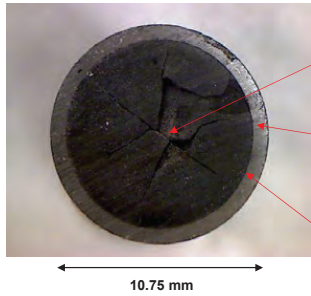
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From cradle to grave | Materials and methods | Radionuclide analysis | Spectroscopic analysis | Summary



## Interaction layer between fuel and cladding

### ■ Cross section of a nuclear fuel pellet:



**Pellet:** Radial cracks due to temperature gradient during irradiation; migration pathways for radionuclides in the SNF pellet.

**Cladding:** Built-up of an external  $ZrO_2$  layer due to primary circuit water corrosion; thin  $ZrO_2$  layer on the inner side due to  $Zr / UO_2$  reactions.

**Gap:** Closed at burn-ups  $> 40 \text{ GWd/t}_{HM}$ ; Formation of an **interaction layer**.

➔ **Possibility of transport of volatile fission and activation products to the cladding during irradiation and subsequent chemical reactions between fuel and cladding!**

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From cradle to grave | Materials and methods | Radionuclide analysis | Spectroscopic analysis | Summary

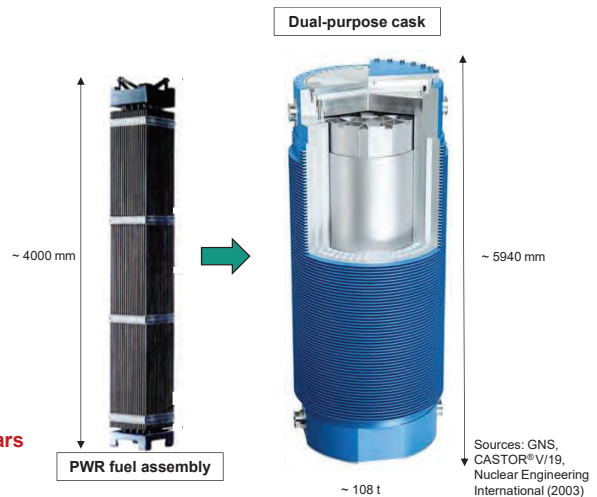


## Interim storage in Germany

### ■ Interim dry storage of used fuel assemblies in dual-purpose casks:

- Dual-purpose cask guarantees **shielding of radiation**, as well as a temporary, **safe enclosure of radionuclides**.
- Interim storage of irradiated fuel assemblies is **licensed for only 40 years**.
- **Final repository not available until at least 2050** and **emplacement of the last fuel assemblies decades later!**

➔ **Necessity of a prolonged interim storage of 65 – 100 years and conditioning of fuel assemblies from dual-purpose cask to final repository waste container!**



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## Interim storage in Germany

- **Interim dry storage** of used fuel assemblies in dual-purpose casks:
    - Dual-purpose cask guarantees **shielding of radiation**, as well as a temporary, **safe enclosure of radionuclides**.
    - Interim storage of irradiated fuel assemblies is licensed for only **40 years**.
    - Final repository not available until at least **2050** and emplacement of the last fuel assemblies decades later!
  - Several phenomena affect the cladding integrity during interim storage:
    - **Increase in pressure** due to swelling of the pellet and ongoing  $\alpha$ -decays.
    - **Irradiation damage of cladding** via  $\alpha$ -decays.
    - Cracking due to **hydride re-orientation**.  
$$\text{Zr} + 2 \text{H}_2\text{O} \rightarrow \text{ZrO}_2 + 2 \text{H}_2$$
    - **Corrosion of cladding induced by fission and activation products**.
- ➔ **Formation of agglomerates on the inner side of the cladding due to thermal gradient in SNF and possibility of halogen induced stress corrosion cracking.**

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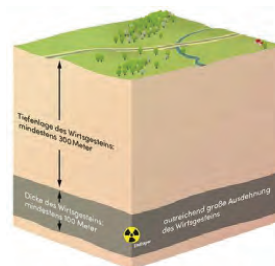
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## Final disposal in Germany

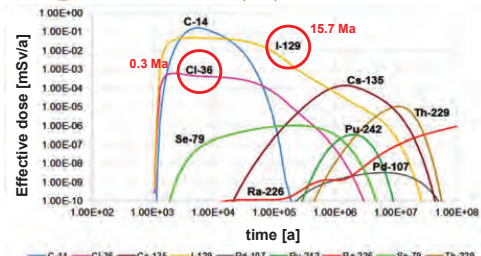
- Deep geological disposal:
  - **3 different lithologies** (clay, salt or crystalline rock) are under investigation.
  - **Safe enclosure for long timescale** needs to be guaranteed (1 million years).



Source: [https://www.einblicke.de/fileadmin/images/magazin/Einblicke\\_6/Kriterien\\_zur\\_Endlagersuche.jpg](https://www.einblicke.de/fileadmin/images/magazin/Einblicke_6/Kriterien_zur_Endlagersuche.jpg) (aufgerufen am 04.04.2022)

[FLA18]: D. Flamikova, V. Necas, *Creation of Reference Biosphere Model for Safety Assessment of Deep Geological Repository*, AIP Conference Proceedings 1996, 020009 (2018).

Safety analyses require profound knowledge on the occurrence and chemical behaviour of long-lived and dose relevant radionuclides (e.g.  $^{36}\text{Cl}$ ,  $^{129}\text{I}$ ,  $^{135}\text{Cs}$ )



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T. König et al. – Chemical and spectroscopic investigations on the distribution and enrichment of radionuclides in fuel-cladding interfaces of irradiated high burn-up  $\text{UO}_x$  and MOX fuels

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## Open questions

- If, after breaching of the (geo-) technical barriers, water intrusion appears,  **$^{36}\text{Cl}$  and  $^{129}\text{I}$  are quickly immobilised from the SNF!** In which concentration and chemical form are  $^{36}\text{Cl}$  and  $^{129}\text{I}$  present in used nuclear fuel rods?
  - Quantification and localisation of the repository relevant and mobile isotopes  $^{36}\text{Cl}$  and  $^{129}\text{I}$  in SNF and cladding.
  - Comparison of experimental determined radionuclide concentrations to expected inventory data derived from calculations.

➡ **Reducing uncertainties on inventory data.**
- In which condition is the fuel-cladding interface during interim storage?
  - In which chemical speciation are possible cladding degrading elements such as chlorine or iodine present in SNF and cladding?
  - Is a halogen induced pitting corrosion possible at temperatures prevailing during interim dry storage?

➡ **Reducing uncertainties on degrading processes.**

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## SNF specimens

### Fuel rod segment N0204, irradiated in the pressurised water reactor Gösgen (CH):

- Fuel type:  $\text{UO}_x$ , initial 3.8%  $^{235}\text{U}$  enrichment.
- Cladding alloy: Zircaloy-4.
- Full power days: 1226 days in 4 cycles.
- Average linear power: 260 W/cm.
- Average burn-up: **50.4 GWd/t<sub>HM</sub>**.
- Decay time: ~ 32 years.



### Fuel rod 5810, irradiated in the pressurised water reactor Obrigheim (DE):

- Fuel type: **MOX**, initial 3.2%  $\text{Pu}_{\text{fiss}}$  enrichment.
- Cladding alloy: Zircaloy-4.
- Full power days: 1157 days in 4 cycles.
- Average linear power: 200 W/cm.
- Average burn-up: **38.0 GWd/t<sub>HM</sub>**.
- Decay time: ~ 35 years.



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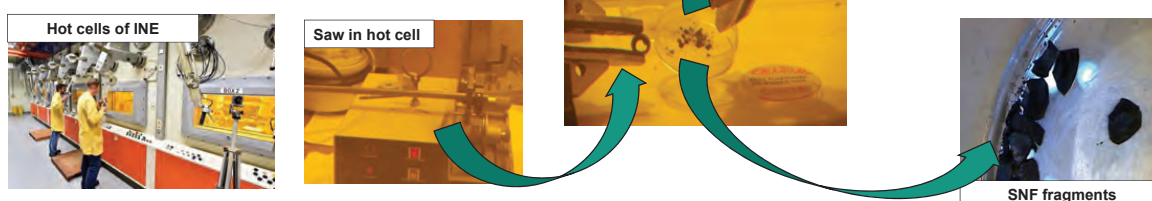
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From cradle to grave Materials and methods Radionuclide analysis Spectroscopic analysis Summary



## Preparation of the SNF specimens

- Segmentation of the SNF specimens in specially equipped laboratories (**hot cells**) due to the high dose rate!
- Selective sampling in order to analyse local radionuclide enrichments:
  - Fragments from central position (“**CORE**”).
  - Fragments from peripheral position (“**RIM**”).
  - **Zircaloy cladding segments.**



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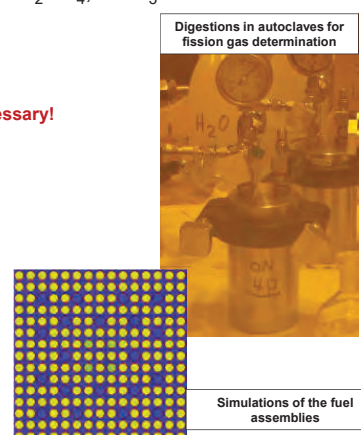
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From cradle to grave Materials and methods Radionuclide analysis Spectroscopic analysis Summary



## Radiochemical analytic & numerical calculations

- **Acidic and alkaline digestions of Zircaloy and fuel specimens** in HF / H<sub>2</sub>SO<sub>4</sub>, HNO<sub>3</sub> / HCl or (NH<sub>4</sub>)<sub>2</sub>CO<sub>3</sub> / H<sub>2</sub>O<sub>2</sub>:
  - **γ-spectrometry:** <sup>241</sup>Am, <sup>134</sup>, <sup>137</sup>Cs, <sup>125</sup>Sb, <sup>154</sup>, <sup>155</sup>Eu, <sup>60</sup>Co, <sup>129</sup>I.
  - **Liquid scintillation counting (LSC):** <sup>129</sup>I, <sup>36</sup>Cl, <sup>90</sup>Sr. ➔ **High purity of samples necessary!**
  - **ICP-MS:** <sup>235</sup>, <sup>238</sup>U, <sup>237</sup>Np, <sup>239</sup>, <sup>240</sup>Pu, <sup>241</sup>Am, <sup>244</sup>Cm.
  - **Gas-MS:** Kr- and Xe-isotopes.
- **Calculations of the radionuclide inventory with MCNP Code** for neutron flux and **CINDER module** for burn-up calculations:
  - Numerical calculations for the respective fuel assemblies, reactor types and irradiation conditions.
  - Radionuclide concentrations in central and peripheral part of pellets.



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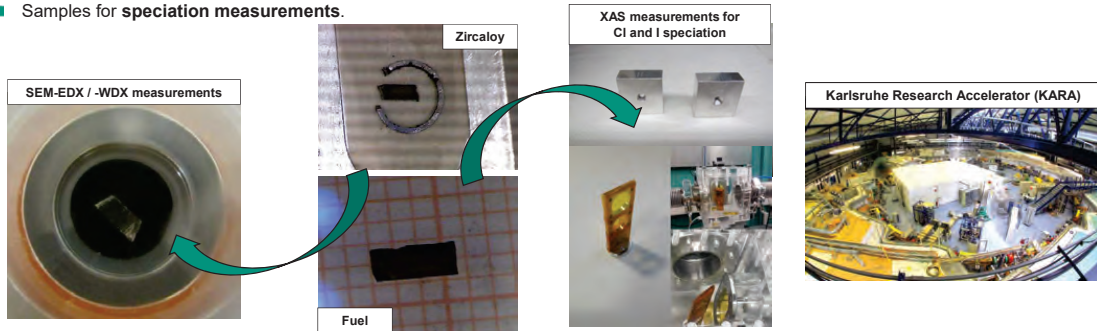
From cradle to grave Materials and methods Radionuclide analysis Spectroscopic analysis Summary

## Spectroscopic measurements



- Preparation of fuel fragments and Zircaloy segments for analyses by SEM-EDX / -WDX, and XAS at the KIT Light Source. ➔ **Enormous radiation protection measures necessary!**

- Samples for examination of the chemical composition.
- Samples for speciation measurements.

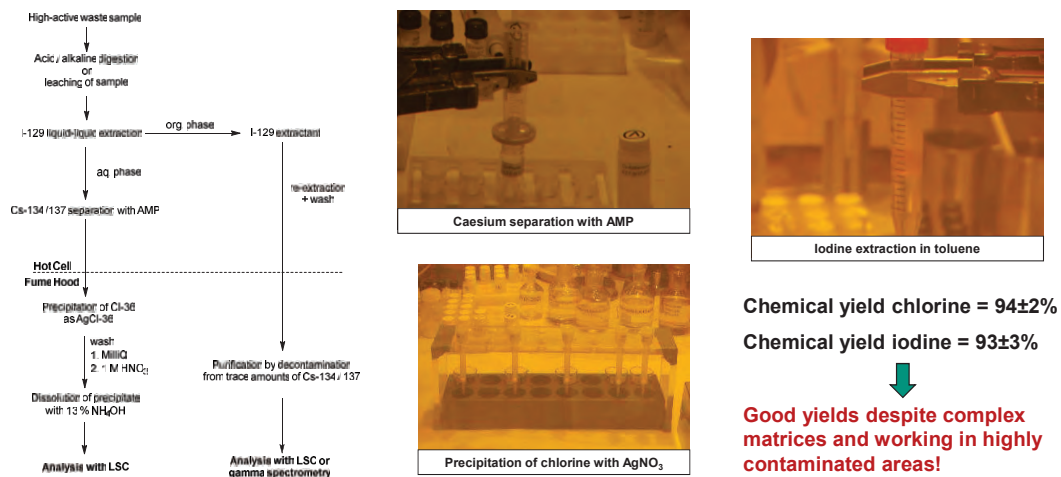


13 December 22, 2022 T. König et al. – Chemical and spectroscopic investigations on the distribution and enrichment of radionuclides in fuel-cladding interfaces of irradiated high burn-up UO<sub>x</sub> and MOX fuels

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From cradle to grave Materials and methods Radionuclide analysis Spectroscopic analysis Summary

## Radionuclide analysis – Separation of <sup>36</sup>Cl and <sup>129</sup>I

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From cradle to grave → Materials and methods → Radionuclide analysis → Spectroscopic analysis → Summary



## Radionuclide analysis – <sup>36</sup>Cl in SNF and Zircaloy

<sup>36</sup> Cl inventories	SNF		Zircaloy cladding		<sup>35</sup> Cl (n,γ) <sup>36</sup> Cl
	Specimen	UO <sub>x</sub> 50.4 GWd/t <sub>HM</sub> [Bq/t <sub>HM</sub> ]	MOX 38.0 GWd/t <sub>HM</sub> [Bq/t <sub>HM</sub> ]	UO <sub>x</sub> 50.4 GWd/t <sub>HM</sub> [Bq/t <sub>HM</sub> ]	
experimental		3.62(±0.54)×10 <sup>8</sup>	5.80(±0.87)×10 <sup>8</sup>	6.32(±0.28)×10 <sup>8</sup>	5.33(±0.24)×10 <sup>8</sup>
calculated		4.73×10 <sup>8</sup>	3.68×10 <sup>8</sup>	6.57×10 <sup>8</sup>	5.23×10 <sup>8</sup>
ratio (exp/calc)		0.77 ± 0.12	1.58 ± 0.24	0.96 ± 0.04	1.02 ± 0.05

→ Numerical calculations based on literature data assuming 15 ppm <sup>35</sup>Cl precursor in SNF and Zircaloy [HÄK19].

→ Experimental activity inventories in good agreement with calculations.

[HÄK19] S. Hakkinen, *Impurities in LWR fuel and structural materials*, VTT, Finland (2019).

→ **First ever analysis of <sup>36</sup>Cl in PWR fuel rod components!**

15 December 22, 2022 T. König et al. – Chemical and spectroscopic investigations on the distribution and enrichment of radionuclides in fuel-cladding interfaces of irradiated high burn-up UO<sub>x</sub> and MOX fuels

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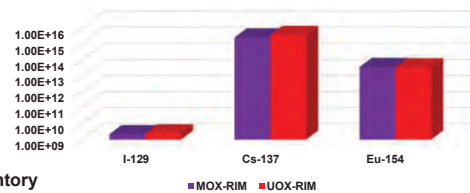
From cradle to grave → Materials and methods → Radionuclide analysis → Spectroscopic analysis → Summary



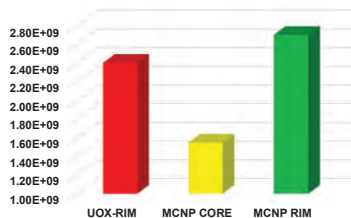
## Radionuclide analysis – Fission products

- Determination of the fission product inventory in SNF fragments originating from the fuel-cladding interaction layer and comparison with MCNP calculations.
- No significant differences between UO<sub>x</sub> (50.4 GWd/t<sub>HM</sub>) and MOX (38.0 GWd/t<sub>HM</sub>) fuel.

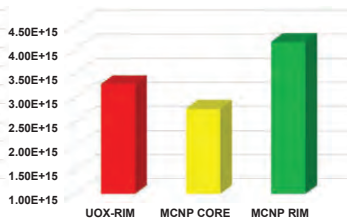
Comparison MOX and UO<sub>x</sub> SNF [Bq/t<sub>HM</sub>]



Comparison of <sup>129</sup>I inventory [Bq/t<sub>HM</sub>]



Comparison of <sup>137</sup>Cs inventory [Bq/t<sub>HM</sub>]




→ Elevated <sup>129</sup>I and <sup>137</sup>Cs activity due to enrichment effect at the cladding interface, originating from the higher local burn-up and transport of iodine along a thermal gradient in SNF pellet.

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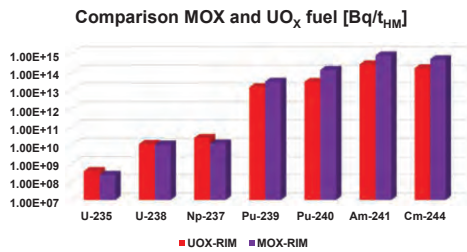
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From cradle to grave | Materials and methods | **Radionuclide analysis** | Spectroscopic analysis | Summary

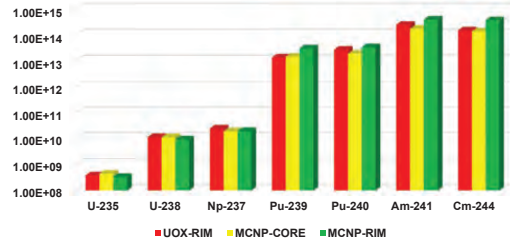


## Radionuclide analysis – Actinides

- Experimentally derived and calculated inventory data for different regions in fuel pellet of actinides.
- MOX fuel shows elevated activity of minor actinides compared to  $UO_x$  fuel due to initial enrichment with Pu.



Comparison of actinide inventory [Bq/t<sub>HM</sub>]



Knowledge on the amount of transuranium isotopes is of importance for calculations on  $\alpha$ -radiation induced damage of the cladding tube during interim storage.

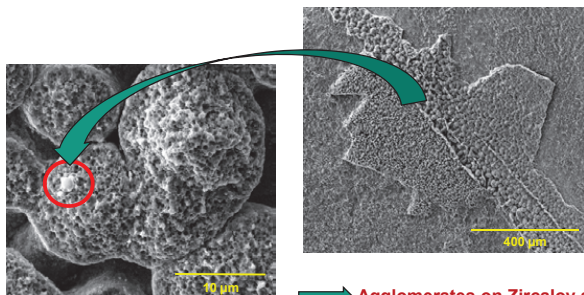
From cradle to grave | Materials and methods | Radionuclide analysis | **Spectroscopic analysis** | Summary



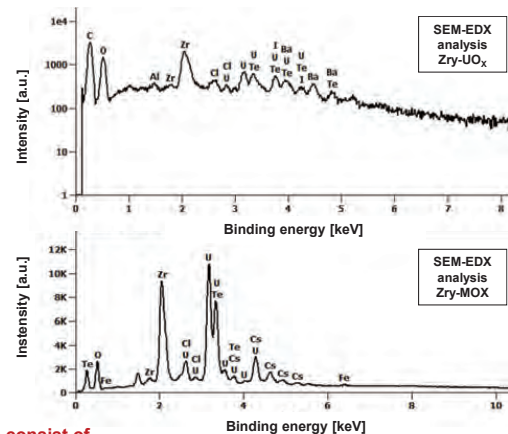
## Spectroscopic analysis – SEM-EDX / -WDX

- Zircaloy in contact with spent  $UO_x$  / MOX fuel:

- SEM-EDX: Cl, Te, I, Cs, Fe, Zr, Ba, U.
- XPS: Cl, Te, Cs, Fe, Zr, Ba, U.



Agglomerates on Zircaloy surface consist of U-O-Zr-Cs-Cl-I rich phases.

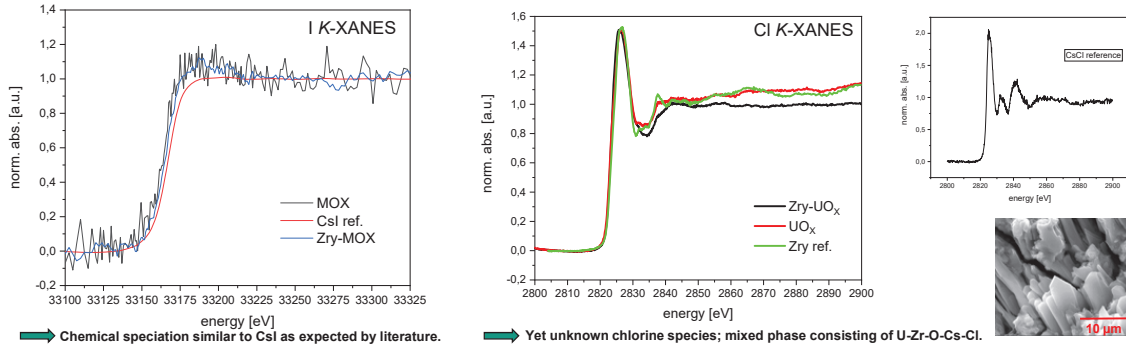


From cradle to grave | Materials and methods | Radionuclide analysis | **Spectroscopic analysis** | Summary



## Spectroscopic analysis – XAS

- Knowledge on the chlorine (and iodine) inventory and speciation in fuel and Zircaloy **afflicted with large uncertainties**.
- Initial maximum impurity assumptions of up to **25 ppm Cl in the fuel and 20 ppm Cl in Zircaloy-4 cladding**.
- First ever XAS measurements for chlorine (and iodine) speciation in fuel and cladding.** → **Complex mixed phases.**



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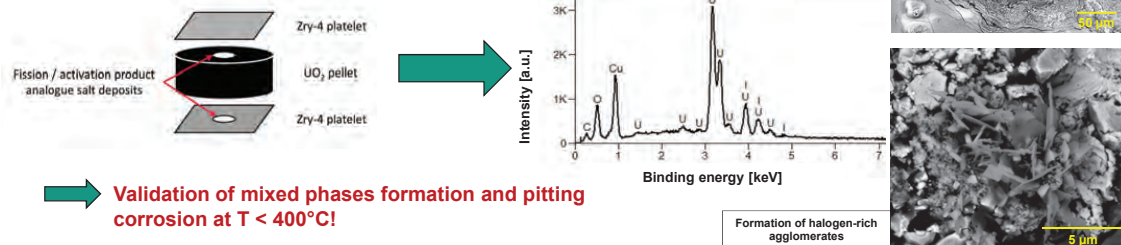
From cradle to grave | Materials and methods | Radionuclide analysis | **Spectroscopic analysis** | Summary



## Spectroscopic analysis – Model systems

- Laboratory experiments for formation of agglomerates and pitting corrosion under simulated interim dry storage conditions:

- Caesium halides in contact with Zircaloy and  $UO_2$  pellet under Ar atmosphere.**
- Reduction of temperature over 3 months from 400°C to room temperature.**
- Subsequent analysis with SEM-EDX and XPS.



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## Summary



### ■ Radionuclide analysis:

- Development of separation method for  $^{36}\text{Cl}$  and  $^{129}\text{I}$  in high active waste specimens.
- **First ever analysis of  $^{36}\text{Cl}$  inventory** in PWR fuel rod components.
- **Verification** of iodine enrichment in interaction layer between fuel and cladding.
- Good agreement between calculated and experimentally determined radionuclide inventory data.

### ■ Spectroscopic analysis:

- **First ever measurements of Cl K- and I K-edge** in high active waste specimens (SNF and Zircaloy).
- Agglomerates in interaction layer consist, amongst others, of halogen-rich mixed phases (**Cl and I**), as well as Cs, Te, Ba, U and Pu.
- **Validation of agglomerate-formation and pitting corrosion at  $T < 400^\circ\text{C}$  under laboratory conditions.**

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**Thank you for your kind attention and stay healthy!**

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**5.5 Experimentelle und numerische Bestimmungen des Radionuklidinventars von abgebrannten Kernbrennstoffen als eine Grundlage für die vorläufige Sicherheitsuntersuchung (vSU); R. Dagan, T. König et al., KIT; Tage der Standortauswahl; 08 - 10/06/2022**





# Experimentelle und numerische Bestimmungen des Radionuklidinventars von abgebrannten Kernbrennstoffen als eine Grundlage für die vSU

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## Einleitung

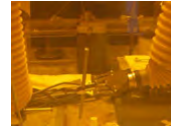
In den vorläufigen Sicherheitsuntersuchungen (vSU) wird gemäß § 27 StandAG das Endlagersystem in seiner Gesamtheit betrachtet und hinsichtlich seiner Sicherheit bewertet, wobei abdeckende Annahmen zur Menge, Art und Eigenschaften der radioaktiven Abfälle herangezogen werden [BGB17]. Hierbei sind die zu betrachtenden Radionuklidinventare der Ausgangspunkt für die Bewertung des sicheren Einschusses der Abfälle und Dosisabschätzungen in den vSU [BGE22]. Neben den Inventaren sind die chemische Speziation und lokale Verteilung der Radionuklide entscheidend für deren Mobilisierung aus den Abfällen.

In unserer Studie bestimmen wir experimentell die Radionuklidinventare von  $UO_x$  (Abbrand 50,4  $GWd/t_{HM}$ ) bzw. Mischoxid (MOX) (Abbrand 38,0  $GWd/t_{HM}$ ) Brennstabsegmenten, welche in Leistungsreaktoren eingesetzt wurden. Die gemessenen Radionuklidaktivitäten werden mit Inventarberechnungen, die wir mit den Programmen MCNP / CINDER und webKORIGEN ermitteln, verglichen. Aufgrund der relativ hohen Mobilität von  $^{36}Cl$  und  $^{129}I$  unter Endlagerbedingungen, liegt das Hauptaugenmerk unserer Untersuchungen auf den Inventaren und der Verteilung der beiden Aktivierungs- und Spaltprodukte.

## Kernbrennstoffe

**Brennstabsegment N0204, bestrahlt im Druckwasserreaktor, DWR Gösgen:**

Brennstofftyp:  $UO_x$  mit 3,8%  $^{235}U$  Anreicherung.  
 Hüllrohr: Zircaloy-4.  
 Volllasttage: 1226 Tage in 4 Zyklen.  
 Durchschnittliche lineare Leistung: 260 W/cm.  
 Durchschnittlicher Abbrand: **50,4  $GWd/t_{HM}$** .  
 Abklingzeit: ~ 32 Jahre.



**Brennstab 5810, bestrahlt im Druckwasserreaktor, DWR Obrigheim:**

Brennstofftyp: MOX mit 3,2%  $Pu_{Tot}$  Anreicherung.  
 Hüllrohr: Zircaloy-4.  
 Volllasttage: 1157 Tage in 4 Zyklen.  
 Durchschnittliche lineare Leistung: 200 W/cm.  
 Durchschnittlicher Abbrand: **38,0  $GWd/t_{HM}$** .  
 Abklingzeit: ~ 35 Jahre.



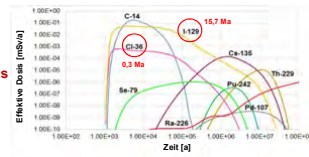
## Endlagerung von abgebranntem Kernbrennstoff

**Tiefengeologische Endlagerung:**

- 3 unterschiedliche Gesteinsarten (Ton-, Salz- und Kristallingestein) werden in Betracht gezogen.
- Sicherer Einschluss über langen Zeitraum muss gewährt werden (1 Million Jahre).



Sicherheitsbewertung erfordert grundlegende Kenntnisse über das Vorkommen und chemisches Verhalten von langlebigen und dosisrelevanten Radionukliden (z. B.  $^{36}Cl$ ,  $^{129}I$ ,  $^{135}Cs$ )



Quellen: BASE, [FLA18]

## Radionuklidinventarbestimmung

Saurer und alkalischer Aufschluss von Zircaloy- sowie Brennstoffproben aus dem zentralen und Randbereich der Pellets in  $HF / H_2SO_4$ ,  $HNO_3 / HCl$ ,  $(NH_4)_2CO_3 / H_2O_2$ :

- Neuentwickelte Abtrennungsmethode für  $^{36}Cl$  und  $^{129}I$  aus hochradioaktiven Proben.
- $\gamma$ -Spektrometrie:  $^{241}Am$ ,  $^{134}Cs$ ,  $^{137}Cs$ ,  $^{125}Sb$ ,  $^{154}Eu$ ,  $^{155}Eu$ ,  $^{60}Co$ ,  $^{129}I$ .
- Flüssigszintillationsmessung:  $^{129}I$ ,  $^{36}Cl$ ,  $^{90}Sr$ ,  $^{241}Pu$ .
- ICP-MS:  $^{235}U$ ,  $^{237}Np$ ,  $^{239}Pu$ ,  $^{240}Pu$ ,  $^{242}Pu$ ,  $^{241}Am$ ,  $^{243}Am$ ,  $^{244}Am$ ,  $^{245}Am$ ,  $^{246}Cm$ .
- Gas-MS: Kr- und Xe-Isotope.



Berechnungen des Radionuklidinventars mittels webKORIGEN sowie MCNP Code für Neutronenfluss und CINDER Modul für Abbrand-Berechnungen:

- Numerische Berechnungen für die jeweiligen Brennstoffanordnungen, Reaktortypen und Bestrahlungsbedingungen.
- Radionuklidkonzentrationen im zentralen und Randbereich des Pellets.

## $^{36}Cl$ Inventar in Kernbrennstoff und Hüllrohr

$^{36}Cl$ Inventare	Kernbrennstoff [ $Bq/t_{HM}$ ]		Zircaloy-Hüllrohr [ $Bq/t_{HM}$ ]	
	$UO_x$ 50,4 $GWd/t_{HM}$	MOX 38,0 $GWd/t_{HM}$	$UO_x$ 50,4 $GWd/t_{HM}$	MOX 38,0 $GWd/t_{HM}$
Experimentell	$3,62(\pm 0,54) \times 10^8$	$5,80(\pm 0,87) \times 10^8$	$6,32(\pm 0,28) \times 10^8$	$5,33(\pm 0,24) \times 10^8$
Berechnet	$4,73 \times 10^8$	$3,68 \times 10^8$	$6,57 \times 10^8$	$5,23 \times 10^8$
Verhältnis (exp/ber)	$0,77 \pm 0,12$	$1,58 \pm 0,24$	$0,96 \pm 0,04$	$1,02 \pm 0,05$

Numerische Berechnungen auf Grundlage von Literaturdaten, ausgehend von 15 ppm  $^{36}Cl$  Precursor in KBS und Hüllrohr [HÄK19].

Erstmalige Analyse von  $^{36}Cl$  in DWR-Brennstoffkomponenten!

## $^{129}I$ Inventar in Kernbrennstoff

**Vergleich des  $^{129}I$  Inventars [ $Bq/t_{HM}$ ]**

Sample Type	$^{129}I$ Inventory [ $Bq/t_{HM}$ ]
MOX-RIM	~ 2.0E+09
MOX-RM	~ 1.5E+09
MCNP-RM	~ 1.0E+09
MCNP-CORE	~ 0.5E+09

Erhöhte  $^{129}I$  Aktivität durch einen Anreicherungseffekt an der Hüllrohrgrenzfläche auf Grund des höheren lokalen Abbrands und dem Transport von Iod entlang eines thermischen Gradienten im Pellet.

## Quellen

- [BGB17] Bundesgesetzblatt I S. 1074, Gesetz zur Suche und Auswahl eines Standortes für ein Endlager für hochradioaktive Abfälle, Deutschland (2017).
- [BGE22] Bundesgesellschaft für Endlagerung, Methodenbeschreibung zur Durchführung der vSU gemäß EndSIUnV, BGE, Deutschland (2022).
- [FLA18] D. Flamičková, V. Necas, Creation of Reference Biosphere Model for Safety Assessment of Deep Geological Repository, AIP Conf. Proceed. 1996, 020009 (2018).
- [HÄK19] S. Häkkinen, Impurities in LWR fuel and structural materials, VTT, Finland (2019).

## Zusammenfassung

- > Abtrennungsmethode für  $^{36}Cl$  und  $^{129}I$  aus hochradioaktiven Proben entwickelt.
- > Erstmalige Analyse des  $^{36}Cl$  Inventars in DWR-Brennstoffkomponenten.
- > Nachweis von Iod-reichen Anreicherungen in der Wechselwirkungsschicht zwischen KBS und Zircaloy-Hüllrohr.
- > Gute Übereinstimmung zwischen Berechnungen und experimentell bestimmten Radionuklidinventardaten für etliche Isotope wie  $^{36}Cl$ ,  $^{129}I$  und  $^{137}Cs$ ; jedoch auch Abweichungen ersichtlich bei z. B.  $^{60}Co$ ,  $^{235}U$ ,  $^{245}Cm$ .



**5.6 Passive gamma and neutron measurements for  
characterization of spent nuclear fuel; V. Solans, UU; 31th  
Spent Fuel Workshop; 19 – 21/10/2022**





## PASSIVE GAMMA AND NEUTRON MEASUREMENTS FOR CHARACTERIZATION OF SPENT NUCLEAR FUEL.

Virginie SOLANS (Uppsala University)

Henrik Sjöstrand, Sophie Grape, Erik Branger (Uppsala University)

Alessandro Borella, Riccardo Rossa (SCK CEN)

Peter Schillebeeckx (IRC), Anders Sjöland (SKB & Lund University)



This project has received funding from the European Union's Horizon 2020 research and innovation programme 2014-2018 under grant agreement N°847593

September 2022

IAEA CRP

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### EURAD GOALS

#### Ä In deep geological repositories, spent nuclear fuel needs to be characterized:

- Reactivity
- Decay heat
- Gamma's and neutron's dose
- Safeguards parameters

#### Ä Before encapsulation the fuel parameters need to be determined

- Ä calculated by the state of the art codes
- Ä emphasis on uncertainties
- Ä verify (update) with experimental measurements.

#### Ä Experimental measurements:

- Calorimetric measurements
- **Gamma-ray scans**
- **Neutron measurements**



## GOALS

### • Neutron measurements (DDSI)

• Predict BU and IE

### • Gamma measurements

• Cs-137, Cs-134/Cs-137, Eu-154/Cs-137 -> BU indicators, verify predicted isotopic composition

**A neutron and a gamma measurement techniques are planned to be used for all SNFs at the encapsulation plant in Sweden**



## SKB50

- Set of 25 BWR and 25 PWR assemblies
- Used in Swedish reactors
- Various burnup, initial enrichment, cooling time, manufacturers
- Gamma scans
- Calorimetric measurements
- Neutron measurements
- Chosen around 2013-2014

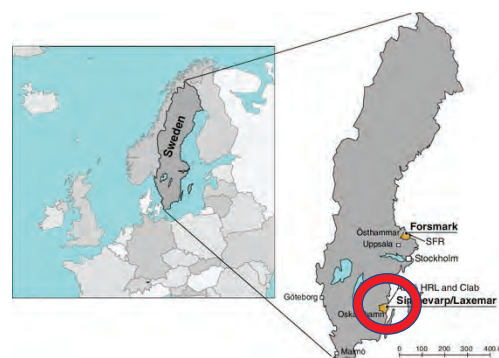


Image reference: Andersson, J., Skagius, K., Winberg, A. et al. Site-descriptive modelling for a final repository for spent nuclear fuel in Sweden. *Environ Earth Sci* 69, 1045–1060 (2013). <https://doi.org/10.1007/s12665-013-2226-1>





### DIFFERENTIAL DIE-AWAY SELF INTERROGATION INSTRUMENT (DDSI)

- Passive instrument developed and built in LANL
- Use neutron from Cm244 to interrogate the assembly
- Detect neutrons in coincidence (Rossi-alpha distribution)
  
- 56 <sup>3</sup>He tubes detect thermal neutrons
- Polyethylene to slow down neutrons
- Lead to reduce gamma-ray dose rate

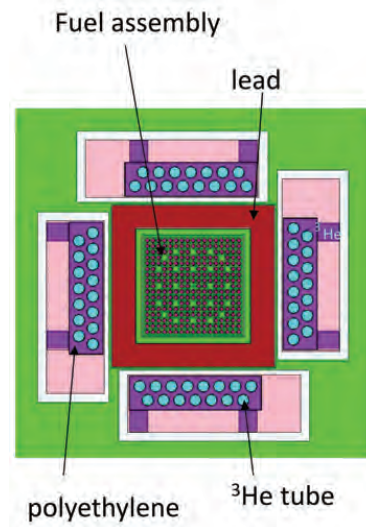
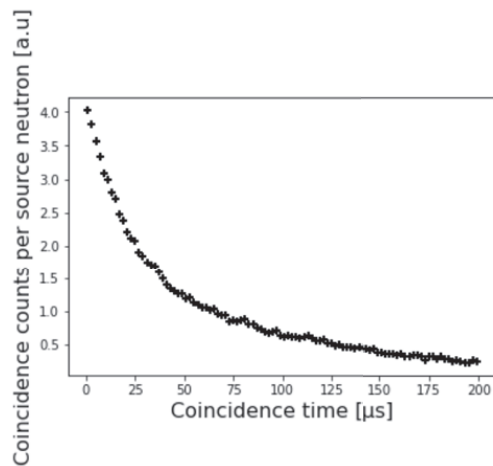


Image courtesy of Li Balkestahl



### ROSSI-ALPHA DISTRIBUTION (RAD)



#### Output of the DDSI:

- Rossi-alpha distribution (RAD) describing neutrons detected in coincidence
- Total number of neutrons detected





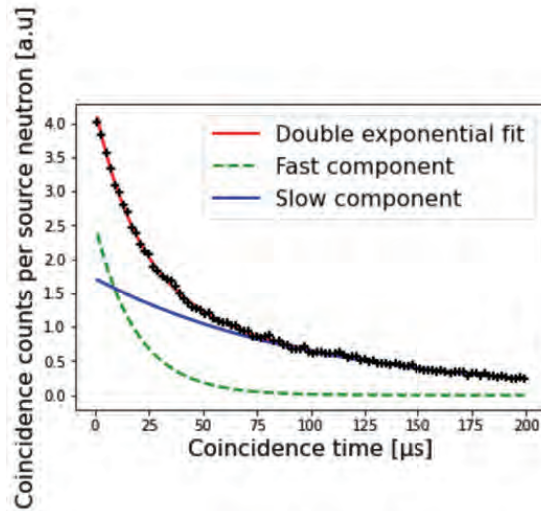
### DOUBLE EXPONENTIAL

• A fast and a slow component

• Fast is not only direct detection or fast multiplication

• Slow is neutrons that have time to thermalized before fission

$$RAD_{double}(t) = A_{fast} \cdot \exp(-\tau_{fast} t) + A_{slow} \cdot \exp(-\tau_{slow} t)$$

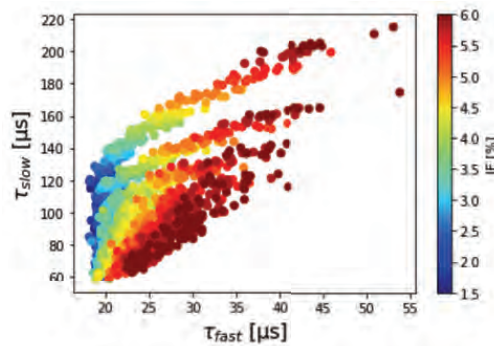
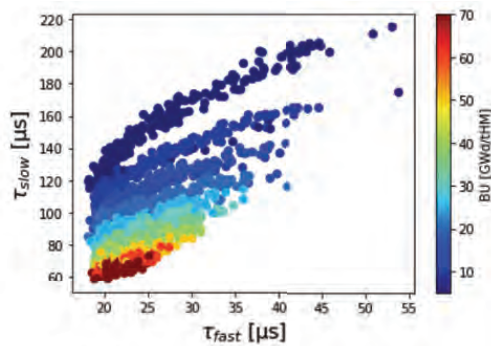


Increase in **absorbers decrease** the fission chain → **lower** amplitudes and a **shorter** slow component

Increase in **fissile content increase** the fission chain → **larger** amplitudes and a **longer** slow component



### TAU FAST VERSUS TAU SLOW



Indication that there is more information  
Same data point with different colouring indicating BU or IE





**MODEL**

• Use a KNN model

• Trained on the simulated dataset

• Tested on the simulated dataset and the experimental data

Input:

•  $\tau_{fast}$

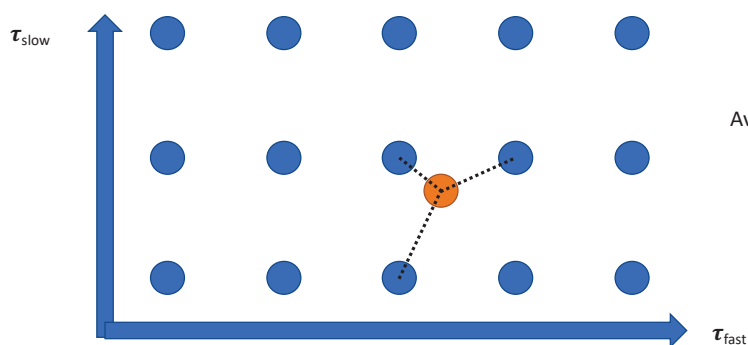
•  $\tau_{slow}$

• Ratio amplitude

Output:

• IE

• BU



Average of the 3 closet neighbours



**RESULTS**

RMSE	BU [GWd/tHM]	IE [%]
Test set simulation	4.51	0.284
Experimental after KNN	11.86	0.963
Experimental after bias correction	2.65	0.324





# GAMMA MEASUREMENTS



Date

Event



## DIFFERENT CAMPAIGNS

### • Campaign 1

- Done in 2014
- Static measurement

### • Campaign 2

- Done in 2014
- Axial measurement

### • Campaign 3

- Done in 2016-2019
- Axial measurement

Different detectors, attenuation plates, ...

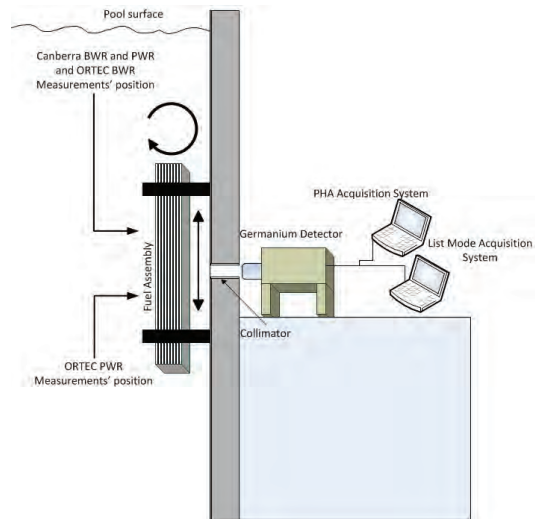
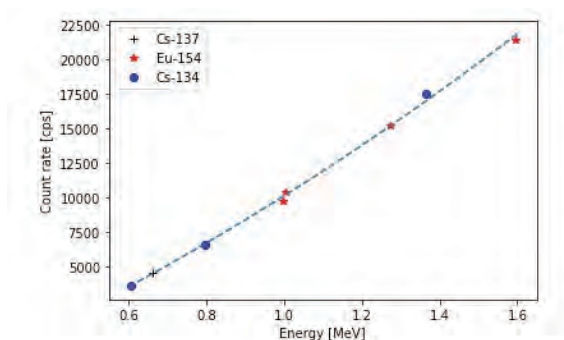


Image reference: S. Vaccaro, et al., PWR and BWR spent fuel assembly gamma spectra measurement, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, Volume 833, 2016





## INTRINSIC SELF-CALIBRATION



5 parameters to optimized : a, b, c, R<sub>1</sub> and R<sub>2</sub>

$$\begin{cases} C_{Cs-137}/BR_{Cs-137} = (a \cdot E^2 + b \cdot E + c) \\ C_{Eu-154}/BR_{Eu-154} = (a \cdot E^2 + b \cdot E + c) \cdot R_1 \\ C_{Cs-134}/BR_{Cs-134} = (a \cdot E^2 + b \cdot E + c) \cdot R_2 \end{cases}$$

Date

Event



## RESULTS – SELF CALIBRATION

$\bar{\Delta}$  Even if the measurement conditions were different between the campaigns, mean deviation between campaigns obtained were:

$\bar{\Delta}$ With self-calibration $\bar{\Delta}$ 2.3% for Eu-154/Cs-137 $\bar{\Delta}$ 1.9% for Cs-134/Cs-137	}	High reproducibility!
$\bar{\Delta}$ Without self-calibration $\bar{\Delta}$ 1.4% for Cs-137 $\bar{\Delta}$ 8.1% for Eu-154/Cs-137 $\bar{\Delta}$ 4.0% for Cs-134/Cs-137		





## RESULTS - REPRODUCIBILITY

### • Standard deviation of the best determined peak:

- The standard deviation in the inter-campaign reproducibility for the best-determined gamma peaks is between 2 and 3%.



## CONCLUSION

### Neutron measurement:

- Only 17x17 PWRs assemblies
- Rossi alpha distribution from the DDSI instrument has been analysed with a double exponential fit
- BU and IE are predicted using a *k*NN algorithm

### Gamma measurement:

- HPGe detectors
- Intrinsic self calibration for the experimental gamma measurements applied to the SKB-50
- Reproducibility of the SKB50 measurement campaigns has been investigated between 1.4 to 2.3 %
- The standard deviation in the inter-campaign reproducibility for the best-determined gamma peaks is between 2 and 3%.







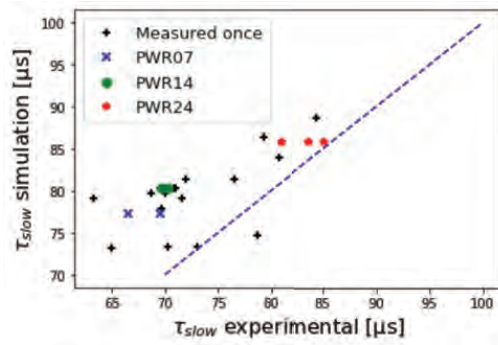
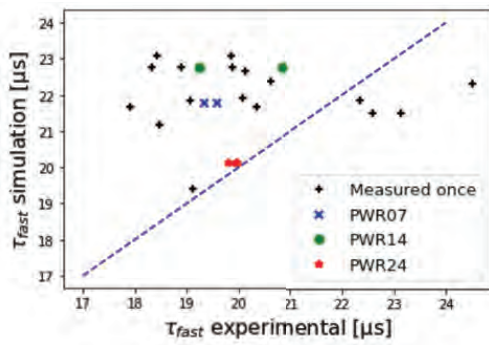
## APPENDIX

Date

Event




## EXPERIMENTAL RESULTS

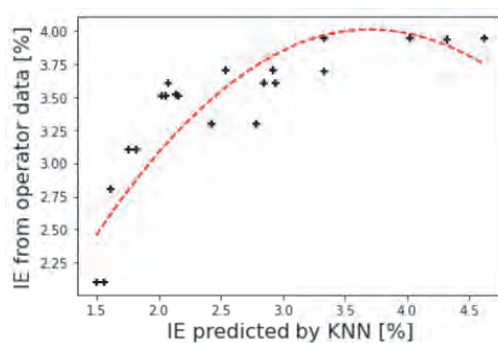
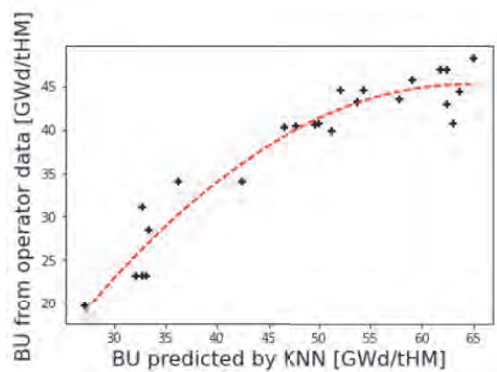


Dotted line is the unity line





**RESULTS**



**RESULTS**

RMSE	BU [GWd/tHM]	IE [%]
Test set simulation	4.51	0.284
Experimental After KNN	11.86	0.963
Experimental After fit	2.65	0.324
Simulated set After fit	2.69	0.104



**5.7 Characterisation of spent nuclear fuel for a typical PWR; G.  
Žerovnik, JSI; 31th Spent Fuel Workshop; 19 – 21/10/2022**



# Characterisation of spent nuclear fuel for a typical PWR

Žerovnik, G.<sup>1\*</sup>, Cabezas, M.<sup>2</sup>, Čalič, D.<sup>1</sup>, Fiorito, L.<sup>2</sup>, Kromar, M.<sup>1</sup>, Romojaro, P.<sup>2</sup>, Schillebeeckx, P.<sup>3</sup> and Stankovskiy, A.<sup>2</sup>

<sup>1</sup> Jožef Stefan Institute (JSI). Ljubljana, Slovenia

<sup>2</sup> Belgian Nuclear Research Centre (SCK CEN). Mol, Belgium

<sup>3</sup> European Commission, Joint Research Centre Geel (JRC Geel). Geel, Belgium

\* [gasper.zerovnik@ijs.si](mailto:gasper.zerovnik@ijs.si)

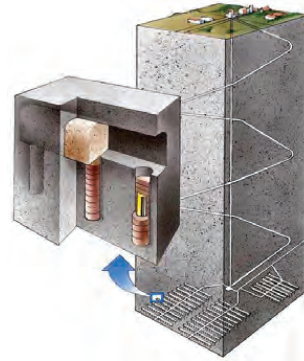
## Overview

- Motivation
- Main contributors to NDA observables
- Depletion code comparison
- Sensitivity/uncertainty analysis
- Neutron emission measurements
- Conclusions

## Spent Nuclear Fuel (SNF) storage or disposal

A **safe, secure, ecological** and **economic** storage and final disposal requires that **SNF** is **characterised** for the main observables of interest:

- Decay heat
- Neutron emission
- $\gamma$ -ray emission
- Reactivity

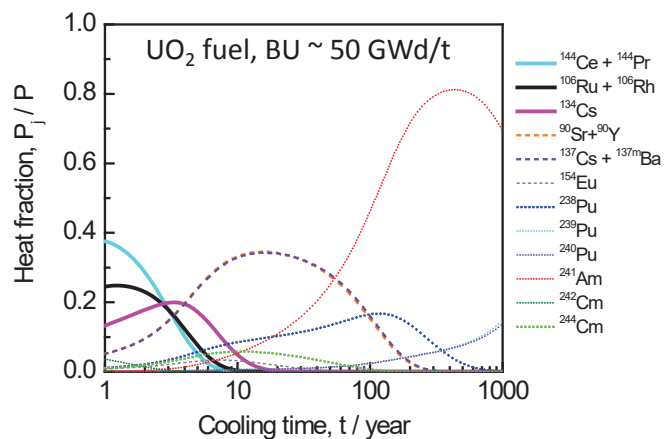


Research funded by EU project EURAD

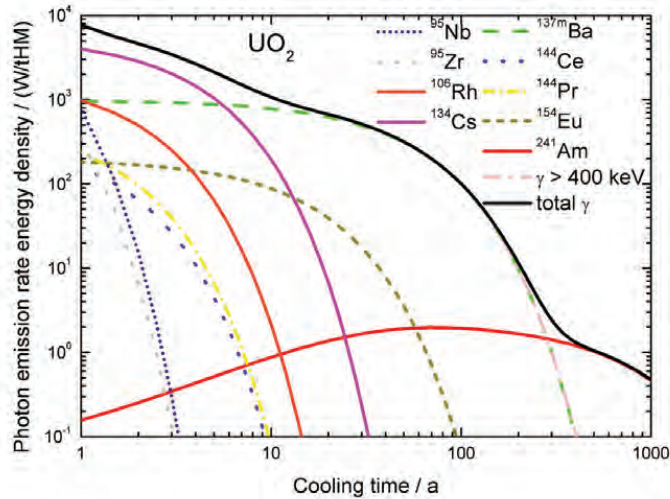
## Decay heat of SNF: main contributing nuclides

Decay heat rate:  $H(t) = \sum_j H_j(t)$

- $1 \text{ a} \leq t_c \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$  &  $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t_c \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$  &  $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t_c$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$



## γ-ray emission by SNF: main contributing nuclides



Photon emission rate energy density:

$$H_{\gamma}(t) = \sum_j H_{\gamma,j}(t) = \sum_j N_j(t) \lambda_j E_{\gamma,j}$$

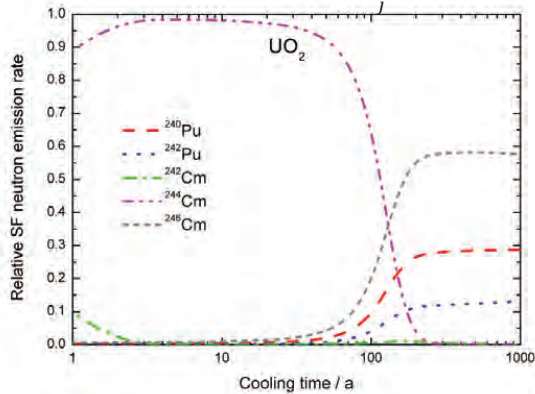
= Contribution of γ-rays to decay heat

- 1 a ≤ t ≤ 10 a
  - 134Cs
  - 137Cs / 137mBa
  - 106Ru / 106Rh
- 10 a ≤ t ≤ 300 a
  - 137Cs / 137mBa
  - 154Eu
  - 241Am
- 300 a ≤ t
  - 241Am
  - 137Cs / 137mBa

## Neutron emission of SNF: main contributing nuclides

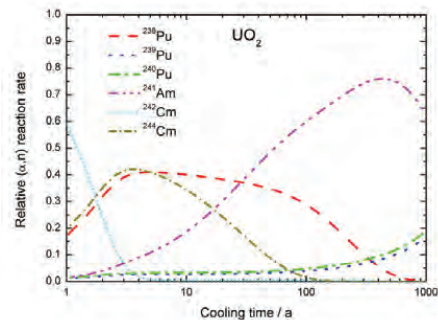
Neutron emission rate:

$$S_n(t) = \sum_j S_{n,j}(t)$$



**Contribution from SF dominating!**

- for cooling time < 100 a, (α, n) rate at least 10× lower than SF n. emission rate



$S_n(t) \Rightarrow$  sensitive to  $^{244}\text{Cm}$  production

## Code comparison: definition of the study case

2D PWR 17×17, reflective boundary conditions. Zircaloy-4, 4% enriched UO<sub>2</sub> fuel, 4 × 300 d fuel cycles, cooling periods 30 d. Fuel radius 4.095 mm, clad inner/outer radii 4.18/4.75 mm, rod pitch 12.6 mm.

### Simplified operating conditions:

- Power levels 50, 50, 40 and 30 MW/tHM during each cycle.
- Coolant density 0.655 kg/cm<sup>3</sup>, constant boron level 800 ppm.
- Fuel density (95% theoretical density): 10.4 g/cm<sup>3</sup>.
- Constant  $T$ : fuel and gap: 900 K; coolant and cladding: 600 K.

### Numerical approximations:

- 4 equi-volume radial depletion zones
- Time steps per cycle: 1 d, 10 d, 14 d, 3 × 25 d, 2 × 50 d.

**Codes:** **Serpent** (v2.1.29), Aleph2, SCALE/Polaris, DRAGON4

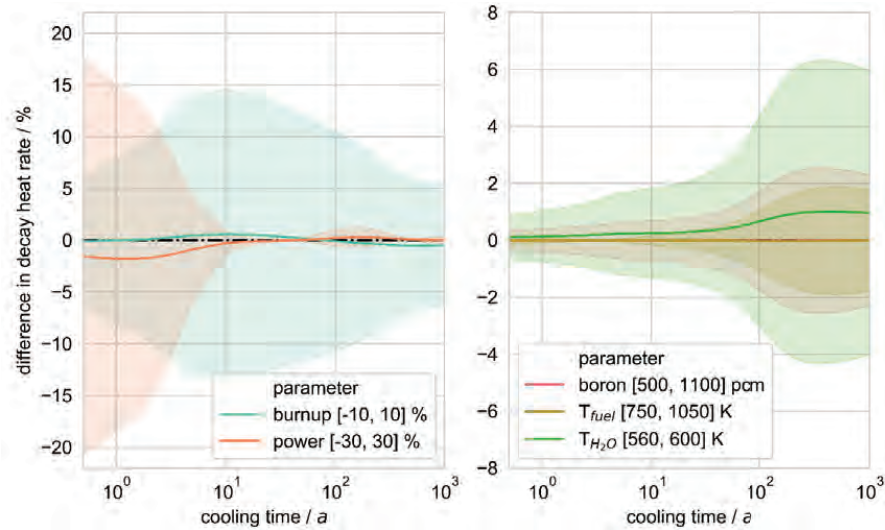
**Nuclear data library:** ENDF/B-VII.1

## Code comparison: nuclide vector @ $t_c = 5$ a

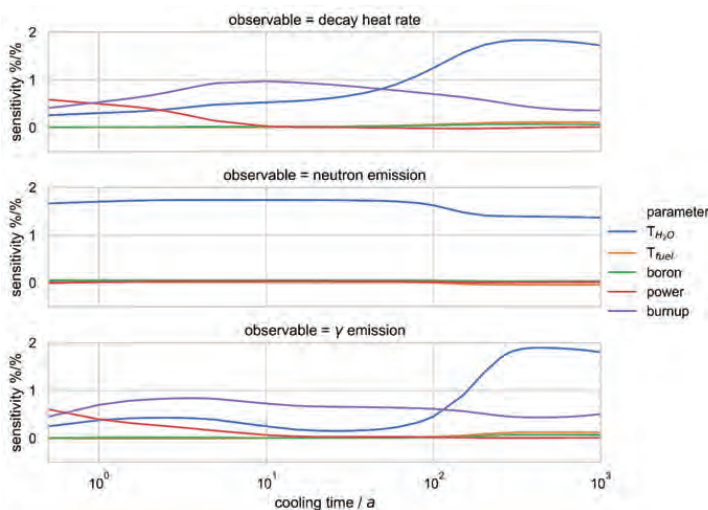
**Output:** **nuclide vector** and derived quantities (observables of interest)

Code Nuclide	Serpent $c_p$ /(g/tHM)	ALEPH2 $c$ /(g/tHM)	$\Delta c/c_p$	SCALE $c$ /(g/tHM)	$\Delta c/c_p$	Dragon $c$ /(g/tHM)	$\Delta c/c_p$
<sup>90</sup> Sr	678.56(2)	678.86	0.04%	675.43	-0.46%	679.08	0.08%
<sup>134</sup> Cs	43.86(2)	43.68	-0.43%	41.11	-6.28%	43.64	-0.51%
<sup>137</sup> Cs	1638.0(0)	1640.2	0.13%	1643.2	0.32%	1639.8	0.11%
<sup>235</sup> U	7109.9(14)	7064.5	-0.64%	7283.3	2.44%	7119.6	0.14%
<sup>238</sup> Pu	426.44(18)	426.55	0.03%	429.22	0.65%	434.35	1.85%
<sup>239</sup> Pu	6747.4(18)	6786.5	0.58%	6947.2	2.96%	6825.4	1.16%
<sup>240</sup> Pu	3065.2(13)	3044.1	-0.69%	2976.3	-2.90%	3056.1	-0.30%
<sup>241</sup> Pu	1556.7(6)	1561.8	0.33%	1608.5	3.33%	1570.8	0.91%
<sup>242</sup> Pu	970.92(30)	967.77	-0.32%	990.42	2.01%	963.26	-0.79%
<sup>241</sup> Am	499.66(17)	499.79	0.03%	516.77	3.43%	503.06	0.68%
<sup>244</sup> Cm	109.38(8)	108.80	-0.52%	102.37	-6.41%	106.86	-2.32%

## DH sensitivity to operational parameters

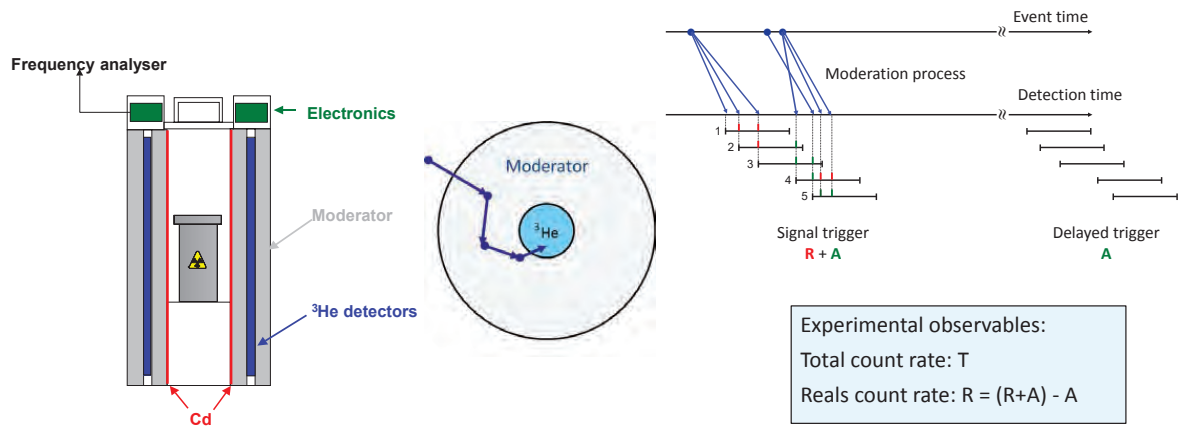


## Sensitivity of NDA observables





# Prompt fission neutron detection



# Neutron correlation counting: Hage's point model

- Neutron emission rata due to (sf) :  $S_{sf}$
- Relative ( $\alpha, n$ ) contribution :  $\alpha$
- Detection efficiency :  $\varepsilon$
- Leakage multiplication :  $M$
- Probability for a (n,f) reaction :  $p$
- Factorial moments multiplicity distribution

$$v_{sf(j)} = \sum_{v=j}^{\infty} \binom{v}{j} P_{sf}(v) \quad v_{nf(j)} = \sum_{v=j}^{\infty} \binom{v}{j} P_{nf}(v)$$

$$T = \varepsilon_{sf} S_{sf} M [1 + \alpha]$$

$$R = \varepsilon_{sf}^2 f S_{sf} M^2 \left[ \frac{v_{sf(2)}}{v_{sf(1)}} + \frac{p v_{nf(2)}}{1-p v_{nf(1)}} (1 + \alpha) \right]$$

W. Hage and D.M. Cifarelli, Nucl. Sci; Eng. 89 (1985) 159

W. Hage and D.M. Cifarelli, Nucl. Instr. Meth. A236 (1985) 165

# Neutron output of SNF segment sample

Code	Library	$(\alpha, n)$		$S_{sf} / (g^{-1}s^{-1})$	$S_{\alpha} / (g^{-1}s^{-1})$	Calculation/Experiment	
		Method	Library			$S_{sf}$	$S_{\alpha}$
SCALE	ENDF/B-VII.1	Y( $\alpha, n$ )		653	11.0	0.96	0.45
SERPENT(1)	ENDF/B-VII.1	Y( $\alpha, n$ )		689	14.3	1.01	0.58
SERPENT(2)	ENDF/B-VII.1	Y( $\alpha, n$ )		694	14.2	1.02	0.58
	ENDF/B-VIII.0	Y( $\alpha, n$ )		691	14.1	1.01	0.57
	JEFF-3.1.2	Y( $\alpha, n$ )		629	13.2	0.92	0.54
	JEFF-3.3	Y( $\alpha, n$ )		654	13.7	0.96	0.56
	JEFF-4TO	Y( $\alpha, n$ )		695	13.7	1.02	0.56
	JENDL-4.0			719	14.5	1.05	0.59
ALEPH28	ENDF/B-VIII.0	Y( $\alpha, n$ )		662	13.1	0.97	0.53
		$\sigma(\alpha, n)$	TENDL2015		12.6		0.51
		$\sigma(\alpha, n)$	JENDL_AN/500		10.6		0.43
	JEFF-3.3	Y( $\alpha, n$ )		641	12.9	0.94	0.53
		$\sigma(\alpha, n)$	TENDL2015		12.7		0.52
		$\sigma(\alpha, n)$	JENDL_AN/500		10.5		0.43

All data normalised to  $^{148}\text{Nd}$  inventory

REGAL sample ( $\text{UO}_2$ ):  
NPP Tihange

**experimental:**

$$S_{sf} = 682 (10) \text{ g}^{-1} \text{ s}^{-1}$$

$$S_{\alpha} / S_{sf} = 0.036 (15)$$

⇒ influence

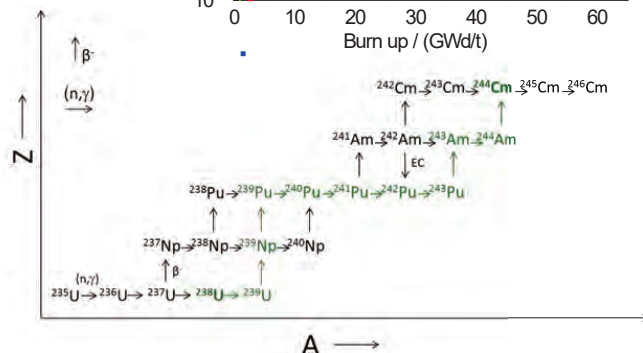
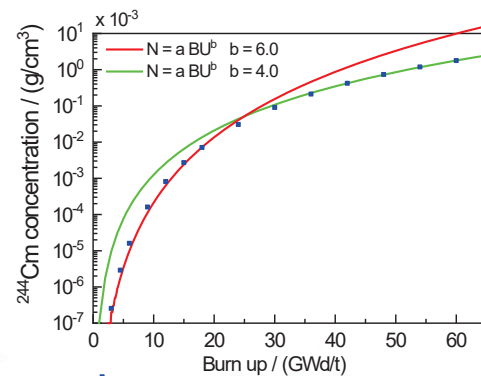
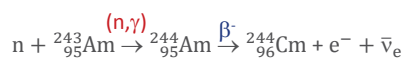
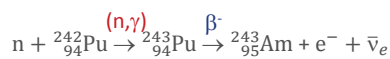
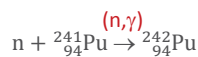
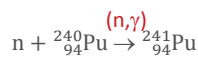
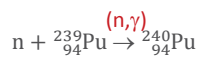
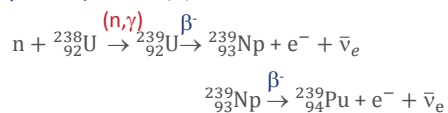
- nuclear data
- burnup code

## Production of $^{244}\text{Cm}$

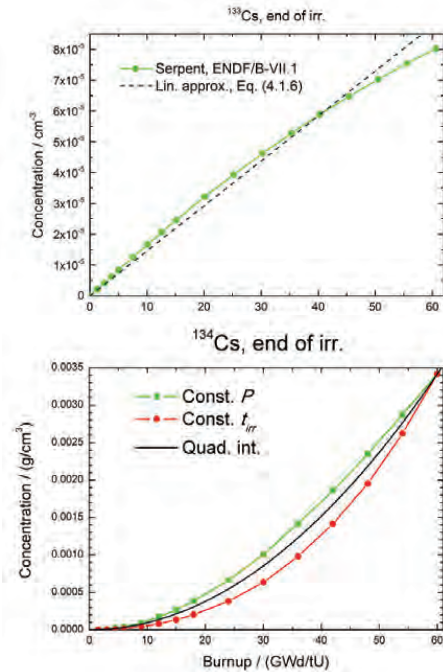
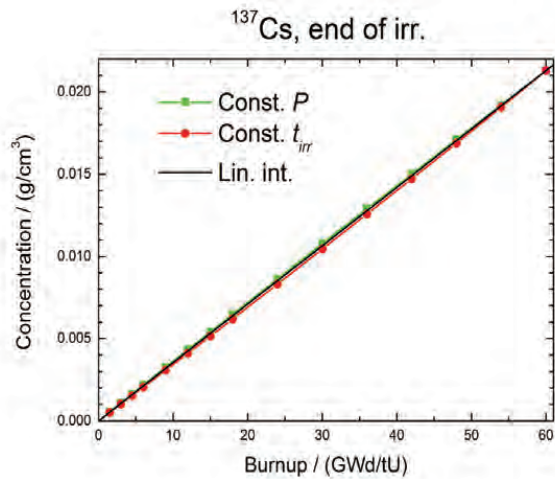
Main production root of  $^{244}\text{Cm}$  is a sequence of

- (n,  $\gamma$ ) reactions (6)

-  $\beta^-$  decays (4)



## Production of Cs isotopes



## Conclusions

- NDA: powerful tool for SNF characterisation
- Few nuclides contributing to NDA observables at a fixed cooling time
- NDA observables are very sensitive to moderator temperature (density)
- Both deterministic and stochastic codes give consistent results for SNF
- Importance of nuclear data and neutron detection for SNF characterisation
- BU/irradiation time dependence of some nuclides described by simple analytical functions

## **5.8 Impact of Some 3-D Modelling Effects on the Spent Fuel Characterization; 31th Spent Fuel Workshop; 19 – 21/10/2022**

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## Impact of Some 3-D Modelling Effects on the Spent Fuel Characterization



Marjan Kromar, Dušan Čalič  
„Jožef Stefan“ Institute, Slovenia



31<sup>st</sup> Spent Fuel Workshop

Barcelona, October 19-21, 2022



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### Content

- Introduction/motivation
- 3-D case
- Impact of the fuel grids
- Fuel segmentation – real case
- Conclusions



## Introduction/motivation

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- Spent fuel characterization:
  - Reactor core simulators such as VERA-CS and CASMO5/SIMULATE/SNF, where detail observables distributions are obtained directly from the 3-D reactor core depletion.
  - Codes capable of specific 2-D or 3-D depletion on the fuel assembly level, such as TRITON/NEWT from the SCALE package or the Monte Carlo code Serpent2.

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## Introduction/motivation

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- The first approach is more straightforward, but requires significant computer resources.
- For industrial applications, the second approach is more commonly used.
- In this approach, the fuel assemblies are divided into few independent regions (domains), which leads to additional uncertainties resulting from this process.
  - Spectral end-effects are not accounted for.
  - In domains the average fuel input parameters such as the fuel burnup, temperature, moderator density, etc. are used.
  - However, characterization observables (decay heat) do not depend linearly on the input parameters. Therefore, the segmentation of the fuel has a noticeable effect on the accuracy of the whole process.

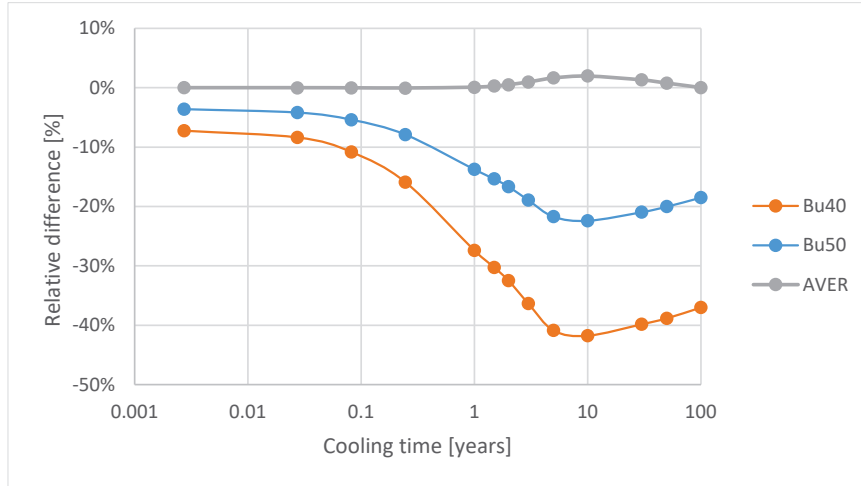
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Introduction/motivation

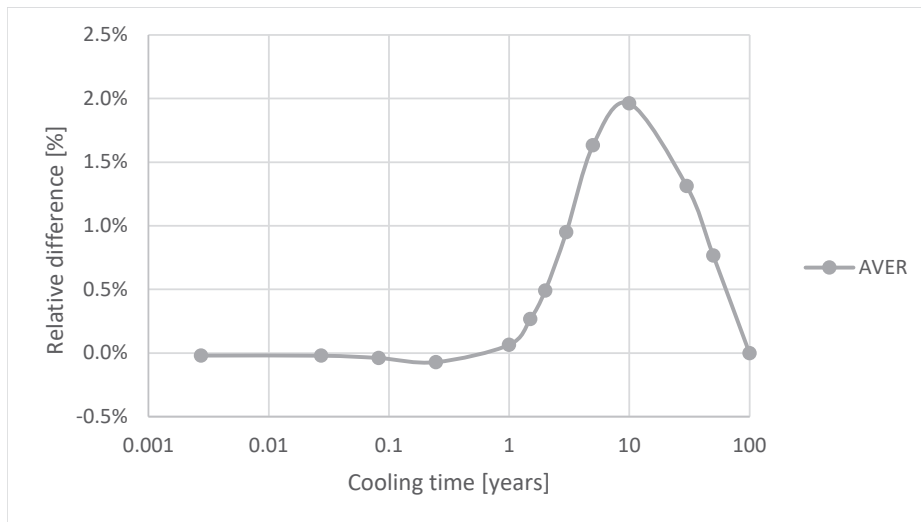
NPP Krško, Westinghouse 2-loop PWR, 16x16 fuel



Impact of the fuel burnup on the decay heat (relative difference to the 60 MWd/kgU, averaging process)



Introduction/motivation

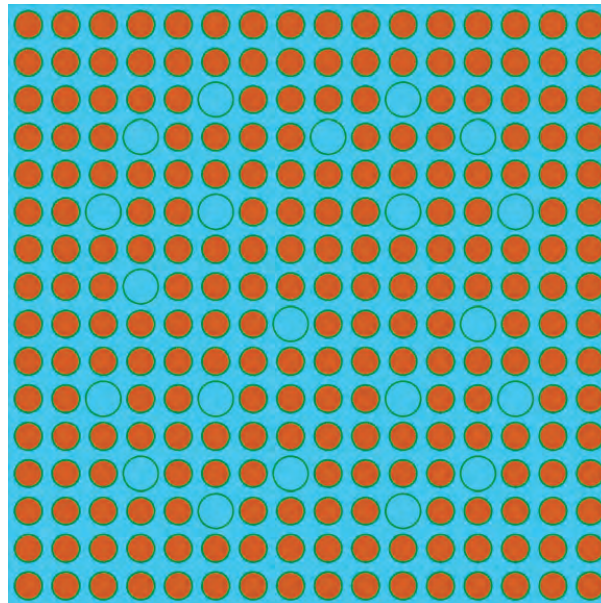
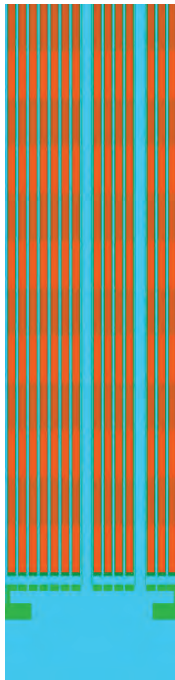


Deficiency of the ±10 MWd/kgU averaging process



3-D case

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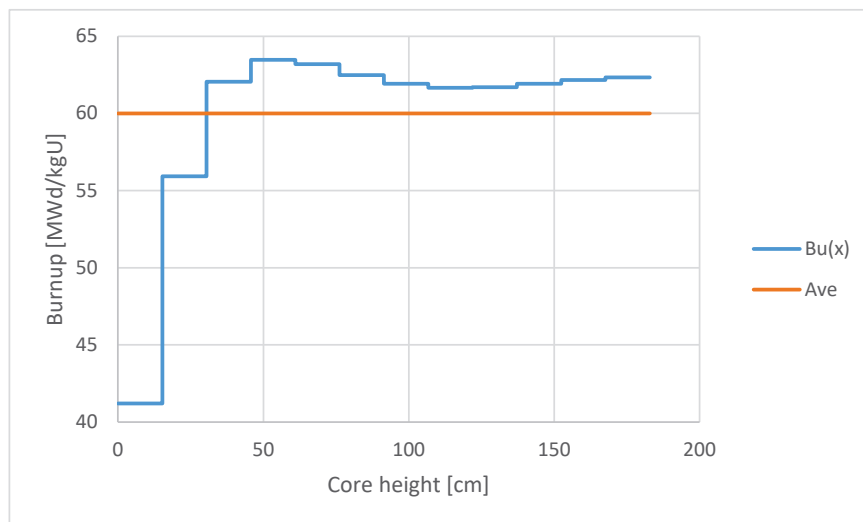


Geometry (16×16, 12 axial layers)



3-D case

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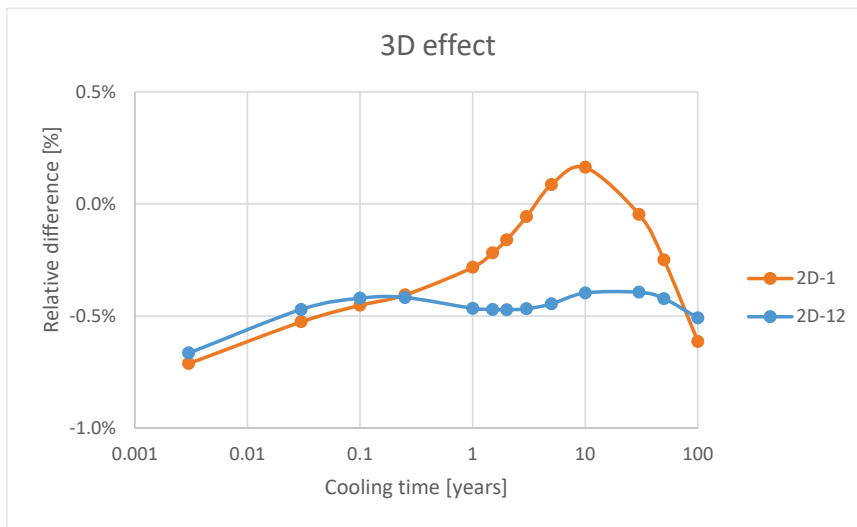
Burnup profile after irradiation of 60 MWd/kgU at averaged HFP conditions





3-D case

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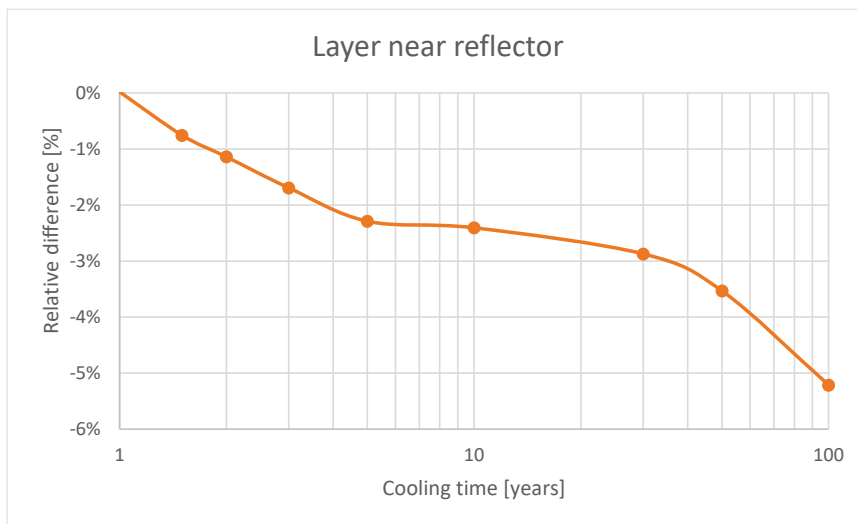


Decay heat relative difference (3-D vs. various 2-D)



3-D case

10/21



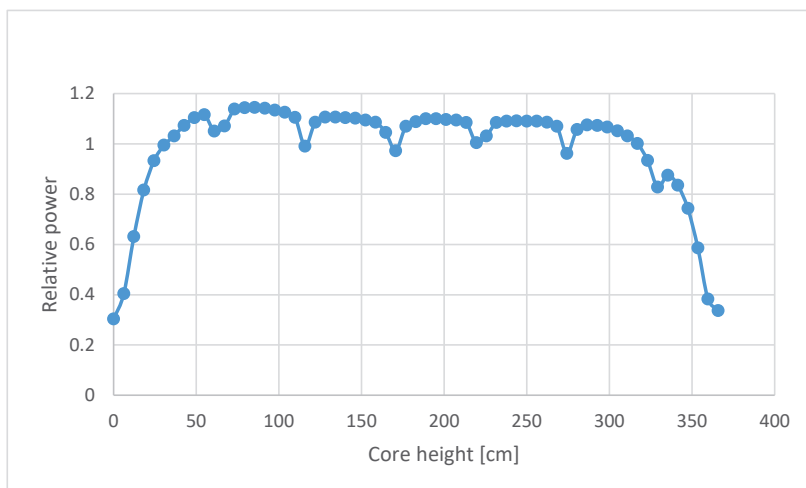
Decay heat relative difference in the layer closest to the axial reflector (3-D vs. 2-D)



## Grid impact

11/21

- The effect of the NPP Krško Inconel-718 grids on the decay heat was investigated



Effect of the grids on the power distribution

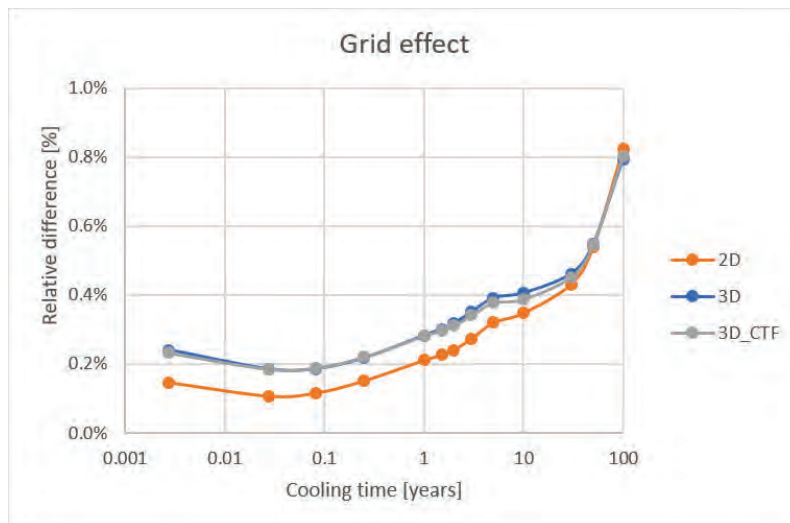
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## Grid impact

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Effect of the grids on the decay heat

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## Grid impact

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- The total grid impact is less than 1 %.
- 2-D and 3-D approaches give very similar results confirming suitability of the axial smearing approximation.
- Impact of power feedback effects is negligible.

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## Fuel segmentation – real case

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- NPP Krško fuel - ~1400 fuel assemblies
- Operational database (Bu, T, P ...) available on 10 axial layers from CORD-2 simulator
- Relative thicknesses (1, 1, 2, 4, 4, 4, 4, 2, 1, 1), where the unit is 15,24 cm (6 inch)
- The most accurate approach would be to take all 10 axial regions treated in FA database explicitly.
- However, such approach is time consuming. It would take more than 3 years of the CPU time to calculate 1400 FAs with the TRITON/NEWT sequence. Even ORIGAMI would require several days of calculation.
- Some kind of homogenization is therefore necessary.

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## Fuel segmentation – real case

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- Fuel segmentation process should correctly represent axial profiles.
- It seems natural to explore axial blankets first, since there are large material heterogeneities and large flux gradients present.
- To get a proper feeling, a few typical cases have been evaluated:
  - A – standard FA without axial blankets (cycles 1-7)
  - B – FA with natural uranium axial blankets (cycles 7-16)
  - C – FA with slightly enriched annular axial blankets (from cycle 16 onward)

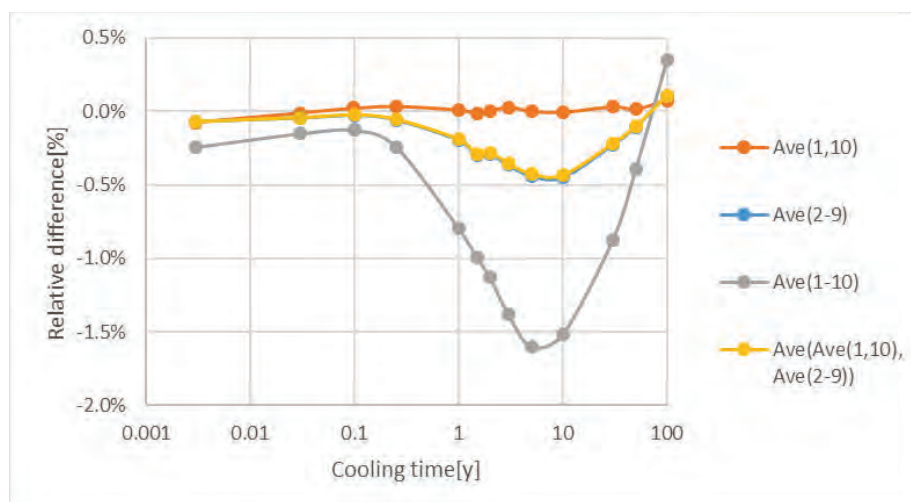
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## Fuel segmentation – real case

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Impact of the homogenization on the decay heat – case A

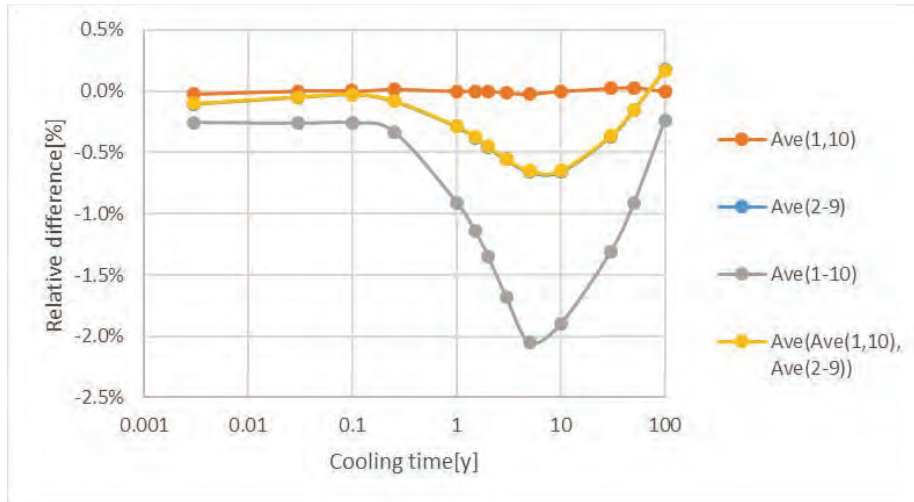
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### Fuel segmentation – real case

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### Impact of the homogenization on the decay heat – case B

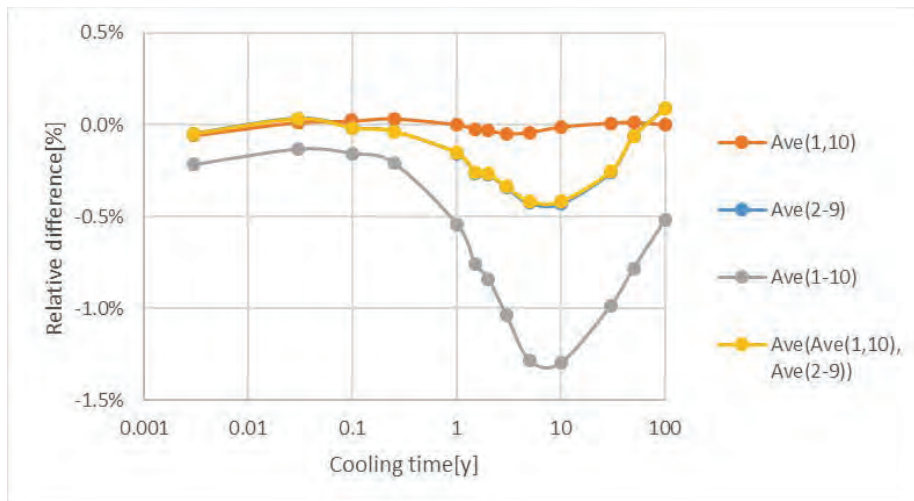
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### Fuel segmentation – real case

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### Impact of the homogenization on the decay heat – case C

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## Conclusion

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- Differences between 3-D and 2-D computational models were evaluated.
- Sufficiently fine fuel segmentation can preclude discrepancies coming from the averaging process.
- To properly account spectral end-effects 3-D approach is needed.
- Impact of the Inconel grids can be covered by the material smearing in axial direction.
- A few FA cases based on the real data have been analyzed to demonstrate reasonable axial discretization.

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## Acknowledgements

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**Thank you for your attention!**

**Questions?**

**5.9 Burnup credit application in CONSTOR SNF cask criticality analysis for RBMK-1500 fuel; R. Plukiene, FTMC; 31th Spent Fuel Workshop; 19 – 21/10/2022**





FIZINIŲ IR  
TECHNOLOGIJOS MOKSLŲ  
CENTRAS

## Burnup credit application in CONSTOR SNF cask criticality analysis for RBMK-1500 fuel

V. Barkauskas, R. Plukienė and A. Plukis

Center for Physical Sciences and Technology,  
Department of Nuclear Research,  
Vilnius, Lithuania

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## Content



- Current status - Lithuania
- Criticality safety and Burnup credit application
- Modeling of RBMK fuel composition
- CONSTOR RBMK-1500/M2 cask  $k_{\text{eff}}$  calculations
- Results and burnup credit application possibilities

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# Current status: Ignalina NPP



**Location:** Far north-east corner of Lithuania. Immediately bordering Latvia and Belarus



**Design:** 2 × RBMK-1500 water-cooled, graphite-moderated channel-type power reactors



**Capacity:** Intended to supply NW region of former USSR (not Lithuania). After independence, one unit could produce 80% of Lithuanian electricity demand



**Operation:**  
 Unit 1 commissioned Dec 1983 / closed Dec 2004  
 Unit 2 commissioned Aug 1987 / closed Dec 2009

<https://am.lrv.lt/uploads/am/documents/files/INPP%2BDecom%2B2021-04-12eng.pdf>

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# Current status: SNF



Spent nuclear fuel

Fuel Assemblies

21,571 item



- By now storage of SNF is realized at interim storage facility at Ignalina NPP site for 50 years:
  - ✓ #1 SNF storage contains 118 containers works from 1999;
  - ✓ #2 SNF storage facility for ~200 containers started at 2020 (146 stored already).

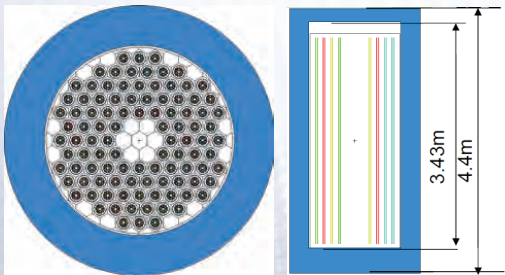


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# Current status: SNF storage casks



- 3 types of SNF storage casks (GNB (Germany)) are used:
  - ✓ CASTOR (metal)
  - ✓ CONSTOR (reinforced concrete)
  - ✓ New type CONSTOR RBMK-1500/M2 with 80% increased capacity for RBMK-1500 SNF



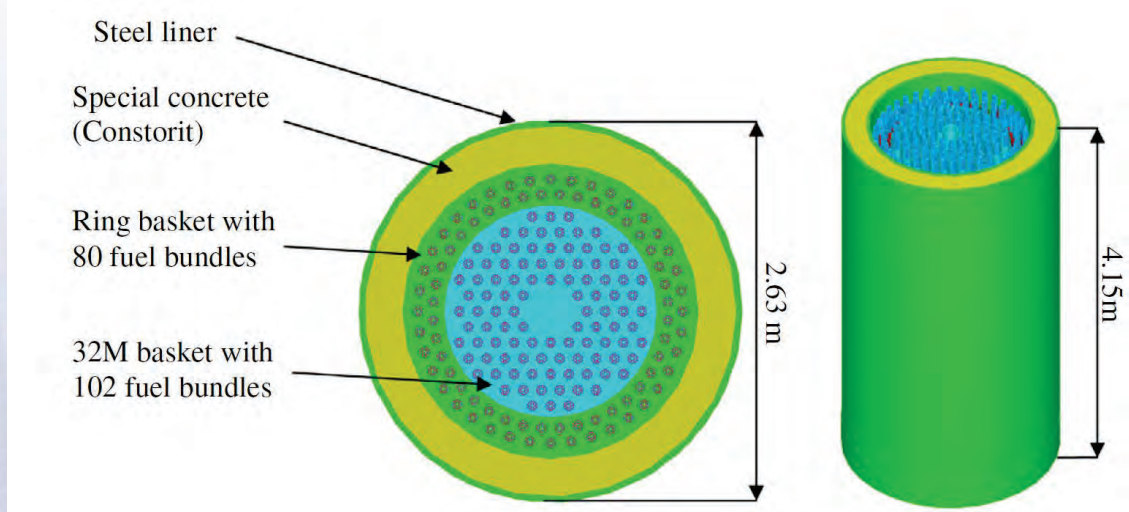
MCNP model of CASTOR container: 102 half-assemblies bundles

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# CONSTOR M2/RBMK-1500 cask



- transport and storage container CONSTOR M2/RBMK-1500 consist of: cylindrical basket 32M (stainless steel) and 454 mm thick ring basket (made of aluminum alloy)
- Modeling of accident scenario: H<sub>2</sub>O in all cavities, FA standard (design) configuration.



SCALE 6.1 model of CONSTOR® RBMK-1500/M2 SNF cask

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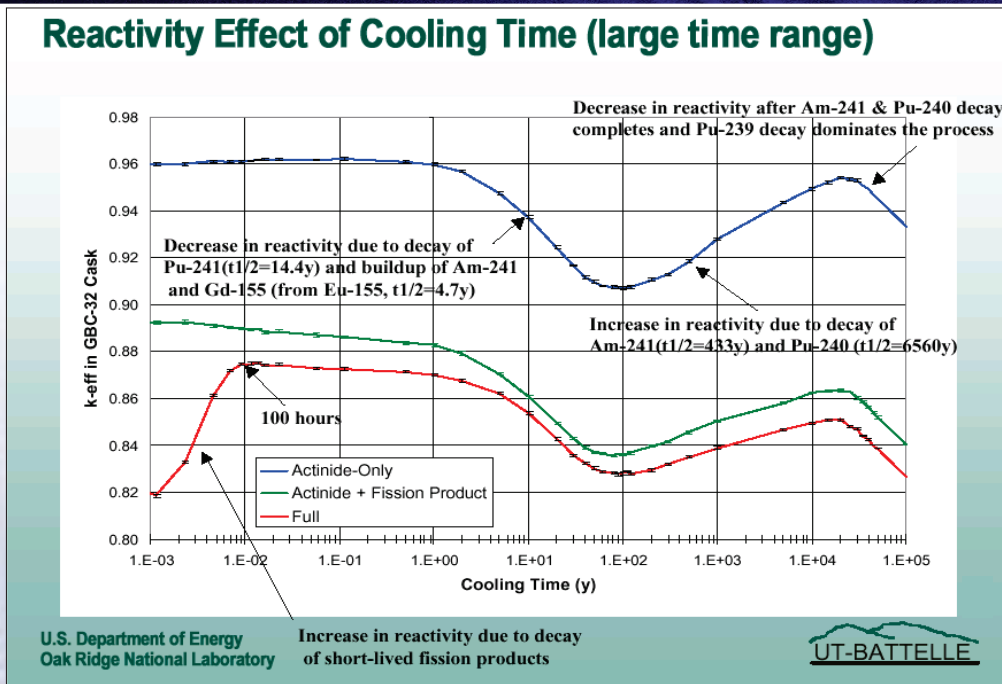
# Criticality safety



- According to the Lithuanian national regulations the  $k_{eff}$  shall not exceed 0.95 during normal operation and postulated accident scenarios.
- Goal : to ensure sub-criticality of system with fissile materials ( $k_{eff} < 0.95$ )
- Fissile isotopes –  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ ,  $^{241}\text{Pu}$ , etc.
- Safety justifications are based on conservative assumption of fresh fuel
- In case of different SNF burnup, the conservatism may be too high -> the cost of storage systems increases
- Burn-up credit (BUC) approach calculations takes into account the reduced SNF reactivity due to depletion of fissile isotopes and accumulation of neutron absorbing isotopes during fuel burn-up

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**Example: Reactivity behavior in the GBC-32 cask as a function of cooling time for fuel with 4.0%  $^{235}\text{U}$  initial enrichment and 40 GWd/MTU burnup**



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Ref. [NRC-2012-0100]

# K<sub>eff</sub> calculation assumptions



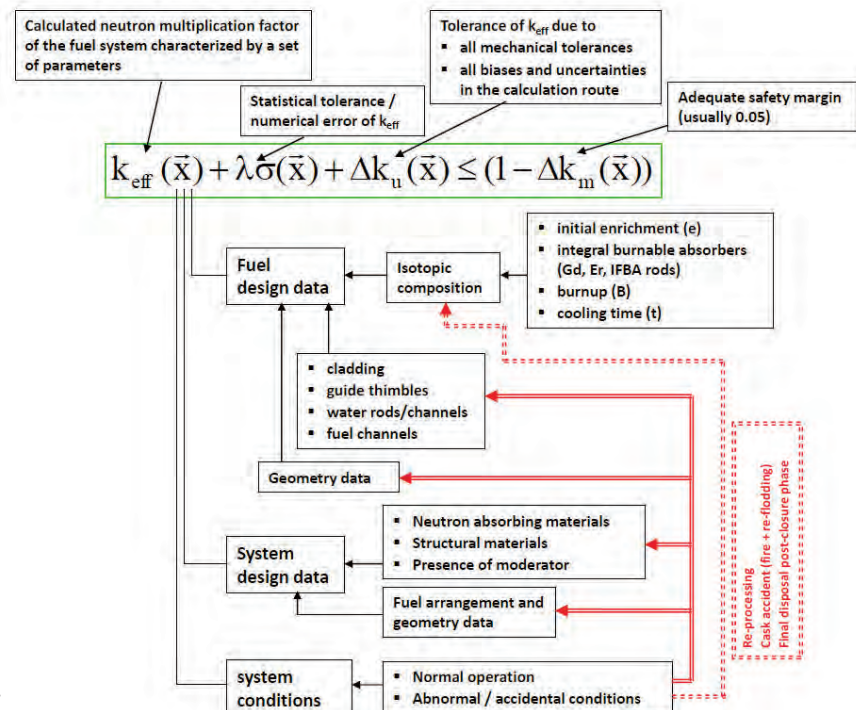
- SCALE6.1: STARBUCKS (ORIGEN-ARP, CENTRM, KENO VI, ENDF/B-VII.0 238 energy group data library),
- Mirror boundary conditions were applied for 2.64-2.64 4.52m cask surrounding cuboid.
- A triangular pitch of 125 mm between fuel bundles (centered in its position tube of 102 mm outer diameter with 2 mm thick wall).
- 2.0% and 2.8% <sup>235</sup>U enrichment RBMK fuel mixture composition and 0 (fresh fuel assumption) – 22.5 GWd/tU burn-up
- 5 years cooling time was used
- horizontal burn-up profile uniform but axial burn-up profile taken into account : “end-effect” – slightly higher criticality for the upper fuel bundle profile due to water density varying from 0.8 to 0.2 g/cm<sup>3</sup>.
- uniform water density distribution from 0.1 to 1.0 g/cm<sup>3</sup>
- conservative uniform temperature of 100°C (conservative accident scenario)

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# K<sub>eff</sub> evaluation for BUC



Ref.[IAEA-TECDOC-1241]



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## Burnup credit calculation



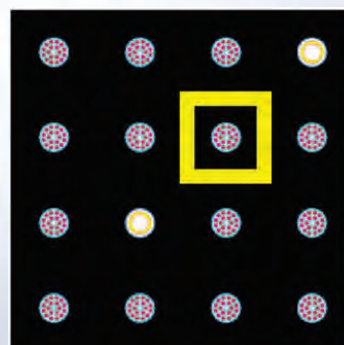
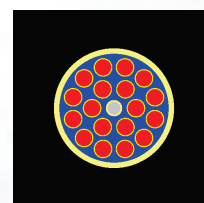
- Actinide-only approach: fuel with most important actinides ( $^{234-236}\text{U}$ ,  $^{238}\text{U}$ ,  $^{238-242}\text{Pu}$ ,  $^{241-243}\text{Am}$ ,  $^{237}\text{Np}$ ) were included in keff calculation
- Fission product case for BUC additionally includes:  $^{95}\text{Mo}$ ,  $^{99}\text{Tc}$ ,  $^{101}\text{Ru}$ ,  $^{103}\text{Rh}$ ,  $^{109}\text{Ag}$ ,  $^{133}\text{Cs}$ ,  $^{143}\text{Nd}$ ,  $^{145}\text{Nd}$ ,  $^{147}\text{Sm}$ ,  $^{149-152}\text{Sm}$ ,  $^{153}\text{Eu}$ ,  $^{155}\text{Gd}$  and  $^{166-168}\text{Er}$ ,  $^{170}\text{Er}$ .

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## RBMK SNF - Pre-generated ARP libraries for fast burn-up inventory modeling



- ~7 m length fuel assembly with 18 fuel elements
- 14 fuel assemblies and 2 control rods segment with infinitive lattice approach
- SCALE6.1:
  - TRITON with NEWT ir ORIGEN-S
  - ORIGEN-ARP (Automatic Rapid Processing)
  - ENDF/B-VII nuclear data library
  - One group cross-section libraries for non-erbium fuel with 2 % enrichment and 2.4 % (with 0.41 % mass of  $\text{Er}_2\text{O}_3$ ), 2.6 % (0.5 %  $\text{Er}_2\text{O}_3$ ) and 2.8 % (0.6 %  $\text{Er}_2\text{O}_3$ ) enrichment fuel



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# Validation of RBMK SNF one group cross-section libraries



## Very few experimental data:

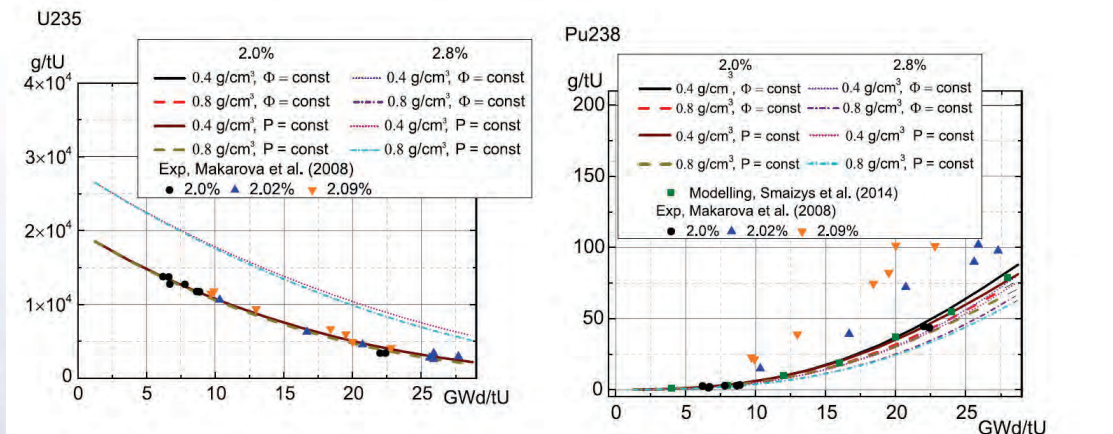
- KORENKOV, A. G., et al. Destructive Analysis Determination of Neutron Emission from Spent RBMK Fuel, Atomic Energy, 2002, Vol. 93, No. 4, p. 815-822 (only some of actinides present in 22 2% of samples)
- MAKAROVA, T. P., et al. Destructive Analysis of the Nuclide Composition of Spent Fuel of WWER-440, WWER-1000, and RBMK-1000 Reactors, Radiochemistry, 2008, Vol. 50, No. 4, p. 414-426. (2% enrichment fuel, only two burnup cases)

### Modeling of RBMK fuel:

- Plukienė, R., et al., Numerical sensitivity study of irradiated nuclear fuel evolution in the RBMK reactor, Lithuanian journal of physics. ISSN 1648-8504. Vol. 49, no. 4 (2009), p. 461-469
- Šmaižys, A., et al. Numerical modelling of radionuclide inventory for RBMK irradiated nuclear fuel, Nuclear Engineering and Design, 2014, Vol. 277, p. 28–35.

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# Validation of nuclear data libraries (1)



- The comparison shows an acceptable agreement between the values obtained using created one-group cross-section libraries and experimental data as well as point depletion calculations.
- The exception was observed only for <sup>238</sup>Pu, which was caused by the initial composition of nuclear fuel (most probably presence of <sup>236</sup>U the parent nuclide of <sup>237</sup>Np which is obtained through the activation)

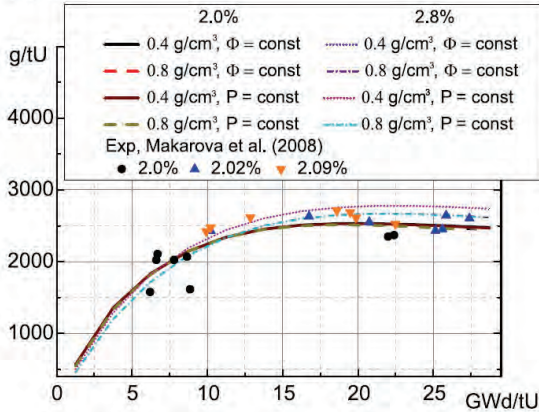
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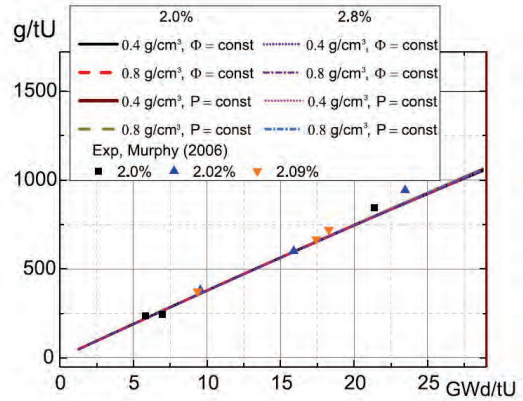
# Validation of nuclear data libraries (2)



Pu239



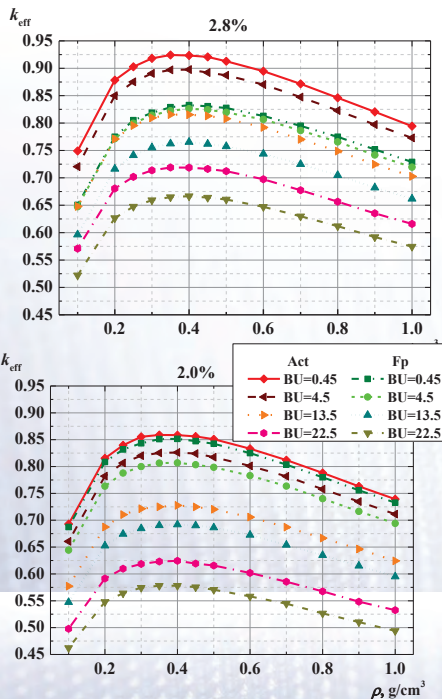
Cs137



- Agreement of the experimental data and the calculated values is satisfactory for other plutonium isotopes – the difference between the experimental and calculated values is 5–6% for <sup>239</sup>Pu, 5–25% (the highest difference for low burn-up) for <sup>240</sup>Pu, 5–15% for <sup>241</sup>Pu and 5–19% for <sup>242</sup>Pu, as well as for FP (<sup>137</sup>Cs).
- At the highest modelled burn-up (29 GWd/tU) the isotopic composition differences between 2 and 2.8% enrichment fuel burn-up for actinides important to BUC applications vary from 11 to 52%

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## $k_{eff}$ as a function of water density in the CONSTOR® RBMK-1500/M2 storage cask (1)



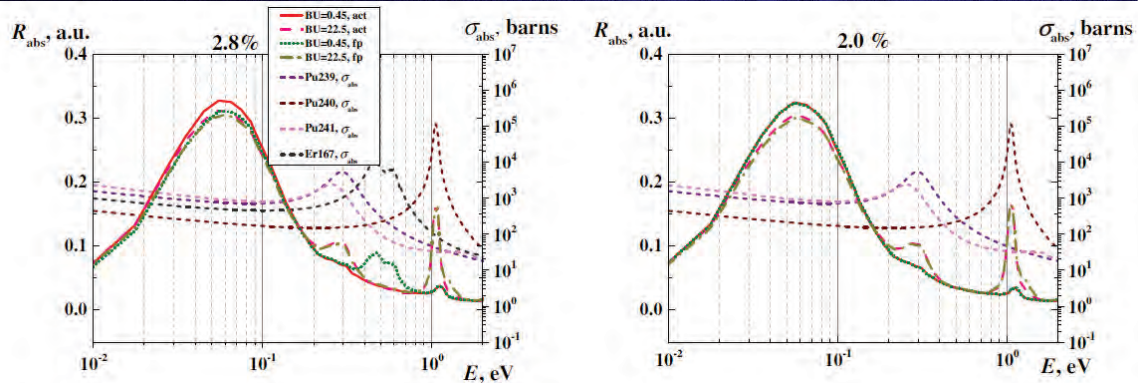
$k_{eff}$  as a function of water density inside SNF cask cavities for various burn-up 2.8% and 2.0% enrichment fuel taking into account actinide-only (Act) and fission products (Fp) including burnable absorber erbium

Most critical conditions region is identified: 0.3-0.5 g/cm<sup>3</sup> water density inside CONSTOR.

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### Neutron absorption rate (R) spectra inside CONSTOR® RBMK-1500/M2 storage cask (2)



Neutron absorption rate ( $R \sim \Phi \cdot \sigma_{abs}$ ) spectra inside SNF cask in case of 0.35 g/cm<sup>3</sup> water density for 2.8% and 2.0% enrichment fuel. Pu neutron absorption cross sections on the right for information.

Most critical conditions: low burn-up (0.45 GWd/tU) SNF.

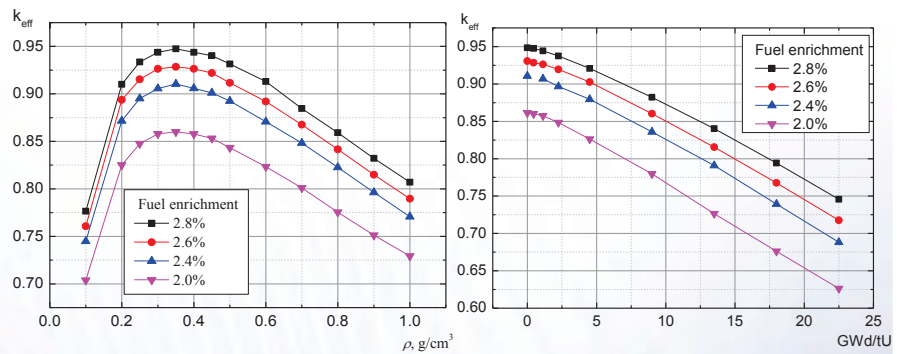
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### Isotopic composition differences for 2% and 2.8% enrichment SNF at CONSTOR® RBMK-1500/M2 storage cask (3)



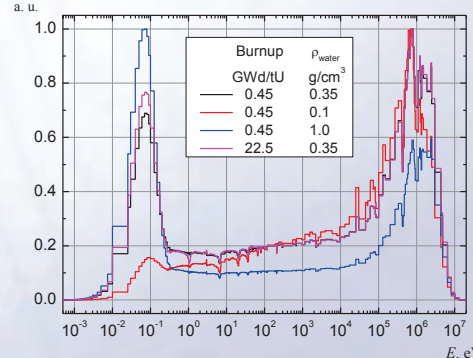
Isotopic composition differences for actinides between 2% and 2.8% enrichment fuel at 29GWd/tU burn-up

Nuclide	$(N_{2.8} - N_{2.0}) / N_{2.8}$
<sup>234</sup> U	32%
<sup>236</sup> U	23%
<sup>238</sup> Pu	-28%
<sup>239</sup> Pu	-11%
<sup>240</sup> Pu	-15%
<sup>241</sup> Pu	11%
<sup>242</sup> Pu	-36%
<sup>237</sup> Np	15%
<sup>241</sup> Am	-40%
<sup>243</sup> Am	-52%
<sup>242</sup> Cm	-27%
<sup>244</sup> Cm	-60%



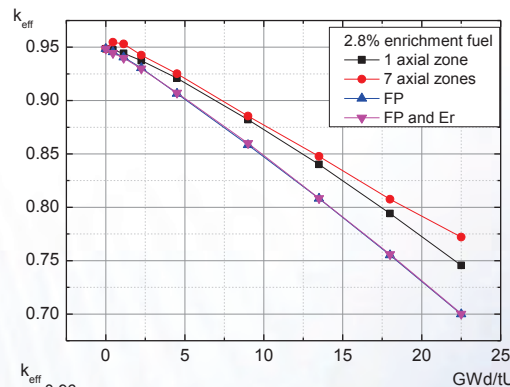
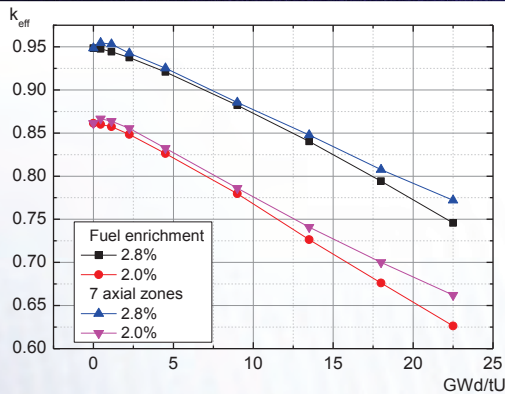
Most critical conditions: high enrichment (2.8%), low burn-up (0.45 GWd/tU) of SNF and 0.3-0.5 g/cm<sup>3</sup> water density.

Neutron spectra for 2.8% enrichment fuel at low 0.45 GWd/tU burn-up at different water density in the cask.



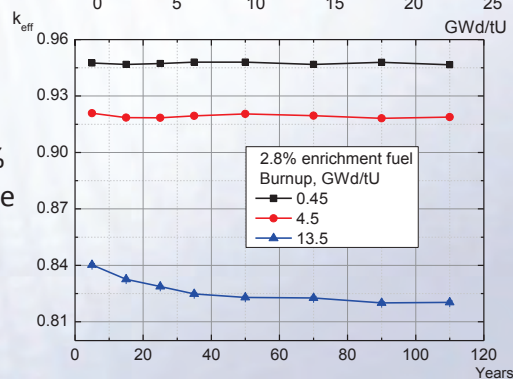
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## $k_{eff}$ calculations of 2.8% enrichment RBMK-1500 SNF at CONSTOR® RBMK-1500/M2 storage cask (4)



The marginal cases: less reactive 2.0% enrichment and most reactive case (2.8% enrichment, multiple ( $z=7$ ) zones, actinide only case) was analyzed more exactly.

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## Conclusions



- Criticality calculations of CONSTOR® RBMK-1500/M2 storage cask were performed using pre-generated ORIGEN-ARP SNF libraries and STARBUCKS BUC evaluation tool from SCALE 6.1 code package.
- Worst condition  $k_{eff}=0.924 \pm 0.003 (>0.95)$  with 2.8%  $^{235}\text{U}$  SNF enrichment using actinides only approach at 0.45GWd/tU. In case of FP and Er  $k_{eff}$  decreases due to  $^{167}\text{Er}$ , which burns at higher burnups.
- $k_{eff}=0.859$  of 2.0%  $^{235}\text{U}$  SNF enrichment fresh fuel is due to less fissile material.
- Non-uniform uranium depletion is responsible for end effect in RBMK-1500 SNF whereas build-up of plutonium has no significant effect.
- Most critical conditions region is identified: 0-3 GWd/tU burn-up fuel and 0.3-0.5 g/cm<sup>3</sup> water density inside SNF.

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Thank you for attention!

#### **ACKNOWLEDGEMENTS**

This work was performed as part of WP8 Spent Fuel Characterization and Evolution Until Disposal (SFC) of Euratom research and training programme 2018-2020 under grant agreement No 847593 to fulfill the objective to provide contributions to operational safety concepts for fuel handling at SNF packaging facilities by using state-of-the-art characterization techniques for spent nuclear fuel during its evolution from reactor unloading until disposal.

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## 6. Participation to an Event other than a Conference or a Workshop

- Effect of modelling parameters on calculated PWR spent fuel observables; G. Žerovnik, JRC; Serpent User Meeting 2020; 29/10/2020
- Fuel properties characterisation and related uncertainty analysis: overview, status and planning; P. Schillebeeckx, JRC Geel; 1st research coordination meeting on the CRP on spent fuel characterisation; 06 - 10/12/2021
- Neutron resonance analysis and applications to material characterisation; P. Schillebeeckx, JRC Geel; LANL P/T Colloquium, April 2022; 28/04/2022
- Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten LWR-Brennstoffproben; R. Dagan, T. König et al., KIT; BGZ Studierendentag; 05 – 06/05/2022
- SFC Task 2: Fuel properties characterisation and related uncertainty analysis (summary and status); P. Schillebeeckx, JRC Geel; IAEA CRP spent fuel characterization ; 22 – 23/09/2022
- Performance assessment and uncertainty evaluation of the clab calorimeter; P. Schillebeeckx, JRC Geel; WPNCS Subgroup 12 meeting; 01/12/2022

**6.1 Effect of modelling parameters on calculated PWR spent fuel observables; G. Žerovnik, JRC; Serpent User Meeting 2020; 29/10/2020**

# Effect of modelling parameters on calculated PWR spent fuel observables

G. Žerovnik, D. Čalič, L. Fiorito, A. Hernandez Solis, B. Kos, M. Kromar, P. Romojaro, A. Stankovskiy

EC-JRC Geel, Retieseweg 111, B-2440 Geel  
SCK•CEN, Boeretang 200, B-2400 Mol  
Jožef Stefan Institute, Jamova cesta 39, SI-1000 Ljubljana

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## Modelling uncertainties

- Modelling, computational, numerical?
- Uncertainties, biases, errors?
- Types of modelling uncertainties?



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## Modelling uncertainties: Monte Carlo vs. deterministic

### Monte Carlo n. transport

- Continuous energy
- Continuous direction
- Continuous time (e.g. for n. kinetics)
- Space continuum (particle tracking)
- Counting statistics from n. history

### Deterministic n. transport

- Energy intervals (multi-group)
- Solid angle discretization ( $S_n$ ) or polynomial expansion ( $P_n$ )
- Discretization of the time variable
- Discretization of the spatial variables
- „Exact“ solution (except round-off)



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- **Apart from counting statistics, are there any other sources of numerical error in continuous energy MC particle transport codes?**



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- Discretization of the spatial variables
- „Exact“ solution (except round-off)

- **Apart from counting statistics, are there any other sources of numerical error in continuous energy MC particle transport codes?**

- **YES:**

- **Discretization of thermal scattering data** (e.g. Serpent 2.1.29 → fixed in 2.1.32)
- **Ignoring Doppler Broadening Rejection Correction (DBRC)** (e.g. MCNP)
- **Energy release per fission proportional to atomic mass** (e.g. Serpent before v. 2.1.31)
- **etc.**



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## Modelling uncertainties: depletion vs. n. transport

### MC neutron transport

- Continuous energy
- Continuous direction
- Continuous time (e.g. for n. kinetics)
- Space continuum (particle tracking)
- Counting statistics from n. history

### Material depletion by n. irradiation

- Reaction rates from continuous  $E$
- Not needed for depletion ( $4\pi$  int.)
- Depletion time steps
- Depletion geometric zones
- Counting statistics from n. history

### Additional modelling uncertainties:

- Model simplifications (e.g. 2D)
- Physical approximations (e.g. no DBRC)
- Energy deposition model (fission; all n reactions;  $n+\gamma$ )



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## Types of modelling uncertainties

- Counting statistics
- **Discretization**
  - Independent variables
  - Conditions (e.g. temperature, density)
- Physical approximations
- Simplifications (e.g. 3D→2D, boundary conditions)
- Round-off (negligible in double precision for well-conditioned problems)



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## Discretization parameters

### Independent variables:

- Irradiation time steps:
  - Depletion solver (i.e. mathematical method used to solve Bateman equations)
  - Implicit/explicit
  - Interpolation/extrapolation scheme
  - Substeps
- Depletion geometrical zones:
  - Radial zones within pin (to model „rim effect“)
  - Pins grouped in separate zones (to account for asymmetry, e.g. due to boundary conditions)
  - Axial zones (in 3D model or 2D slices with different irradiation conditions)
  - Azimuthal regions within pin (not studied, probably negligible effect?)

### Conditions:

- Fuel temperature profiles: radial, axial (negligible)
- Moderator axial density and temperature profiles



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## SNF observables

Main studied observables:

- Decay heat rate :  $H$
- Neutron emission rate :  $S_n$
- $\gamma$ -ray emission rate :  $S_\gamma$

Possible to measure, but different difficulties...

- ⇒ Determined/estimated by **theoretical calculations**
- ⇒ Summation formula starting from **nuclide vector**

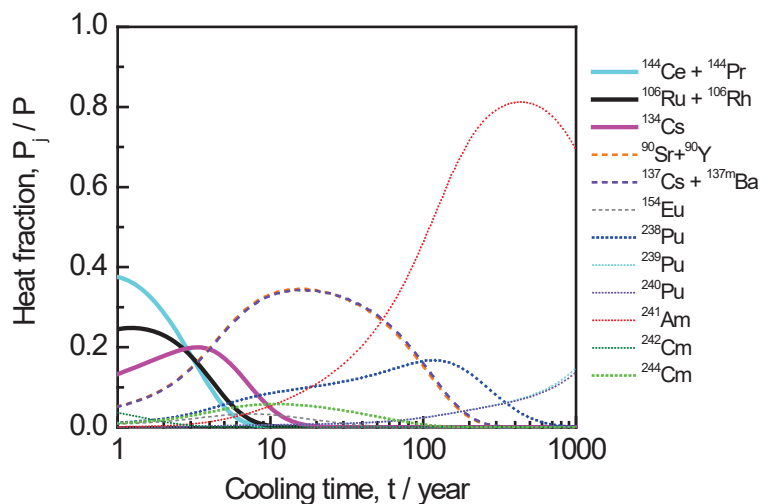


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## Decay heat of SNF: main contributing nuclides

Decay heat rate:  $H(t) = \sum_j H_j(t)$

- $1 \text{ a} \leq t_c \leq 10 \text{ a}$ 
  - $^{144}\text{Ce} / ^{144}\text{Pr}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
  - $^{134}\text{Cs}$
  - $^{90}\text{Sr} / ^{90}\text{Y}$  &  $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
- $10 \text{ a} \leq t_c \leq 100 \text{ a}$ 
  - $^{90}\text{Sr} / ^{90}\text{Y}$  &  $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{238}\text{Pu}$
  - $^{241}\text{Am}$
  - $^{244}\text{Cm}$
- $100 \text{ a} \leq t_c \leq 1000 \text{ a}$ 
  - $^{241}\text{Am}$
  - $^{238}\text{Pu}$
  - $^{239,241}\text{Pu}$



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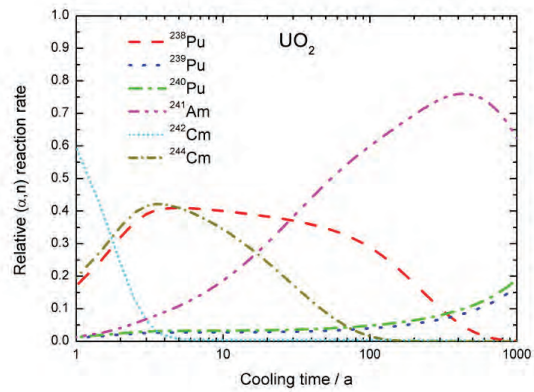
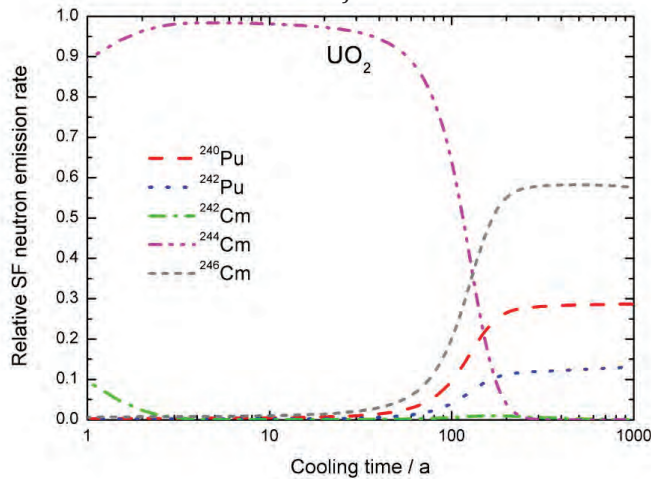
## Neutron emission of SNF: main contributing nuclides

Neutron emission rate:

$$S_n(t) = \sum_j S_{n,j}(t)$$

Contribution from SF dominating!

- for cooling time < 100 a, ( $\alpha, n$ ) rate at least 10× lower than SF n. emission rate



$S_n(t) \Rightarrow$  sensitive to  $^{244}\text{Cm}$  production



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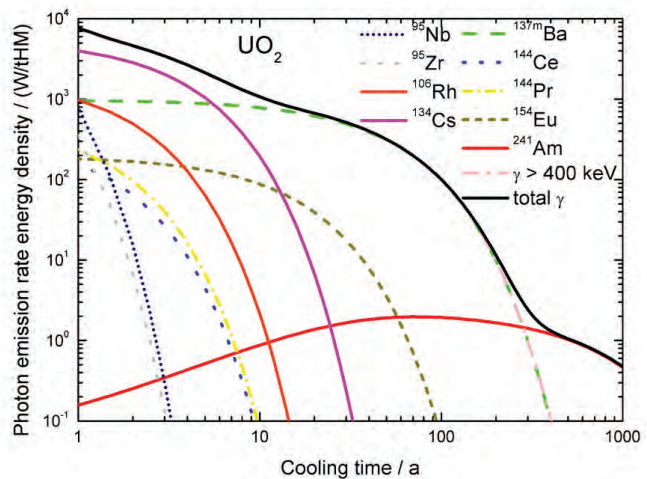
## $\gamma$ -ray emission by SNF: main contributing nuclides

Photon emission rate energy density:

$$H_\gamma(t) = \sum_j H_{\gamma,j}(t) = \sum_j N_j(t) \lambda_j E_{\gamma,j}$$

= Contribution of  $\gamma$ -rays to decay heat

- $1 \text{ a} \leq t_c \leq 10 \text{ a}$ 
  - $^{134}\text{Cs}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{106}\text{Ru} / ^{106}\text{Rh}$
- $10 \text{ a} \leq t_c \leq 300 \text{ a}$ 
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$
  - $^{154}\text{Eu}$
  - $^{241}\text{Am}$
- $300 \text{ a} \leq t_c \leq 1000$ 
  - $^{241}\text{Am}$
  - $^{137}\text{Cs} / ^{137\text{m}}\text{Ba}$



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## Definition of the study case

2D PWR 17×17, Zircaloy-4, 4% enriched UO<sub>2</sub> fuel, 4 × 300 d fuel cycles, cooling periods 30 d. Fuel radius 4.095 mm, clad inner/outer radii 4.18/4.75 mm, rod pitch 12.6 mm.

### Simplified operating conditions:

- Power levels 50, 50, 40 and 30 MW/tHM during each cycle.
- Coolant density 0.655 kg/cm<sup>3</sup>, constant boron level 800 ppm.
- Fuel density (95% theoretical density): 10.4 g/cm<sup>3</sup>.
- Constant T: fuel and gap: 900 K; coolant and cladding: 600 K.

### Numerical approximations (ref. model):

- 4 equi-volume radial depletion zones
- Time steps per cycle: 1 d, 10 d, 14 d, 3 × 25 d, 2 × 50 d
- reflective boundary conditions

Code: **Serpent** (v2.1.29/30)

Nuclear data library: ENDF/B-VII.1



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## Counting statistics: nuclide vector at cooling time 5 a

No. of neutron histories:  $2.5 \times 10^6$  (5000 n. in 500 active cycles)

Count. stat. unc.: estimated from **50 runs** with different random seeds

Nuclide	$c_0/(g/tHM)$	$\sigma_c/c_0$	Nuclide	$c_0/(g/tHM)$	$\sigma_c/c_0$
<sup>90</sup> Sr	678.56 (2)	0.003%	<sup>238</sup> Pu	426.44 (18)	0.04%
<sup>133</sup> Cs	1621.7 (1)	0.01%	<sup>239</sup> Pu	6747.4 (18)	0.03%
<sup>134</sup> Cs	43.86 (2)	0.04%	<sup>240</sup> Pu	3065.2 (13)	0.04%
<sup>137</sup> Cs	1638.0 (0)	0.001%	<sup>241</sup> Pu	1556.7 (6)	0.04%
<sup>148</sup> Nd	567.92 (6)	0.01%	<sup>242</sup> Pu	970.92 (30)	0.03%
<sup>235</sup> U	7109.9 (14)	0.02%	<sup>241</sup> Am	499.66 (17)	0.03%
<sup>238</sup> U	920116 (4)	0.0004%	<sup>244</sup> Cm	109.38 (8)	0.08%



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## Depletion zone discretization: pin level, radial

- Burn card: equi-volume
- Div card: equi-thickness
- Manual: 2 zones to study the ring effect

No. of radial zones	1	2	4 (ref.)	6	8	10	1+1 (ring)
<sup>244</sup> Cm / ref.	0.984	0.994	1	0.999	1.002	1.002	0.997
<sup>241</sup> Am / ref.	1.002	1.000	1	1.000	1.000	1.000	1.001
<sup>239</sup> Pu / ref.	1.005	1.002	1	1.000	0.999	1.000	1.001



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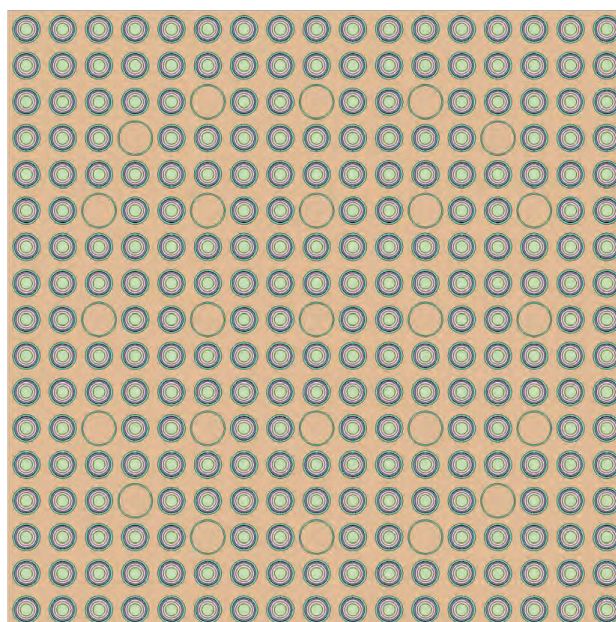
## Depletion zone discretization: assembly level; boundary conditions

### Reference model:

- 17 × 17 pins
  - 264 equal fuel pins
  - 25 empty positions (for CR)
- All pins grouped in a single depletion zone
- 4 radial (equi-volume) zones
- Reflective boundary conditions

### Separate pin treatment study:

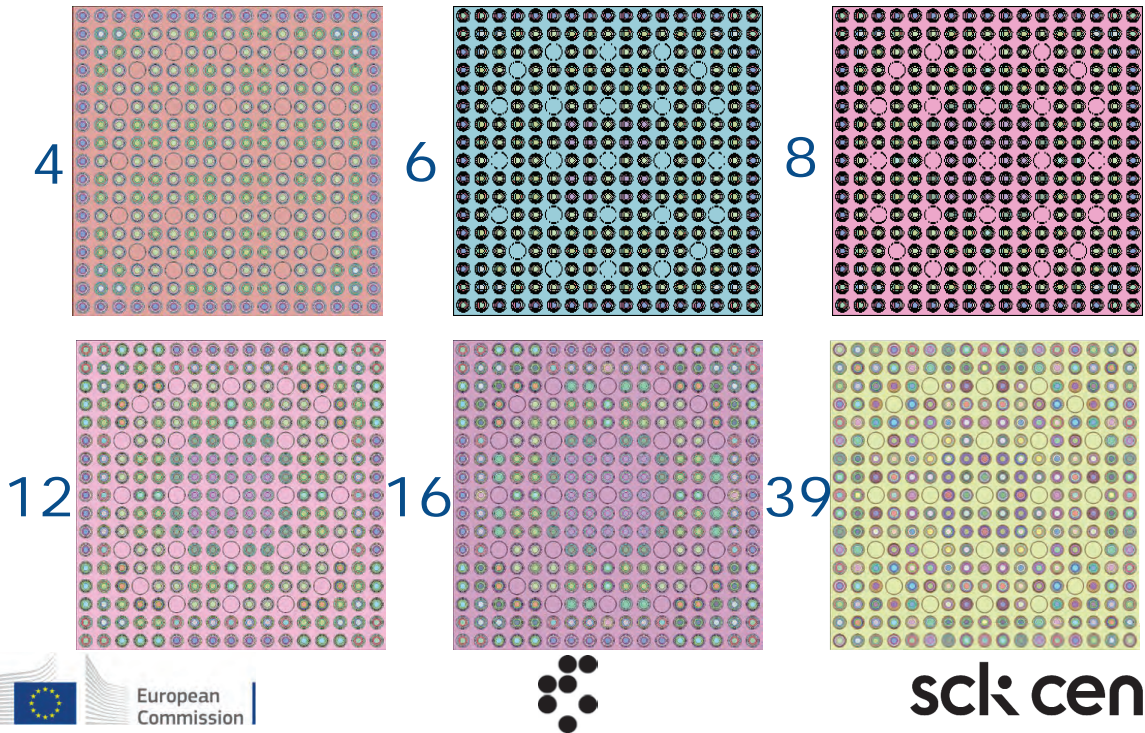
- As a function of boundary conditions (1-group albedo)
- Optimal pin grouping?
- Effect on observables



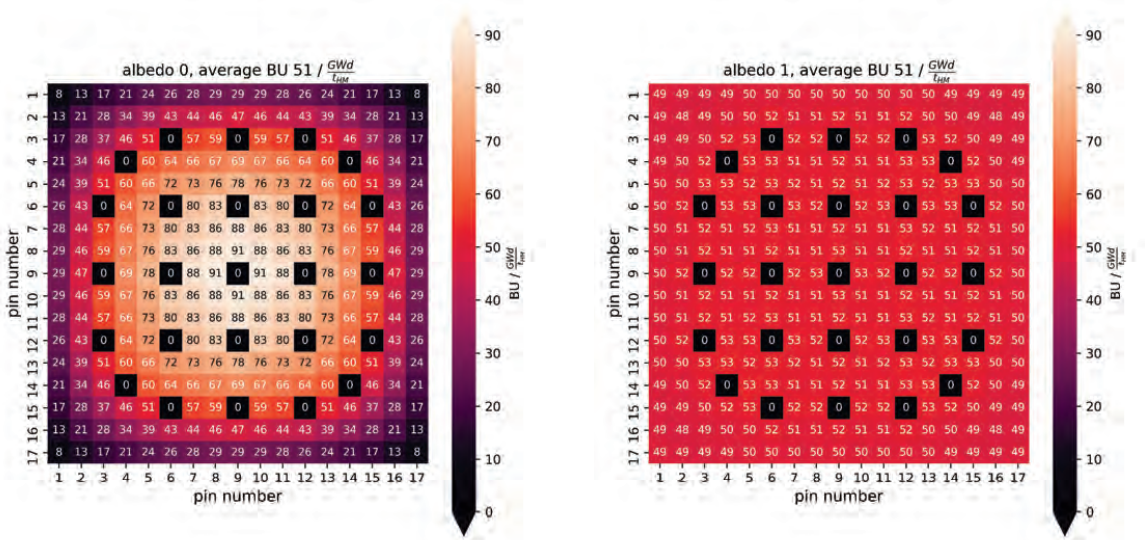
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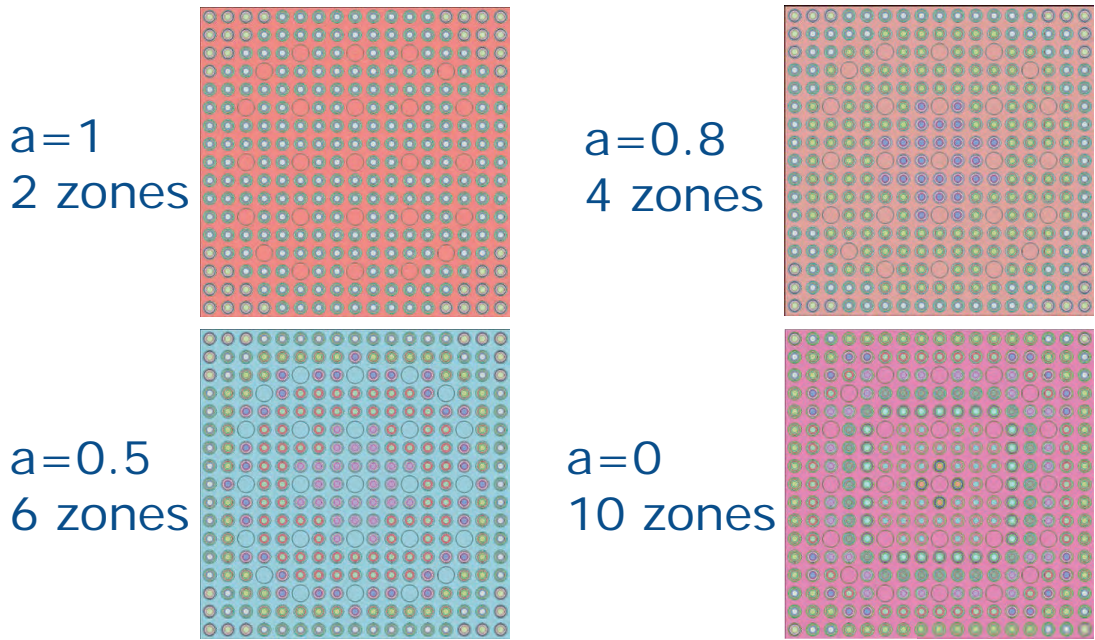
# Pin grouping: by „feeling“



# Pin burnup distributions

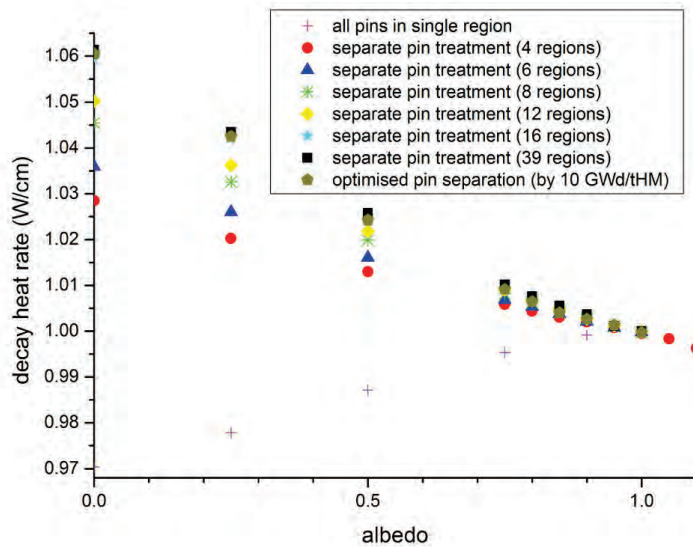


## Pin grouping: by burnup, separated by 10 GWd/tHM



**sck cen**

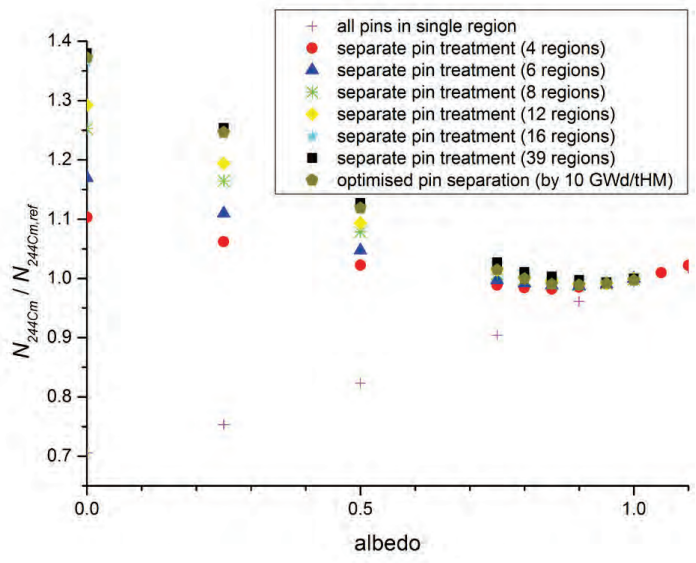
## Separate pin treatment: results (decay heat rate at 5 a cooling)



**sck cen**



## Separate pin treatment: results (<sup>244</sup>Cm – n. emission)

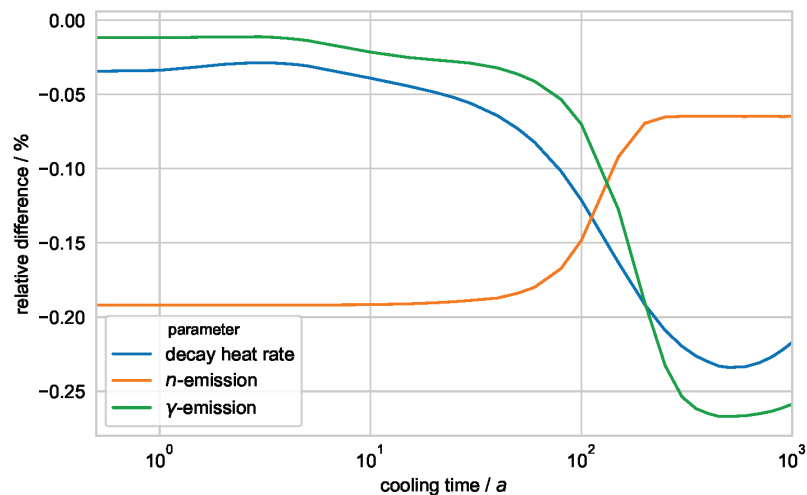


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## Irradiation conditions: fuel temperature profile

$T_f$ : 4 equi-volume radial regions @ different  $T$   
 Ref. case:  $T$  independent of radial position

Radial temperature profile



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## Irradiation conditions: moderator density and temperature

### Moderator temperature profile in a typical PWR:

- Bottom: ~560 K ( $\rho = 0.752 \text{ g/cm}^3$  @ 15.5 MPa)
- Top: ~600 K ( $\rho = 0.661 \text{ g/cm}^3$  @ 15.5 MPa)
- 2D slices at different conditions: **T effect small,  $\rho$  effect large**

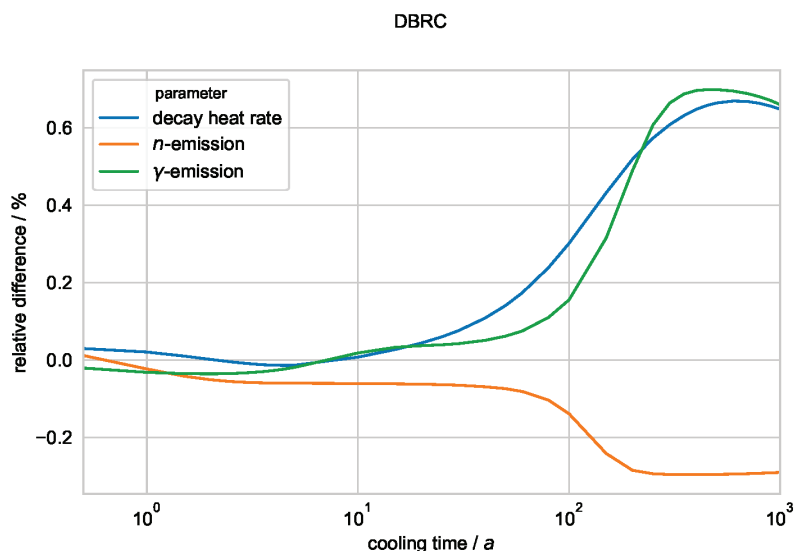
Nucl.	$c(600 \text{ K}) / c(580 \text{ K}) - 1$	$c(560 \text{ K}) / c(580 \text{ K}) - 1$	Nucl.	$c(600 \text{ K}) / c(580 \text{ K}) - 1$	$c(560 \text{ K}) / c(580 \text{ K}) - 1$
<sup>90</sup> Sr	-0.73%	0.54%	<sup>238</sup> Pu	3.21%	-2.51%
<sup>134</sup> Cs	2.24%	-1.54%	<sup>239</sup> Pu	<b>5.09%</b>	<b>-3.77%</b>
<sup>137</sup> Cs	0.00%	0.00%	<sup>240</sup> Pu	8.83%	-5.82%
<sup>148</sup> Nd	-0.05%	0.04%	<sup>241</sup> Pu	2.49%	-1.76%
<sup>149</sup> Sm	8.33%	-5.28%	<sup>242</sup> Pu	6.84%	-4.72%
<sup>235</sup> U	6.53%	-4.80%	<sup>241</sup> Am	7.18%	-4.94%



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## Physical approximations: DBRC (on/off)

DBRC: used for <sup>238</sup>U, <sup>240,242</sup>Pu and <sup>241</sup>Am  
 No DBRC: ref. case



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## Summary and conclusions

Analysis of modelling uncertainties/biases – case study:

- Calculations: neutron transport (MC, det.) + depletion
- Case: simplified PWR assembly
- ND library: ENDF/B-VII.1
- Observed quantities: Nuclide vector, decay heat, neutron and  $\gamma$ -ray emission

Analysis of modelling uncertainties/biases – main results:

- Time discretization: optimal time step scheme is problem dependent.
- Spatial discretization of the depletion zones:
  - Optimal pin grouping depends on boundary conditions
  - For  $\text{UO}_2$  fuel, 4 equi-volume radial depletion zones are sufficient (<0.1% bias for  $^{244}\text{Cm}$ ); 2 regions with optimized border are almost sufficient
- Operational conditions:
  - Axial moderator density important – non-linear effect (either 3D or 2D slices).
  - Radial fuel temperature: small differences, 1 radial zone almost sufficient.
- DBRC causes <1% difference in observables (has to be studied in more detail).



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## Future work

⇒ Detailed sensitivity studies

- ⇒ Nuclear data
- ⇒ Operational history
- ⇒ Geometry & materials
- ⇒ Model parameters (depletion time steps, depletion zones, nuclide vector, etc.)

⇒ Experimental validation

- ⇒ Decay heat measurements from SNF (e.g. SKB-50, „Blind Test“)
- ⇒ Neutron emission measurements from SNF (JRC/SCK)
- ⇒ SFCOMPO database
- ⇒ Nuclear data measurements (decay energies, actinide cross sections, etc.)



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**6.2 Fuel properties characterisation and related uncertainty analysis: overview, status and planning; P. Schillebeeckx, JRC Geel; 1st research coordination meeting on the CRP on spent fuel characterisation; 06 - 10/12/2021**



## TASK 2 FUEL PROPERTIES CHARACTERISATION AND RELATED UNCERTAINTY ANALYSIS

Summary and status

P. Schillebeeckx, D. Rochman, M. Verwerft, R. Dagan, M. Seidl



The project leading to this application has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement n° 847593.



### TASK 2: SNF CHARACTERISATION – SOURCE TERMS OF INTEREST

**Main observables of SNF** that are of interest for transport, handling, storage and disposal:

- Decay heat rate
- Neutron emission
- $\gamma$ -ray emission
- Reactivity (burnup credit, nuclides with high neutron absorption cross section)
- Fissile material (Safeguards, non-proliferation), i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- Specific long-lived radionuclides (Long term safety), e.g.  $^{14}\text{C}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$

⇒ requires knowledge of a **complex inventory of nuclides** with different characteristics

⇒ a full characterisation can only be obtained by **theoretical calculations**

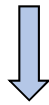




### THEORETICAL CALCULATIONS OF NUCLIDE INVENTORY

Burnup code: coupled neutron transport – nuclide depletion/creation calculations

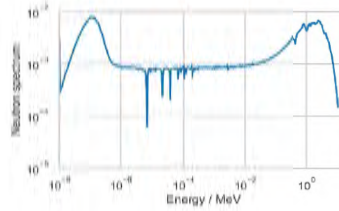
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

Update nuclide vector



### TASK 2: IMPROVE PERFORMANCE OF BURNUP CALCULATIONS

**Nuclear data**

- Cross sections: (n,γ), (n,f), ...
- Fission Yields
- Decay data
  - Half-lives
  - Emission probabilities
  - Recoverable energy

**Burnup code**

**SNF input data**

- Fuel properties
  - design
  - material data (IE)
- Operational history
  - burn-up (BU)
  - cooling time (CT)
  - ...

**Validate by experiment**

**Source terms**

- Thermal power
- Neutron emission
- γ-ray
- <sup>239</sup>Pu
- ...

**Verify experimentally in industrial conditions**





## TASK 2: FUEL PROPERTIES CHARACTERISATION AND RELATED UNCERTAINTY ANALYSIS

- Subtask 2.1 “Theoretical study of SNF source terms” (Theory)
  - co-ordinator PSI (D. Rochman)
  - partners CIEMAT, JSI, JRC Geel, NAGRA, PSI, SCK CEN, VTT
- Subtask 2.2 “Develop, improve and demonstrate NDA methods/systems for SNF characterisation” (NDA)
  - co-ordinator SCK CEN (M. Verwerft)
  - partners CIEMAT, ENRESA (ENUSA), JRC Geel & Ispra, SCK CEN, SKB (UU)
- Subtask 2.3 “Calculate and determine experimentally the inventory of activation and FP in cladding” (Cladding)
  - co-ordinator KIT (R. Dagan)
  - partners CIEMAT, KIT, LEI, NAGRA, VTT, SURAO(CTU)
- Subtask 2.4 “Define and verify procedures to determine source terms of SNF with realistic confidence limits”
  - co-ordinator PEL (KIT) (M. Seidl)
  - partners CIEMAT, CPST, JRC Geel, ENRESA, JSI, PEL, SSTC NRS, KIT, SCK CEN, TUS, SKB (UU)



### SUBTASK 2.1 THEORETICAL STUDY OF SNF SOURCE TERMS

- Cases to verify the performance of different codes and perform sensitivity and uncertainty analysis defined
  - BWR
    - Gundremmingen-7 sample (SFCOMPO)  
( $UO_2$ , 25 MWd/kg, 4 cycles, 2.5 %)
    - ENRESA  
( $UO_2$ , 41 MWd/kg, 3.95 %)
  - PWR
    - SF95-5 from the Takahama-3 reactor (SFCOMPO)  
( $UO_2$ , 30 MWd/kg, 2 cycles, 4.1 %)
    - GU1 from ARIANE (public report)  
( $UO_2$ , 60 MWd/kg, 4 cycles, 3.5 %)
    - GU3 from ARIANE (public report)  
( $UO_2$ , 52 MWd/kg, 4 cycles, 3.5 %)
    - BM1 from ARIANE (public report)  
(MOX, 45-47 MWd/kg, 5 cycles, 4.2 % fissile)
    - NPP Krško  
( $UO_2$ , 40 MWd/kg, 4.95 %)
  - Calculated case:  
(sensitivity and uncertainty analysis)
    - S1.PWR ( $UO_2$ , 51 MWd/kg, 4.0 %)
  - Decay heat: PWR and BWR fuel assemblies
    - SKB-2006
    - GE-Morris





### SUBTASK 2.1 THEORETICAL STUDY OF SNF SOURCE TERMS

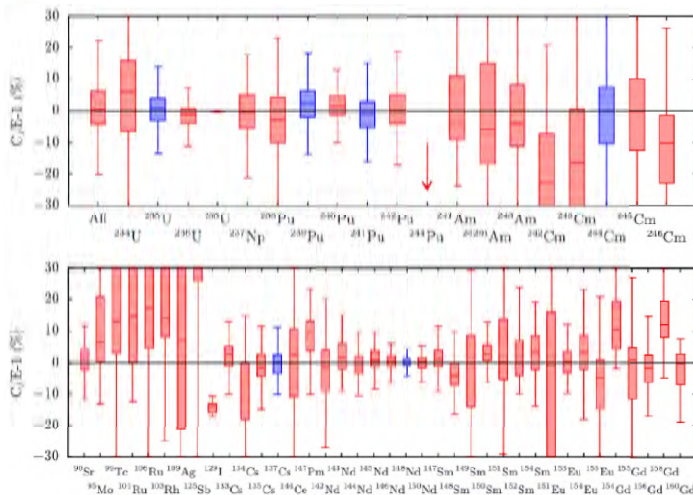
- Cases to verify the performance of different codes and perform sensitivity and uncertainty analysis defined
- All results of calculations reported

Partner	Code(s)	Cases studied
CIEMAT	MCNP/EVOLCODE, MCNP/CINDER	SF95-5
ENRESA/ENUSA	POLARIS	BWR(ENRESA)
JSI (JRC)	SCALE (TRITON/NEWT, POLARIS), SERPENT2	S1.PWR, NPP Krško, SF95-5, SKB-2006
SCK CEN	MCNP/ALEPH2, SERPENT2	S1.PWR, SF95-5, SKB-2006
KIT	MCNP/CINDER, Nucleonica	SF95-5
NAGRA	SCALE(TRITON, POLARIS)	SF95-5, BM1, BWR(ENRESA), Gundremmingen-7 (B23), GE-Morris, SKB-2006
PSI	CASMO, CASMO/SIMULATE/SNF	GU1, GU3, BM1, BWR(ENRESA), GE-Morris, SKB-2006
VTT	SERPENT2	Gundremmingen-7 (B23)

+ in kind contribution from IRSN (FR) and Studsvik in the analysis of the data and preparation of final paper



### SUBTASK 2.1: NUCLIDE INVENTORY



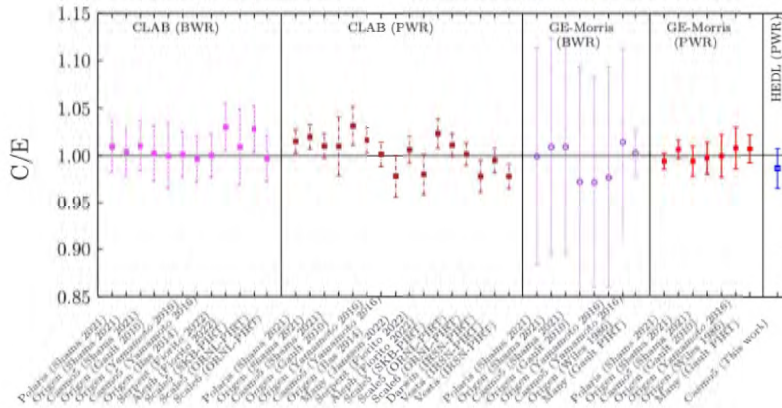
- C: calculated concentration
- E: experimentally determined



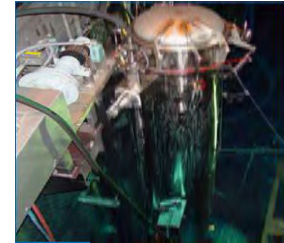




**SUBTASK 2.1: DECAY HEAT RATE**



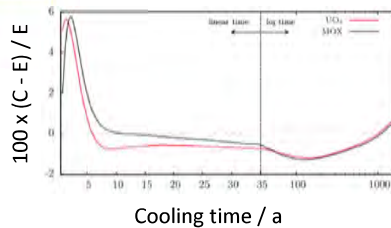
CLAB calorimeter



⇒ More detailed study: Romojo et al., "On the use of decay heat measurements for code validation" in *Frontiers in Energy Research*



**SUBTASK 2.1 RECOMMENDATIONS**



EPRI PIRT report + Ilas et al., Nucl. Eng. Des. 319 (2017) 176



	<sup>148</sup> Nd	<sup>137</sup> Cs	<sup>235</sup> U	<sup>239</sup> Pu	BU	Decay heat rate
Relative uncertainty	4 %	5 %	4 %	4 %	5 %	> 4%
Relative difference	- 0.1%	- 0.4%	0.2%	2.5%	-	See fig.

Data set	Data set	Uncertainty (1σ) (%)
Modeling data	Fuel design	0.20
	Operating data	0.85
	Total	0.87
Nuclear data	Cross sections	0.88
	Fission yields	0.26
	Total	0.92
<b>Overall effect</b>	<b>Total</b>	<b>1.27</b>

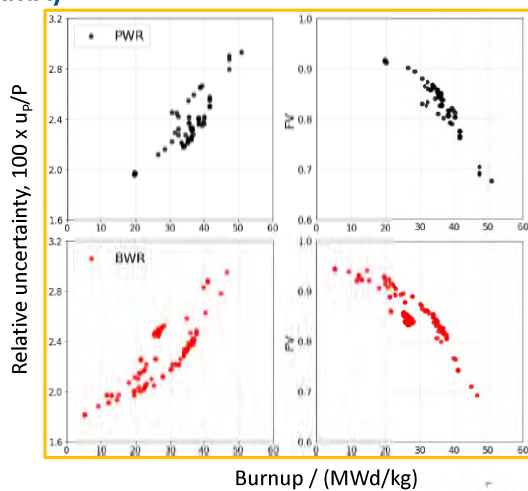
BWR, BU = 37 MWd/kg and CT = 15.6 a





### UNCERTAINTY ANALYSIS (PHD AHMED SHAMA)

Data set	Decay heat rate, C/E	
	Average	St. Deviation
CLAB, BWR (81)	1.010	0.051
CLAB, PWR (71)	1.015	0.023
CLAB (152)	1.012	0.041



eurad

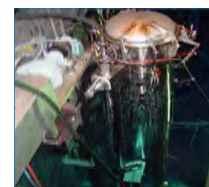


### BLIND TEST (NOT INCLUDED IN EURAD): PAPER PUBLISHED

NUCLEAR SCIENCE AND ENGINEERING - VOLUME 196 - 1125-1145 - SEPTEMBER 2022  
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 DOI: <https://doi.org/10.1080/00295639.2022.2053489>

**ANS**

**Blind Benchmark Exercise for Spent Nuclear Fuel Decay Heat**



- PWR assemblies
- Decay heat rate determined at CLAB

Assembly ID	BU	CT	IE	Decay heat rate	Gamma-escape
BT01	53 MWd/kg	4.5 a	3.95 wt%	1662 W	58 W
BT02	55 MWd/kg	8.6 a	3.95 wt%	1068 W	30 W
BT03	50 MWd/kg	9.8 a	3.95 wt%	895 W	21 W
BT04	51 MWd/kg	13.5 a	3.70 wt%	768 W	15 W
BT05	50 MWd/kg	21.4 a	3.60 wt%	663 W	12 W

eurad

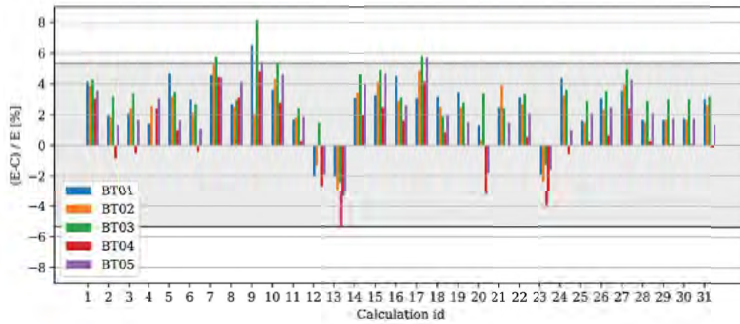


**BLIND TEST: CODES + LIBRARIES**

Code	Library	Appendix Section
ALEPH 2.7.2	ENDF/B-VII.1	A.I.A
APOLLO2.8/DARWIN2.3	JEFF-3.1.1	A.I.B
CASMO-4E + ORIGEN-S	JEFF-2.2	A.I.C
CASMO-5 (2.03)	ENDF/B-VII.1	A.I.D
CASMO-5 (2.12.00) + SNF (1.07.02)	ENDF/B-VII.1	A.I.E
DRAGON 4.0.5	ENDF/B-VII.1	A.I.F
EVOLCODE (MCNP + ACAB)	JEFF-3.3	A.I.G
MCNP-CINDER + Nukleonika (2D)	ENDF/B-VII.1	A.I.H
Monteburns v3 + CINDER	ENDF/B-VII.1	A.I.I
MOTIVE (KENO-VI + VENTINA)	ENDF/B-VII.1	A.I.J
MOTIVE (OpenMC + VENTINA)	ENDF/B-VIII	A.I.K
MVP 3	ENDF/B-VII.1	A.I.L
MVP 3	JEFF-3.2	A.I.M
MVP 3	JENDL-4.0	A.I.N
OREST	JEP-2.2 + ENDF/B-VI	A.I.O
SCALE 6.0; ORIGEN-ARP	ENDF/B-V	A.I.P
SCALE 6.1.3; ORIGEN-ARP	ENDF/B-V	A.I.Q
SCALE 6.2.3; ORIGAMI	ENDF/B-VII.1	A.I.P
SCALE 6.2.3; Polaris	ENDF/B-VII.1	A.I.R
SCALE 6.2.3; ORIGEN	ENDF/B-VII.1	A.I.R
SCALE 6.2.3; TRITON/KENO	ENDF/B-VII.1	A.I.S
SCALE 6.2.3; TRITON/NEWT	ENDF/B-VII.1	A.I.T
SEADep	JEFF-3.1.1	A.I.U
Serpent 2.1.29	ENDF/B-VII.1	A.I.V
Serpent 2.1.29	JEFF-3.1.1	A.I.W
Serpent 2.1.31	JEFF-3.2 + JEFF-3.1.1	A.I.X



**BLIND TEST: RESULTS**



Assembly ID	CT	100 x (C-E)/E	St. dev.
BT01	4.5 a	2.5	1.9
BT02	8.6 a	2.3	1.8
BT03 (+ Gd)	9.8 a	3.3	1.9
BT04	13.5 a	0.6	2.3
BT05	21.4 a	2.1	2.1

EPRI report +Ilas et al., Nucl. Eng. Des. 319 (2017) 176

Data set	Data set	Uncertainty (1σ) (%)
Modeling data	Fuel design	0.20
	Operating data	0.85
	Total	0.87
Nuclear data	Cross sections	0.88
	Fission yields	0.25
	Total	0.92
	Overall effect	Total

⇒ Uncertainty of 1.3 % realistic?





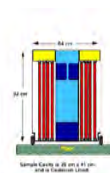
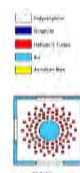
## SUBTASK 2.2: DEVELOP AND IMPROVE NDA METHODS/SYSTEM

- Provide data to validate burnup codes
  - Neutron emission rate of a SNF by NDA at SCK CEN
  - Radiochemical analysis of BWR samples
  - Performance assessment and uncertainty evaluation of CLAB calorimeter (MSc Thesis of J. Ekman, A. Mehic)
- Improve NDA methods to characterise SNF assemblies (PhD Thesis V. Solans)
  - Gamma-ray scanning device at CLAB
  - Differential Die-away Self-Interrogation (DDSI)



## SUBTASK 2.2: DEVELOP AND IMPROVE NDA METHODS/SYSTEMS

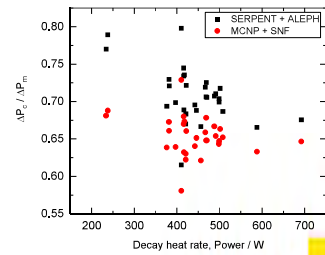
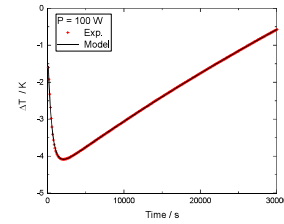
- Neutron emission rate of a SNF by NDA at SCK CEN
  - Experiments of REGAL sample at SCK CEN (finalised)
    - Publication data book in progress
    - Experiments finalised and reported (EUR30379 EN) (Journal paper in progress)
  - Experiments with improved detection system (delayed: summer 2023)
    - Design of improved transfer container finalised
    - Construction: delayed due to administrative procedures
- Radiochemical analysis of a set of BWR samples (November 2022)
  - Data book finalised and distributed (21/03/2022)
  - Radiochemical analysis in progress (complications with radiochemical analysis: very instructive)
    - problems with nuclide inventory determined by Laser ablation ↔ radiochemical analysis
    - problems revealed by comparison with calculated data





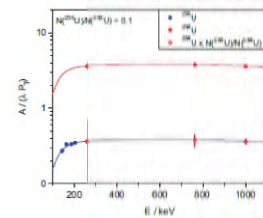
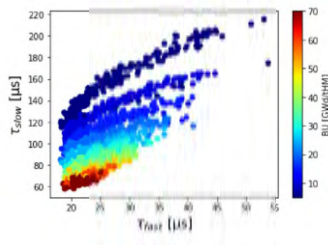
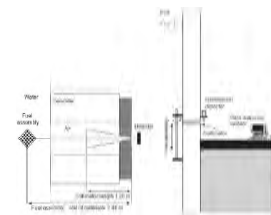
### SUBTASK 2.2: CALORIMETER AT CLAB

- Improve analysis procedure for calorimeter at CLAB (MSc Thesis of J. Ekman, A. Mehic) (collaboration Vattenfall (SKB), JRC, JSI, SCK CEN)
  - Analytical model to describe heat transfer (finalised)
  - Study of the  $\gamma$ -ray escape from the calorimeter (ongoing)
    - MCNP ( $\gamma$ -ray transport ) + SNF (fuel depletion)
    - SERPENT ( $\gamma$ -ray transport ) + ALEPH2 (fuel depletion)
    - ⇒ Compare results with present approach ( $\gamma$ -ray dosimeters combined with analytical expressions for the  $\gamma$ -ray transport)
  - Uncertainty assessment (December 2022, journal paper in progress)
    - Calibration electrical heater
    - Gamma-ray correction + correction for difference electrical heater – fuel assembly
    - Least squares fit procedures



### SUBTASK 2.2: DEVELOP AND IMPROVE NDA METHODS/SYSTEMS

- Improve analysis procedure for neutron and  $\gamma$ -ray based NDA measurements at CLAB (PhD Thesis of V. Solans, presentation at this meeting)
  - Details: presentation of V. Solans
    - $\gamma$ -ray measurements: finalised (presentation at IAEA symposium, journal paper in preparation) (intrinsic calibration for gamma-ray attenuation in assembly based on well-known principle applied for enrichment determination)
    - Differential Die away Self-Interrogation (DDSI): in progress

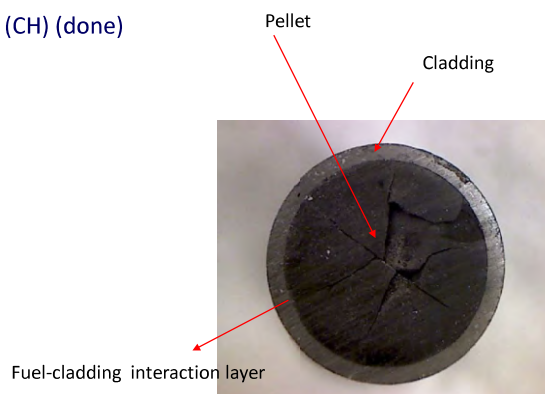




### SUBTASK 2.3: CALCULATE AND DETERMINE THE INVENTORY IN CLADDING

Cladding composition: important to study fuel integrity (PhD Tobias Köning, August 2022)

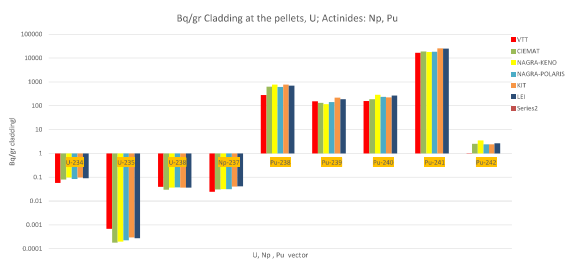
- Selection of Zircaloy samples irradiated in a PWR Gösgen (CH) (done)
  - UO<sub>2</sub>, 50.4 GWd/t, 4 cycles, 3.8%, 32 years cooling time
  - Zircaloy-4 of UO<sub>x</sub> fuel rod segment
  - Zircaloy-4 plenum of UO<sub>x</sub> fuel rod segment
  - UO<sub>x</sub> fuel fragment
- Experiments using various techniques at KIT
  - Scanning Electron Microscopy (SEM)
  - Wave Length X-ray spectroscopy (WDX)
  - Energy Dispersive X-ray spectroscopy (EDX)
  - X-ray Photo-electron spectroscopy (XPS)
  - Radiochemical analysis ( $\alpha$ -spec,  $\gamma$ -spec, LSC, HR-ICP-MS)



### SUBTASK 2.3: CALCULATE AND DETERMINE THE INVENTORY IN CLADDING

#### Code validation

- Calculations (done)
  - MCNP/EVOLCODE CIEMAT,
  - MCNP/CINDER KIT
  - SCALE (TRITON) LEI
  - SCALE (KENO) NAGRA
  - SCALE (POLARIS 2D) NAGRA
  - VTT SERPENT2



#### • Interpretation of data (in progress)

- Good agreement for the cladding of the plenum and the cladding around the pellets
- Singular deviations are being checked for their origin (input issues, code deficiencies, source of uncertainties, ...)
- Comparison with experimental data used to assess how much fuel is adherent to the inner surface of the cladding during manufacturing: important to estimate the risk of radiation damage during interim storage

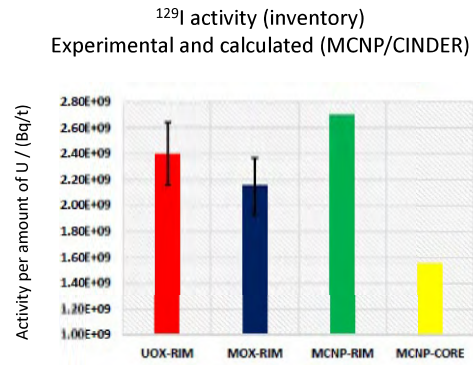
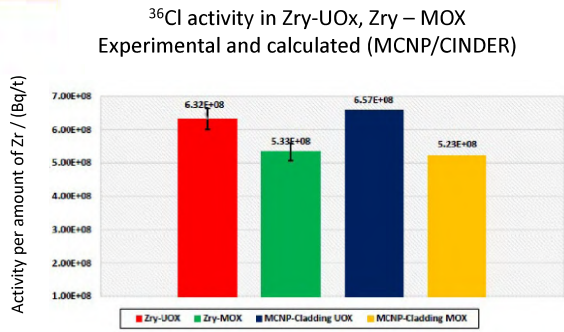






**INVENTORY OF <sup>36</sup>Cl AND <sup>129</sup>I**

(PhD Tobias Köning, August 2022)



- First ever analysis of <sup>36</sup>Cl in PWR fuel rod components
- Calculations: 15 ppm <sup>35</sup>Cl in fuel and zircaloy (Häkkinen, Impurities in LWR fuel and structural materials, Finland 2019)

©-Akti@S. Häkkinen, Impurities in LWR fuel and structural materials, VTT, Finland 2019.



**SUBTASK 2.4: DEFINE AND VERIFY PROCEDURES TO DETERMINE SOURCE TERMS OF SNF WITH REALISTIC CONFIDENCE LIMITS**

Planning was reviewed to account for delays due to COVID and signing of agreements

**1. REGAL Sample from Task 2.2 (SCK CEN, JSI, JRC) (December 2022)**

- Data book/report in preparation
- Neutron output: calculations with ALEPH2, SCALE, SERPENT2 (journal paper in preparation)
- Report: February 2023

**2. BWR SNF sample from task 2.2 (ENRESA/ENUSA) (in progress)**

- Data book/report produced and distributed (March 2022)
- Calculations with MCNP/EVOLCODE (CIEMAT), SCALE (PEL)
- Report: December 2022

**3. SKB-50 (in progress, December 2023) (details: presentation M. Seidl)**

- Non-Disclosure agreements signed by all partners
- Analysis procedure defined
- Interaction with different partners to improve the data book (dedicated VC meetings)
- Report: December 2023

Code	Library	Method	(α,n)	S <sub>α</sub> / (g <sup>-1</sup> s <sup>-1</sup> )	S <sub>n</sub> / (g <sup>-1</sup> s <sup>-1</sup> )	Calculation/Experiment	S <sub>α</sub>	S <sub>n</sub>
SCALE	ENDF/B-VIII.1	Y(α,n)		653	11.0	0.96	0.45	
SERPENT(1)	ENDF/B-VIII.1	Y(α,n)		689	14.3	1.01	0.58	
SERPENT(2)	ENDF/B-VIII.1	Y(α,n)		694	14.2	1.02	0.58	
	ENDF/B-VIII.0	Y(α,n)		691	14.1	1.01	0.57	
	JEFF-3.1.2	Y(α,n)		629	13.2	0.92	0.54	
	JEFF-3.3	Y(α,n)		654	13.7	0.96	0.56	
	JEFF-4T0	Y(α,n)		695	13.7	1.02	0.56	
	JENDL-4.0	Y(α,n)		719	14.5	1.05	0.59	
ALEPH28	ENDF/B-VIII.0	Y(α,n)		662	13.1	0.97	0.53	
		σ(α,n)	TENDL2015		12.6		0.51	
		σ(α,n)	JENDL_AN/500		10.6		0.43	
	JEFF-3.3	Y(α,n)		641	12.9	0.94	0.53	
		σ(α,n)	TENDL2015		12.7		0.52	
		σ(α,n)	JENDL_AN/500		10.5		0.43	





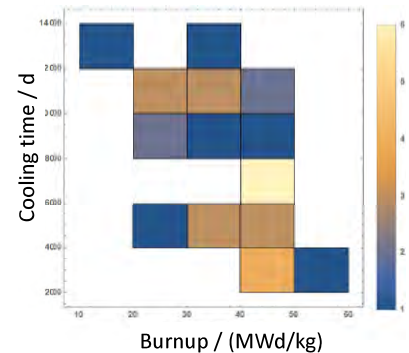
## TASK 2.4 SKB-50

- SKB50 data was received in Q2/22
- SKB50 data book is limited
- SKB50 pin data has been guessed by PEL's knowledge and/or published data
- SKB50 has been converted into standardized xml format to facilitate automation.
- SKB50 data has been distributed without measurement data to facilitate blind test (with participants from PEL, CIEMAT, (JSI, NAGRA, KIT, PSI, SCK CEN)



## TASK 2.4 SKB-50

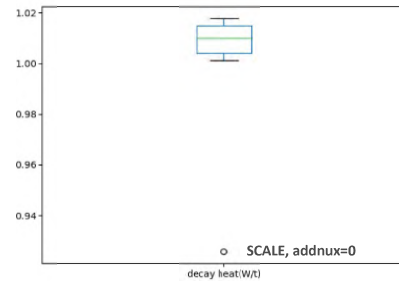
- SKB50: 2 main PWR types and 4 main BWR types:
  - 15x15 AFA/KWU, 17x17 F/HTP/AA/W
  - SVEA96, SVEA100, AA 8\*8-1, Atrium 10B
- Not all assemblies have :  
decay heat rate & neutron & gamma-ray data
- First step: automatic SCALE runs by PEL and CIEMAT







- PWR1: 8 cases were created to study robustness of simulations
  - CASMO5
  - SCALE6.2, v7-238, addnux=4, 1 average fuel region, NEWT deterministic transport
  - SCALE6.2, v7-252, addnux=4, 1 average fuel region, NEWT deterministic transport
  - SCALE6.2, v7-56, addnux=4, 1 average fuel region, NEWT deterministic transport
  - SCALE6.2, v7-238, addnux=0, 1 average fuel region, NEWT deterministic transport
  - SCALE6.2, v7-238, addnux=1, 1 average fuel region, NEWT deterministic transport
  - SCALE6.2, v7-238, addnux=1, 8 different fuel region, NEWT deterministic transport
  - SCALE6.2, v7-238, addnux=4, 1 average fuel region, KENOVI Monte Carlo transport



SCALE6 addnux parameter: for depletion calculations trace quantities of certain nuclides are added to the inventories of depletion materials in order to accurately track the nuclides' impact on cross section processing and transport calculations



## CONTRIBUTION TO CRP TECDOC (JRC GEEL)

### Overview NDA techniques for the characterisation of SNF

Missing:

- Active neutron interrogation
  - Differential Die Away
  - Detection delayed gamma (and neutron)
- References



## Keep in touch



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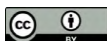


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# Thank you



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**6.3 Neutron resonance analysis and applications to material characterisation; P. Schillebeeckx, JRC Geel; LANL P/T Colloquium, April 2022; 28/04/2022**



# Neutron resonance analysis and applications to material characterisation

P. Schillebeeckx, H. Postma†, S. Kopecky and C. Paradela

European Commission

Joint Research Centre, Geel (BE)

*LANL P/T Colloquium, April 2022*



## Contents

- Neutron facilities at JRC Geel
- Basic principles of Neutron Resonance Analysis (NRA)
- Applications
  - Cultural heritage and archaeology
  - Nuclear waste
  - Validation of nuclear data (resonance parameters)
- Analysis of complex samples
- Characterisation of SNF



## Joint Research Centre

Headquarters in Brussels and research facilities located in 5 Member States:

- **Belgium (Geel)**
- Germany (Karlsruhe)
- Italy (Ispra)
- The Netherlands (Petten)
- Spain (Seville)



## JRC-Geel site



**40** ha



**14**  
major buildings



Around **230** staff  
from **4** JRC Directorates

JRC.G.2 about 30%



## Nuclear facilities at JRC - Geel



### GELINA

neutron time-of-flight facility for high-resolution neutron measurements



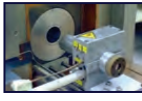
### MONNET

tandem accelerator based fast neutron source



### TARGET

nuclear target preparation laboratories



### RADMET

laboratories for standardisation of radionuclide activity



### HADES

low-level gamma-spectrometry laboratory



### METRO

nuclear reference material and measurement facility



Operated by JRC.G.2 Unit

- Nuclear data
- Radionuclide measurements
- Nuclear safeguards metrology



## Nuclear data group: neutron induced interactions



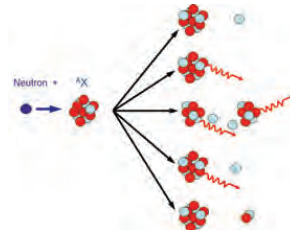
### GELINA

neutron time-of-flight facility for high-resolution neutron measurements

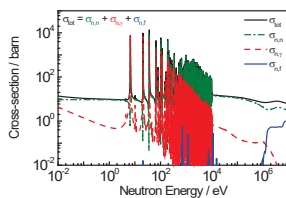


### MONNET

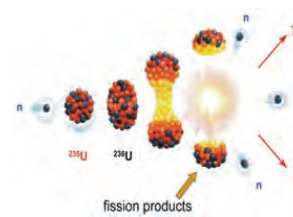
tandem accelerator based fast neutron source



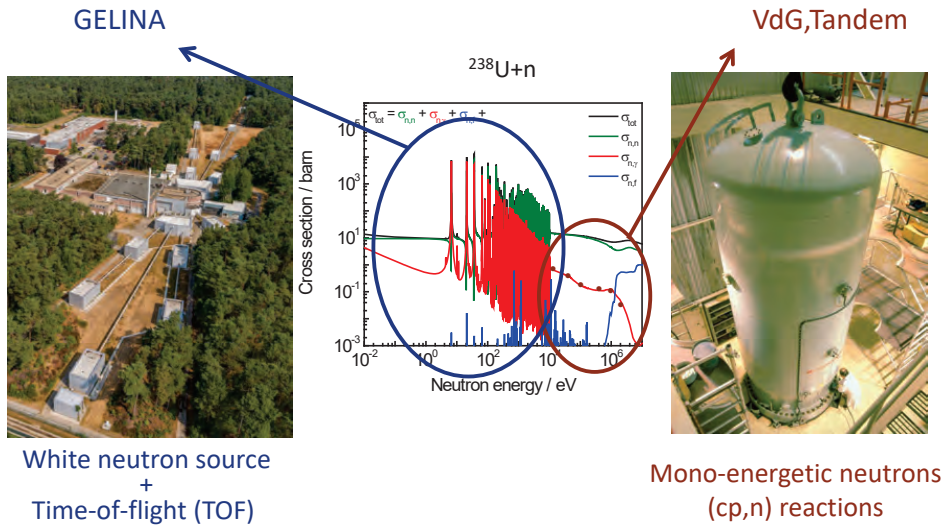
Neutron induced interaction cross sections



Fission process



## Neutron facilities: GELINA and MONNET



## GELINA - Experimental set-ups (see presentation C. Paradela)

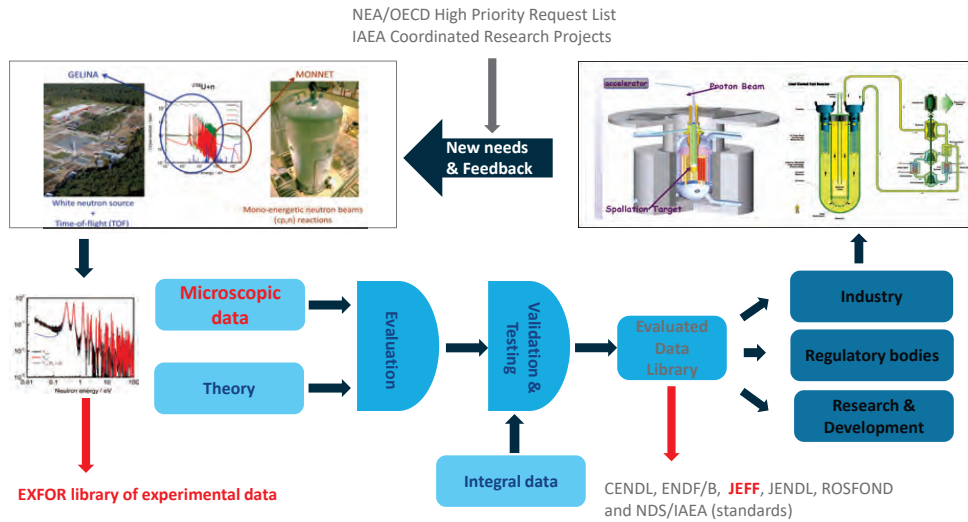


- Transmission
  - 10 m, 30 m, 50 m
- Capture
  - 10 m, 30m, 60 m
- Elastic, in-elastic scattering
  - 30 m
- In-elastic scattering ( $n, n'\gamma$ )
  - 30 m, 100 m
- Fission, ( $n,p$ ), ( $n,\alpha$ ),
  - 10 m



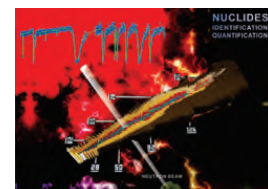
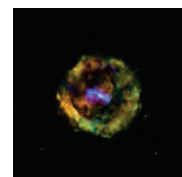
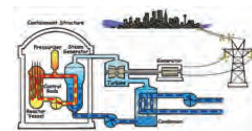


## Nuclear data libraries for nuclear applications



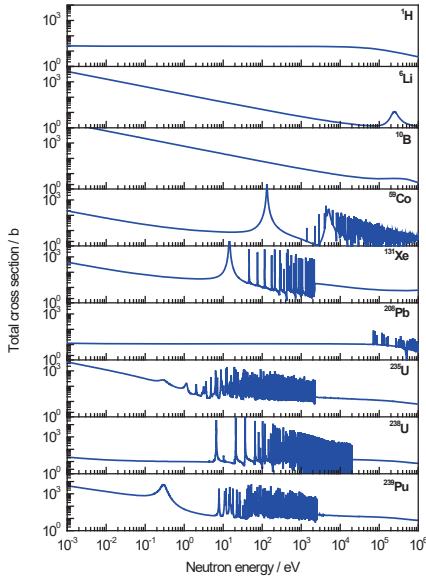
## Applications

- **Nuclear data for energy technology**
  - Safety of current systems
  - Development of innovative systems (e.g. MYRRHA)
  - Back-end: Spent Nuclear Fuel (Burn Up Credit, Decay heat, ...)
    - o Intermediate storage
    - o Transport of SNF
    - o Reprocessing facilities
    - o Final Disposal of SNF
- Nuclear physics
- Nuclear medicine: diagnostics and therapy
- Nucleosynthesis and nuclear astrophysics
- Detector development
- Materials research (NAA, PGAA, Neutron Resonance Analysis, ...)
- ....





## Neutron Resonance Analysis (NRCA & NRTA)



- Resonances appear at energies that are specific for each nuclide
- Position and amplitude of resonances can be used as fingerprints to
  - identify and quantify nuclides
  - elemental & isotopic composition
- Neutron Resonance Capture and Transmission Analysis (NRCA & NRTA)
  - Non-Destructive Analysis (NDA)
  - no sample preparation required
  - sensitive to almost all nuclides (except light)
  - **requirements:**
    - TOF-measurements at a white neutron source** (e.g. GELINA, LANSCE, J-PARC, ISIS)



## Cross section measurements

**Total cross section**

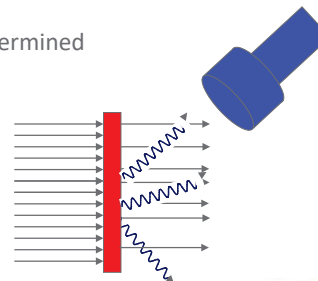
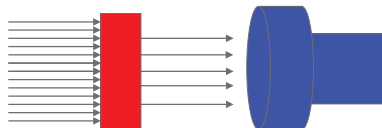
$$T \cong e^{-n \sigma_{tot}}$$

**Capture cross section**

$$Y_\gamma \approx (1 - e^{-n \sigma_{tot}}) \frac{\sigma_\gamma}{\sigma_{tot}}$$

**Well-characterised (reference) samples**  
 n: total number of atoms per unit area is well-known

↓  
**accurate cross-sections can be determined**



Schillebeeckx et al., Nuclear Data Sheets 113 (2012) 3054



## Neutron resonance analysis

**NRTA**

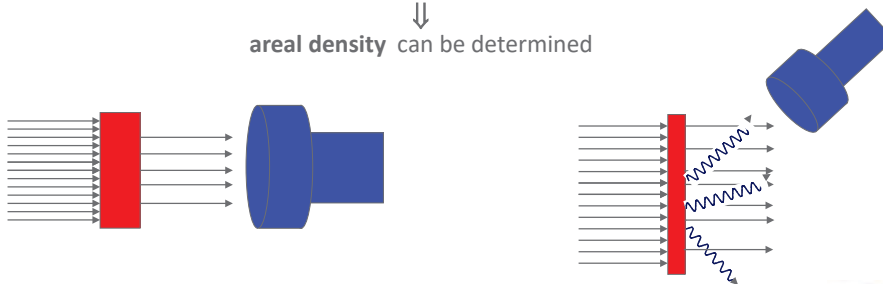
$$T \cong e^{-n \sigma_{tot}}$$

**NRCA**

$$Y_\gamma \approx (1 - e^{-n \sigma_{tot}}) \frac{\sigma_\gamma}{\sigma_{tot}}$$

Well-known cross sections

areal density can be determined



Schillebeeckx et al., Report EUR 26848-EN (2014)



## Neutron Resonance Analysis

**NRTA**

$$T_{exp} = \frac{C_{in}}{C_{out}}$$

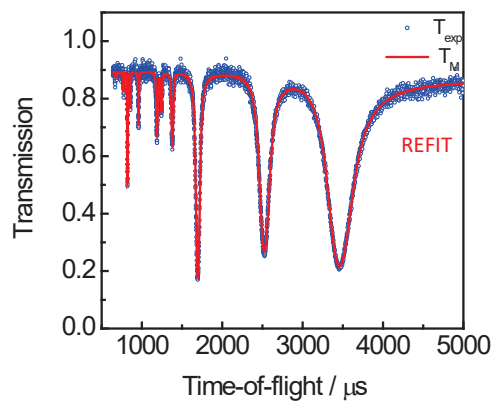
Resonance Shape Analysis: REFIT

$$\chi^2(n) = (T_{exp} - T_M(t, n))^T V_{T_{exp}}^{-1} (T_{exp} - T_M(t, n))$$

$$T_M(t) = \int R(t, E) T(E) dE$$

$$T(E) = e^{-n \sigma_{tot}(E)}$$

n : areal density  
total number of nuclei per unit area

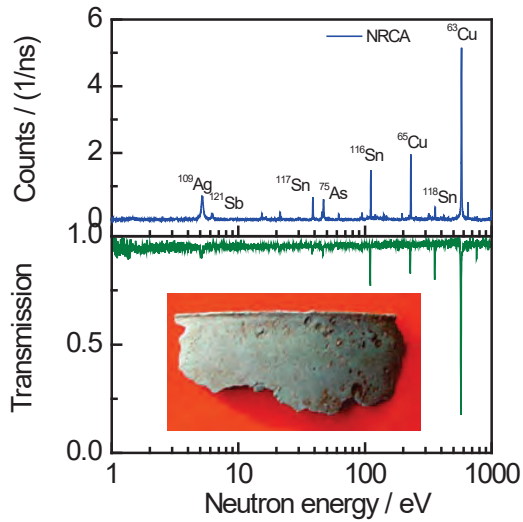


Schillebeeckx et al., Report EUR 26848-EN (2014)



### NRTA and NRCA

Transmission: areal density Cu: 0.55 (2) g/cm<sup>2</sup>



Element	Isotope	E <sub>r</sub> / eV	wt%
Cu	<sup>63</sup> Cu	579.0	77.76 (11)
	<sup>65</sup> Cu	230.0	
Sn	<sup>112</sup> Sn	94.8	20.85 (10)
	<sup>116</sup> Sn	111.2	
	<sup>117</sup> Sn	38.8	
	<sup>118</sup> Sn	45.7	
	<sup>119</sup> Sn	222.6	
	<sup>120</sup> Sn	427.5	
	<sup>124</sup> Sn	62.0	
Fe	<sup>56</sup> Fe	1147.4	0.77 (1)
As	<sup>75</sup> As	47.0	0.34 (1)
Sb	<sup>121</sup> Sb	6.2	0.20 (2)
	<sup>123</sup> Sb	21.4	
Ag	<sup>107</sup> Ag	16.3	0.09 (1)
	<sup>109</sup> Ag	5.2	
In	<sup>115</sup> In	1.46	0.0061 (3)

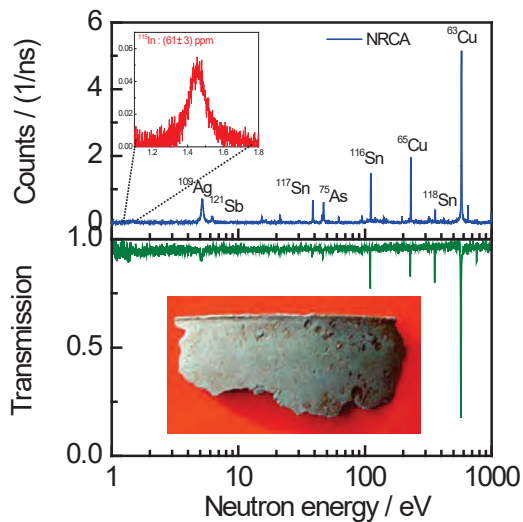
Uncertainties: only counting statistics



H. Postma and P. Schillebeeckx, in Neutron Methods for Archaeology and Cultural Heritage (Springer)

### NRTA and NRCA

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In	<sup>115</sup> In	1.46	0.0061 (3)

Uncertainties: only counting statistics

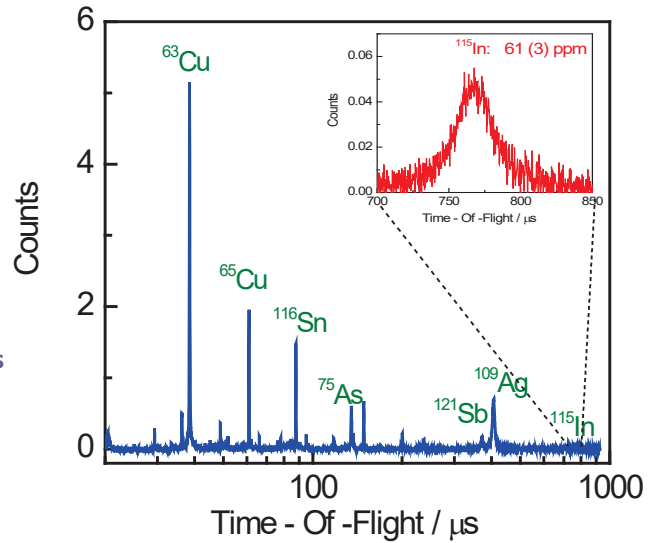


H. Postma and P. Schillebeeckx, in Neutron Methods for Archaeology and Cultural Heritage (Springer)

### NRCA ⇔ PGAA at continuous incident beam



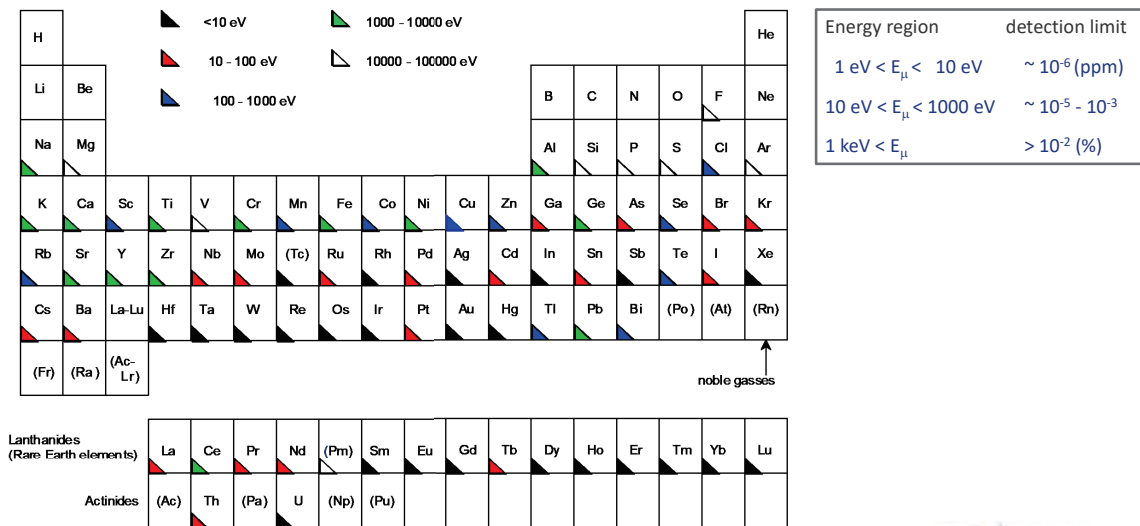
⇒ detection of In is **not hindered** by strong resonances of **other elements** (e.g. Cu)



Postma et al., Czech. J. Phys. 53 (2003) A233



### NRA: which elements can be detected?



H. Postma and P. Schillebeeckx, in Neutron Methods for Archaeology and Cultural Heritage (Springer)



## NRA for cultural heritage and archaeology

Started in 2000 by a collaboration between Univ. Delft and JRC Geel initiated by **Prof. H. Postma**

### Journal papers

- Postma et al., *J. Radioanal. Nucl. Chem.* 248 (2001) 115  
 Postma et al., *Czech. J. Phys.* 53 (2003) A233 – A240  
 Postma et al., *Archaeometry*, 46 (2004) 635  
 Postma and Schillebeeckx, *J. Radioanal. Nucl. Chem.* 265 (2005) 297  
 Postma et al., *Il Nuovo Cimento*, 30C (2007) 105  
 Perego et al., *J. Radioanal. Nucl. Chem.* 271 (2007) 89  
 Postma et al., *J. Radioanal. Nucl. Chem.* 271 (2007) 95  
 Schut et al., *J. Radioanal. Nucl. Chem.* 278 (2008) 151  
 Postma et al., *J. Radioanal. Nucl. Chem.* 283 (2010) 641  
 Perelli et al., *Nucl. Instr. Meth. Phys. Res. A* 623 (2010) 693  
 Perelli et al., *J. Anal. At. Spectrom.* 26 (2011) 992  
 Postma et al., *J. Archaeol. Sci.* 38 (2011) 1810  
 Schillebeeckx et al., *J. Instrumentation*, 7 (2012) C03009  
 Postma et al., *Analecta Praehistorica Leidensia*, 47 (2017) 37



## NRA for cultural heritage and archaeology

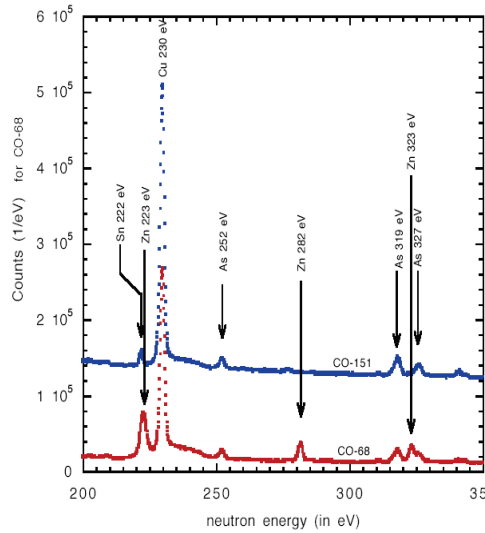
Started in 2000 by a collaboration between Univ. Delft and JRC Geel initiated by **Prof. H. Postma**

### Chapters in books

- H. Postma and P. Schillebeeckx, "Neutron resonance capture and transmission analysis"  
 In: *Encyclopedia of analytical chemistry* (chapter a9070),  
 R.A. Meyers (Ed.), John Wiley & Sons Ltd. (2009)
- H. Postma and P. Schillebeeckx, "Neutron Resonance Analysis"  
 In: *Neutron Methods for Archaeology and Cultural Heritage* (chapter 12),  
 N. Kardjilov and G. Festa (Eds.), Springer International Publishing Switzerland (2017)
- P. Schillebeeckx and H. Postma, "Neutron resonance analysis (NRA)"  
 In: *The SAS Encyclopedia of Archaeological Sciences*,  
 S.L. Lopez Varela (Ed.), Wiley-Blackwell (2018)
- P. Schillebeeckx and H. Postma, "Neutron Resonance Analysis methods for archaeological and cultural heritage applications"  
 In: *Handbook of Cultural Heritage Analysis* (pp. 145 – 187)  
 S. D'Amico and V. Venuti (Eds.), Springer International Publishing Switzerland (2022)



## NRCA: Authenticity of Etruscan artefacts

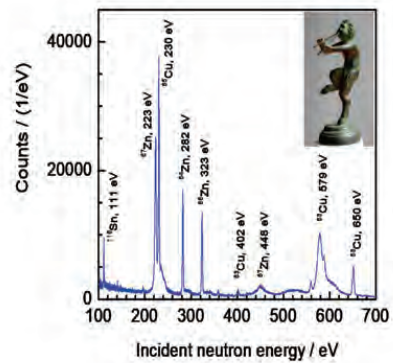
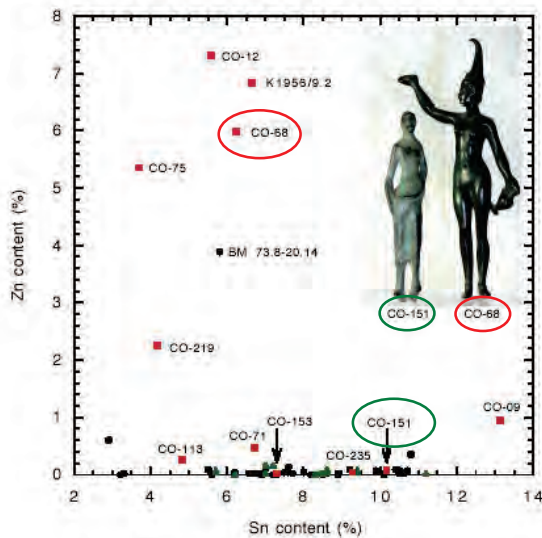


Statuettes from a collection assembled in the 18<sup>th</sup> century by count Corazzi of Cortona (It).  
Now at the National Museum of Antiquities in Leiden (NL).

Postma et al., Archaeometry, 46 (2004) 635



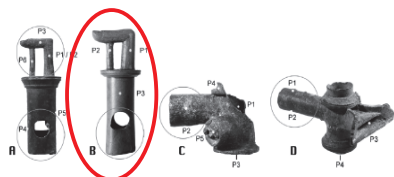
## NRCA: Authenticity of artefacts



NRCA measurements at a 12.5 m station of GELINA of a figurine that is supposed to present the Greek god Pan.  
Zn/Cu ratio: replica



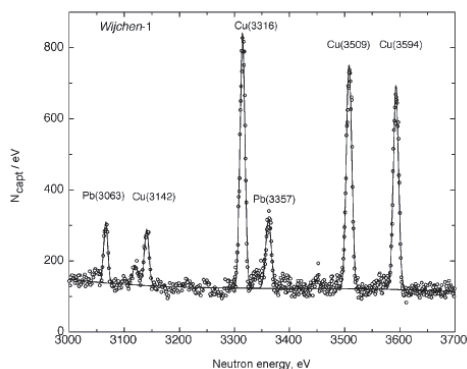
## Roman water taps: NRCA combined with Neutron Diffraction (ND)



NRCA : material composition

ND : fabrication process

NRCA: 4.8 (5) g/cm<sup>2</sup> Cu



Element weight ratio	NRCA (GELINA)	Neutron diffraction (ISIS)		
		P1	P2	P3
Pb/Cu	0.335 (34)	0.415	0.337	0.402
Sn/Cu	0.0868 (25)	0.094	0.098	0.094
Zn/Cu	0.0036 (3)			
Sb/Cu	0.00167 (3)			
Fe/Cu	0.0012 (3)			
As/Cu	0.00098 (3)			
Ag/Cu	0.00096 (3)			

Schut et al., J. Radioanal. Nucl. Chem. 278 (2008) 151

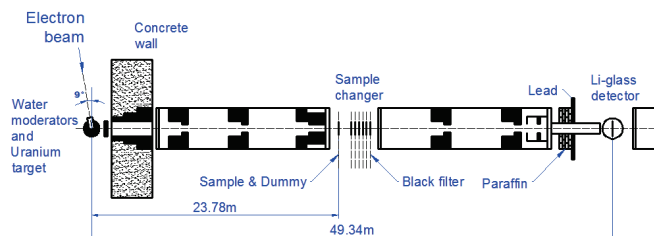


## Characterisation of PbI<sub>2</sub> by NRTA at GELINA

- JRC Geel target preparation group extracted:
  - 150 g Iodine (powder) from 210 liter from **reprocessed waste** (Le Hague)
  - (1.3 g/l Iodine and 40 MBq/l)
- Sample characterisation: by mass spectrometry , NAA and **NRTA**



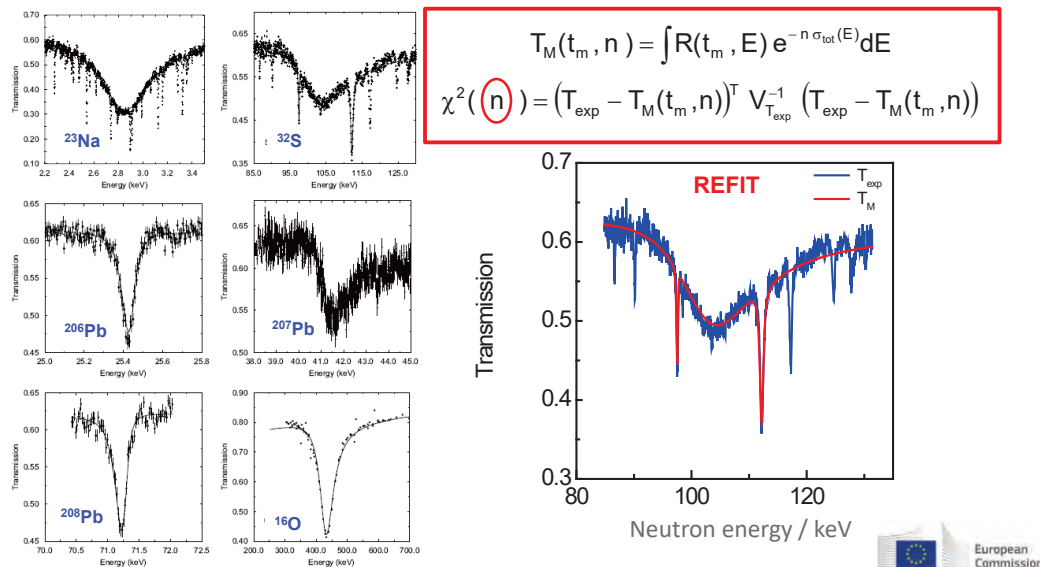
Fig.3. Addition of Pb(NO<sub>3</sub>)<sub>2</sub> to the iodide solution to precipitate lead iodide.



Noguere et al., Nucl. Instr. Meth. Phys. Res. A 575 (2007) 476



## Characterisation of $PbI_2$ by NRTA at GELINA



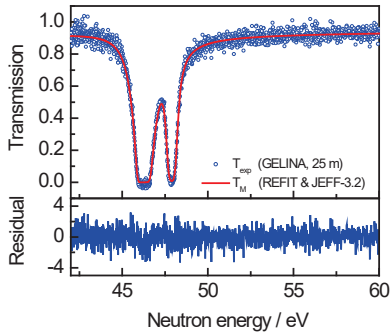
## NRTA compared with NAA and ICP-MS

Element		NRTA	NAA	Mass spectrometry (PSI)
Iodine	total	20.24 (41)	19.75 (61)	19.86 (41)
	$^{127}I$	3.44 (5)	3.35 (10)	3.36 (8)
	$^{129}I$	16.80 (40)	16.40 (60)	16.50 (40)
Lead	Total	52.3 (17)	51.1 (1.8)	
	$^{206}Pb$	12.8 (5)		
	$^{207}Pb$	11.5 (1)		
	$^{208}Pb$	27.1 (17)		
Sulfur		5.44 (3)		
Sodium		0.72 (2)		1.0 (2)
Oxygen		13.92 (5)		14.5 (15)
Hydrogen		<0.13		0.020 (2)
Nitrogen				1.2 (4)

- NRTA ↔ NAA, ICPMS :
- more elements analysed
  - isotopic composition of Pb



## NRTA of W sample: validation of resonance parameters

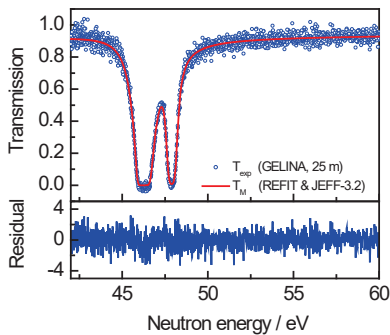


- Sample: metallic disc of <sup>nat</sup>W (1 mm thick)
  - homogeneous sample
  - areal density n : from weight and area  
 $\Rightarrow u_n/n < 0.2\%$
- Transmission : absolute measurement
  - absolute measurement
  - methodology well understood (background, dead time correction,...)  
Nuclear Data Sheets 113 (2012) 3054 – 3100  
 $\Rightarrow u_{T_{exp}}/T_{exp} < 0.3\%$

$\Rightarrow$  NRTA: one of the most accurate benchmark experiments to validate resonance parameters



## NRTA of W sample: validation of resonance parameters

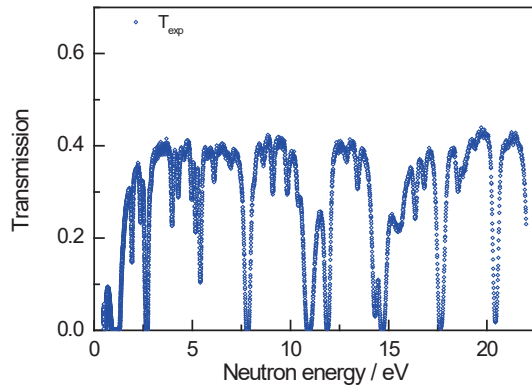


Reference	$E_r = 46.26 \text{ eV}$		$E_r = 47.80 \text{ eV}$		$n_{NRTA}/n_{REF}$
	$\Gamma_n / \text{meV}$	$\Gamma_\gamma / \text{meV}$	$\Gamma_n / \text{meV}$	$\Gamma_\gamma / \text{meV}$	
Lynn et al. 2002	162 (1)	72	126 (2)	72	0.983 (10)
Mughabghab 1984	140 (4)	77 (8)	108 (10)	78 (10)	1.198 (34)
Mughabghab 2006	162 (2)	77 (8)	122 (2)	78 (10)	0.992 (14)
JEFF-3.2	163.4	75.3	120.8	61.5	1.002 (5)
JENDL-3.3	154.0	46.0	119.0	81.0	1.113 (5)
<b>ENDF/B-VII.1</b>	<b>154.0 (8)</b>	<b>46.0 (21)</b>	<b>119.0 (12)</b>	<b>81.0 (51)</b>	<b>1.113 (11)</b>

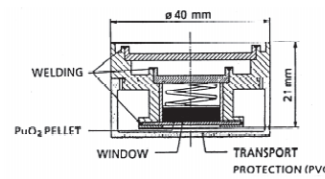
$\Rightarrow$  Parameters in ENDF/B-VII.1 (JENDL-3.3) strongly biased and covariance data not reliable



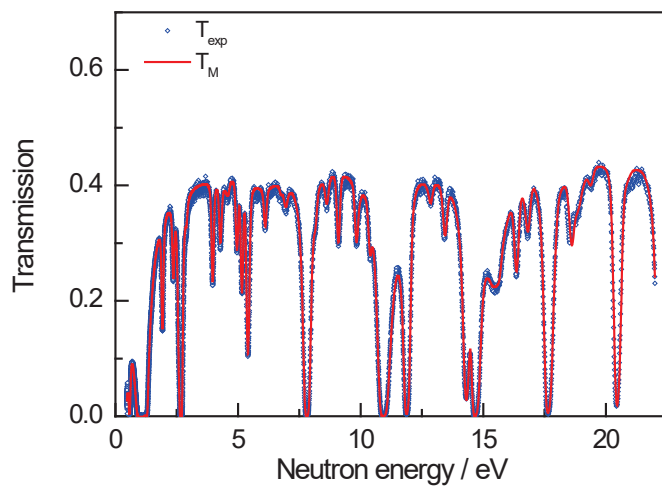
### NRTA of PuO<sub>2</sub> sample: validation of resonance parameters



CBNM - 271



### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



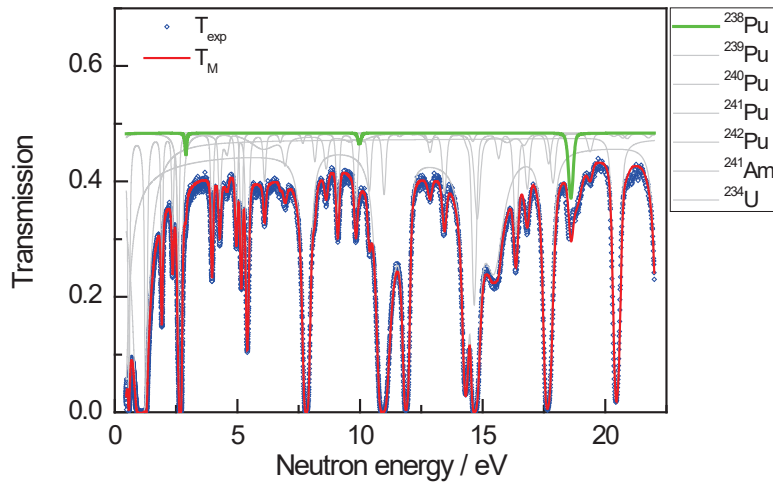
$$T_M(t_m, n) = \int R(t_m, E) e^{-n \sigma_{tot}(E)} dE$$

$$\chi^2(\mathbf{n}) = (T_{exp} - T_M(t_m, \mathbf{n}))^T V_{T_{exp}}^{-1} (T_{exp} - T_M(t_m, \mathbf{n}))$$

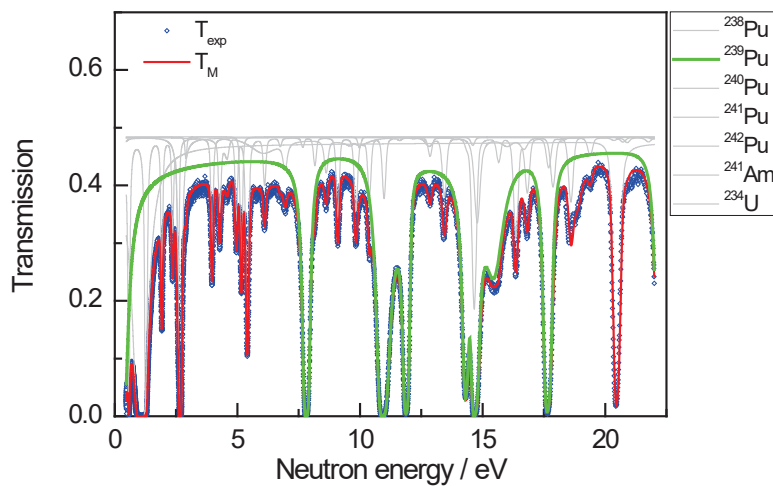
REFIT



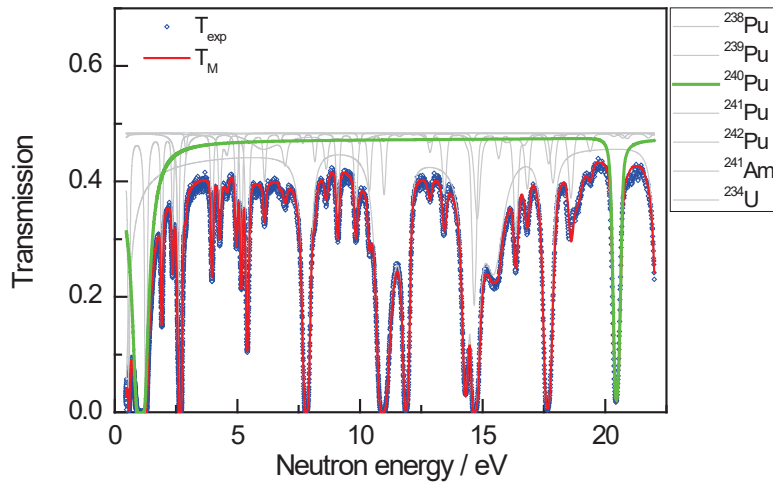
NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



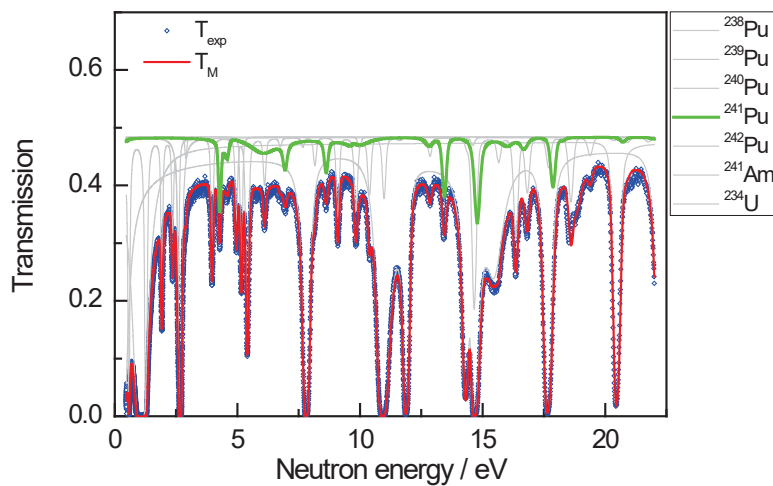
NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



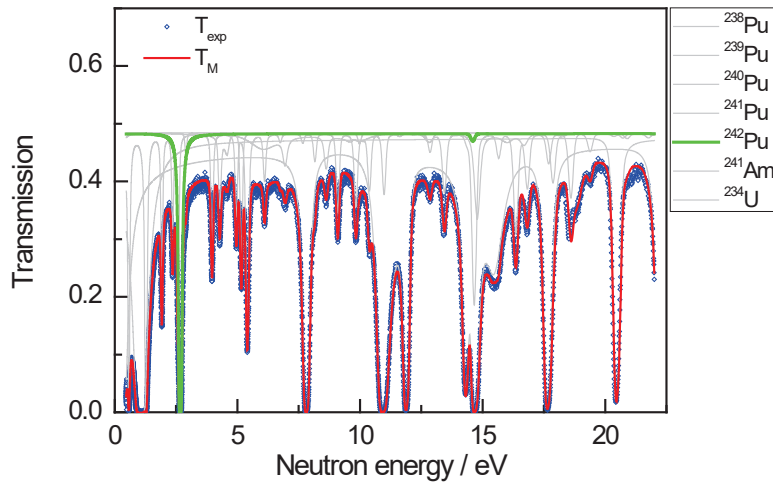
NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



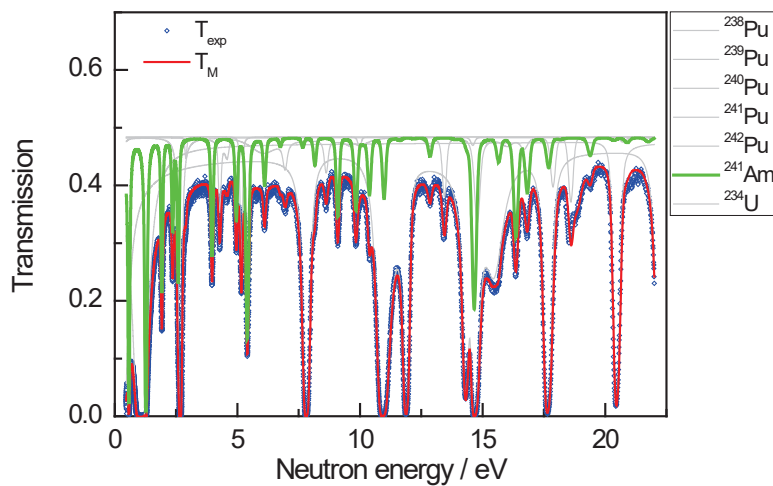
NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



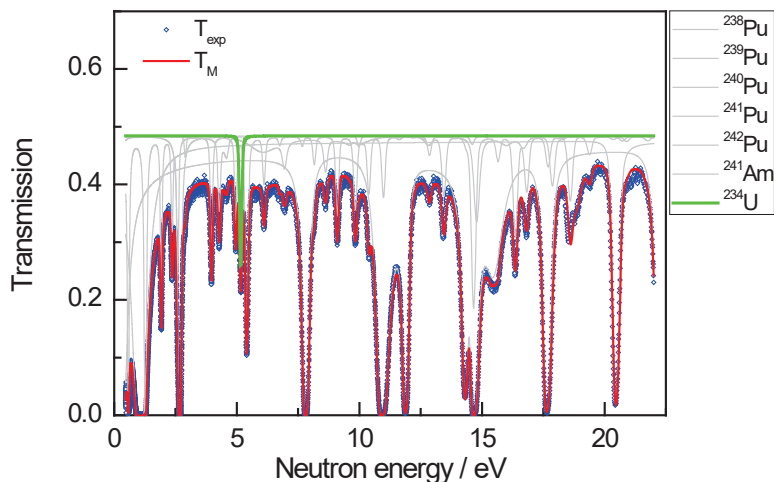
NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



### NRTA of PuO<sub>2</sub> sample (pressed pellet) at GELINA (CBNM – 271)



### NRTA of PuO<sub>2</sub> sample: validation of resonance parameters

Nuclide	n <sub>REF</sub>	n <sub>X</sub> /n <sub>Pu</sub>			
		n <sub>NRTA</sub>		n <sub>NRTA</sub> / n <sub>REF</sub>	
		ENDF/B-VIII.0	JEFF-3.2	ENDF/B-VIII.0	JEFF-3.2
<sup>238</sup> Pu	0.009514 (20)	0.00783 (70)	0.00898 (70)	0.823 (74)	0.944 (74)
<sup>239</sup> Pu	0.62603 (28)	0.62154 (90)	0.61530 (95)	0.9928 (14)	0.9829 (15)
<sup>240</sup> Pu	0.25273 (24)	0.25699 (36)	0.26240 (32)	1.0169 (14)	1.0383 (13)
<sup>241</sup> Pu	0.015697 (20)	0.01574 (10)	0.01577 (10)	1.0028 (64)	1.0045 (65)
<sup>242</sup> Pu	0.041489 (60)	0.04334 (10)	0.04300 (10)	1.0447 (25)	1.0365 (24)
<sup>241</sup> Am	0.06290 (63)	0.07236 (21)	0.06059 (20)	1.1503 (33)	0.9633 (32)
<sup>234</sup> U	0.002918 (10)	0.00289 (10)	0.00287 (10)	0.989 (34)	0.982 (35)

RP in ENDF/B-VIII.0 for <sup>241</sup>Am are strongly biased:  
 $\sigma(n,\gamma)$  underestimated

n: atomic abundance relative to total Pu  
 NRTA uncertainties only due to counting statistics



## NRTA: characterisation of melted fuel

For **particle**- and **rock**- like debris of melted fuel the Lambert – Beer law is not directly applicable

Transmission is a non-linear function of n

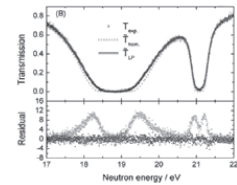
- Homogeneous sample :  $T = e^{-n \sigma_{tot}}$
- Heterogeneous sample :  $\langle T \rangle = \langle e^{-n \sigma_{tot}} \rangle \neq e^{-\langle n \rangle \sigma_{tot}}$



### Levermore-Pomraning model (J. Math. Phys. 27, 2526, (1986))

- widely used for other problems dealing with radiation transport through stochastic media, e.g. scattering of sunlight in clouds
- starts from microscopic properties of the sample such as grain size
- in particular applicable for powder samples

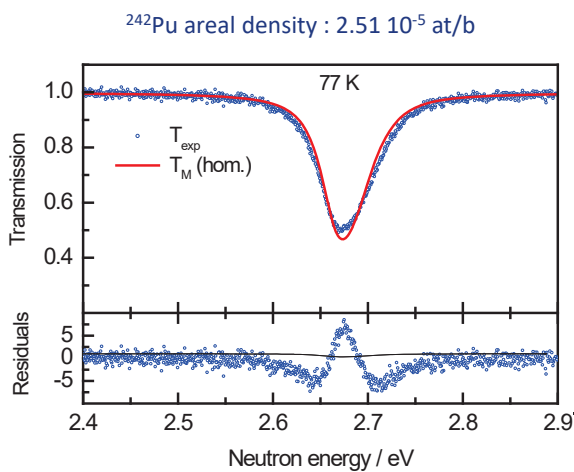
implemented in **REFIT** and **validated** by experiments at **GELINA**



Becker et al., Eur. Phys. J. Plus 129 (2014) 58



## PuO<sub>2</sub> mixed with carbon powder: NRTA at GELINA



$$T_M(t_m, n) = \int R(t_m, E) T(E, n) dE$$

$$T(E, n_{1, \dots, k}) = e^{-\sum_{j=1}^k n_j \sigma_{tot,j}(E)}$$

Suppose homogeneous without holes

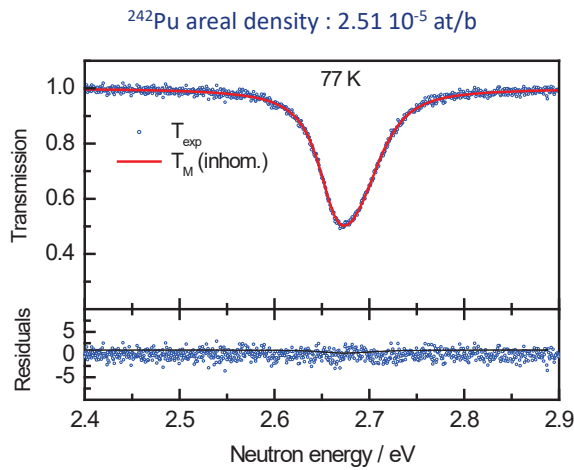
Model	Areal density <sup>242</sup> Pu
Homogeneous	1.65 10 <sup>-5</sup> at/b

Underestimated by 35 %

Kopeccky et al., ND2007, Nice, 2007



## PuO<sub>2</sub> mixed with carbon powder: NRTA at GELINA



$$T_M(t_m, n) = \int R(t_m, E) T(E, n) dE$$

$$T(E, n) = \left[ \int e^{-\sum_{j=1}^k n_j \sigma_{tot,j}(E)} p(x) dx \right] (1 - f_h) + f_h$$

$$n_j = \frac{n_j}{1 - f_h} \quad p(x) = \frac{1}{x\sqrt{2\pi}s^2} \exp\left(-\frac{(\ln x + s^2/2)^2}{2s^2}\right)$$

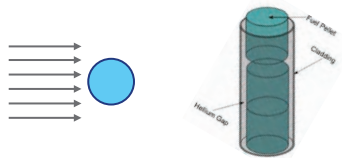
Model	Areal density <sup>242</sup> Pu
Homogeneous	1.65 10 <sup>-5</sup> at/b
Inhomogeneous	2.50 10 <sup>-5</sup> at/b

⇒ bias < 1%

Model developed, implemented and validated at JRC Geel (S. Kopecky)



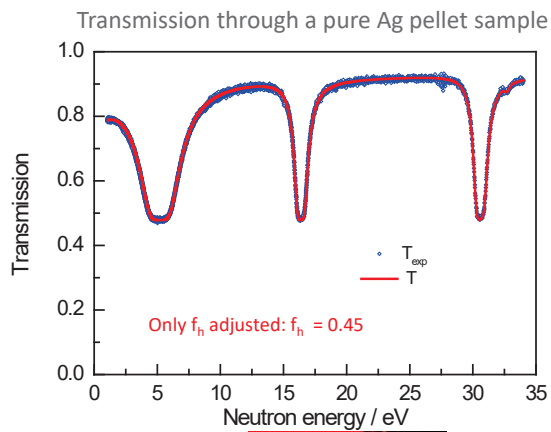
## NRTA model for pellet samples



$$T(E) = f_h + (1 - f_h) \int_0^1 \frac{x}{\sqrt{1-x^2}} e^{-\rho \sigma_{tot}(E) x} dx$$

REFIT - x : track length (divided by 2R)

- f<sub>h</sub> : holes fraction
- ρ : volume number density
- R : radius



Model developed, implemented and validated at JRC Geel (S. Kopecky)

Fei Ma et al., J. Anal. At. Spectrom. 35 (2020) 478

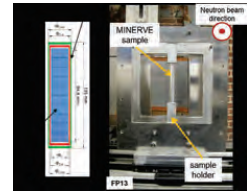
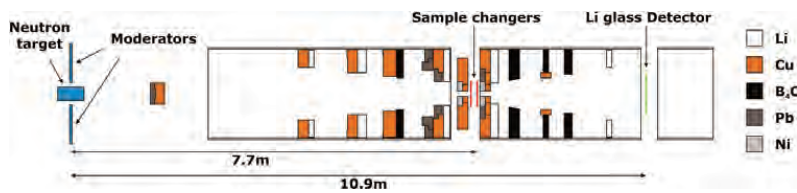




## NRTA: MINERVE samples

Collaboration with CEA Cadarache

- NRTA of irradiated MINERVE pellet samples at GELINA (part of MAESRTRO)
  - Identification and quantification of impurities
  - Validation of resonance parameters of fission products
- Important for criticality safety studies based on Burn Up Credit (BUC)
- New transmission station (L = 10 m) constructed at GELINA

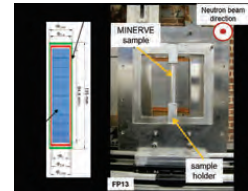


- $^{103}\text{Rh}$
- $^{107,109}\text{Ag}$
- $^{133}\text{Cs}$
- $^{143,145}\text{Nd}$
- $^{147,149,152}\text{Sm}$ ,
- $^{151,153}\text{Eu}$
- $^{161,162,163,164}\text{Dy}$
- $^{168,170}\text{Er}$
- $^{180}\text{Hf}$

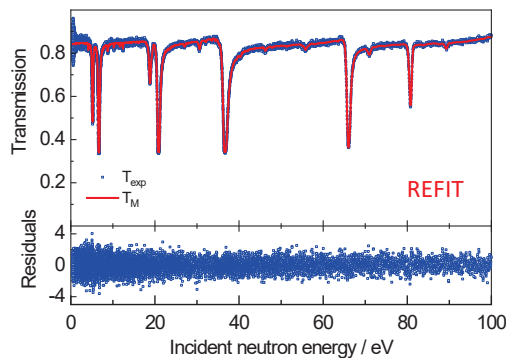


## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA (part of MAESRTRO)
  - Identification and quantification of impurities
  - Validation of resonance parameters of fission products
- Important for criticality safety studies based on Burn Up Credit (BUC)



$^{109}\text{Ag}$



Note:

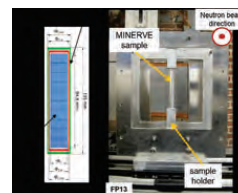
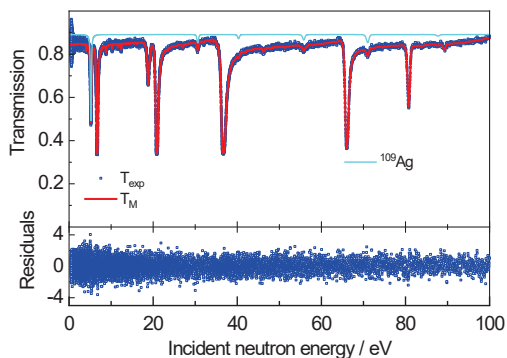
RP used result from a new evaluation for  $^{107,109}\text{Ag}$  based on capture and transmission experiments at GELINA

Šalamon et al., Nucl. Instr. Meth. B 446 (2019) 19



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA (part of MAESRTRO)
  - Identification and quantification of impurities
  - Validation of resonance parameters of fission products
- Important for criticality safety studies based on Burn Up Credit (BUC)

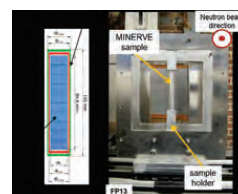
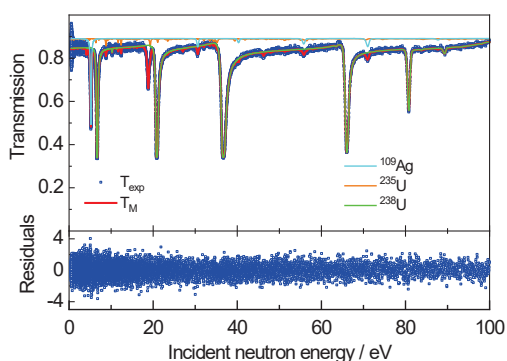


<sup>109</sup>Ag



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA (part of MAESRTRO)
  - Identification and quantification of impurities
  - Validation of resonance parameters of fission products
- Important for criticality safety studies based on Burn Up Credit (BUC)

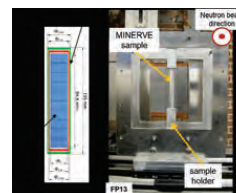
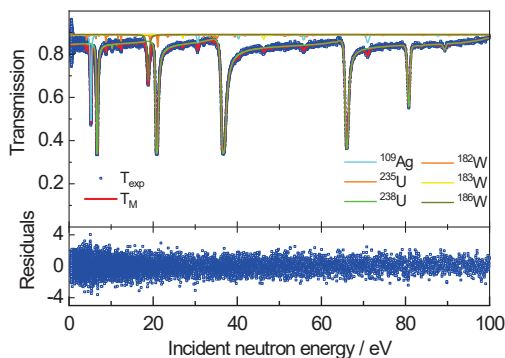


<sup>109</sup>Ag



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA (part of MAESRTRO)
  - Identification and quantification of impurities
  - Validation of resonance parameters of fission products
- Important for criticality safety studies based on Burn Up Credit (BUC)

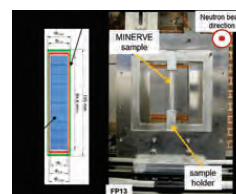


<sup>109</sup>Ag



## NRTA: MINERVE samples

- NRTA of irradiated MINERVE pellet samples at GELINA (part of MAESRTRO)
  - Identification and quantification of impurities
  - Validation of resonance parameters of fission products
- Important for criticality safety studies based on Burn Up Credit (BUC)



<sup>109</sup>Ag

	AG9C1		AG9C2	
	ICPMS	This work	ICPMS	This work
<sup>109</sup> Ag	6.30 (8) × 10 <sup>-4</sup>	6.03 (2) × 10 <sup>-4</sup>	6.82 (8) × 10 <sup>-5</sup>	6.54 (2) × 10 <sup>-5</sup>
<sup>235</sup> U	8.31 (10) × 10 <sup>-5</sup>	8.35 (20) × 10 <sup>-5</sup>	8.39 (10) × 10 <sup>-5</sup>	8.45 (20) × 10 <sup>-6</sup>
<sup>238</sup> U	1.119 (14) × 10 <sup>-2</sup>	1.126 (5) × 10 <sup>-2</sup>	1.129 (14) × 10 <sup>-2</sup>	1.136 (5) × 10 <sup>-2</sup>
<sup>182</sup> W		1.30 (4) × 10 <sup>-5</sup>		6.1 (3) × 10 <sup>-6</sup>
<sup>183</sup> W		6.6 (2) × 10 <sup>-6</sup>		3.1 (2) × 10 <sup>-6</sup>
<sup>186</sup> W		1.36 (1) × 10 <sup>-5</sup>		6.11 (3) × 10 <sup>-6</sup>

10<sup>24</sup> at/cm<sup>3</sup>

Šalamon et al., J. Radioanal. Nucl. Chem. 321 (2019) 519

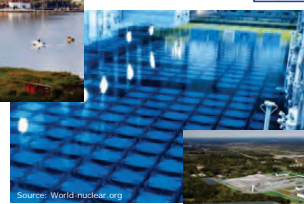


## Back-end of the fuel cycle: spent fuel characterisation (SFC)

A **safe, secure, ecological** and **economic** handling, transport, intermediate storage and final disposal requires that **Spent Nuclear Fuel (SNF)** is **characterised** for the main observables or source terms of interest:

- Decay heat
- Neutron emission
- $\gamma$ -ray emission
- Reactivity (BurnUp Credit)  
(i.e. Fission Product (FP), actinides)
- Fissile material (Nuclear Safeguards, i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ )
- Specific nuclides (Long term safety)  
i.e.  $^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$ ,  $^{237}\text{Np}$

⇒ requires knowledge of a **complex nuclide inventory**  
 ⇒ can only be determined by **theoretical calculations**



## Burnup calculations: e.g. SCALE, MCNP/CINDER, MCNP/ALEPH2, ...

Coupled neutron transport – nuclide depletion/production

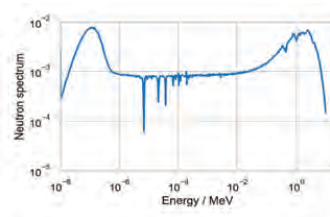
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_{i \rightarrow k} \lambda_i N_i + \sum_{j \rightarrow k} \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

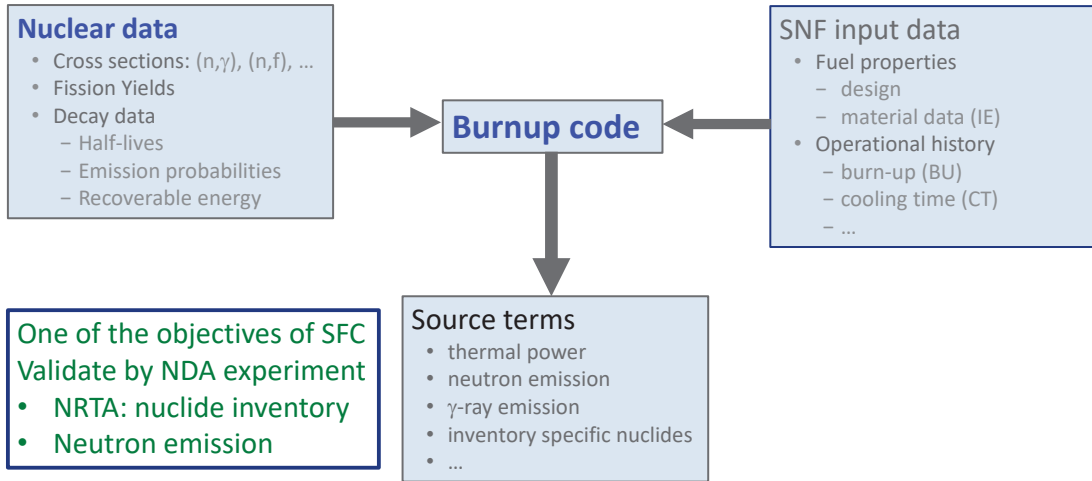
Update nuclide vector



Training material



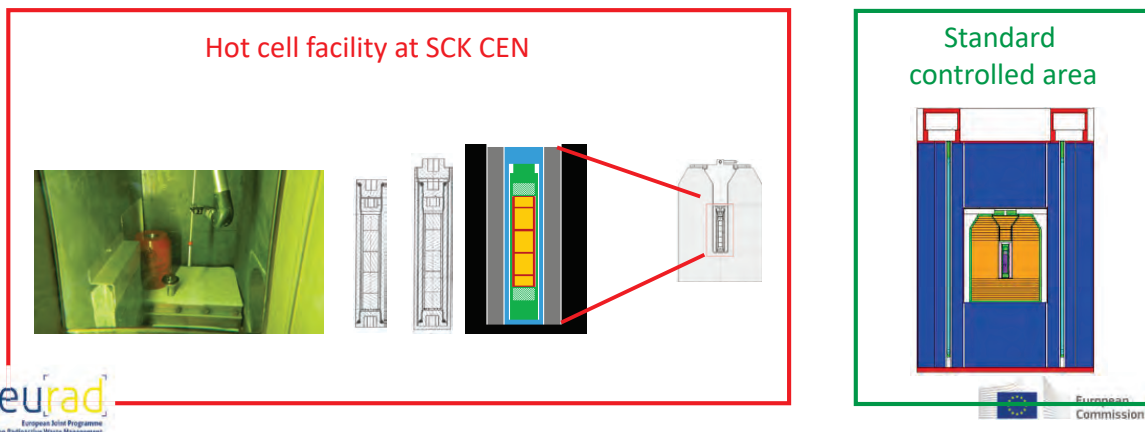
## Burnup calculations need to be validated



## Validation of depletion codes: neutron emission rate of SNF

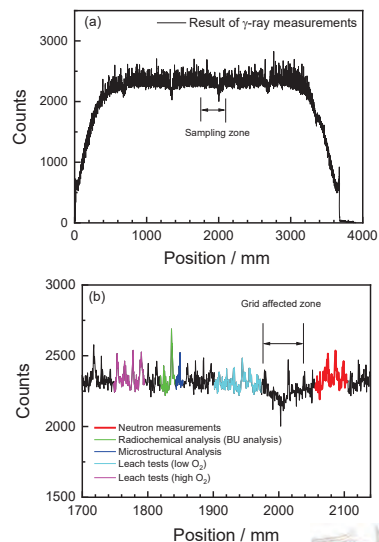
**NDA method** to determine the neutron output of a **SNF** sample under **standard controlled area** conditions

Collaboration SCK CEN



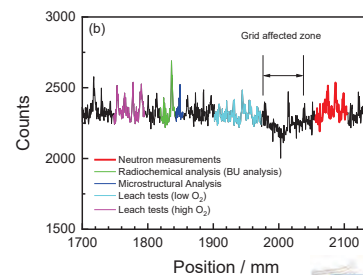
## EURAD: Validation of depletion codes

- **Irradiation history of the SNF**
  - Segment (~ 50 mm) from rod D05 of FT1X57 (PWR)
  - PWR Assembly (15 x 15):  
188 UO<sub>2</sub> rod (4.5 wt% <sup>235</sup>U/U) and 16 (U,Gd)O<sub>2</sub> rods
  - Irradiated at Tihange 1
  - Rod used for other international project (First-Nuclides, REGAL, WETFUEL & AGAF, SF-ALE)
- **SNF segment sample by NDA**  
Part of a set of 4 samples (REGAL project)
  - Radiochemical analysis (BU)
  - Microstructural analysis
  - Leach tests (low O<sub>2</sub>)
  - Leach tests (high O<sub>2</sub>)



## Results of radiochemical analysis

BU indicator	Date of analysis	Nuclide inventory mg/g	Cumulative fission yield (x 100)	Burnup GWD/t
<sup>137</sup> Cs	10/21/2013	1.288 (28)	6.334	52.6 (11)
<sup>143</sup> Nd + <sup>144</sup> Nd	02/05/2014	3.029 (32)	10.158	53.95 (56)
<sup>145</sup> Nd + <sup>146</sup> Nd	02/05/2014	1.962 (21)	6.479	53.05 (56)
<sup>148</sup> Nd	02/05/2014	0.534 (12)	1.724	53.3 (12)
<sup>150</sup> Nd	02/05/2014	0.257 (11)	0.836	52.2 (23)
				Average: 52.78 (37)



Schillebeeckx et al., JRC Technical Reports, EUR 30379 EN (2020)



## Absolute neutron output of SNF segment sample: results

- SNF segment sample: characteristics

Parameter	Value
Length	52.01 (4) mm
Segment weight	42.616 (1) g
Cladding weight	6.71 (4) g
Net fuel weight	35.91 (4) g

- Neutron emission rate (exp) <sup>CT 18 a</sup>

$$S_{sf} = 24505 (375) \text{ s}^{-1}$$

$$S_{\alpha n} / S_{sf} = 0.036 (15)$$

$$\rho(S_{sf}, \alpha) = -0.972$$

Neutron correlation analysis: Hage's point model

Hage and Cifarelli, Nucl. Instr. Meth. A236 (1985) 165

Detector calibrated with certified <sup>252</sup>Cf(sf) sources (Mn bath)

Note: neutron emission rate reflects <sup>244</sup>Cm inventory  
radiochemical analysis uncertainty > 3%



Schillebeeckx et al., JRC Technical Reports, EUR 30379 EN (2020)



## Absolute neutron output of SNF segment sample: code validation

Code	Library	.....(α,n).....		S <sub>sf</sub> / (g <sup>-1</sup> s <sup>-1</sup> )	S <sub>α</sub> / (g <sup>-1</sup> s <sup>-1</sup> )	Calculation/Experiment	
		Method	Library			S <sub>sf</sub>	S <sub>αn</sub>
SCALE	ENDF/B-VII.1	Y(α,n)		653	11.0	0.96	0.45
SERPENT(1)	ENDF/B-VII.1	Y(α,n)		689	14.3	1.01	0.58
SERPENT(2)	ENDF/B-VII.1	Y(α,n)		694	14.2	1.02	0.58
	ENDF/B-VIII.0	Y(α,n)		691	14.1	1.01	0.57
	JEFF-3.1.2	Y(α,n)		629	13.2	0.92	0.54
	JEFF-3.3	Y(α,n)		654	13.7	0.96	0.56
	JEFF-4T0	Y(α,n)		695	13.7	1.02	0.56
	JENDL-4.0			719	14.5	1.05	0.59
ALEPH28	ENDF/B-VIII.0	Y(α,n)		662	13.1	0.97	0.53
		σ(α,n)	TENDL2015		12.6		0.51
		σ(α,n)	JENDL_AN/500		10.6		0.43
	JEFF-3.3	Y(α,n)		641	12.9	0.94	0.53
		σ(α,n)	TENDL2015		12.7		0.52
		σ(α,n)	JENDL_AN/500		10.5		0.43

All data normalised to <sup>148</sup>Nd inventory

$$S_{sf} = 682 (10) \text{ g}^{-1} \text{ s}^{-1}$$

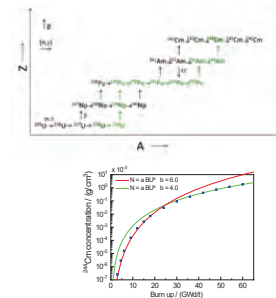
$$S_{\alpha n} / S_{sf} = 0.036 (15)$$

⇒ influence

- nuclear data
- burnup code

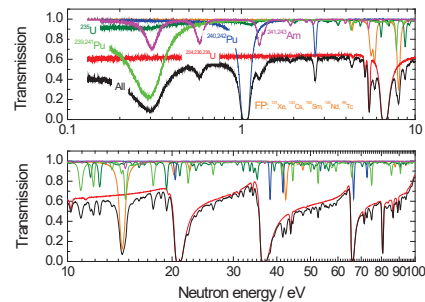
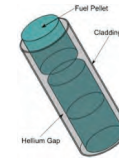
Neutron emission rate:

- <sup>244</sup>Cm inventory
- Nuclear data: <sup>241</sup>Pu(n,γ) & <sup>243</sup>Am(n, γ)
- Very sensitive to BU

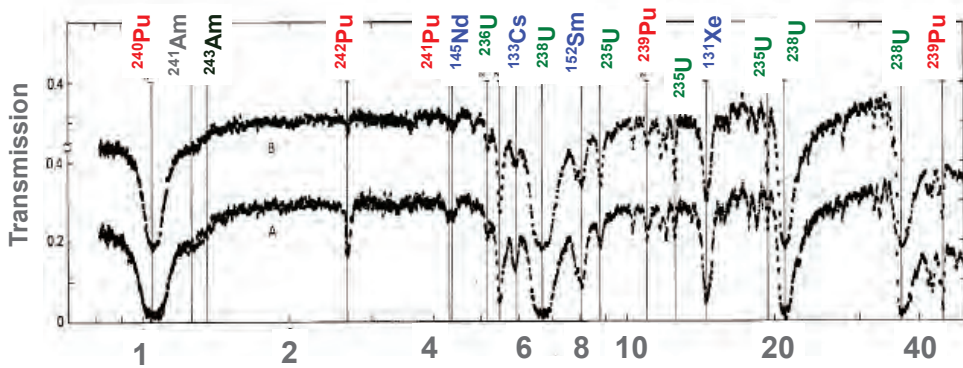


## NRTA on irradiated pellet $\Rightarrow$ nuclide vector

- NRTA on spent fuel pellet at GELINA  
 $\Rightarrow$  **Nuclide vector by NDA** avoiding chemical analysis
- Analytical models already implemented in REFIT and validated at GELINA
- *Construct a transfer container fulfilling NRTA measurement requirements at GELINA*



## SNF: complex transmission spectrum, Priesmeyer et al.



A : centre of fuel pin  
 B : end of fuel pin

H.G. Priesmeyer and U. Harz, Atomenergy 25 (1975) 109





## Summary

- The use of NRCA & NRTA as NDA techniques for the characterisation of material and objects was presented
- Can be applied for a wide range of applications
  - Archaeology and cultural heritage
  - Validation of nuclear data
  - Nuclear waste
  - Imaging in case of high intense pulsed neutron beams (LANSCE, J-PARC)
  - ...
- Use of NDA techniques important for SNF characterisation
  - Absolute determination of the neutron emission rate important to validate burnup codes: estimation of the  $^{244}\text{Cm}$  inventory
  - NRTA: determine nuclide inventory (scheduled 2024...)

### scientific reports

OPEN **3D isotope density measurements by energy-resolved neutron imaging**

A. S. Losko<sup>1,2\*</sup> & S. C. Vogel<sup>1</sup>



## Keep in touch



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Thank you



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**6.4 Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten LWR-Brennstoffproben; R. Dagan, T. König et al., KIT; BGZ Studierendentag; 05 – 06/05/2022**



## Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

T. König, R. Dagan, K. Dardenne, M. Herm, V. Metz, T. Prüßmann, J. Rothe, D. Schild, A. Walschburger und H. Geckis

Karlsruher Institut für Technologie (KIT) - Institut für Nukleare Entsorgung (INE), 76344 Eggenstein-Leopoldshafen, Deutschland



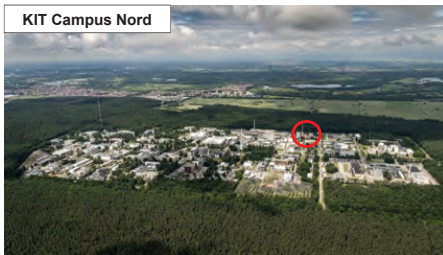
KIT – Die Forschungsuniversität in der Helmholtz-Gemeinschaft

[www.kit.edu](http://www.kit.edu)

## Vorstellung: Das Institut für Nukleare Entsorgung



### Wer sind wir?



→ ~90 Mitarbeiter und viele Studenten, Praktikanten, ausländische Gäste etc.

2 06.05.2022

T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

Institut für Nukleare Entsorgung (INE)

## Gliederung

- **Einleitung:**
  - Kernbrennstoff – Vom Reaktor ins Endlager
- **Experimentelles:**
  - Untersuchte Kernbrennstoffe – *UO<sub>x</sub> und MOX Brennstoff*
  - Radionuklidanalyse – *Inventarbestimmung von abgebrannten Kernbrennstoffen*
  - Spektroskopische Analysen – *Wechselwirkungsschicht zwischen Brennstoff und Hüllrohr*
  - Modellsysteme – *Experimente zur Bildung von Agglomeraten und Korrosion an der Reaktionsschicht*
- **Zusammenfassung**
- **Ein- & Ausblicke** – *Weitere Forschungsfelder am KIT-INE zu Zwischen- und Endlagerung*

3 06.05.2022

T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

Institut für Nukleare Entsorgung (INE)

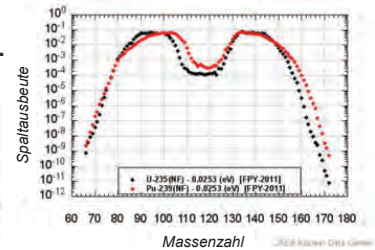
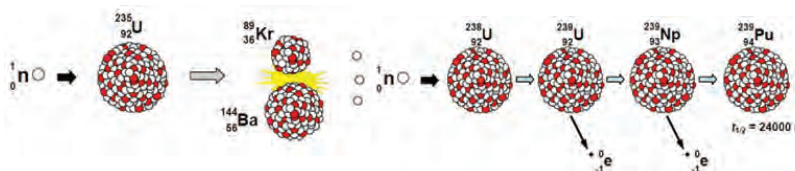


## Kernspaltung in Leichtwasserreaktoren

- **Neutroneninduzierte Fission** von spaltbarem Material (<sup>235</sup>U, <sup>239</sup>Pu, etc.):
  - Freisetzung von Neutronen ⇒ **Aufrechterhaltung der Kettenreaktion.**
  - Generierung von Spaltprodukten ⇒ **2 – 3 Spaltfragmente pro Kernspaltung.**
  - Neutroneneinfangsreaktionen ⇒ **Aufbau von Transuranen (Np, Pu, Am, etc.) & Aktivierungsprodukten (<sup>14</sup>C, <sup>36</sup>Cl).**

- Brennstoffnutzung wird als **Abbrand** beschrieben:

➡ **Produzierte Energie pro Masse initialem Schwermetall [GWd/t<sub>SM</sub>].**



4 06.05.2022

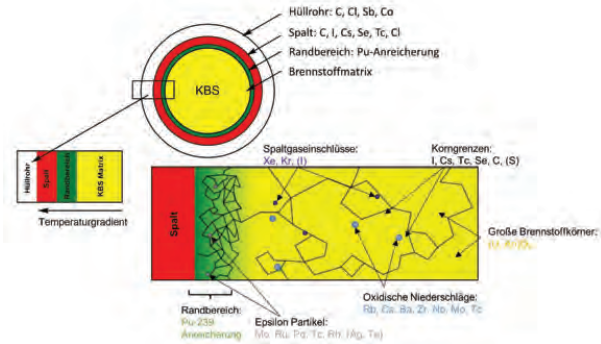
T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

Institut für Nukleare Entsorgung (INE)

## Abgebrannter Kernbrennstoff (KBS)

■ Zusammensetzung von abgebranntem KBS (4,0% <sup>235</sup>U, 52 GWd/t<sub>SM</sub>) in einem Leichtwasserreaktor:

- **93,4% UO<sub>2</sub> Matrix:**  
92% <sup>238</sup>U, < 1% <sup>235</sup>U, < 0,5% <sup>236</sup>U
- **1,2% Transurane / Actinide:**  
1% <sup>239</sup>Pu, <sup>240</sup>Pu, <sup>241</sup>Pu, <sup>237</sup>Np > <sup>244</sup>Cm > <sup>241</sup>Am,
- **5,4% Spaltprodukte:**  
1,7% <sup>90</sup>Sr, <sup>135</sup>, <sup>137</sup>Cs, <sup>129</sup>I, etc.  
1,6% Lanthaniden  
1,3% ε-Phasen (<sup>99</sup>Tc, <sup>109</sup>Pd, etc.)  
0,8% Spaltgase (Krypton, Xenon)



- **Aktivierungsprodukte:**  
z. B. <sup>14</sup>C, <sup>93</sup>Zr, <sup>36</sup>Cl → <sup>35</sup>Cl (n,γ) <sup>36</sup>Cl

→ **Heterogene Verteilung der Radionuklide.**

Quelle: Hippler, Reaktorchemie, Leibniz Universität Hannover

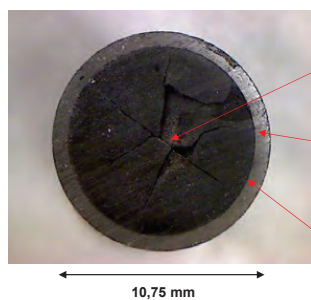
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## Wechselwirkungsschicht zwischen KBS und Hüllrohr

■ Querschnitt einer Kernbrennstofftablette:



**Pellet:** Radiale Rissbildung durch Temperaturgradienten während der Bestrahlung; Migrationspfade für Radionuklide in der KBS Tablette.

**Hüllrohr:** Aufbau einer äußeren ZrO<sub>2</sub> Schicht durch Korrosion auf Grund des Primärkreislaufwassers; dünne ZrO<sub>2</sub> Schicht auf der Innenseite durch Zr / UO<sub>2</sub> Reaktionen.

**Ringspalt:** Schließt sich bei Abbränden > 40 GWd/t<sub>SM</sub>; Ausbildung einer **Wechselwirkungsschicht**.

→ **Möglichkeit des Transports volatiler Spalt- und Aktivierungsprodukten zum Hüllrohr während der Bestrahlung und nachfolgende chemische Reaktionen zwischen KBS und Hüllrohr!**

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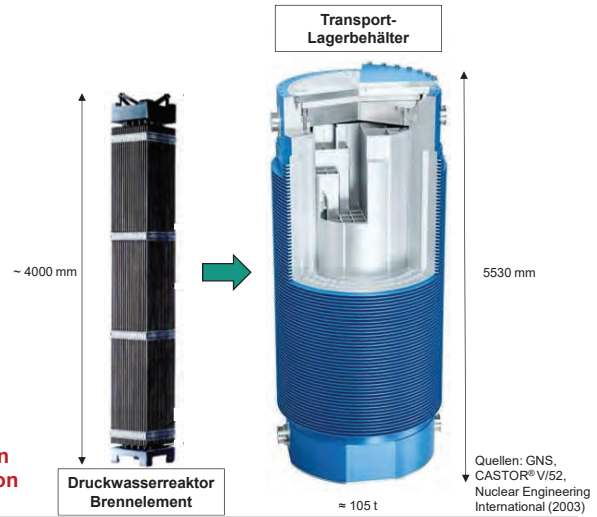
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## Zwischenlagerung in Deutschland

- **Trockene Zwischenlagerung** ausgedienter Brennelemente in Transport-Lagerbehältern (TLB).
  - TLB garantiert **Abschirmung der Strahlung**, sowie einen temporären, **sicheren Einschluss der Radionuklide**.
  - Zwischenlagerung bestrahlter Brennelemente ist lediglich **für 40 Jahre genehmigt**.
  - Endlager voraussichtlich **erst 2050 verfügbar und Einlagerung der letzten Brennelemente erst einige Jahrzehnte später möglich!**

➔ **Notwendigkeit einer verlängerten Zwischenlagerung von 65 – 100 Jahren sowie Umlagerung (Konditionierung) von TLB in Endlagerbehälter!**



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  - Endlager voraussichtlich **erst 2050 verfügbar und Einlagerung der letzten Brennelemente erst einige Jahrzehnte später möglich!**
- Verschiedene Effekte beeinflussen die Integrität des Hüllrohrs während der Zwischenlagerung:
  - **Erhöhung des Hüllrohrinnendrucks** durch Schwellen der Pellets und  $\alpha$ -Zerfälle.
  - **$\alpha$ -Strahlungsinduzierte Schädigung** des Hüllrohrs.
  - Rissbildung durch **Hydrid Re-Orientierung**.  

$$\text{Zr} + 2 \text{H}_2\text{O} \rightarrow \text{ZrO}_2 + 2 \text{H}_2$$
  - **Korrosion des Hüllrohrs durch Spalt- und Aktivierungsprodukte.**

➔ **Bildung von Agglomeraten an Hüllrohrinnenseite durch thermischen Gradienten im KBS und somit Möglichkeit einer halogeninduzierten Spannungsrisskorrosion.**

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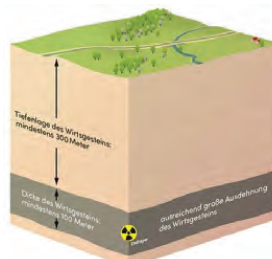
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## Endlagerung in Deutschland

- Tiefengeologische Endlagerung:
  - **3 unterschiedliche Gesteinsarten** (Ton-, Salz- und Kristallingestein) werden in Betracht gezogen.
  - **Sicherer Einschluss über langen Zeitraum** muss gewährt werden (1 Million Jahre).

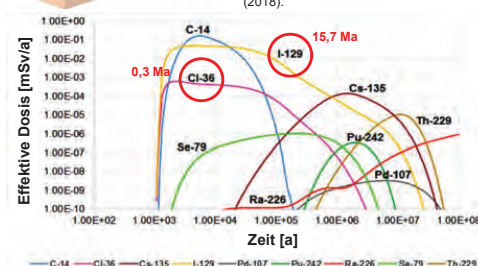


Quelle:  
[https://www.einblicke.de/fileadmin/imag/magazin/Einblicke\\_6/Kriterien\\_zur\\_Endlagersuche.jpg](https://www.einblicke.de/fileadmin/imag/magazin/Einblicke_6/Kriterien_zur_Endlagersuche.jpg) (aufgerufen am 04.04.2022)

[FLA18]: D. Flamikova, V. Necas, *Creation of Reference Biosphere Model for Safety Assessment of Deep Geological Repository*, AIP Conference Proceedings 1996, 020009 (2018).



**Sicherheitsbewertung erfordert grundlegende Kenntnisse über das Vorkommen und chemisches Verhalten von langlebigen und dosisrelevanten Radionukliden (z. B. <sup>36</sup>Cl, <sup>129</sup>I, <sup>135</sup>Cs)**



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## Fragestellung

- Wenn nach längerer Zeit (geo-) technische Barrieren den Zutritt von Wasser nicht mehr vollständig verhindern, werden <sup>36</sup>Cl und <sup>129</sup>I in Kernbrennstoff relativ wenig zurückgehalten! In welcher Konzentration und in welcher Form liegen <sup>36</sup>Cl und <sup>129</sup>I in Brennstäben vor?
  - **Quantifizierung und Lokalisierung von den unter Endlagerbedingungen relativ mobilen Radionukliden <sup>36</sup>Cl und <sup>129</sup>I in Kernbrennstoff und Hüllrohr.**
  - **Vergleich experimentell bestimmter Radionuklidkonzentrationen mit berechneten Inventardaten aus (neutronen-) physikalischen Modellierungen.**
- In welchem Zustand ist die Brennstoff-Hüllrohr-Grenzfläche während der Zwischenlagerung?
  - **In welcher Form liegen eventuell hüllrohrschädigende Elemente wie Chlor oder Iod in KBS und Hüllrohr vor?**
  - **Ist eine halogeninduzierte Lochfraßkorrosion auch bei Zwischenlagerungstemperaturen möglich?**

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## Kernbrennstoffproben

### Brennstabsegment N0204, bestrahlt im Druckwasserreaktor, DWR Gösgen:

- Brennstofftyp: **UO<sub>x</sub>** mit 3,8% <sup>235</sup>U Anreicherung.
- Hüllrohr: Zircaloy-4.
- Volllasttage: 1226 Tage in 4 Zyklen.
- Durchschnittliche lineare Leistung: 260 W/cm.
- Durchschnittlicher Abbrand: **50,4 GWd/t<sub>SM</sub>**.
- Abklingzeit: ~ 32 Jahre.



### Brennstab 5810, bestrahlt im Druckwasserreaktor, DWR Obrigheim:

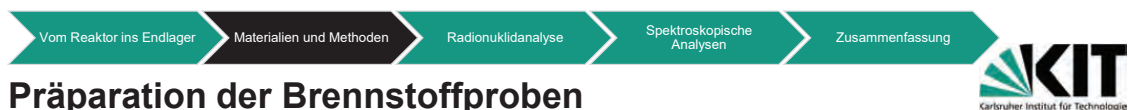
- Brennstofftyp: **MOX** mit 3,2% Pu<sub>fiss</sub> Anreicherung.
- Hüllrohr: Zircaloy-4.
- Volllasttage: 1157 Tage in 4 Zyklen.
- Durchschnittliche lineare Leistung: 200 W/cm.
- Durchschnittlicher Abbrand: **38,0 GWd/t<sub>SM</sub>**.
- Abklingzeit: ~ 35 Jahre.



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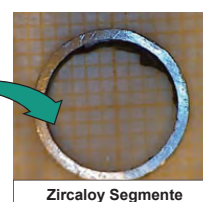
*T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben*

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## Präparation der Brennstoffproben

- Zuschneiden der Brennstoffproben in speziell ausgestatteten Laboren (**Heiße Zellen**) auf Grund der enormen Dosisleistung!
- Selektive Probennahme zur **Analyse lokaler Radionuklidanreicherungen**:
  - Fragmente aus **zentraler Position** („CORE“).
  - Fragmente aus **peripherer Position** („RIM“).
  - **Zircaloy-Hüllrohrsegmente**.



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Vom Reaktor ins Endlager    Materialien und Methoden    Radionuklidanalyse    Spektroskopische Analysen    Zusammenfassung

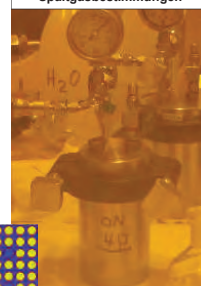


## Radiochemische Analytik & numerische Berechnungen

■ **Saurer und alkalischer Aufschluss** von Zircaloy- und Brennstoffproben in HF / H<sub>2</sub>SO<sub>4</sub>, HNO<sub>3</sub> / HCl oder (NH<sub>4</sub>)<sub>2</sub>CO<sub>3</sub> / H<sub>2</sub>O<sub>2</sub>:

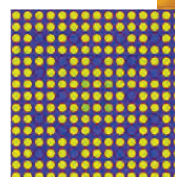
- **γ-Spektrometrie:** <sup>241</sup>Am, <sup>134, 137</sup>Cs, <sup>125</sup>Sb, <sup>154, 155</sup>Eu, <sup>60</sup>Co, <sup>129</sup>I.
- **Flüssigszintillationsmessung:** <sup>129</sup>I, <sup>36</sup>Cl, <sup>90</sup>Sr. ➔ **Sehr hohe Reinheit der Proben erforderlich!**
- **ICP-MS:** <sup>235, 238</sup>U, <sup>237</sup>Np, <sup>239, 240</sup>Pu, <sup>241</sup>Am, <sup>244</sup>Cm.
- **Gas-MS:** Kr- und Xe-Isotope.

Aufschluss in Autoklaven für Spaltgasbestimmungen



■ **Berechnungen des Radionuklidinventars** mittels **MCNP Code** für Neutronenfluss und **CINDER Modul** für Abbrand-Berechnungen:

- Numerische Berechnungen für die jeweiligen Brennstoffanordnungen, Reaktortypen und Bestrahlungsbedingungen.
- Radionuklidkonzentrationen im zentralen und Randbereich des Pellets.



Simulationen der Brennstoffanordnungen

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## Spektroskopische Messungen

■ Präparation von Brennstofffragmenten und Zircaloy-Segmenten für Analysen mittels **SEM-EDX/WDX, XPS** und **XAS an der KIT Light Source**. ➔ **Enorme Strahlenschutzmaßnahmen erforderlich!**

- Proben für **Bestimmung der chemischen Zusammensetzung**.
- Proben für **Speziationsmessungen**.

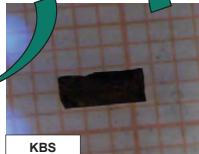
SEM-EDX-WDX / XPS Messungen



Zircaloy



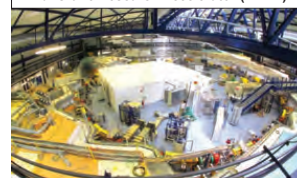
KBS



XAS Messungen für Cl und I Speziation



Karlsruhe Research Accelerator (KARA)



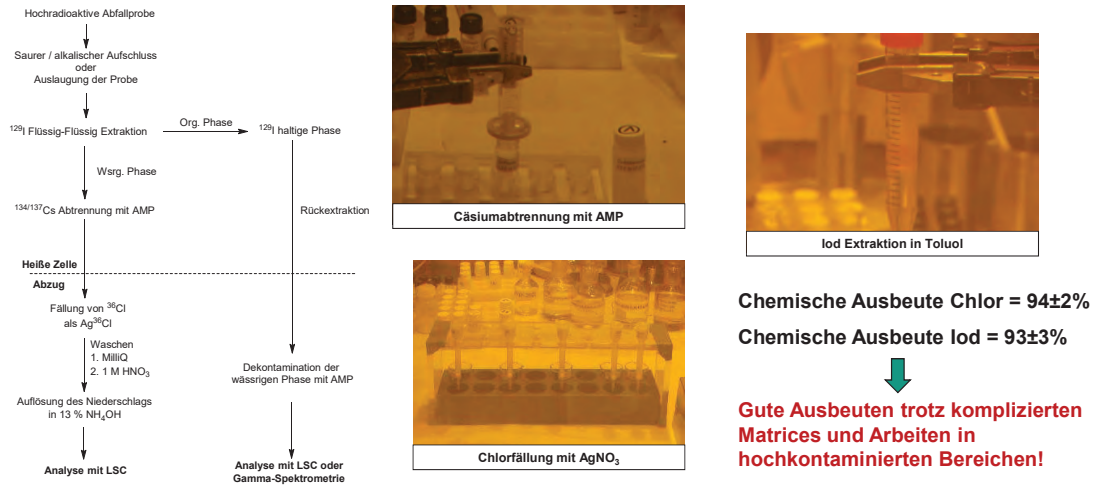
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Vom Reaktor ins Endlager | Materialien und Methoden | Radionuklidanalyse | Spektroskopische Analysen | Zusammenfassung

**Radionuklidanalyse – Trennungsgang <sup>36</sup>Cl / <sup>129</sup>I**

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**Radionuklidanalyse – <sup>36</sup>Cl in KBS und Zircaloy**



<sup>36</sup> Cl Inventare	KBS		Zircaloy-Hüllrohr		<sup>35</sup> Cl (n,γ) <sup>36</sup> Cl
<b>Probe</b>	UO <sub>x</sub> 50,4 GWd/t <sub>SM</sub> [Bq/t <sub>SM</sub> ]	MOX 38,0 GWd/t <sub>SM</sub> [Bq/t <sub>SM</sub> ]	UO <sub>x</sub> 50,4 GWd/t <sub>SM</sub> [Bq/t <sub>SM</sub> ]	MOX 38,0 GWd/t <sub>SM</sub> [Bq/t <sub>SM</sub> ]	
<b>Experimentell</b>	3,62(±0,54)×10 <sup>8</sup>	5,80(±0,87)×10 <sup>8</sup>	6,32(±0,28)×10 <sup>8</sup>	5,33(±0,24)×10 <sup>8</sup>	
<b>Berechnet</b>	4,73×10 <sup>8</sup>	3,68×10 <sup>8</sup>	6,57×10 <sup>8</sup>	5,23×10 <sup>8</sup>	
<b>Verhältnis (exp/ber)</b>	<b>0,77 ± 0,12</b>	<b>1,58 ± 0,24</b>	<b>0,96 ± 0,04</b>	<b>1,02 ± 0,05</b>	

➡ Numerische Berechnungen auf Grundlage „expert judgement“ 15 ppm <sup>35</sup>Cl Precursor in KBS und Hüllrohr [HÄK19].

➡ Experimentelle Aktivitätsinventare sind in Einklang mit Berechnungen.

[HÄK19] S. Häkkinen. Impurities in LWR fuel and structural materials, VTT, Finland (2019).

➡ **Erstmalige Analyse von <sup>36</sup>Cl in DWR Brennstoffkomponenten!**

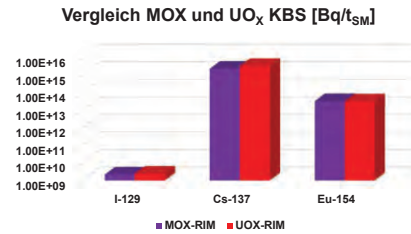
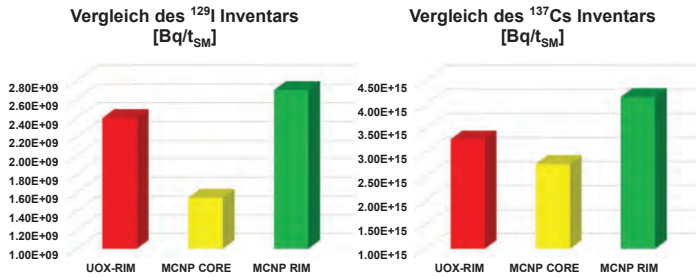
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## Radionuklidanalyse – Spaltprodukte

- Bestimmung des Spaltproduktinventars von **KBS Fragmenten aus der Wechselwirkungsschicht** und Vergleich mit MCNP Berechnungen.
- Keine signifikanten Unterschiede zwischen **UO<sub>x</sub> (50,4 GWd/t<sub>SM</sub>)** und **MOX (38,0 GWd/t<sub>SM</sub>)** Brennstoff.



Erhöhte <sup>129</sup>I und <sup>137</sup>Cs Aktivität durch einen Anreicherungseffekt an der Hüllrohrgrenzfläche auf Grund des höheren lokalen Abbrands und dem Transport von Iod entlang eines thermischen Gradienten im Pellet.

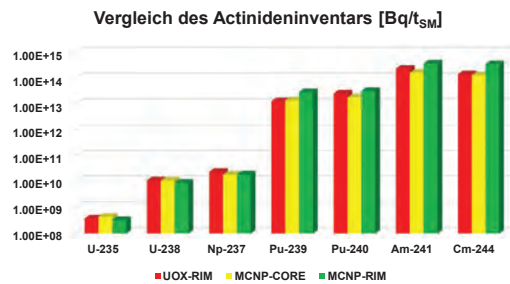
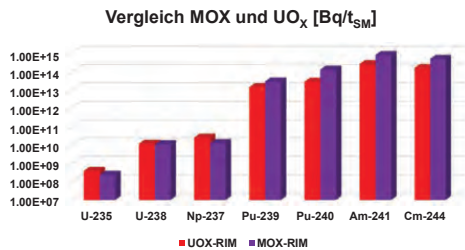
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## Radionuklidanalyse – Actiniden

- Experimentelle und berechnete Inventardaten der Actiniden für verschiedene Regionen im Pellet in UO<sub>x</sub> KBS.
- MOX Brennstoff zeigt im Vergleich zu UO<sub>x</sub> Brennstoff eine **erhöhte Aktivität von minderen Actiniden** auf Grund des **erhöhten initialen Pu Gehalts**.



Inventarkennnisse der Transurane sind wichtig für Berechnungen zu α-Strahlungsinduzierter Schädigung des Hüllrohrs während der Zwischenlagerung.

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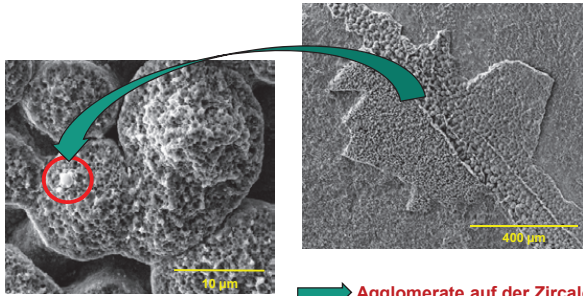
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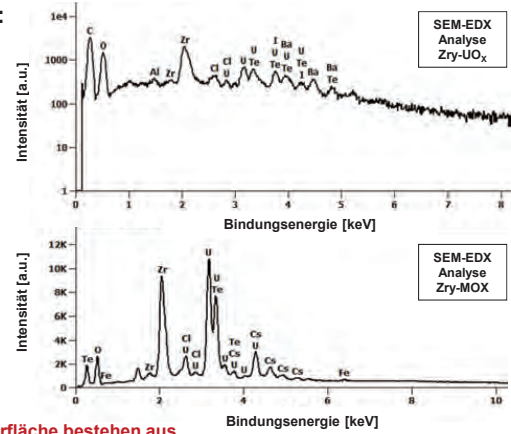
## Spektroskopische Analysen – SEM-EDX

### Zircaloy in Kontakt mit abgebranntem UO<sub>x</sub> / MOX KBS:

- SEM-EDX: Cl, Te, I, Cs, Fe, Zr, Ba, U.
- XPS: Cl, Te, Cs, Fe, Zr, Ba, U.



Agglomerate auf der Zircaloy Oberfläche bestehen aus U-O-Zr-Cs-Cl-I haltigen Phasen.



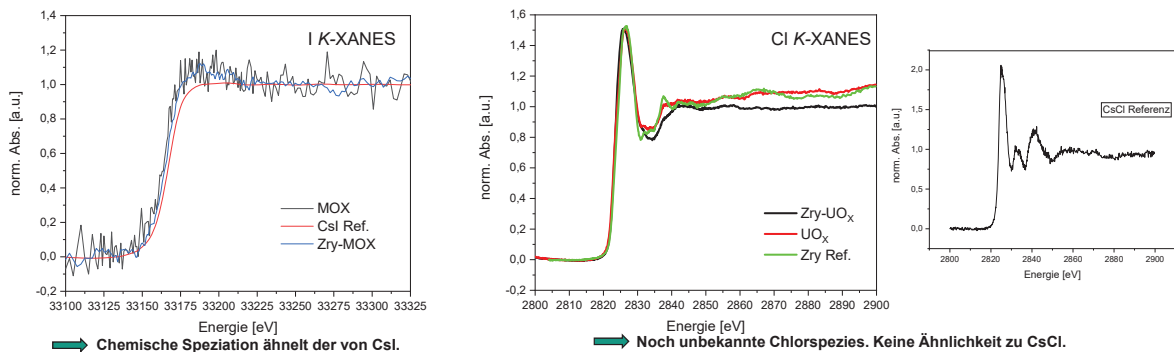
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## Spektroskopische Analysen – XAS

- Kenntnisse zur Konzentration und zur Speziation von Chlor (und Iod) in KBS und Zircaloy sind mit großen Unsicherheiten verbunden.
- Annahmen zur maximalen Chlor-Verunreinigung beziehen sich auf bis zu 25 ppm Cl im KBS und 20 ppm Cl in Zircaloy-Hüllrohren.
- Erstmalige XAS Messungen für Iod und Chlor Speziation in KBS und Zircaloy. ➡ **Komplexe Mischphasen!**



Chemische Speziation ähnelt der von CsI.

Noch unbekannte Chlorspezies. Keine Ähnlichkeit zu CsCl.

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## Spektroskopische Analysen – Modellsystem

- Laborexperimente zur Ausbildung von Agglomeraten und Lochfraßkorrosion unter simulierten

Zwischenlagerbedingungen:

- Cäsiumhalogenide in Kontakt mit Zircaloy und  $UO_2$  Pellet unter Ar Atmosphäre.
- Temperaturreduktion über 3 Monate von 400°C auf Raumtemperatur.
- Anschließende Analyse mit SEM-EDX und XPS.



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## Zusammenfassung

### ■ Radionuklidanalyse:

- Abtrennungsmethode für  $^{36}\text{Cl}$  und  $^{129}\text{I}$  aus hochradioaktiven Proben entwickelt.
- **Erstmalige Analyse des  $^{36}\text{Cl}$  Inventars** in Druckwasserreaktor-Brennstoffkomponenten.
- **Nachweis** von Iod-reichen Anreicherungen in der Wechselwirkungsschicht zwischen KBS und Zircaloy-Hüllrohr.
- Gute Übereinstimmung zwischen Berechnungen und experimentell bestimmten Radionuklid-Inventardaten.

### ■ Spektroskopische Analysen:

- **Erstmalige Cl K- und I K-Kanten Messungen** an hochradioaktivem Material (KBS und Zircaloy).
- Agglomerate in der Wechselwirkungsschicht bestehen unter anderem aus **halogenreichen Mischphasen (Cl und I)**, sowie Cs, Te, Ba, U und Pu.
- **Bestätigung der ausgebildeten Agglomerate und Lochfraßkorrosion bei  $T < 400^\circ\text{C}$  unter Laborbedingungen.**

22 06.05.2022

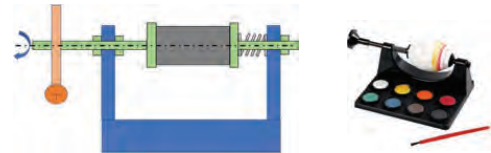
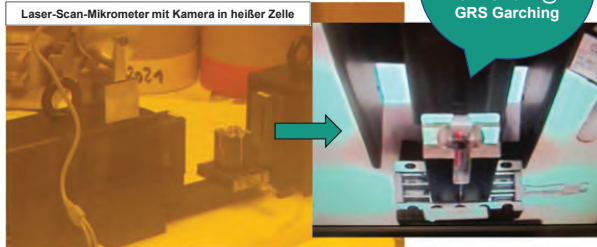
T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

Institut für Nukleare Entsorgung (INE)

## Ein- & Ausblicke – (Nano-)mechanische Prüfverfahren

- Experimente zur Untersuchung der strukturellen Integrität von Hüllrohren nach Bestrahlung.  
 → **Anschwellen der KBS-Tablette.**
- Bestimmung des **Hüllrohrdurchmessers** und **Berechnung von Umfangsspannungen** vor und nach Entfernen des Brennstoffs.  
 → **INE-Beitrag zu BMWK SPIZWURZ.**

Vortrag von M. Marchetti SEDS 2022 @ GRS Garching



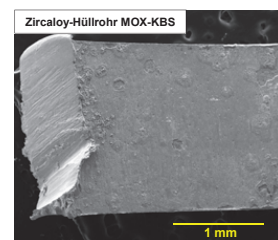
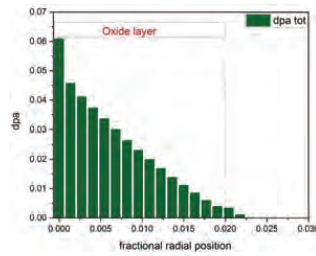
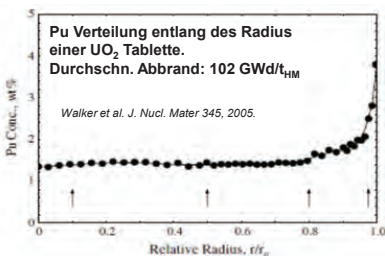
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Institut für Nukleare Entsorgung (INE)

## Ein- & Ausblicke – Strahlungsschäden

- **Untersuchungen von Strahlungsschäden** verursacht durch Actiniden an der Hüllrohr-KBS-Grenzfläche.
- Akkumulierte Schädigung während der Zwischenlagerung kann mittels **Monte Carlo** basierten Codes (z.B. FLUKA) und / oder **Messungen der Defekte mittels XRD / TEM** bestimmt werden.
- Untersuchung der **Korrelation zwischen mechanischen Eigenschaften** des Hüllrohrs bei Raumtemperatur und **Strahlungsschäden, zusammen mit Hydridgehalt und Hydrid-Morphologie.**



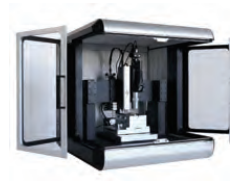
24 06.05.2022

T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

Institut für Nukleare Entsorgung (INE)

## Ein- & Ausblicke – „Neues“ Equipment am INE

- Raman-Sonden (532 und 633 nm) in heißen Zellen.
- Kalt-Einbettpresse (VACUMET 52).
- Schleif- und Poliermaschinen (Bühler MiniMet 1000 und VibroMet 2).
- Nano-Indenter (Femto-Indenter FT-104).



 **In heißer Zelle!** 

 **In Handschuhboxen** 

25 06.05.2022

*T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben*

Institut für Nukleare Entsorgung (INE)

## BMWK KEK geförderte Doktorandenstelle



- **Untersuchung von Hüllrohr-Degradationsprozessen, insbesondere den kombinierten Einfluss von Hydriden, lokalen Spannungen und der Rolle von Strahlungsschäden während der trockenen Zwischenlagerung von abgebranntem KBS.**
- **Doktorarbeit ist in drei Arbeitspakete (AP) unterteilt:**
  - **AP1:** Probenpräparation und Charakterisierung; Hydridgehalt und Hydrid-Morphologie, Dicke der Oxidschicht und Material-Mikrostrukturanalysen mittels **SEM, EBSD und Synchrotron XRD**.
  - **AP2:** Evolution von mechanischen Eigenschaften des Hüllrohrs: **Lokale Elastizitätsmodule**, Härte wird mit **Nano-Indentierung** untersucht.
  - **AP3:** Untersuchung des **Einflusses von Strahlungsschäden** auf das Hüllrohr mit Modellen (z.B. FLUKA, PHITS).

 **Bei Interesse: Einfach anfragen, anschreiben oder anrufen!**

26 06.05.2022

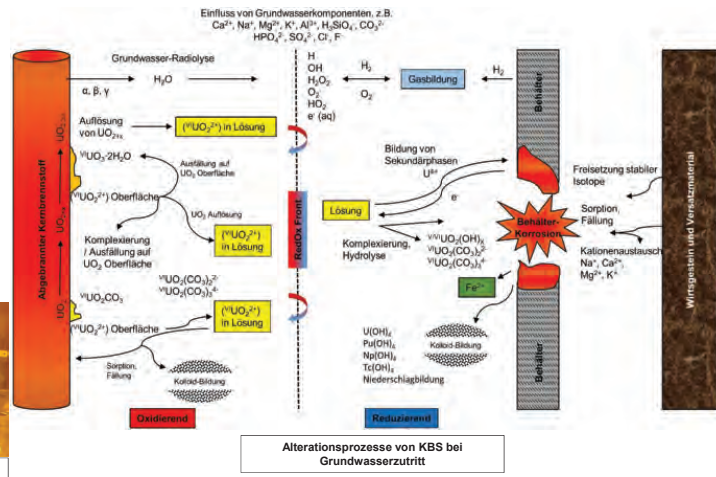
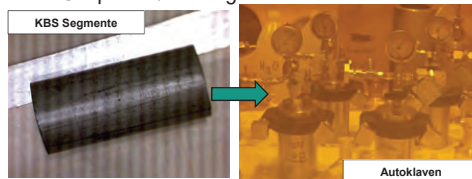
*T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben*

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## Ein- & Ausblicke – KBS Korrosionsexperimente

- **Langzeituntersuchungen (~ 4 Jahre) zum Freisetzungsverhalten von Radionukliden** aus abgebranntem KBS in z.B. simulierten Grundwasserlösungen.
- **Korrosionsexperimente in Autoklaven unter Endlagerbedingungen (pH, red. Bedingungen, etc.)** und Analyse der Gasphase / Lösung.



27 06.05.2022

T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

Institut für Nukleare Entsorgung (INE)



1980 - 2020

**INE - 40**

Institut für Nukleare Entsorgung



This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement N°847593

## Danke für Ihre Aufmerksamkeit.

28 06.05.2022

T. König et al. – Untersuchung des Radionuklidinventars und chemischer Wechselwirkungsprozesse an der Grenzfläche zwischen Kernbrennstoff und Zircaloy-Hüllrohr von bestrahlten Leichtwasserreaktor-Brennstoffproben

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**6.5 SFC Task 2: Fuel properties characterisation and related uncertainty analysis (summary and status); P. Schillebeeckx, JRC Geel; IAEA CRP spent fuel characterization ; 22 – 23/09/2022**



## Task 2: Fuel properties characterisation and related uncertainty analysis

Ron Dagan	KIT
Dimitri Rochman	PSI
Peter Schillebeeckx	<b>JRC Geel (co-ordinator)</b>
Marcus Seidl	PEL
Marc Verwerft	SCK•CEN

### Partners:

CIEMAT, CPST, CTU (SURAO), ENRESA, ENUSA, JRC, JSI, KIT, LEI, NAGRA, PEL, PSI, SCK•CEN, SKB, SSTC NRS, TUS, VTT, UU

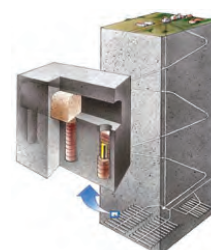
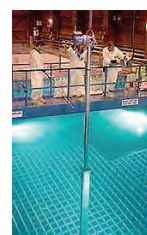
ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



## Spent Nuclear Fuel (SNF) intermediate storage or final disposal

A **safe, secure, economic** and **ecological** transport, storage and final disposal requires that **SNF is characterised** for the main source terms of interest:

- Decay heat
- Neutron emission
- $\gamma$ -ray emission
- **Reactivity** (burnup credit)  
nuclides with high neutron absorption cross section)
- **Fissile material (Safeguards)**  
i.e.  $^{235}\text{U}$ ,  $^{239}\text{Pu}$
- **Specific long-lived radionuclides (Long term safety)**  
e.g.  $^{14}\text{C}$ ,  $^{79}\text{Se}$ ,  $^{94}\text{Nb}$ ,  $^{99}\text{Tc}$ ,  $^{129}\text{I}$ ,  $^{226}\text{Ra}$



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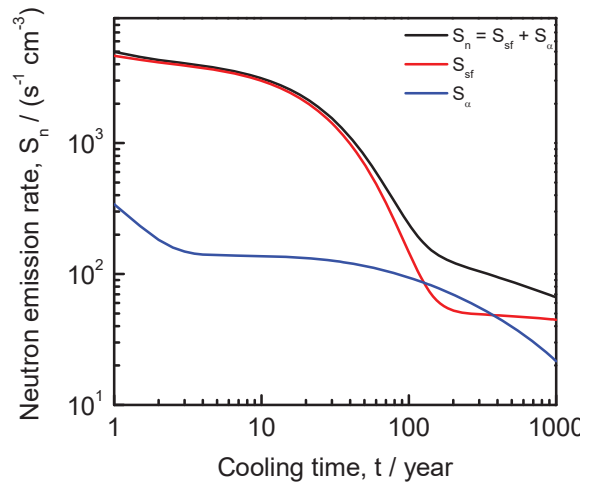


## Neutron emission by SNF

$$S_n(t) = \sum_k S_{n,k}(t)$$

- $S_{n,k}(t)$  : contribution of radionuclide k
- $S_{n,k}(t) = (s_{sf,k} + s_{\alpha n,k}) N_k(t)$ 
  - $N_k(t)$  : number of nuclei of nuclide k at time t
  - $s_{sf,k}$  : specific neutron emission rate of nuclide k due to sf
  - $s_{\alpha,k}$  : specific neutron emission rate of nuclide k due to  $(\alpha,n)$  reactions

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/t



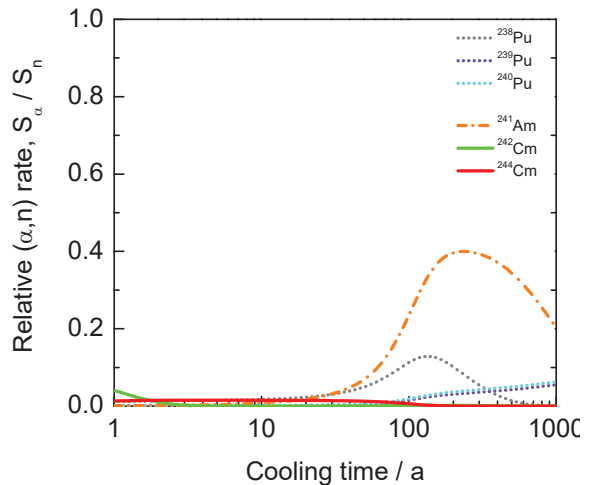
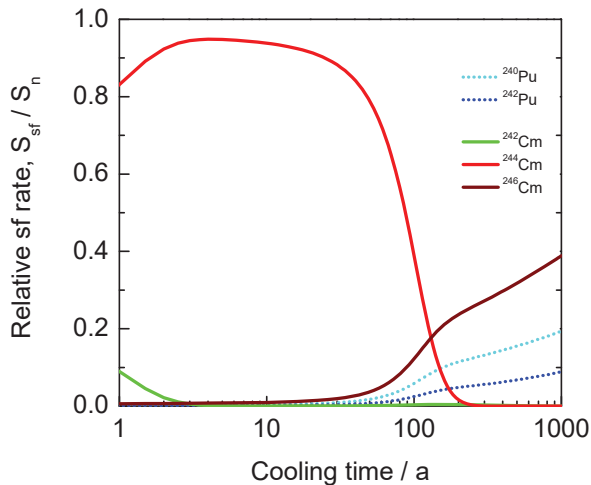
ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



## Neutron emission by SNF

$$S_n(t) = \sum_k (s_{sf,k} + s_{\alpha n,k}) N_k(t)$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/t



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

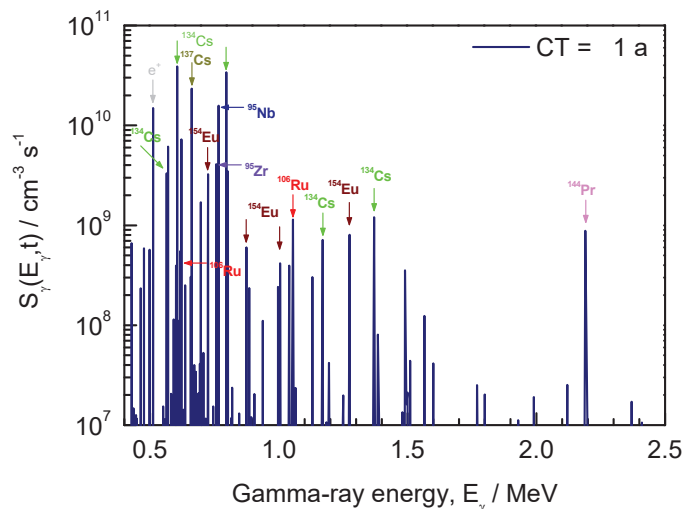


## Gamma-ray emission by SNF

$$S_\gamma(t) = \sum_k S_{\gamma,k}(E_\gamma, t)$$

PWR UO<sub>2</sub> pellet (5 g)  
<sup>235</sup>U/U = 4.8 %  
 burnup = 44 GWd/t

<sup>95</sup> Nb	35.0 d
<sup>95</sup> Zr	64.0 d
<sup>144</sup> Ce/ <sup>144</sup> Pr	284.9 d
<sup>106</sup> Ru/ <sup>106</sup> Rh	1.02 a
<sup>134</sup> Cs	2.06 a
<sup>154</sup> Eu	8.8 a
<sup>137</sup> Cs/ <sup>137m</sup> Ba	30.0 a



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

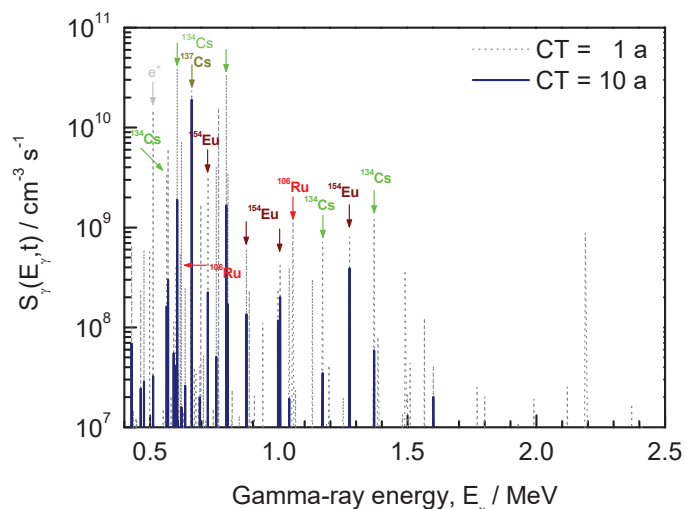


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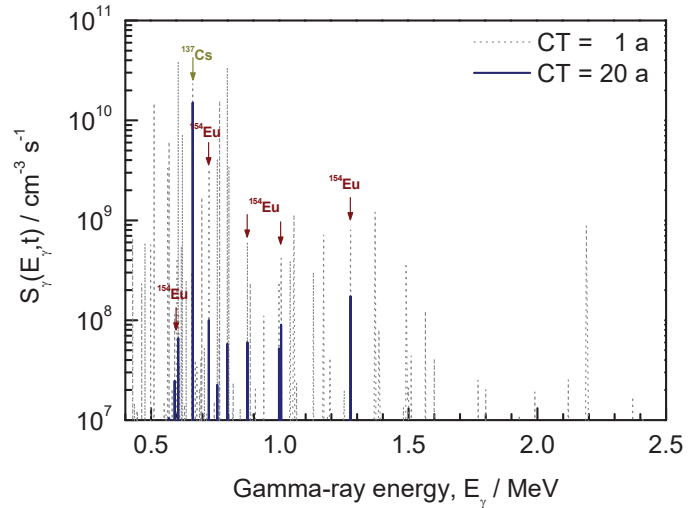


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ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

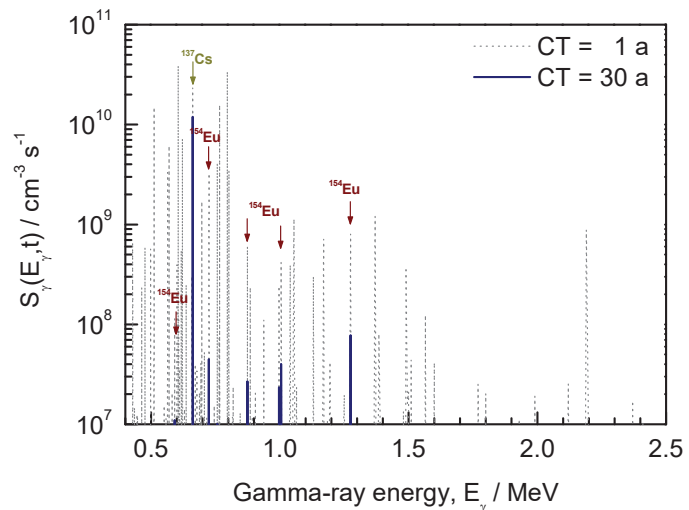


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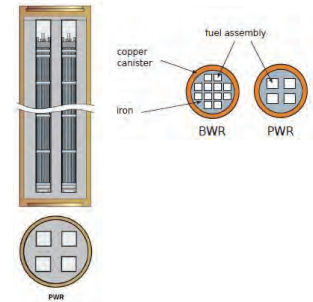
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## Characterisation of SNF

### Main source terms of interest:

- Decay heat : H
- Neutron emission :  $S_n$
- $\gamma$ -ray emission :  $S_\gamma$
- Reactivity :  $^{235}\text{U}, ^{239}\text{Pu}, ^{241}\text{Am}, \text{Fission Products (BUC)}$
- Fissile material :  $^{235}\text{U}, ^{239}\text{Pu}$
- Long-term safety : e.g.  $^{14}\text{C}, ^{79}\text{Se}, ^{94}\text{Nb}, ^{99}\text{Tc}, ^{129}\text{I}, ^{226}\text{Ra}$



### Contributions of nuclides with different characteristics

Difficult to be measured directly, in particular during industrial operation

e.g. decay heat by calorimetry at CLAB: accurate but long measurement times

⇒ Estimated by **theoretical calculations** using a burnup code

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$(N_k(t_0), k = 1, \dots, n)$ : by theoretical calculations

### Coupled neutron transport – nuclide depletion/creation calculation

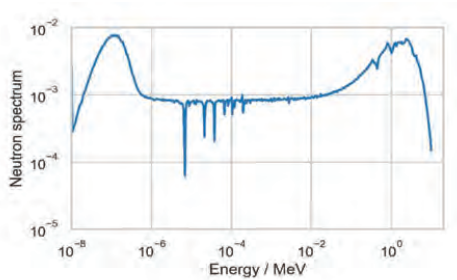
Neutron transport



Bateman equation

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

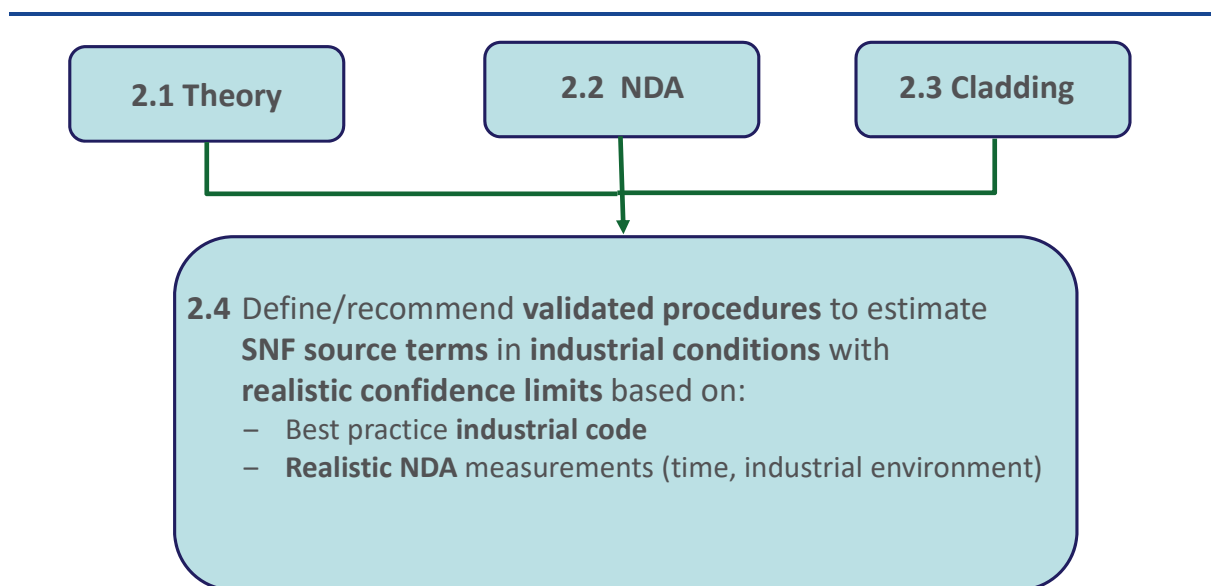
Update nuclide vector



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## SFC – Task 2 (structure)



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## SFC- Task 2: Code comparison

- CIEMAT : EVOLCODE (MCNP)
- JRC Geel : SERPENT, SCALE
- JSI : SCALE, DRAGON
- KIT : MCNP-CINDER
- NAGRA : SCALE
- PSI : CASMO
- SCK CEN : ALEPH-2 (MCNP)
- VTT : SERPENT

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## Sensitivity and Uncertainty (S/U) analysis

• Input data:

– Nuclear Data (ND)

- Cross sections (neutron interactions)
- Fission yields
- Neutron emission probabilities
- Decay data

– Fuel History (FH)

- Fuel properties (design, composition)  
e.g. Initial enrichment (IE)
- Reactor operation and irradiation conditions  
e.g. Burnup (BU)
- Cooling time (CT)

BurnUp (BU):

time integrated power per mass of initial fuel (MWd/kg)

$\propto$  total number of fission  $\times$  energy per fission event

• Computational

- Method: stochastic/deterministic
- Model (2D/3D, boundary conditions, ...)
- Numerical approximations (depletion time steps, depletion zones, ...)

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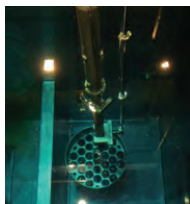
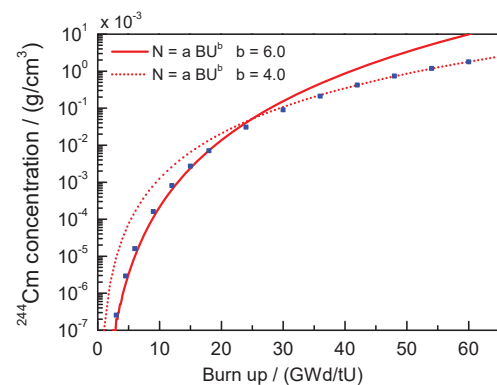
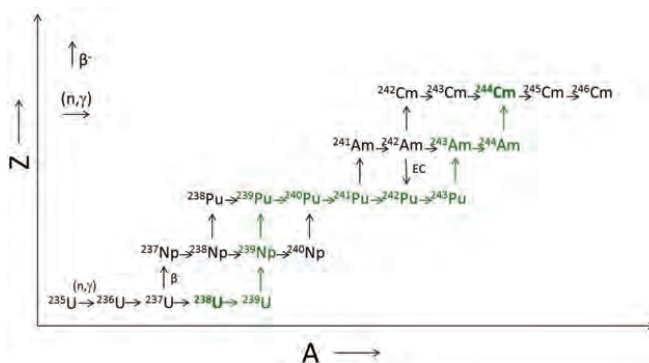


### S/U analysis: <sup>244</sup>Cm production

$$\frac{dN_k}{dt} = Y N_f \sigma_f \phi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \phi - (\lambda_k + \sigma_{k,a} \phi) N_k$$

$N = aBU^b$

$b = 6$  for BU < 20 GWd/t



⇒ <sup>244</sup>Cm : burnup indicator

⇒ Neutron emission rate : burnup indicator

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## S/U analysis: estimation of <sup>244</sup>Cm inventory

$$\frac{dN_k}{dt} = Y N_f \sigma_f \varphi + \sum_i \lambda_i N_i + \sum_j \sigma_j N_j \varphi - (\lambda_k + \sigma_{k,a} \varphi) N_k$$

Ref.	Library	Reactor	Fuel	BU Gwd/t	IE wt%	<sup>244</sup> Cm
Rochman	ENDF/B-VII.0	PWR	UO <sub>2</sub>	10	4.1	18.7 %
	ENDF/B-VII.0	PWR	UO <sub>2</sub>	20	4.1	16.9 %
	ENDF/B-VII.0	PWR	UO <sub>2</sub>	30	4.1	15.5 %
	ENDF/B-VII.0	PWR	UO <sub>2</sub>	40	4.1	14.1 %
Zwermann	SCALE-6.1	PWR	UO <sub>2</sub>	40	4.1	8.5 %
Leary	ENDF/B-VII.1	PWR	UO <sub>2</sub>	54	3.4	9.6 %
Rochman	ENDF/B-VII.1	PWR	UO <sub>2</sub>	54	3.4	9.1 %
Rochman	ENDF/B-VII.1	PWR	UO <sub>2</sub>	40	4.1	9.7 %

<sup>244</sup>Cm inventory prediction production

- uncertainty due to nuclear data : ~10%
- due to <sup>242</sup>Pu(n,γ), <sup>243</sup>Am(n,γ)

⇒ Systematic study for key nuclides

⇒ Improve nuclear data

- Input HPRL NEA/OECD

- Input to SANDA (DG-RTD)

<https://cordis.europa.eu/project/id/847552>  
Supplying Accurate Nuclear Data for energy and non-energy Applications

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## Innovative NDA methods/systems for SNF characterisation

- **Innovative NDA methods to characterise pin segments**
  - **Validate codes** (alternative to radiochemical analysis)
  - Production of a reference pellet
- **NDA methods to characterise fuel assemblies (SKB-50)**
  - Improve theoretical source term predictions during industrial routine operation
  - Improve fuel history data:** e.g. BU
  - Validate codes
- **Study new detectors**
  - CLYC, CVD

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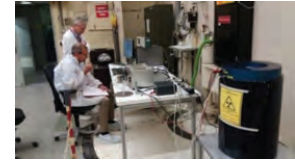


## NDA methods to characterise pin segments

- **Neutron emission rate** of a SNF pin segment

(collaboration SCK CEN – JRC Geel, Ispra)

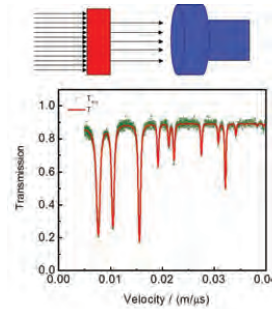
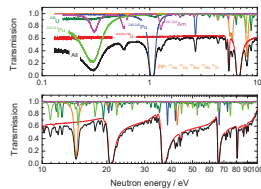
- Non-destructive method to determine  $^{244}\text{Cm}$  content
  - Measurements in conventional controlled area conditions
- Hage's point model, JRC Ispra (B. Pedersen)



- **Nuclide vector** of SNF pin segment by **NRTA**

(collaboration SCK CEN – JRC Geel)

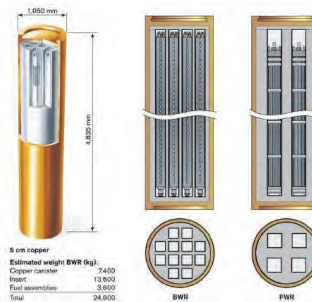
- **Non-destructive**; no chemical analysis
- **Absolute** measurement (no calibration)
- Measurements at **GELINA** facility of JRC Geel



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## Experiments at CLAB: SKB-50



### Installed systems

- Calorimeter
- Gamma-ray spectroscopic scanner

### Testing of advanced systems (LANL)

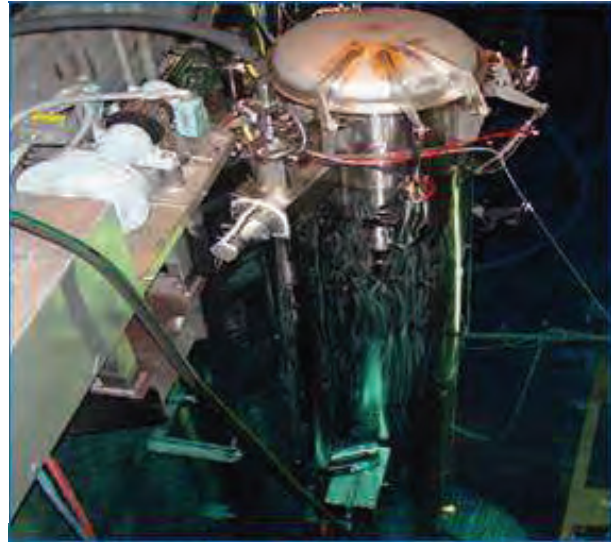
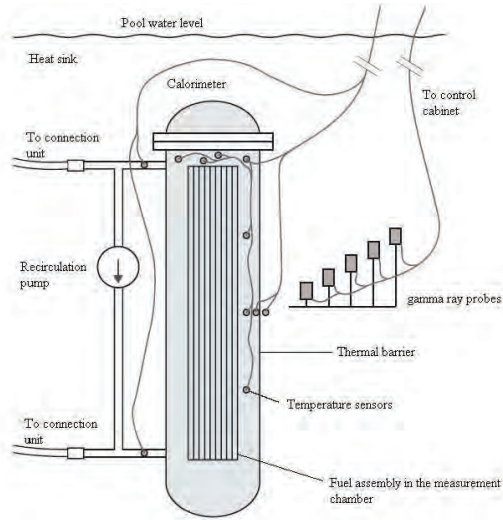
- Differential Die-Away Self-Interrogation (DDSI)
- Differential Die-Away (DDA)



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### Calorimeter at CLAB

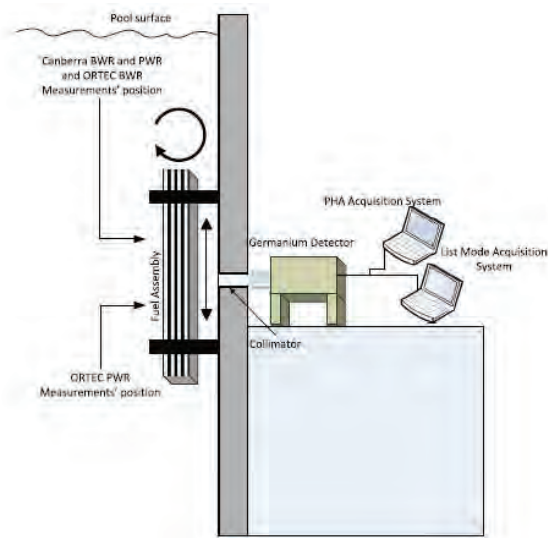


- ⇒ Target value uncertainty  $\leq 2\%$
- ⇒ Reference instrument for decay heat of SNF

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### Gamma-ray spectroscopic scanning system at CLAB



Vaccaro et al. NIMA 830 (2016) 325  $^{134}\text{Cs}$ ,  $^{137}\text{Cs}$ ,  $^{154}\text{Eu}$

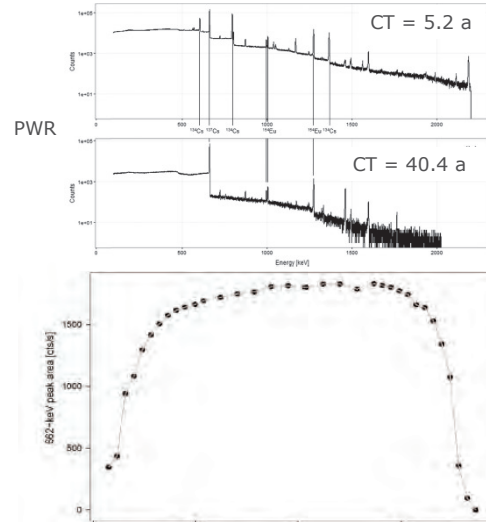


Fig. 8. Count rate for the 662-keV  $^{137}\text{Cs}$  net peak area as a function of axial location along BWRs. These data were measured with the ORTEC GMX detector and Canberra Lynx MCA from the 45° corner. The axial location is specified as downward along the uranium containing portion of the fuel (The indicated absolute positions are accurate to  $\pm 10$  cm, the error bars are much smaller than the data points).

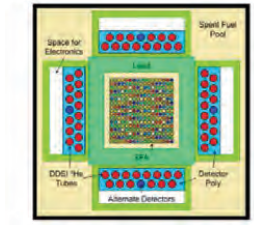
ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



## Fuel assemblies: DDSI and DDA at CLAB (LANL development, NGSi)

- **Differential Die Away Self-Interrogation (DDSI, passive)**

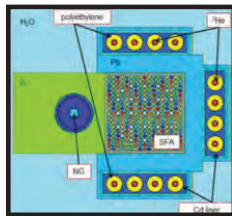
A.C. Trahan, LA-UR\_16\_20026 Kaplan et al., NIMA 764 (2014) 347 - 351



⇒ Optimise data analysis procedures for source term determination (not only safeguards)

- **Differential Die Away (DDA, active)**

V. Henzl, LANL-UR-123025



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)

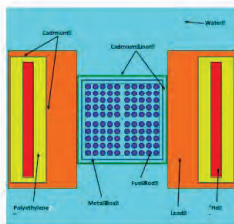


## Fuel assemblies: Finland

- **Passive Neutron Albedo Reactivity (PNAR, NGSi)**

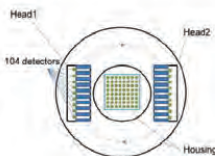
LANL development, Tobin et al., NIMA 897 (2018) 32 - 37

Tobin et al., ESARDA bulletin 56 (2018) 12 - 18



- **Passive Gamma Ray Emission Tomography (PGET)**

IAEA development, Honkamaa et al., Symp. Int. Safeguards, IAEA Vienna 2014



ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



## EURAD-SFC (4 years project)

---

Define/recommend **validated procedures** to estimate **SNF source terms** (including fissile material) in **industrial conditions** with **realistic confidence limits** based on:

- Best practice **industrial code**
- **Realistic NDA** measurements (time, industrial environment)

ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)



- 
- EURAD project (SNF characterisation)
    - <https://www.ejp-urad.eu/about-urad>
    - NUGENIA, <http://nugenia.org/call-for-mobility-grants-open/>
  - ARIEL  
support for open access, scientific visits, training early researchers, ...
    - [www.ariel-h2020.eu](http://www.ariel-h2020.eu)
  - JRC Geel open access
    - <https://ec.europa.eu/jrc/en/research-facility/open-access>

ESARDA, 6 - 7 february 2020, SCK CEN Mol (BE)





**6.6 Performance assessment and uncertainty evaluation of the  
clab calorimeter; P. Schillebeeckx, JRC Geel; WPNCS Subgroup  
12 meeting; 01/12/2022**



## PERFORMANCE ASSESSMENT AND UNCERTAINTY EVALUATION OF THE CLAB CALORIMETER

Work part of EURAD/SFC/Task2

P. Schillebeeckx,

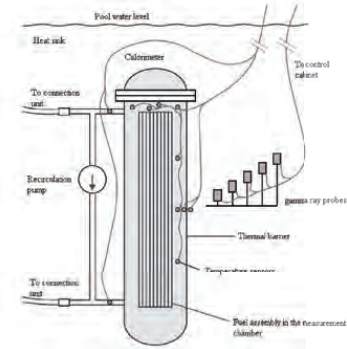
European Commission, Joint Research Centre (JRC), Geel, Belgium

Contributors:

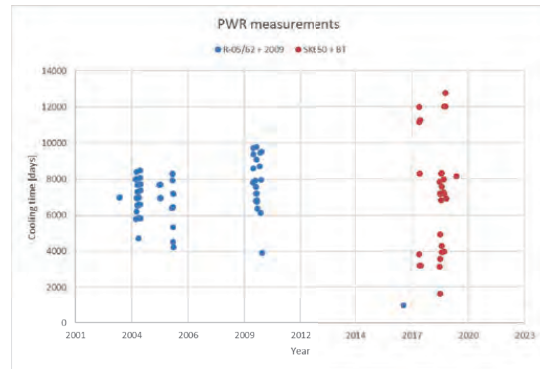
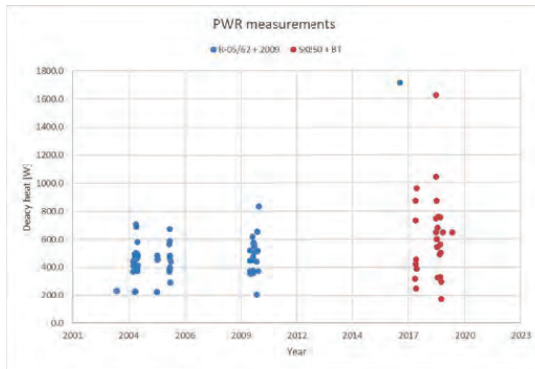
JRC Geel, SKB (Vattenfall), SCK CEN and JSI



sck cen



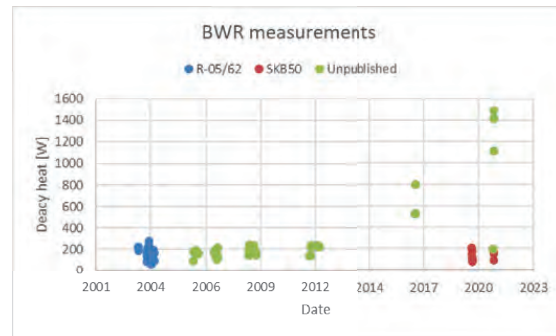
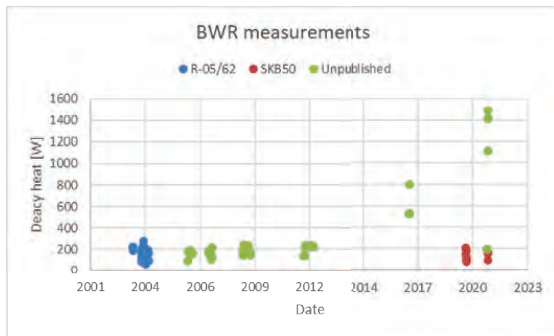
## OVERVIEW OF DATA AT CLAB: PWR



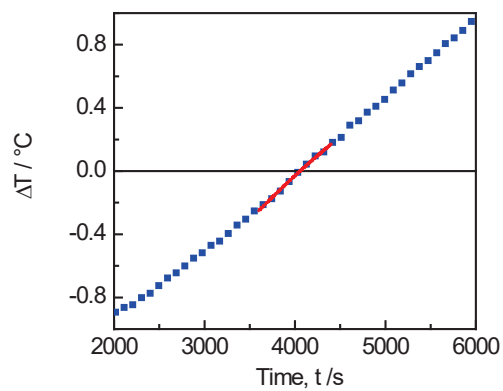




### OVERVIEW OF DATA AT CLAB: BWR



### PERFORMANCE ASSESSMENT AND UNCERTAINTY EVALUATION OF THE CLAB CALORIMETER

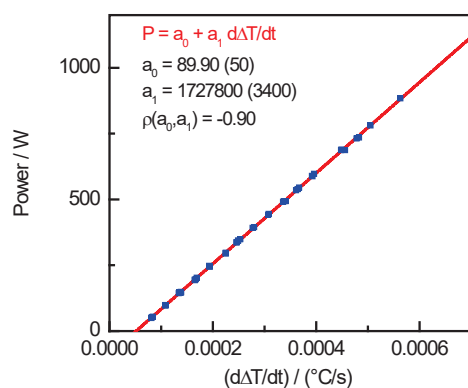


- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$





## PERFORMANCE ASSESSMENT AND UNCERTAINTY EVALUATION OF THE CLAB CALORIMETER



### Calibration with an electrical heater

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$
- Fit to data:  $P = a_0 + a_1 \frac{d\Delta T}{dt}$



## PERFORMANCE ASSESSMENT AND UNCERTAINTY EVALUATION OF THE CLAB CALORIMETER

### Spent nuclear fuel assembly

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  when  $\Delta T = 0$
- $Q = a_0 + a_1 K \frac{d\Delta T}{dt}$
- $P = Q + P_e$ 
  - $K$  : correction factor due to thermal capacity difference between electrical heater and fuel assembly
  - $P_e$  : heat loss due to  $\gamma$ -rays escaping from the calorimeter

### Calibration with an electrical heater

- Determine  $\Delta T = T_c - T_p$  vs time
- Determine  $d\Delta T/dt$  for  $\Delta T = 0$
- Fit to data:  $P = a_0 + a_1 \frac{d\Delta T}{dt}$





## DATA ANALYSIS AND UNCERTAINTY EVALUATION

Define metrological parameters of the full measurement process and identify/quantify related uncertainty components

- Calibration of the heater
- Impact cables: loss due to cable length outside the calorimeter
- Define optimum fit procedure to determine the temperature gradient
- Uncertainty of temperature gradient
- Quality of calibration curve
- Verify repeatability over a long time period
- Correction factor: difference electrical heater – assembly
- Correction factor: loss of gamma-ray energy emitted by assembly

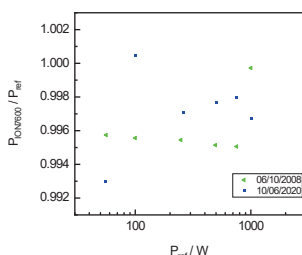
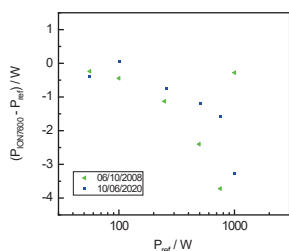


## CALIBRATION ELECTRICAL HEATER

Electrical heater (ION 7600) was calibrated for its power output by a reference instrument

- 06/10/2008 ZERA TPZ 303
- 10/06/2020 ZERA MT3000

⇒ data show that the output of the electrical heater has to be corrected to avoid bias effects.



Average ratio & st.dev. of ratio

- 06/10/2008 0.9961 0.0018
- 10/06/2020 0.9972 0.0025

- Data taken between 2008 and 2020 have to be increased by 0.37% and an uncertainty of 0.2% has to be added due to the calibration
- Future: regular (yearly) calibration!



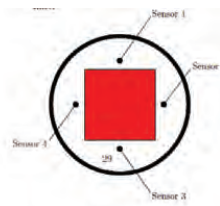
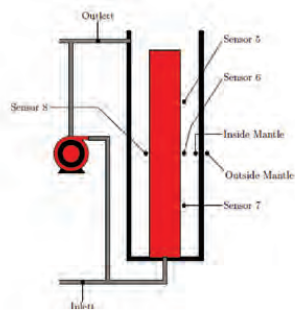


### ENERGY LOSS DUE TO CABLES

- There is a power loss of the power provided by the calibration unit due to cables outside the calorimeter
- The heat loss is estimated from the length and electrical resistance per unit length
  - Outside
    - Length: 2 x 20 m
    - Resistance per unit length: 0.012 Ω/m
  - Inside (heating cable in calorimeter)
    - Length: 261 m
    - Resistance per unit length: 0.1 Ω/m
- ⇒ Power loss fraction:  $26.1 / (26.1 + 0.48) = 0.982$
- Difficult to evaluate an uncertainty since the data are given with without uncertainty, in addition with a limited significant digits!
- Future: provide traceable data!



### DEFINE OPTIMUM PROCEDURE TO DETERMINE TEMPERATURE GRADIENT



To be done :

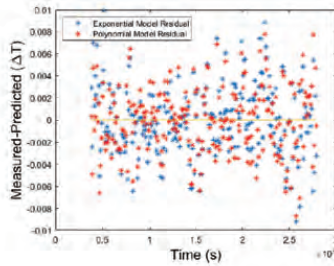
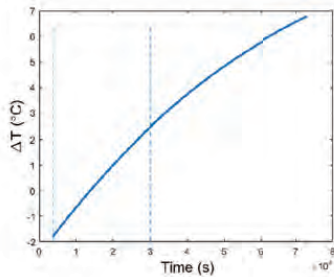
- Define best temperature sensors
- Define optimum time region to fit!

$$\rho C_p \frac{\partial T}{\partial t} - k \frac{\partial^2 T}{\partial x^2} = S \quad \text{Should be 0}$$





**DEFINE OPTIMUM PROCEDURE TO DETERMINE TEMPERATURE GRADIENT**



$$\Delta T_{poly} = c_1 + c_2t + c_3t^2.$$

$$\Delta T_{nl} = a_1 + a_2(1 - e^{-a_3t})$$

⇒ no clear difference

To be done :

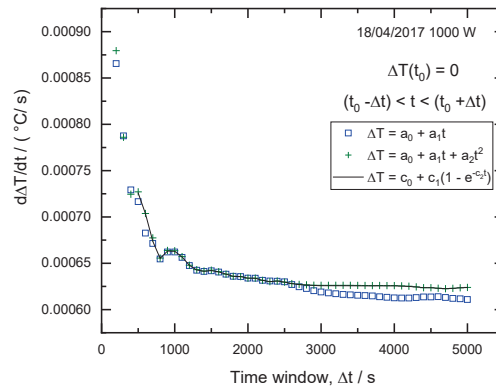
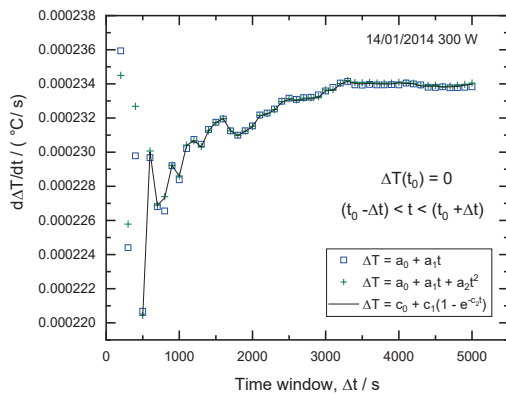
- Define best temperature sensors
- Define optimum time region to fit!

$$\rho C_p \frac{\partial T}{\partial t} - k \frac{\partial^2 T}{\partial x^2} = S \quad \text{Should be 0}$$



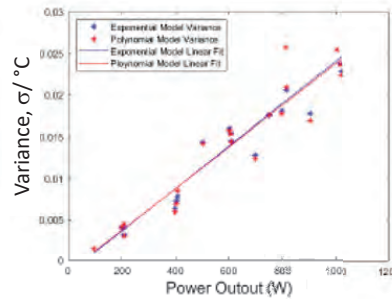
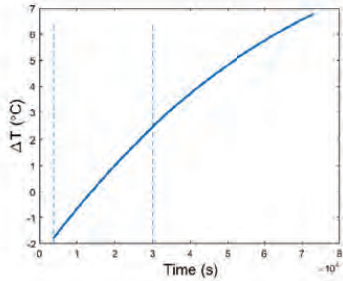
**DEFINE OPTIMUM PROCEDURE: WHICH SENSOR, FUNCTION AND FIT REGION**

Sensor 1





### EVALUATE THE UNCERTAINTY OF THE GRADIENT (VARIANCE ANALYSIS)



$$\sigma = \frac{\sum_i (\Delta T_i - \Delta T_{fit})^2}{N - 1}$$

To be done

- Compare uncertainty with uncertainty of temperature output (assumed uncertainty is 0.01 °C)
- Propagate the uncertainty to the uncertainty of the slope value!



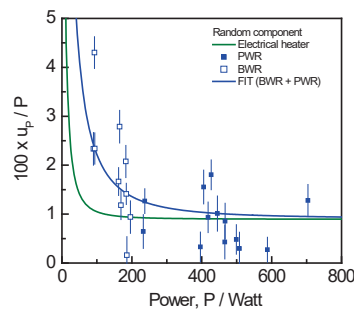
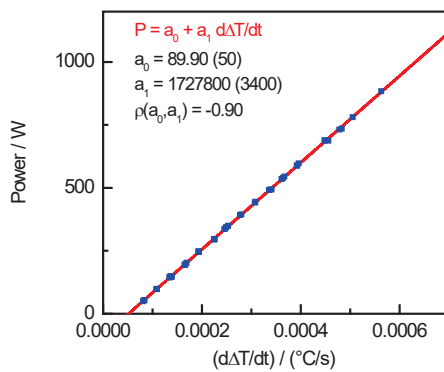
### FIT DATA + REPEATABILITY

Electrical heater

Uncertainty evaluation based on variance analysis: **green line**

SNF assemblies

Repeated measurements







## CALORIMETER AT CLAB – DATA ANALYSIS AND UNCERTAINTY EVALUATION

MSc Thesis: J. Ekman (10/12/2021)

**Correction factor K:** difference between electrical heater and assembly

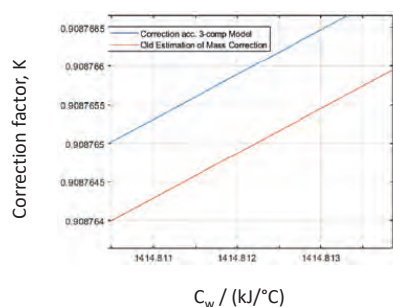
$$P_m = a_0 + a_1 K d\Delta T/dt$$

- Present correction factor based on total heat capacity:

$$P = P_m + P_e$$

ratio of total heat capacity of calorimeter with fuel assembly and with electrical heater

- Use analytical model: ratio of the slope  $d\Delta T/dt$  with fuel assembly and with electrical heater



⇒ negligible difference

⇒ uncertainty evaluation in progress

⇒ Requires specifics of the materials



### Keep in touch



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Thank you



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